

Supplementary Material

1 SUPPLEMENTARY TABLES

In this section we list the important results of the calculations in tabular form. Listed in Table S1 are the calculated lattice constants, cohesive energy, and formation energy of the considered Heusler compounds. Table S2 lists the calculated magnetic ground state, total spin moment, atomic spin magnetic moments, magnetization energy, spin polarization, Curie temperature, as well as the total magnetization derived by Slater-Pauling rule. Mechanical properties of the Heusler compounds are listed in Table S3, it includes elastic constants, bulk modulus B , shear modulus G , Young's modulus E , anisotropy factor A , Poisson's ratio ν , and Pugh's ratio B/G . Table S4 lists calculated thermodynamics related results such as the density ρ , longitudinal v_l , transverse v_t , average v_m sound velocity, Debye temperature Θ_D , melting temperature T_m , and minimum thermal conductivity κ_{min} .

Table S1. Calculated equilibrium lattice constant (Å), cohesive energy (eV/f.u.), and formation energy (eV/f.u.) of X_2YZ Heusler alloys. L2₁ and XA denote the normal and inverse structure, respectively.

X_2YZ	structure	lattice constant Å			cohesive energy eV/f.u.			formation energy eV/f.u.		
		Z= Al	Ga	Si	Z= Al	Ga	Si	Z= Al	Ga	Si
Fe ₃ Z	L2 ₁	5.736	5.750	5.601	19.870	18.691	21.449	-0.924	-0.603	-1.479
Fe ₂ CrZ	L2 ₁	5.658	5.680	5.583	18.621	17.297	20.074	-1.131	-0.665	-1.561
	XA	5.785	5.810	5.649	18.257	17.222	19.973	-0.768	-0.590	-1.460
Cr ₂ FeZ	L2 ₁	5.889	5.845	5.687	16.513	15.505	17.882	-0.480	-0.330	-0.825
	XA	5.754	5.777	5.616	17.102	15.916	18.795	-1.069	-0.740	-1.738
Cr ₃ Z	L2 ₁	5.909	5.917	5.726	15.809	14.783	17.475	-1.233	-1.064	-1.874
Fe ₂ MnZ	L2 ₁	5.668	5.692	5.582	18.553	17.318	20.231	-0.939	-0.561	-1.593
	XA	5.730	5.724	5.589	18.318	17.006	19.986	-0.703	-0.248	-1.347
Mn ₂ FeZ	L2 ₁	5.705	5.729	5.623	16.757	15.640	15.189	-0.473	-0.214	2.119
	XA	5.743	5.772	5.577	17.175	16.048	14.797	-0.891	-0.622	2.510
Mn ₃ Z	L2 ₁	5.787	5.814	5.641	15.778	14.709	17.664	-0.826	-0.614	-1.687
Fe ₂ CoZ	L2 ₁	5.726	5.756	5.583	19.744	18.541	21.104	-0.744	-0.399	-1.081
	XA	5.700	5.720	5.602	20.213	18.970	21.687	-1.214	-0.828	-1.664
Co ₂ FeZ	L2 ₁	5.699	5.717	5.623	20.636	19.343	21.684	-1.583	-1.147	-1.607
	XA	5.686	5.717	5.577	19.941	18.692	21.293	-0.887	-0.496	-1.215
Co ₃ Z	L2 ₁	5.672	5.693	5.578	20.148	18.854	21.338	-1.041	-0.604	-1.207

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- Ahmad A, Mitra S, Srivastava S, Das A. Structural, magnetic, and magnetocaloric properties of fe2coal heusler nanoalloy. *Journal of Magnetism and Magnetic Materials* **540** (2021) 168449.
- Du Y, Xu G, Zhang X, Liu Z, Yu S, Liu E, et al. Crossover of magnetoresistance in the zero-gap half-metallic heusler alloy fe2cosi. *EPL (Europhysics Letters)* **103** (2013) 37011.

