

# Brain-inspired Predictive Coding Improves the Performance of Machine Challenging Tasks

# **1 COMPARISON METHODS FOR INCREMENTAL LEARNING**

We provide a brief introduction to the learning algorithms we utilized.

# 1.1 SGD

We trained each task with pre-defined order using stochastic gradient descent (SGD) (Ruder, 2016). We denoted an approach that froze the parameters except for that of the last layer as SGD-F.

# 1.2 EWC

To combat the catastrophic forgetting, Kirkpatrick et al. (2017) introduced Elastic Weight Consolidation (EWC) algorithm as a regularization approach. It helps for the posterior probability to maintain the important parameters for the previously learned tasks and jointly preserve the ability to learn new tasks.

## 1.3 IMM

Lee et al. (2017) introduced a method, called incremental moment matching (IMM) to resolve catastrophic forgetting. To approximate the posterior distribution of parameters, IMM utilizes a Gaussian distribution for each task. The goal of IMM is to investigate for the optimal parameters of the Gaussian approximation and it is categorized into two algorithms. First, IMM-MEAN calculates the weighted average of two networks by minimizing the local KL-divergence. While IMM-MODE focuses on the searching the mode that maximizes the posterior.

## 1.4 LFL

Jung et al. (2016) proposed a less-forgetting method to alleviate catastrophic forgetting. By constructing source and target networks, the goal of LFL minimize the discrepancy between the feature vectors of from two networks.

## 1.5 LWF

Li and Hoiem (2017) designed a less forgettable architecture in incremental learning. The architecture is constructed with multiple output layers where each layer is appended when the network learns a new task. To effectively maintain information from previously learned, LWF utilizes knowledge distillation loss.

# 2 COMPARISON METHODS FOR CLASS-IMBALANCED LEARNING

We provide a brief introduction to the learning objectives we utilized.

## 2.1 Cross-Entropy Loss

The most common criterion used for classification tasks. Inspired from the information theory, the goal of cross-entropy loss is to make the probability distribution be as close as possible to the target distribution.

#### 2.2 Mixup

Mixup (Zhang et al., 2017) generates synthetic training examples via linear interpolation as follows:  $\tilde{x} = \lambda x_i + (1 - \lambda)x_j$ , and  $\tilde{y} = \lambda y_i + (1 - \lambda)y_j$ , where  $(x_i, y_i)$  and  $(x_j, y_j)$  are two training examples, and  $\lambda \in [0, 1]$  is the mixing coefficient. It is demonstrated that the training with virtual examples enhances the performance of classification and increases the robustness of networks.

#### 2.3 Focal Loss

As a representative technique for skewed data distribution, focal loss (Lin et al., 2017) is designed when the object detector encountered class imbalance. It is implemented by multiplying a re-weighting factor  $\alpha(1-p)^{\gamma}$  on the cross-entropy loss where  $\alpha$  indicates the class-wise weight.

#### 2.4 Class-Balanced Focal Loss

Class-balanced loss (Cui et al., 2019) considers the effective number of samples to adjust the decision boundary by inverse class frequency. The effective number for each class is defined as  $E_n = \frac{1-\beta^n}{1-\beta}$  and it is multiplied by the cross-entropy loss.

#### 2.5 Label Distribution Aware Margin Loss

Cao et al. (2019) proposed a loss function that adjusts the decision boundary of which a class having a small number of samples has a wider margin to effectively handle the imbalanced data and a re-balancing scheduler for the efficient optimization of the re-weighting strategy.

#### 2.6 Balanced Meta-SoftMax Loss

Ren et al. (2020) focused on the distribution mismatch between training and testing dataset, and propose a balanced softmax. However, due to the property of mini-batch training, the balanced softmax does not showed successful performance due to the over-balance problem. To resolve this problem, Ren et al. (2020) introduced a meta sampler which is a trainable version of a class-balanced sampler.

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