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Scaling factors for 1-D ground response amplification in a soft soil basin

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Basin presence is believed to affect the ground surface response due to earthquakes, particularly in areas around the basin edge. Previous studies showed that 1-D and 2-D wave propagation analyses resulted in significant differences in amplification at the basin edge. However, the link between 1-D and 2-D responses has not been studied for engineering practices. In practical application, seismic studies were commonly performed using 1-D analysis, for example, to develop a city micro-zonation map. Based on practical considerations, it is necessary to estimate the scaling factor for the 1-D analysis by considering the basin presence, particularly for one containing soft soil. There are three stages carried out in this study. The first stage: collecting data on some basin geometries for the 2-D modeling references and then defining selected site class and input motions. The second stage: modeling 1-D and 2-D wave propagation using D-MOD and Fast Lagrangian Analysis of Continua (FLAC), respectively. The third stage: comparing spectral acceleration resulting from the 1-D and 2-D analyses to obtain the scaling factors. This research studied and reported the relationship between PGA values varied as 0.2 g, 0.3 g, 0.4 g, and 0.5 g, basin geometry (e.g., the angle was set to 5°, 10°, 15°, 30°, and 45°, with depth and width variations of 0.0125, 0.025, 0.05, 0.075, 0.1, 0.2, and 0.4, while the basin width was adjusted to 500 m, 1 km, 2 km, and 4 km), and the spectral acceleration in several observation points on the ground surface. Based on this evaluation, a series of scaling factors are proposed. These factors can be used for spectral acceleration from available hazard maps, commonly developed based on 1-D analysis. The application example of this scaling factor is presented in this study, using the Bandung Basin case.

KEYWORDS

basin, basin edge, D-MOD 2000, earthquake response, FLAC, scaling factor, spectral acceleration

1 Introduction

Body waves propagate from an earthquake source at fault in a bedrock to all directions. At the interface between soil or rock layers, the waves can be forwarded or reflected (Figure 1A). The waves eventually reach the surface and introduce ground surface motion. The presence of the basin results in complexity in wave propagation, particularly from the bedrock to the surface around the basin edge (Figure 1B).

The presence of the basin introduces a combination of entrapment and reverberation of seismic waves on the soft sedimentary deposits above the bedrock basin surface (Ayoubi, 2018).





Mexico City, which is located above a soft soil sedimentary basin, experienced significant damages associated with the 1985 Michoacán earthquake. It is believed that this 8.1 M_w earthquake resulted in a relatively large amplification of seismic waves and a long duration of ground motion in a sedimentary basin of Mexico City. The bowl-like shape of the basin containing soft alluvial soil can trap body waves, causing some of the incoming body waves to propagate through the soil as surface waves (Kramer, 1996). These surface waves produce stronger and longer shocks than body waves.

The effect of basin geometry on ground response acceleration has been investigated using the 1-D, 2-D, and 3-D wave propagation analysis methods. Bard and Gariel (1986) studied the basin effect on ground motion by comparing amplification at the edge and the center of the basin resulting from the 1-D and 2-D methods. They reported significant differences in the amplification from these methods, particularly in the long period. Bakir et al. (2002) compared 1-D and 2-D methods for evaluating the presence of the basin using the 1995 Dinar earthquake in Turkey. They described the possible explanation about effects of the basin edge on spectral acceleration using 1-D and 2-D analyses. The results showed that the 1-D analysis did not predict the spectral response in heavily damaged areas, located at the basin edge. They proposed the 2-D and 3-D methods to eliminate the shortcomings of the 1-D method, particularly at the basin edge. The amplification from the 1-D analysis needs to be adjusted or scaled using that of the 2-D and 3-D analyses.

The 2-D and 3-D methods are commonly more suitable for the basin area than the 1-D method. Nevertheless, the 1-D method is more popular in the engineering practice community due to several reasons. This method requires less computational resources and calculation time than the 2-D and 3-D methods. Additionally, the 1-D method is more readily available than the others. This method has been extensively used



for developing micro-zonation maps for various cities in Indonesia. The current Indonesian micro-zonation maps should be used cautiously if it is implemented in the basin area.