Table S2. Calculated magnetic ground state, total spin magnetization (m_t), atomic spin magnetization ($m_{X(1)}$, $m_{X(2)}$, m_Y and m_Z for X(1), X(2), Y, and Z atom, respectively), total magnetization $M_t = N_v - 24$ given from Slater-Pauling rule, magnetization energy $E_M = E_{FM} - E_{NM}$, spin polarization P and Curie temperature T_c . FM, Fi, AHM, and HM are ferromagnetic, ferrimagnetic, antiferromagnetic, and half-metallic metal, respectively. L2₁ and XA denote the normal and inverse structure, respectively.

X ₂ YZ	structure	mag. state	m_t $\mu_B/\text{f.u.}$	$m_{X(1)}$	$m_{X(2)}$ μ_B/atom	m_Y	m_Z	M_t $\mu_B/\text{f.u.}$	E_M eV/f.u.	P %	T_c K
Fe ₃ Al	L2 ₁	FM	5.95	1.87	1.87	2.38	-0.06	3	-1.1018	-48.875	710 (713 ^b)
Fe ₂ CrAl	L2 ₁	Fi2	1.00	-0.10	-0.10	1.19	-0.01	1	-0.0724	98.385	93
	XA	Fi3	2.38	1.74	2.38	-1.68	-0.01	1	-0.8937	-30.323	1152
Cr ₂ FeAl	L2 ₁	Fi2	0.94	1.68	1.68	-2.60	-0.01	1	-0.6649	-46.581	857
	XA	Fi2	1.01	1.49	-1.17	0.67	-0.00	1	-0.1149	-96.599	148
Cr ₃ Al	L2 ₁	Fi2	2.92	2.22	2.22	-1.64	-0.01	3	-0.4313	-66.422	278
Fe ₂ MnAl	L2 ₁	Fi2	2.00	-0.18	-0.18	2.34	-0.01	2	-0.5970	78.925	770
	XA	Fi3	1.95	1.43	2.32	-1.74	-0.00	2	-0.7960	43.716	1026
Mn ₂ FeAl	L2 ₁	Fi2	-0.96	0.74	0.74	-2.45	-0.03	1	-0.6163	-90.811	795
	XA	Fi1	1.00	-1.76	2.63	0.13	0.01	1	-0.4782	99.416	617
Mn ₃ Al	L2 ₁	AF-HM	0.00	-1.40	-1.40	2.79	0.02	0	-0.4804	100.000	309 (342 ^a)
Fe ₂ CoAl	L2 ₁	FM	5.68	2.03	2.03	1.77	-0.04	4	-0.8675	-57.675	1119
	XA	FM	4.98	1.59	2.53	1.03	-0.05	4	-1.2235	-54.334	1578 (830 ^c)
Co ₂ FeAl	L2 ₁	FM	4.99	1.19	1.19	2.76	-0.03	5	-1.4923	79.433	1924 (1261 ^c)
	XA	FM	4.51	1.00	1.75	1.92	-0.03	5	-0.7502	-55.171	967
Co ₃ Al	L2 ₁	FM	4.00	1.23	1.23	1.69	-0.03	6	-0.7049	-68.590	454
Fe ₃ Ga	L2 ₁	FM	6.05	1.89	1.89	2.42	-0.15	3	-1.2222	-48.428	788
Fe ₂ CrGa	L2 ₁	Fi2	1.00	-0.16	-0.16	1.30	-0.02	1	-0.1184	99.082	153
	XA	Fi3	2.23	1.76	2.48	-1.99	-0.03	1	-1.0320	-38.511	1331
Cr ₂ FeGa	L2 ₁	FM	5.00	1.78	1.78	1.33	-0.02	1	-0.5965	97.270	769
	XA	Fi2	0.99	1.70	-1.39	0.67	0.01	1	-0.1482	-96.130	191
Cr ₃ Ga	L2 ₁	Fi2	2.87	2.27	2.27	-1.75	-0.00	3	-0.4692	-35.693	303
Fe ₂ MnGa	L2 ₁	Fi2	2.03	-0.26	-0.25	2.48	-0.02	2	-0.7122	75.072	917
