

Supplementary Material

1 Supplementary Figures and Tables

1.1 Supplementary Figures

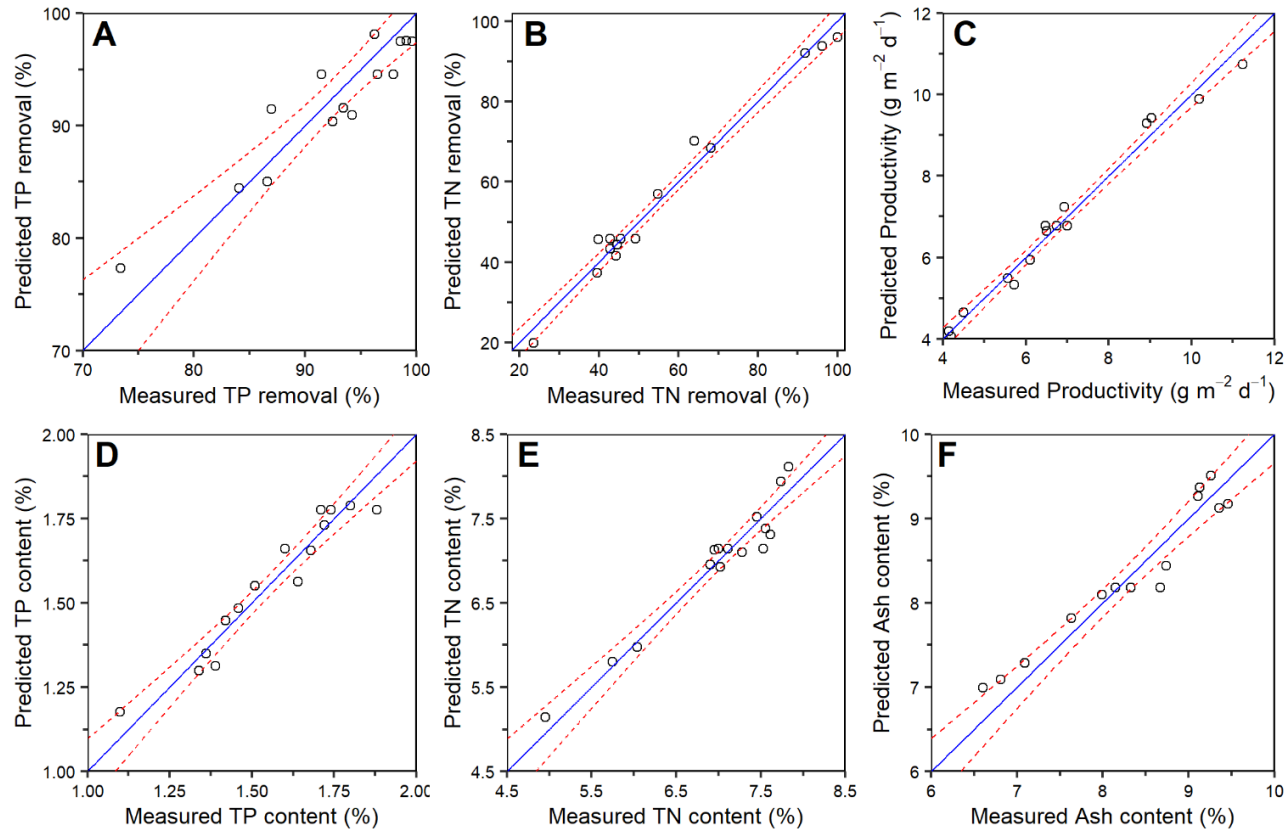
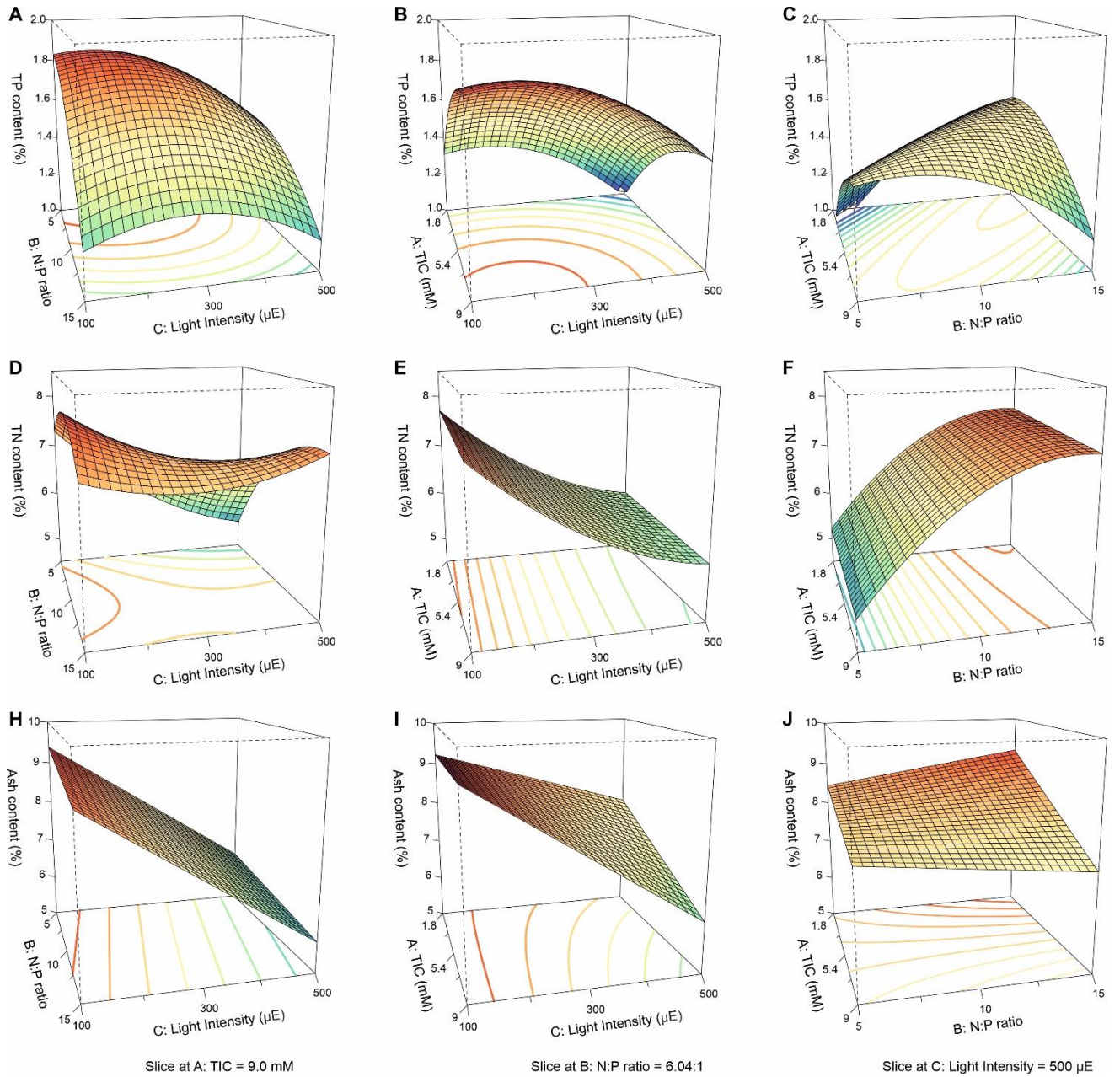