In this study, the 1-D and 2-D methods were applied to a basin area containing site Class E soft soil. The effects of PGA, basin inclination or angle, and basin depth to width ratio on the ground surface acceleration response, particularly around the basin edge, were assessed using these methods. The amplification results from these methods were compared and evaluated to propose scaling factors. These scaling factors can be used to facilitate engineering practice to evaluate the ground response located around the basin, where the 1-D method is immediately available, but 2-D and 3-D methods are not accessible. Examples of scaling factor application in a 1-D-based micro-zonation map of Bandung, Indonesia, which is located on a basin, are presented in this study.

2 Basin effect on ground acceleration response

2.1 Ground response analysis

Ground surface response analysis is commonly used to solve many geotechnical earthquake engineering problems. For instance, it can be used to develop a design spectral response. Additionally, it is applied to assess liquefaction potential. This analysis is also important to evaluate the stability of soil embankments and retaining wall structures during an earthquake. Ground surface response analysis can be performed using a simple 1-D method or even more complex approaches, such as the 2-D and 3-D methods. To assist with the calculation, a variety of free and commercial license computer programs are available. In this study, the 1-D analysis was performed using D-MOD 2000 (Matasovic and Ordonez, 2007), a non-linear effective stress ground response computer program. Soil non-linear response is expressed by a backbone curve with an inelastic behavior following the unloading-reloading of extended Masing rules (Pyke, 1979). This program can evaluate time-dependent pore water pressure and its effect on soil stiffness during earthquakes. Pore water pressure for sand and clay is regulated by semi-empirical models developed by Vucetic and Dobry (1988) and Matasovic and Vucetic (1995), respectively.

Although the 1-D site response method is widely used in geotechnical engineering practice, not all cases can be analyzed using the 1-D method. Complicated cases, including the presence of inclined/irregular ground surfaces, embedded structures, walls, and tunnels, demand 2-D or even 3-D methods. Ground response analysis around a basin edge also generally requires 2-D or 3-D methods (e.g., Bakir et al., 2002).

In this study, 2-D ground response analysis was conducted using the Fast Lagrangian Analysis of Continua (FLAC) computer program (Itasca, 2008). FLAC analyzes soil behavior based on explicit finite differences. The soil is modeled as a collection of discrete elements. Each element is defined by nodal points. The soil response is represented by nodal points. The behavior of each element follows linear or non-linear stress–strain laws defined in response to boundary conditions or to applied forces.

2.2 Previous studies

The effect of basin geometry on ground response has been studied by King and Tucker (1984). They measured ground motion along the transverse and longitudinal profiles across the

No	Basin	Width, <i>W</i> (m)	Depth, <i>D</i> (m)	D/ W	Angle of basin, θ (°) (1)	Angle of basin, θ (°) (2)	Source	Description	Site class
1	Caracas	3,500	300	0.086			Schmitz and Audemard (2005)		Site class SD to SC ($V_{s30} =$ 250–400 m/s)
2	Jakarta	50,000	1,500	0.030	1.360	4.503	Cipta et al. (2018)		Site class SE (V _{s30} < 100 m/s)
3	Kirovakan	700	165	0.236	20.136	33.42	Bielak et al. (1999)	Zone 2	Site class SD to SC ($V_{s30} =$ 200–490 m/s)
		1,000	30	0.030			Bielak et al. (1999)	Zone 3	Site class SC ($V_{s30} = 685 \text{ m/s}$)
4	Mexico City	11,000	456	0.041	8.276	7.089	Sanchez-Sesma (1988)		Site class SE ($V_{s30} = 30-100 \text{ m/s}$)
5	Dinar	6,000	250	0.042	22.140	7.38	Khanbabazadeh (2016)		Site class SE to SD ($V_{s30} =$ 150–300 m/s)
6	Izmit	8,000	1,500	0.188	14.930	45	Ozalaybey et al. (2011)		Site class SD ($V_s =$ 200–350 m/s)
		10,000	1,200	0.120			Zor et al. (2010)		Site class SD ($V_s =$ 200–350 m/s)
7	Lower Hutt	4,350	320	0.074			Adams et al. (1999)	Cross-section Petone	Site class SD (V _{s30} = 175–285 m/s)
		3,020	275	0.091			Adams et al. (1999)	Cross-section Hutt Central	Site class SD ($V_{s30} = 175-285 \text{ m/s}$)
8	Wellington	1,100	140	0.127	4.289	20.136	Adams et al. (1999)		Site class SE ($V_{s30} = 100-150 \text{ m/s}$)
9	Nice	2000	60	0.030	35.880	11.31	Semblat et al. (2002)		Site class SD ($V_{s30} =$ 300 m/s)
10	Osaka	40,000	1800	0.045			Hatayama et al. (1995)		Site class SC ($V_{s30} = 500 \text{ m/s}$)
11	Kobe	55,000	2,100	0.038			Pitarka et al. (1998)		Site class SC ($V_{s30} = 600 \text{ m/s}$)
12	Long Valley Dam	175	61	0.348	29.685	42.436	Lai and Seed (1985)		
13	Bandung	13,000	200	0.015	5.710		Sengara et al. (2011)		