	XA	Fi3	2.01	1.53	2.38	-1.87	-0.01	2	-0.8738	59.656	1127
Mn ₂ FeGa	L2 ₁	Fi2	-0.99	0.79	0.79	-2.53	-0.04	1	-0.7104	-89.173	916
	XA	Fi1	1.03	-2.03	2.78	0.24	-0.00	1	-0.6920	96.560	892
Mn ₃ Ga	L2 ₁	AF-HM	0.01	-1.53	-1.53	2.99	0.05	0	-0.7105	100.000	458 (482 ^a)
Fe ₂ CoGa	L2 ₁	FM	5.96	2.17	2.17	1.75	-0.11	4	-0.9114	-72.853	1175
	XA	FM	5.13	1.68	2.57	1.01	-0.13	4	-1.3053	-40.000	1683
Co ₂ FeGa	L2 ₁	FM	5.00	1.17	1.17	2.77	-0.10	5	-1.5135	74.957	1952
	XA	FM	4.80	1.09	1.73	2.11	-0.10	5	-0.7685	-66.488	991
Co ₃ Ga	L2 ₁	FM	4.06	1.25	1.25	1.70	-0.08	6	-0.6843	-70.627	441
Fe ₃ Si	L2 ₁	FM	5.04	1.30	1.30	2.53	-0.05	4	-1.0999	-39.975	709 (840 ^b)
Fe ₂ CrSi	L2 ₁	FM-HM	2.00	0.25	0.25	1.51	-0.02	2	-0.2861	100.000	369
	XA	Fi3	2.03	0.93	2.35	-1.27	0.02	2	-0.7130	41.296	919
Cr ₂ FeSi	L2 ₁	Fi2	0.75	-0.82	-0.82	2.33	0.06	2	-0.5936	2.475	765
	XA	NM	0.00					2	0.0000	0.000	
Cr ₃ Si	L2 ₁	Fi2	1.86	1.39	1.39	-0.96	-0.02	4	-0.0557	-36.808	72
Fe ₂ MnSi	L2 ₁	FM-HM	3.00	0.22	0.22	2.53	-0.01	3	-0.9088	100.000	1172
	XA	Fi3	3.06	0.88	2.34	-0.18	0.01	3	-0.6109	83.322	788
Mn ₂ FeSi	L2 ₁	FM	5.47	1.34	1.34	2.79	0.01	2	-1.2635	-58.811	1629
	XA	FM	3.97	0.90	1.59	1.58	-0.03	2	-0.5580	-58.333	720
Mn ₃ Si	L2 ₁	Fi2-HM	1.00	-0.81	-0.81	2.54	0.04	1	-0.4731	100.000	305
Fe ₂ CoSi	L2 ₁	FM	4.37	1.39	1.39	1.70	-0.04	5	-0.4714	-78.869	608
	XA	FM	4.96	1.38	2.65	1.00	-0.03	5	-1.3151	76.749	1696 (1038 ^d)
Co ₂ FeSi	L2 ₁	FM	5.47	1.34	1.34	2.79	0.01	6	-1.2635	-58.811	1629 (1267 ^a)
	XA	FM	3.97	0.90	1.59	1.58	-0.03	6	-0.5580	-58.333	720
Co ₃ Si	L2 ₁	FM	3.80	1.21	1.21	1.47	-0.02	7	-0.4630	-65.662	298

^a Theoretical Curie temperature from Kübler (2006). ^b Experimental Curie temperature from Burch et al. (1979). ^c Experimental Curie temperature from Ahmad et al. (2021). ^d Theoretical Curie temperature from Du et al. (2013)

Table S3. Calculated elastic constants C_{ij} , bulk modulus B , Voigt shear modulus G_V , Reuss shear modulus G_R , shear modulus G , Young's modulus E (GPa), anisotropy factor A , Poisson's ratio ν , and Pugh's ratio B/G for the Heusler compounds. L2₁ and XA denote the normal and inverse structure, respectively.

