

Supplementary Material



**Figure S1.** Wound healing time dependence on treatment beginning time  $t_0$  for different values of treatment duration  $\Delta t$  and actuator position  $r_p$ .



**Figure S2.** Wound healing time dependence on treatment duration  $\Delta t$  for different beginning time  $t_0$  and actuator position  $r_p$ .



**Figure S3.** Wound healing time dependence on actuator position  $r_p$  for different  $\Delta t$  and  $t_0$ 



**Figure S4.** Wound healing time dependence on the ion pump position  $x_p$ , plots for different beginning time  $t_0$ ,  $\Delta t = 1$  day



**Figure S5.** Sensitivity of the model to variation of parameters. Wound healing model simulations were performed without actuator. Wound healing time dependence on the parameters is shown. Each plot corresponds to variation of one parameter, while other parameters were set as in table 1. Red frame marks the main scenario shown in Figure 2 of the main text.



**Figure S6.** Sensitivity of the model results to variation of parameter  $\tilde{D}$ . Wound healing time dependence on: (A) treatment beginning time  $t_0$  ( $\Delta t = 1$  d,  $r_p = 0.9$  mm); (B) treatment duration  $\Delta t$  ( $t_0 = 8$ h,  $r_p = 0.9$  mm); (C) actuator position  $r_p$  ( $t_0 = 0$ ,  $\Delta t = 1$ d 16h).



**Figure S7.** Parametric plane of optimal treatment regimes for several selections of the thresholds: green crosses – the safe and beneficial regimes of treatment; red squares – wound cleaning (defined as time when debris a < threshold is reached) takes longer time than wound healing; blue diamonds – wound healing time is diminished less than estimated percent in comparison with non-treated wound (compare to Figure 7 of the manuscript).