TABLE 1 Collected basin geometry and site class.

TABLE 2 Initial soil parameters.

Soil type	γ (kN/m³)	ho (kg/m³)	V _s (m/s)	c _u (kPa)		K (kPa)	G (kPa)
Soft clay (SE)	16	1,600	100	12	0.4	74,667	16,000
Base rock	22	2,200	760	3,210	0.2	1,694,293	1,270,720

Chushul Valley near the borders of Afghanistan and the former Soviet Union. Interpretation of the small earthquake response showed that 1-D site response analysis could well predict the ground response around the center of the valley. Nevertheless, the 1-D site response poorly predicted the ground response around the edges of the valley.

Bard and Gariel (1986) used an analytical approach to evaluate the 1-D and 2-D site responses of shallow and deep alluvial valleys.

The amplification at the center of the valley for 1-D and 2-D methods was quite similar. However, the amplification at the edge of the valley for 1-D and 2-D cases was very different. The fit between the 1-D and 2-D amplification at the center of the valley is much better than that at the edges. It shows that 1-D analysis could not be used for the location around the basin edge.

Romo and Seed (1986) evaluated the spectral response from two different sites, namely, Universidad Nacional Autonoma de Mexico



TABLE 3 In	put parameters	of [D-MOD	2000.
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Soft	clay (SE) par	ameter	Bedrock parameter					
V_s	100	m/s	V_s	760	m/s			
Ysat	16	kN/m ³	Ysat	22	kN/m ³			
Ywet	15	kN/m ³	Ywet	21	kN/m ³			
Soi	l parameter after	· 30 m	М	KZ model para	neter			
V_s	100-760	m/s	V_s	0.00244				
Ysat	16-22	kN/m ³	γ _{sat}	5				
Ywet	15-21	kN/m ³	Ywet	0.20%				

(UNAM) and the Secretary of Communication and Transportation (SCT). Although the magnitude of the 1985 Michoacán earthquake was large, the acceleration recorded at the UNAM site was only 0.03 g-0.04 g. However, acceleration time history at the SCT site showed that the peak acceleration was up to five times larger than that at the UNAM site. At a period of 2 seconds, the spectral acceleration reached a maximum value at the SCT site with a value 10 times more than that at the UNAM site. This indicates that a basin area containing soft soil yielded a greater amplification than that containing hard soil. Additionally, the spectral acceleration peaking around 2 s suggested that the earthquake possessed a high risk to buildings with 5–20 floors.

Further study about the basin effect was conducted by T. H. Seligman et al. (1989) to investigate the earthquake response of what they called an open-ended 2-D sediment-filled valley after the 1985 September 19 earthquake that devastated downtown Mexico City.

Kawase and Aki (1989) investigated the responses of two types of soft basins for incident SH, SV, P, and Rayleigh waves in a 2-D elastic half-space by using strong motions observed in Mexico City during the Michoacan, Mexico, earthquake of 1985. They showed

Soft clay (SE) parameter											
V_s	100	m/s									
ρ	1,600	kg/m ³									
C _u	12	kPa									
G	16,000	kPa									
K	74,000	kPa									
Bedrock parameter											
V _s 760 m/s											
ρ	2000	kg/m ³									
Cu	3,200	kPa									
G	1,270,000	kPa									
K	1,694,000	kPa									
	Soil parameter after 30 m										
V_s	100-760	m/s									
ρ	1,600–2,200	kg/m ³									
Cu	12-3,210	kPa									
G	16,000-127,000	kPa									
K	74,000-1,694,000	kPa									

TABLE 4 Soil parameters in FLAC 2-D.



the difficulty for simple 1-D models in reproducing the later part of the accelerogram observed in Mexico City.

