

Supplementary Material

1 SUPPLEMENTARY DATA

1.1 Distribution of Electrical Channels

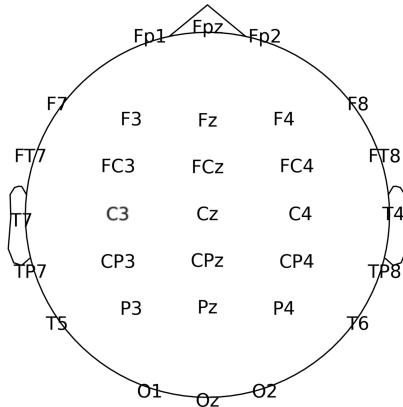


Figure S1. Distribution diagram of electrical channels

1.2 Single-layer Network Measures

In this study, we employed various single-layer network metrics to analyze EEG data, reflecting the connectivity characteristics of brain networks at different levels. Below is a brief description of the metrics used:

$$\text{Node Strength: } k_i^w = \sum_{j \in N} w_{ij}$$

$$\text{Path Length: } L^w = \frac{1}{n} \sum_{i \in N} \frac{\sum_{j \in N, j \neq i} d_{ij}^W}{n-1}$$

$$\text{Local Efficiency: } E_{loc}^w = \frac{1}{2} \sum_{i \in N} \frac{\sum_{j \leq eN, j \neq i} (w_{ij} w_{ji}) [d_{jh}^w(N_i)]^{-1}}{k_i(k_i-1)}^{1/3}$$

$$\text{Betweenness Centrality: } b_i = \frac{1}{(n-1)(n-2)} \sum_{h \neq j, j \neq Ni, j \neq i} \frac{\rho_{ijj}(i)}{\rho_{ijj}}$$

$$\text{Eigenvector Centrality: } \lambda x^T = x^T A$$

$$\text{Clustering Coefficient: } C^w = \frac{1}{n} \sum_{i \in N} \frac{2t_i^W}{k_i(k_i-1)}$$

$$\text{Assortativity: } r^w = \frac{l^{-1} \sum_{(i,j) \in L} w_{ij} k_i^w k_j^w - \left[l^{-1} \sum_{(i,j) \in L} \frac{1}{2} w_{ij} (k_i^w + k_j^w) \right]^2}{l^{-1} \sum_{(i,j) \in L} \frac{1}{2} w_{ij} \left((k_i^w)^2 + (k_j^w)^2 \right) - \left[l^{-1} \sum_{(i,j) \in L} \frac{1}{2} w_{ij} (k_i^w + k_j^w) \right]^2}$$

1.3 Results of single-layer network graph metrics

Table S1. Average of nodal metrics for single-layer networks.

