## Development of three validating wheat populations

RL6058 was crossed with BQM in May 2015 using BQM as pollen donor. In mid-October 2016, 700  $F_2$  seeds were sown in 5-mL centrifuge tubes filled with moist soil with a single germinated seed in each tube, and maintained in growth chambers at  $5 \pm 2$  °C with a relative humidity higher than 70%. The DNA samples extracted from these seedlings were subjected to a selection based on the marker cfd188 for *QLr.cau-6DL* and the DNA marker *cssfr5* for *Lr34*. This selection resulted in four groups of QTL combination, namely, the  $F_2$  seedlings with positive states for both cfd188 and *cssfr5* (representing *QLr.cau-6DL* + *Lr34*), positive states for cfd188 and negative states for *cssfr5* (*QLr.cau-6DL*), negative states for cfd188 and positive states for *cssfr5* (*Lr34*), and negative states for both cfd188 and *cssfr5* (None). From each of the four QTL combination groups, 20  $F_2$  seedlings were kept to the adult plant growth stage and they were self-pollinated in mid-May 2017 to produce  $F_{2:3}$  family seeds.

Likewise, in mid-October 2016, 100 BC $_3F_2$  seeds derived from the cross AK58  $\times$  BQM (Figure S1) were sown in 5-mL centrifuge tubes, and DNA samples from these seedlings were selected for *QLr.cau-6DL* based on the marker cfd188. Five seedlings that were positive for cfd188 (R-group) and another five seedlings that were negative for cfd188 (S-group) were kept to the adult plant growth stage and they were self-pollinated in mid-May 2017 to produce BC $_3F_{2:3}$  family seeds. In the same way, R-group and S-group BC $_3F_{2:3}$  family seeds were obtained from the cross JM22  $\times$  BQM (Figure S1).

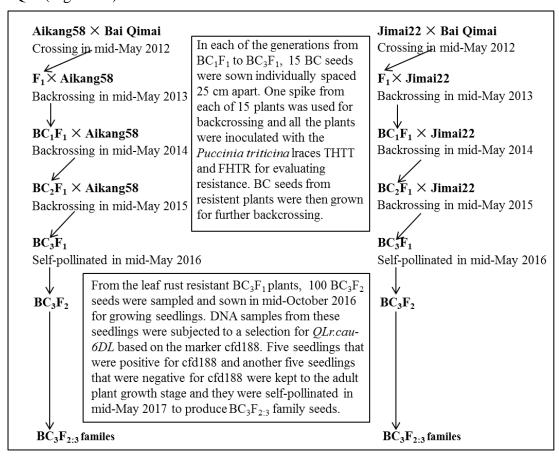


Figure S1. Development of two backcross populations.