To comprehensively study the site effects in the Mexico City basin for the 1985 Michoacan earthquake, Chavez-Garcia and Bard (1994) conducted 1-D and 2-D model analysis of wave propagation. They pointed out some conclusions about the possibility of doing





the experiments and the new data required to find a truly satisfactory explanation of strong ground motion at the Mexico City basin.

Movahedasl and Ghayamghamian (2015) conducted extensive parametrical studies about the effects of 2-D small-scale sedimentary basins on strong ground motion characteristics. They provided numerical and field evidence on the 2-D effects of small basins and gave some recommendations for design codes. Cruz-Atienza et al. (2016) studied ground response acceleration in the Mexican basin. This basin consists of lake beds, transitional areas consisting of alluvial deposits, and hard rock areas. This study indicated that at a frequency of 0.5 Hz, large amplification values were found at the basin edge.

Several 1-D ground response studies on soft soil deposits located at basin areas have also been conducted in the Southeast Asian region. For example, Qodri et al. (2021) conducted a non-linear site response analysis of the Bangkok subsoils triggered by the Three



Pagodas Fault. Then, Somantri et al. (2022) conducted a 1-D ground response study in Bandung, Indonesia. However, there is no basin effect that was considered in their analysis.

Sengara et al. (2011) studied the basin effect on the ground response acceleration in Bandung, Indonesia, to estimate peak ground surface acceleration and the amplification factor using 2-D finite element analysis. The Bandung Basin area is approximately 13 km wide and 200 km deep, extending from Cicadas to Citarum (Figure 2). Based on the geological map, the Bandung Basin is a floodplain deposit over a lake deposit. The lake deposit can be classified as lacustrine deposits. In the center of the basin, supposedly, a thick layer of soft or organic clays is found and is





classified as alluvial and volcanic deposits with various compositions and textures.

It is shown that the area affected by the basin, which is from the basin edge to 5 km, has a greater amplification factor value than the farther locations. As shown in Figure 3, the acceleration value on the edges also shows a greater value than that of the basin center, which is approximately 0.4 g-0.7 g.

All the previous studies clearly show that the presence of the basin affects the ground surface response due to the earthquake, particularly in areas around the basin edge. However, the link between 1-D and 2-D responses has not been studied for engineering practices. Based on practical considerations, it is necessary to estimate the scaling factor for the 1-D analysis by considering the basin presence, particularly for that containing soft soil. These scaling factors can be used to facilitate engineering practice to evaluate the ground response located around the basin, where the 1-D method is immediately available, but 2-D and 3-D methods are not accessible. These are a novelty of the study.

3 Research methodology

This research focused on proposing scaling factors for the 1-D wave propagation analysis. These factors were proposed based on the results of 2-D wave propagation analysis modeling at the basin using FLAC.

Some basin geometries were collected for the 2-D modeling references, as shown in Table 1. The site classes above this basin are also presented in this table. Modeling was carried out using a variety of parameters, such as PGA values, basin angle or inclination (θ), and the ratio of basin depth to basin width (D/W). In this study, the PGA value was varied as 0.2 g, 0.3 g, 0.4 g, and 0.5 g. The basin angle was set to 5°, 10°, 15°, 30°, and 45°. Depth/width variations were 0.0125, 0.025, 0.05, 0.075, 0.1, 0.2, and 0.4. The basin width was adjusted to 500 m, 1 km, 2 km, and 4 km.

3.1 Soil parameters and input motion

The 1-D and 2-D wave propagation analyses were carried out using the undrained total parameters, which are relevant to fast earthquake loading mechanisms. In this study, the shear wave velocity (V_s) value of the soft clay soil (SE site class) was set to 100 m/s. The corresponding standard penetration test value (N) of 2 was evaluated using Ohta and&Goto (1978), as presented in the following equation:

$$V_s = 85.3 \, N^{0.341}. \tag{1}$$

The undrained shear strength (c_u) value was estimated using Terzaghi and Peck (1967), as shown in Eq. 2.

$$c_u = 6^* N \,(\mathrm{kPa}). \tag{2}$$

Based on the standard penetration test value (N) of 2, the undrained shear strength is 12 kPa.