Figure S 1. Recovery rates of predicted and measured dependent variables. Tested were (A) Phosphorus and (B) Nitrogen removal from the medium. And the biomass (C) productivity, and its (D) phosphorus, (E) nitrogen, and (F) ash content, respectively. (—) full recovery of 100%, (- - -) Regression line with 95% confidence interval.



19 **1.2 Supplementary Tables**

20 **Table S 1.** Transfer of atmospheric CO₂ into the culture medium by bubbling.

CO ₂ concentration C _{CO2} (ppm)	CO ₂ volume by bubbling V _{CO2} (mL) = C ÷ 10 ⁶ × 50 mL min ⁻¹ × 10080 min	CO ₂ amount N _C (mmol) = V _{CO2} ÷ 22.4 L mol ⁻¹	CO ₂ molarity c _{CO2} (mM) = N _C ÷ 5 L
407.0	205.13	9.16	1.8
1203.5	606.56	27.08	5.4
2000.0	1008.00	45.00	9.0

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Table S 2. BBD experimental data of the independent variables (coded factors) and of the dependent variables (responses). Data are presented in mean $\pm$ SE (n = 3). TP, Total phosphorus; TN, Total nitrogen.

Run	Coded factors			Responses					
	A	B	C	TP removal (%)	TN removal (%)	Productivity (g m ⁻² d ⁻¹)	TP content (%)	TN content (%)	Ash content (%)
1	-1	-1	0	92.5 $\pm$ 0.88	96.2 $\pm$ 2.38	5.72 $\pm$ 0.39	1.09 $\pm$ 0.04	6.04 $\pm$ 0.21	8.74 $\pm$ 0.11
2	1	-1	0	84.0 $\pm$ 0.84	100 $\pm$ 0	6.49 $\pm$ 0.51	1.79 $\pm$ 0.01	5.74 $\pm$ 0.08	7.63 $\pm$ 0.11
3	-1	1	0	98.5 $\pm$ 0.81	42.8 $\pm$ 2.52	6.09 $\pm$ 0.39	1.71 $\pm$ 0.13	6.94 $\pm$ 0.09	9.45 $\pm$ 0.35
4	1	1	0	93.4 $\pm$ 1.22	39.8 $\pm$ 4.29	6.93 $\pm$ 0.48	1.38 $\pm$ 0.16	6.90 $\pm$ 0.29	7.09 $\pm$ 0.85
5	-1	0	-1	94.2 $\pm$ 1.08	44.5 $\pm$ 2.15	4.14 $\pm$ 0.36	1.63 $\pm$ 0.05	7.82 $\pm$ 0.18	9.25 $\pm$ 0.17
6	1	0	-1	86.6 $\pm$ 2.24	39.5 $\pm$ 4.90	5.56 $\pm$ 0.61	1.60 $\pm$ 0.03	7.74 $\pm$ 0.19	9.36 $\pm$ 0.10
7	-1	0	1	98.7 $\pm$ 0.28	54.7 $\pm$ 5.36	9.02 $\pm$ 0.72	1.35 $\pm$ 0.08	7.27 $\pm$ 0.00	7.98 $\pm$ 0.20
8	1	0	1	96.2 $\pm$ 2.27	68.1 $\pm$ 8.88	11.2 $\pm$ 0.46	1.42 $\pm$ 0.13	7.01 $\pm$ 0.07	6.35 $\pm$ 0.19
9	0	-1	-1	73.4 $\pm$ 2.34	64.0 $\pm$ 4.38	4.18 $\pm$ 0.34	1.68 $\pm$ 0.25	7.56 $\pm$ 0.32	9.11 $\pm$ 0.30
10	0	1	-1	86.9 $\pm$ 1.16	23.5 $\pm$ 3.01	4.49 $\pm$ 0.24	1.50 $\pm$ 0.10	7.61 $\pm$ 0.07	9.13 $\pm$ 0.47
11	0	-1	1	99.6 $\pm$ 0.37	91.9 $\pm$ 1.41	8.92 $\pm$ 0.28	1.34 $\pm$ 0.08	4.94 $\pm$ 0.05	6.59 $\pm$ 0.26
12	0	1	1	99.1 $\pm$ 0.88	44.2 $\pm$ 3.47	10.1 $\pm$ 0.48	1.45 $\pm$ 0.21	7.44 $\pm$ 0.05	6.81 $\pm$ 0.30
13	0	0	0	97.9 $\pm$ 0.85	49.2 $\pm$ 6.46	6.46 $\pm$ 0.56	1.71 $\pm$ 0.22	6.99 $\pm$ 0.18	8.33 $\pm$ 1.13
14	0	0	0	96.4 $\pm$ 0.73	45.3 $\pm$ 2.30	6.73 $\pm$ 0.13	1.73 $\pm$ 0.12	7.52 $\pm$ 0.02	8.15 $\pm$ 0.21
15	0	0	0	91.4 $\pm$ 2.40	42.7 $\pm$ 4.17	6.99 $\pm$ 0.82	1.87 $\pm$ 0.15	7.10 $\pm$ 0.06	8.67 $\pm$ 0.09

26 **Table S 3.** Results under high light (1000 μE) and optimized growth conditions of TIC (9 mM) and
 27 N:P ratio (6.04, TP 10 mg L^{-1}). Data are presented as mean $\pm$ standard error (SE, $n = 3$). TP, Total
 28 phosphorus; TN, Total nitrogen.

Responses	Experimental (mean $\pm$ SE)	Independent t-test p^*
TP removal (%)	96.05 $\pm$ 1.09	0.496
TN removal (%)	92.75 $\pm$ 0.41	0.067
Productivity ($\text{g m}^{-2} \text{d}^{-1}$)	10.96 $\pm$ 0.35	0.445

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