X_2YZ	structure	C_{11}	C_{12}	C_{44}	B	G_V	G_R	G	E	A	ν	B/G
					GPa							
								arbitrary unit				
Fe ₃ Al	L2 ₁	213.1	154.9	138.7	174.3	94.9	55.3	75.1	197.0	4.8	0.31	2.3
Fe ₂ CrAl	L2 ₁	366.7	139.7	120.0	215.3	117.4	117.3	117.3	297.9	1.1	0.27	1.8
	XA	176.6	124.4	138.0	141.8	93.2	50.8	72.0	184.8	5.3	0.28	2.0
Cr ₂ FeAl	L2 ₁	238.8	136.7	134.5	170.7	101.1	81.3	91.2	232.3	2.6	0.27	1.9
	XA	277.6	121.9	108.7	173.8	96.4	93.8	95.1	241.3	1.4	0.29	1.8
Cr ₃ Al	L2 ₁	252.7	71.2	106.1	131.7	100.0	99.4	99.7	238.8	1.2	0.20	1.3
Fe ₂ MnAl	L2 ₁	309.6	136.5	166.7	194.2	134.6	121.7	128.2	315.1	1.9	0.23	1.5
	XA	208.5	112.3	145.5	144.4	106.5	80.4	93.4	230.6	3.0	0.23	1.5
Mn ₂ FeAl	L2 ₁	221.7	168.3	148.6	186.1	99.8	52.6	76.2	201.2	5.6	0.32	2.4
	XA	186.7	128.7	116.2	148.0	81.3	52.7	67.0	174.7	4.0	0.30	2.2
Mn ₃ Al	L2 ₁	119.1	151.6	108.0	140.8	58.3	-52.6	2.8	8.4	-6.6	0.49	50.0
Fe ₂ CoAl	L2 ₁	125.3	153.5	110.3	144.1	60.6	-43.6	8.5	24.9	-7.8	0.47	17.0
	XA	241.9	148.8	139.8	179.8	102.5	77.6	90.1	231.5	3.0	0.29	2.0
Co ₂ FeAl	L2 ₁	264.5	148.3	140.7	187.0	107.7	89.7	98.7	251.8	2.4	0.28	1.9
	XA	160.1	161.0	119.5	160.7	71.5	-1.1	35.2	98.4	-266.7	0.40	4.6
Co ₃ Al	L2 ₁	210.8	163.9	127.6	179.5	86.0	46.0	66.0	176.3	5.4	0.34	2.7
Fe ₃ Ga	L2 ₁	181.9	165.7	127.3	171.1	79.6	18.5	49.1	134.4	15.7	0.37	3.5
Fe ₂ CrGa	L2 ₁	338.1	158.5	109.6	218.4	101.6	100.7	101.2	262.9	1.2	0.30	2.2
	XA	172.6	129.7	132.3	144.0	88.0	43.1	65.5	170.7	6.2	0.30	2.2
Cr ₂ FeGa	L2 ₁	250.7	159.3	139.0	189.8	101.7	76.5	89.1	231.1	3.0	0.30	2.1
	XA	231.9	129.1	94.1	163.4	77.0	70.6	73.8	192.4	1.8	0.30	2.2
Cr ₃ Ga	L2 ₁	239.7	84.4	99.4	136.2	90.7	89.4	90.1	221.4	1.3	0.23	1.5
Fe ₂ MnGa	L2 ₁	289.3	148.0	158.0	195.1	123.1	105.7	114.4	287.1	2.2	0.25	1.7