The shear modulus (G) was evaluated using the relationship between V_s and density (ρ) in the following equation:

$$G = \rho \cdot V_s^2. \tag{3}$$

Given the density (ρ) value of 1,600 kg/m² and shear wave velocity (V_s) of 100 m/s, the shear modulus (G) value is 16,000 kPa.

Assuming a Poisson's ratio (ν) value of 0.4 for soft clay soil (Das, 2006), the bulk modulus (*K*) value was estimated using Eq. 6:

$$K = \frac{2}{3}G\frac{(1+\nu)}{(1-2\nu)}.$$
 (4)

Given the G value of 1,600 kg/m², the bulk modulus (K) value is 74,000 kPa.

Initial soil parameters, including total unit weight (γ), can be seen in Table 2.

The 1989 Loma Prieta earthquake was used as an input motion (Figure 4). The mechanism of this earthquake was a strike–slip on the San Andreas Fault. This movement was attributed to the North American tectonic plate that shifted toward the north, while the large Pacific plate shifted southward with a magnitude of 6.9 and a maximum acceleration of 0.4 g.

X/W	$\theta = 5^{\circ}$											
		D/W =	- 0.010			D/W =			D/W =	0.015		
	0.2 g	0.3 g	0.4 g	0.5 g	0.2 g	0.3 g	0.4 g	0.5 g	0.2 g	0.3 g	0.4 <u>c</u>	g 0.5 g
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0 1.000
1/16	1.154	1.183	1.210	1.219	1.206	1.234	1.276	1.309	1.292	1.322	1.372	2 1.436
1/8	1.027	1.064	1.071	1.072	1.104	1.103	1.133	1.188	1.199	1.195	1.244	4 1.324
1/4	1.003	1.005	1.008	1.014	1.029	1.047	1.055	1.111	1.060	1.073	1.106	5 1.196
1/2	1.001	1.001	1.006	1.009	1.004	1.011	1.012	1.015	1.004	1.006	1.012	2 1.016
X/W						θ =	10°					
			D/W =	0.050					D/W =	= 0.075		
	0.2 g		0.3 g	0.4 g		0.5 g	0.2 g		0.3 g	0.4 g	J	0.5 g
0	1.000		1.000	1.000		1.000	1.000		1.000	1.000		1.000
1/16	1.297		1.308	1.373		1.445	1.284		1.293	1.364		1.430
1/8	1.274		1.294	1.338		1.384	1.260		1.258	1.289		1.339
1/4	1.094		1.099	1.103		1.159	1.058		1.062	1.063		1.151
1/2	1.029		1.034	1.045		1.058	1.021		1.023	1.022		1.030
X/W						θ =	15°					
		D/W =	= 0.050			D/W =	0.075			D/W =	= 0.100	
								g 0.5 g 0.2 g				
	0.2 g	0.3 g	0.4 g	0.5 g	0.2 g	0.3 g	0.4 g	0.5 g	0.2 g	0.3 g	0.4 <u>c</u>	g 0.5 g
0	0.2 g 1.000	0.3 g 1.000	0.4 g 1.000	0.5 g 1.000	0.2 g 1.000	0.3 g 1.000	0.4 g 1.000	0.5 g 1.000	0.2 g 1.000	0.3 g 1.000	0.4 <u>c</u> 1.000	g 0.5 g
0 1/16	0.2 g 1.000 1.454	0.3 g 1.000 1.520	0.4 g 1.000 1.559	0.5 g 1.000 1.597	0.2 g 1.000 1.446	0.3 g 1.000 1.513	0.4 g 1.000 1.556	0.5 g 1.000 1.561	0.2 g 1.000 1.405	0.3 g 1.000 1.495	0.4 <u>c</u> 1.000	g 0.5 g 0 1.000 0 1.544