| Task Type | Metrics | W1 | W2 | W3 | W4 | W5 |
|-----------|--------------|---------|---------|---------|---------|---------|
| NAS | PL- θ | 3.1222 | 3.1186 | 3.1365 | 3.1181 | 3.1045 |
| | PL- α | 3.1883 | 3.1769 | 3.1827 | 3.1863 | 3.1869 |
| | PL- β | 3.1663 | 3.1597 | 3.1654 | 3.1632 | 3.1627 |
| | BC- θ | 11.2756 | 11.0895 | 11.1884 | 10.9846 | 11.1473 |
| | BC- α | 7.9657 | 7.8409 | 7.9477 | 8.0354 | 7.8732 |
| | BC- β | 12.6204 | 12.8419 | 12.7482 | 12.7308 | 12.5955 |
| | EC- θ | 0.1628 | 0.1629 | 0.1629 | 0.1636 | 0.1630 |
| | EC- α | 0.1685 | 0.1687 | 0.1685 | 0.1685 | 0.1683 |
| | EC- β | 0.1622 | 0.1618 | 0.1621 | 0.1620 | 0.1622 |
| | PL- θ | 3.1227 | 3.1203 | 3.1335 | 3.1026 | 3.0960 |
| AS-CE | PL- α | 3.1750 | 3.1802 | 3.1795 | 3.1872 | 3.1853 |
| | PL- β | 3.1602 | 3.1583 | 3.1637 | 3.1641 | 3.1615 |
| | BC- θ | 11.3189 | 10.9515 | 10.9709 | 10.9678 | 11.7202 |
| | BC- α | 7.8695 | 7.9247 | 7.8876 | 7.8634 | 7.8202 |
| | BC- β | 12.1520 | 12.0139 | 12.1218 | 12.1897 | 11.9828 |
| | EC- θ | 0.1632 | 0.1629 | 0.1631 | 0.1634 | 0.1625 |
| | EC- α | 0.1685 | 0.1685 | 0.1686 | 0.1685 | 0.1687 |
| | EC- β | 0.1622 | 0.1625 | 0.1624 | 0.1624 | 0.1625 |
| | PL- θ | 3.1202 | 3.1238 | 3.1292 | 3.1091 | 3.0962 |
| | PL- α | 3.1810 | 3.1825 | 3.1808 | 3.1893 | 3.1815 |
| AS-NC | PL- β | 3.1657 | 3.1611 | 3.1620 | 3.1598 | 3.1613 |
| | BC- θ | 11.0173 | 10.9952 | 10.6098 | 10.7520 | 11.4299 |
| | BC- α | 7.8159 | 7.9705 | 7.9039 | 7.8538 | 7.9906 |
| | BC- β | 12.1895 | 12.1716 | 12.1160 | 12.1232 | 12.5532 |
| | EC- θ | 0.1633 | 0.1627 | 0.1630 | 0.1632 | 0.1627 |
| | EC- α | 0.1687 | 0.1684 | 0.1687 | 0.1680 | 0.1684 |
| | EC- β | 0.1624 | 0.1623 | 0.1627 | 0.1625 | 0.1620 |

Table S2. Average of global metrics for single-layer networks.

| Task Type | Metrics | W1 | W2 | W3 | W4 | W5 |
|-----------|---------------|---------|---------|---------|---------|---------|
| NAS | CC- θ | 0.1768 | 0.1762 | 0.1171 | 0.1758 | 0.1775 |
| | CC- α | 0.1686 | 0.1753 | 0.1677 | 0.1607 | 0.1571 |
| | CC- β | 0.1093 | 0.1072 | 0.1108 | 0.1027 | 0.1050 |
| | Ass- θ | -0.1148 | -0.1103 | -0.1148 | -0.1090 | -0.0947 |
| | Ass- α | -0.1094 | -0.0902 | -0.1011 | -0.1043 | -0.0867 |
| | Ass- β | -0.0947 | -0.0942 | -0.0975 | -0.0878 | -0.1012 |
| | CC- θ | 0.1754 | 0.1812 | 0.1791 | 0.1773 | 0.1690 |
| | CC- α | 0.1701 | 0.1697 | 0.1827 | 0.2081 | 0.1938 |
| | CC- β | 0.1302 | 0.1326 | 0.1364 | 0.1500 | 0.1454 |
| | Ass- θ | -0.1115 | -0.0971 | -0.1118 | -0.1082 | -0.1061 |
| AS-CE | Ass- α | -0.0994 | -0.0931 | -0.0990 | -0.0947 | -0.0929 |
| | Ass- β | -0.0965 | -0.1006 | -0.0851 | -0.0853 | -0.0913 |
| | CC- θ | 0.1781 | 0.1803 | 0.1878 | 0.1881 | 0.1718 |
| | CC- α | 0.1622 | 0.1700 | 0.1734 | 0.1760 | 0.1834 |
| | CC- β | 0.1273 | 0.1334 | 0.1380 | 0.1402 | 0.1254 |
| | Ass- θ | -0.1086 | -0.0969 | -0.1027 | -0.1047 | -0.0993 |
| | Ass- α | -0.0978 | -0.1070 | -0.1046 | -0.0984 | -0.1043 |
| | Ass- β | -0.1071 | -0.1018 | -0.0877 | -0.0973 | -0.1007 |