	XA	182.9	122.2	141.3	142.4	96.9	57.4	77.2	196.1	4.7	0.27	1.8
Mn ₂ FeGa	L2 ₁	164.2	122.3	156.5	136.3	102.3	43.6	73.0	185.7	7.5	0.27	1.9
	XA	159.7	133.8	113.6	142.4	73.4	27.7	50.5	135.5	8.8	0.34	2.8
Mn ₃ Ga	L2 ₁	133.1	159.9	107.6	151.0	59.2	-41.1	9.0	26.6	-8.0	0.47	16.7
Fe ₂ CoGa	L2 ₁	133.2	160.7	92.2	151.5	49.8	-44.3	2.7	8.2	-6.7	0.49	55.4
	XA	197.3	154.8	132.4	168.9	87.9	42.8	65.4	173.7	6.2	0.33	2.6
Co ₂ FeGa	L2 ₁	253.7	161.1	129.8	192.0	96.4	75.4	85.9	224.3	2.8	0.31	2.2
	XA	152.2	169.5	106.9	163.8	60.7	-24.6	18.0	52.2	-12.4	0.45	9.1
Co ₃ Ga	L2 ₁	205.3	170.5	113.7	182.1	75.2	35.4	55.3	150.7	6.5	0.36	3.3
Fe ₃ Si	L2 ₁	295.6	184.7	142.4	221.7	107.6	87.5	97.6	255.2	2.6	0.31	2.3
Fe ₂ CrSi	L2 ₁	198.1	260.2	127.3	239.5	63.9	-122.5	-29.3	-91.5	-4.1	0.56	-8.2
	XA	260.9	156.6	142.0	191.4	106.1	84.0	95.1	244.7	2.7	0.29	2.0
Cr ₂ FeSi	L2 ₁	202.8	164.8	140.1	177.5	91.7	39.5	65.6	175.1	7.4	0.34	2.7
	XA	360.9	194.6	80.6	250.0	81.7	81.6	81.6	220.9	1.0	0.35	3.1
Cr ₃ Si	L2 ₁	251.4	134.3	112.9	173.3	91.2	82.3	86.7	223.0	1.9	0.29	2.0
Fe ₂ MnSi	L2 ₁	242.7	233.2	168.9	236.4	103.2	11.5	57.4	159.2	35.4	0.39	4.1
	XA	320.3	179.3	157.3	226.3	122.6	105.4	114.0	292.8	2.2	0.28	2.0
Mn ₂ FeSi	L2 ₁	244.2	180.7	131.0	201.8	91.3	58.2	74.8	199.6	4.1	0.34	2.7
	XA	228.5	197.4	117.8	207.8	76.9	32.4	54.6	150.7	7.6	0.38	3.8
Mn ₃ Si	L2 ₁	294.8	168.3	131.7	210.4	104.3	91.9	98.1	254.8	2.1	0.30	2.1
Fe ₂ CoSi	L2 ₁	213.5	205.9	107.8	208.4	66.2	9.0	37.6	106.4	28.4	0.41	5.5
	XA	293.4	186.6	139.1	222.2	104.8	84.7	94.8	248.9	2.6	0.31	2.3
Co ₂ FeSi	L2 ₁	244.2	180.7	131.0	201.8	91.3	58.2	74.8	199.6	4.1	0.34	2.7
	XA	228.5	197.4	117.8	207.8	76.9	32.4	54.6	150.7	7.6	0.38	3.8
Co ₃ Si	L2 ₁	215.7	208.2	116.6	210.7	71.5	9.0	40.2	113.5	30.9	0.41	5.2