0 1/16 1/8	0.2 g 1.000 1.454 1.242	0.3 g 1.000 1.520 1.247	0.4 g 1.000 1.559 1.242	0.5 g 1.000 1.597 1.271	0.2 g 1.000 1.446 1.239	0.3 g 1.000 1.513 1.239	0.4 g 1.000 1.556 1.236	0.5 g 1.000 1.561 1.244	0.2 g 1.000 1.405 1.239	0.3 g 1.000 1.495 1.237	0.4 g 1.000 1.540 1.233	g 0.5 g 0 1.000 0 1.544 3 1.251
0 1/16 1/8 1/4	0.2 g 1.000 1.454 1.242 1.018	0.3 g 1.000 1.520 1.247 1.019	0.4 g 1.000 1.559 1.242 1.016	0.5 g 1.000 1.597 1.271 1.058	0.2 g 1.000 1.446 1.239 1.049	0.3 g 1.000 1.513 1.239 1.038	0.4 g 1.000 1.556 1.236 1.043	0.5 g 1.000 1.561 1.244 1.083	0.2 g 1.000 1.405 1.239 1.073	0.3 g 1.000 1.495 1.237 1.072	0.4 c 1.000 1.540 1.233 1.090	O.5 g 0 1.000 0 1.544 3 1.251 0 1.113
0 1/16 1/8 1/4 1/2	0.2 g 1.000 1.454 1.242 1.018 1.016	0.3 g 1.000 1.520 1.247 1.019 1.014	0.4 g 1.000 1.559 1.242 1.016 1.009	0.5 g 1.000 1.597 1.271 1.058 1.025	0.2 g 1.000 1.446 1.239 1.049 1.019	0.3 g 1.000 1.513 1.239 1.038 1.011	0.4 g 1.000 1.556 1.236 1.043 1.008	0.5 g 1.000 1.561 1.244 1.083 1.013	0.2 g 1.000 1.405 1.239 1.073 1.020	0.3 g 1.000 1.495 1.237 1.072 1.007	0.4 c 1.000 1.540 1.233 1.090 1.034	g 0.5 g 0 1.000 0 1.544 3 1.251 0 1.113 4 1.073
0 1/16 1/8 1/4 1/2 X/W	0.2 g 1.000 1.454 1.242 1.018 1.016	0.3 g 1.000 1.520 1.247 1.019 1.014	0.4 g 1.000 1.559 1.242 1.016 1.009	0.5 g 1.000 1.597 1.271 1.058 1.025	0.2 g 1.000 1.446 1.239 1.049 1.019	0.3 g 1.000 1.513 1.239 1.038 1.011 θ =	0.4 g 1.000 1.556 1.236 1.043 1.008 30°	0.5 g 1.000 1.561 1.244 1.083 1.013	0.2 g 1.000 1.405 1.239 1.073 1.020	0.3 g 1.000 1.495 1.237 1.072 1.007	0.4 c 1.000 1.540 1.233 1.090 1.034	g 0.5 g 0 1.000 0 1.544 3 1.251 0 1.113 4 1.073
0 1/16 1/8 1/4 1/2 X/W	0.2 g 1.000 1.454 1.242 1.018 1.016	0.3 g 1.000 1.520 1.247 1.019 1.014	0.4 g 1.000 1.559 1.242 1.016 1.009 = 0.050	0.5 g 1.000 1.597 1.271 1.058 1.025	0.2 g 1.000 1.446 1.239 1.049 1.019	0.3 g 1.000 1.513 1.239 1.038 1.011 θ = D/W =	0.4 g 1.000 1.556 1.236 1.043 1.008 30°	0.5 g 1.000 1.561 1.244 1.083 1.013	0.2 g 1.000 1.405 1.239 1.073 1.020	0.3 g 1.000 1.495 1.237 1.072 1.007	0.4 c 1.000 1.540 1.233 1.090 1.034 = 0.100	g 0.5 g 0 1.000 0 1.544 3 1.251 0 1.113 4 1.073
0 1/16 1/8 1/4 1/2 X/W	0.2 g 1.000 1.454 1.242 1.018 1.016	0.3 g 1.000 1.520 1.247 1.019 1.014 D/W = 0.3 g	0.4 g 1.000 1.559 1.242 1.016 1.009 = 0.050 0.4 g	0.5 g 1.000 1.597 1.271 1.058 1.025 0.5 g	0.2 g 1.000 1.446 1.239 1.049 1.019	$\begin{array}{c} 0.3 \text{ g} \\ 1.000 \\ 1.513 \\ 1.239 \\ 1.038 \\ 1.011 \\ \theta = \\ D/W = \\ 0.3 \text{ g} \end{array}$	0.4 g 1.000 1.556 1.236 1.043 1.008 30° 0.075 0.4 g	0.5 g 1.000 1.561 1.244 1.083 1.013	0.2 g 1.000 1.405 1.239 1.073 1.020	0.3 g 1.000 1.495 1.237 1.072 1.007 D/W = 0.3 g	0.4 c 1.000 1.540 1.233 1.090 1.034 = 0.100 0.4 c	 g 0.5 g h.000 h.1.544 h.1.251 h.1.113 h.1.073 h.1.073 h.5.5 g