Table S4. Calculated density ρ (g/cm³) longitudinal v_l (m/s²), transverse v_t (m/s²), average v_m (m/s²) sound velocity, Debye Θ_D (K), melting T_m (K) temperature, and thermal conductivity κ_{min} (W/mK) from the elastic moduli of the Heusler compounds. Here, we exclude mechanically unstable compounds as shown in Table S3. L2₁ and XA denote the normal and inverse structure, respectively.

Compounds	structure	ρ g/cm ³	v_l m/s ²	v_t m/s ²	v_m m/s ²	Θ_D K	T_m ± 300 K	κ_{min} W/mK
Fe ₃ Al	L2 ₁	6.845	6332	3312	2464	347	1792	1.744
Fe ₂ CrAl	L2 ₁	6.997	7290	4095	3005	429	2700	2.181
	XA	6.543	6029	3318	2445	342	1577	1.699
Cr ₂ FeAl	L2 ₁	6.077	6936	3874	2846	391	1944	1.907
	XA	6.519	6791	3819	2802	394	2174	1.967
Cr ₃ Al	L2 ₁	5.893	6701	4113	2956	404	2026	1.951
Fe ₂ MnAl	L2 ₁	7.061	7190	4260	3089	440	2363	2.224
	XA	6.843	6270	3696	2683	378	1765	1.893
Mn ₂ FeAl	L2 ₁	6.814	6498	3344	2495	352	1843	1.772
	XA	6.762	5925	3149	2336	329	1636	1.649
Fe ₂ CoAl	XA	7.085	6506	3565	2629	373	1963	1.882
Co ₂ FeAl	L2 ₁	7.208	6648	3700	2720	386	2096	1.948
Co ₃ Al	L2 ₁	7.417	6005	2982	2237	319	1779	1.621
Fe ₃ Ga	L2 ₁	8.277	5346	2434	1849	260	1608	1.302
Fe ₂ CrGa	L2 ₁	8.460	6462	3459	2562	365	2531	1.848
	XA	7.908	5409	2879	2135	297	1553	1.473
Cr ₂ FeGa	L2 ₁	7.642	6354	3414	2527	350	2015	1.723
	XA	7.902	5756	3057	2268	317	1904	1.581
Cr ₃ Ga	L2 ₁	7.244	5947	3526	2556	349	1950	1.690
Fe ₂ MnGa	L2 ₁	8.515	6389	3665	2677	380	2243	1.917
	XA	8.370	5414	3036	2228	315	1614	1.580
Mn ₂ FeGa	L2 ₁	8.322	5297	2961	2175	307	1503	1.540
	XA	8.135	5078	2491	1873	262	1477	1.310
Fe ₂ CoGa	XA	8.504	5488	2773	2075	293	1699	1.475
Co ₂ FeGa	L2 ₁	8.657	5950	3150	2338	331	2032	1.666
Co ₃ Ga	L2 ₁	8.875	5369	2496	1890	268	1746	1.360
Fe ₃ Si	L2 ₁	7.393	6898	3633	2699	389	2280	2.003
Fe ₂ CrSi	XA	7.073	6706	3666	2705	387	2075	1.973
Cr ₂ FeSi	L2 ₁	6.685	6295	3132	2349	332	1732	1.676
	XA	7.054	7133	3401	2567	370	2666	1.899
Cr ₃ Si	L2 ₁	6.531	6652	3644	2688	380	2019	1.910
Fe ₂ MnSi	L2 ₁	7.440	6484	2776	2123	307	1967	1.588
	XA	7.412	7144	3921	2891	418	2426	2.153
Mn ₂ FeSi	L2 ₁	7.553	6318	3146	2359	344	1976	1.789
	XA	7.726	6027	2660	2028	298	1883	1.561
Mn ₃ Si	L2 ₁	7.151	6908	3704	2743	393	2275	2.009
Fe ₂ CoSi	L2 ₁	7.582	5840	2227	1721	249	1795	1.285
	XA	7.514	6811	3551	2643	381	2267	1.963
Co ₂ FeSi	L2 ₁	7.553	6318	3146	2359	340	1976	1.741
	XA	7.726	6027	2660	2028	294	1883	1.519
Co ₃ Si	L2 ₁	7.836	5808	2265	1747	253	1808	1.307