0 1/16 1/8 1/4 1/2 X/W	0.2 g 1.000 1.454 1.242 1.018 1.016 0.2 g 1.000	0.3 g 1.000 1.520 1.247 1.019 1.014 D/W = 0.3 g 1.000	0.4 g 1.000 1.559 1.242 1.016 1.009 • 0.050 0.4 g 1.000	0.5 g 1.000 1.597 1.271 1.058 1.025 0.5 g 1.000	0.2 g 1.000 1.446 1.239 1.049 1.019 0.2 g 1.000	$\begin{array}{c} 0.3 \text{ g} \\ \hline 1.000 \\ \hline 1.513 \\ \hline 1.239 \\ \hline 1.038 \\ \hline 1.011 \\ \theta = \\ D/W = \\ \hline 0.3 \text{ g} \\ \hline 1.000 \end{array}$	0.4 g 1.000 1.556 1.236 1.043 1.043 30° 0.075 0.4 g 1.000	0.5 g 1.000 1.561 1.244 1.083 1.013 0.5 g 1.000	0.2 g 1.000 1.405 1.239 1.073 1.020 0.2 g 1.000	0.3 g 1.000 1.495 1.237 1.072 1.007 D/W = 0.3 g 1.000	0.4 <u>c</u> 1.000 1.540 1.233 1.090 1.034 = 0.100 0.4 <u>c</u> 1.000	 9. 0.5 g 1.000 1.544 3. 1.251 1.113 4. 1.073 9. 0.5 g 9. 1.000
0 1/16 1/8 1/4 1/2 X/W 0 1/16	0.2 g 1.000 1.454 1.242 1.018 1.016 0.2 g 1.000 1.395	0.3 g 1.000 1.520 1.247 1.019 1.014 D/W = 0.3 g 1.000 1.474	0.4 g 1.000 1.559 1.242 1.016 1.009 0.050 0.4 g 1.000 1.498	0.5 g 1.000 1.597 1.271 1.058 1.025 0.5 g 1.000 1.524	0.2 g 1.000 1.446 1.239 1.049 1.019 0.2 g 1.000 1.334	$\begin{array}{c} 0.3 \text{ g} \\ 1.000 \\ 1.513 \\ 1.239 \\ 1.038 \\ 1.011 \\ \theta = \\ D/W = \\ 0.3 \text{ g} \\ 1.000 \\ 1.442 \end{array}$	0.4 g 1.000 1.556 1.236 1.043 1.043 30° 0.075 0.4 g 1.000 1.461	0.5 g 1.000 1.561 1.244 1.083 1.013 0.5 g 1.000 1.503	0.2 g 1.000 1.405 1.239 1.073 1.020 0.2 g 1.000 1.334	0.3 g 1.000 1.495 1.237 1.072 1.077 D/W = 0.3 g 1.000 1.395	0.4 c 1.000 1.540 1.233 1.090 1.034 = 0.100 0.4 c 1.000 1.423	g 0.5 g 0 1.000 0 1.544 3 1.251 0 1.113 4 1.073 9 0.5 g 0 1.000 3 1.497
0 1/16 1/8 1/4 1/2 X/W 0 1/16 1/8	0.2 g 1.000 1.454 1.242 1.018 1.016 0.2 g 1.000 1.395 1.071	0.3 g 1.000 1.520 1.247 1.019 1.014 D/W = 0.3 g 1.000 1.474 1.080	0.4 g 1.000 1.559 1.242 1.016 1.009 0.050 0.4 g 1.000 1.498 1.094	0.5 g 1.000 1.597 1.271 1.058 1.025 0.5 g 1.000 1.524 1.143	0.2 g 1.000 1.446 1.239 1.049 1.019 0.2 g 1.000 1.334 1.090	$\begin{array}{c} 0.3 \text{ g} \\ 1.000 \\ 1.513 \\ 1.239 \\ 1.038 \\ 1.011 \\ \theta = \\ D/W = \\ 0.3 \text{ g} \\ 1.000 \\ 1.442 \\ 1.122 \end{array}$	0.4 g 1.000 1.556 1.236 1.043 1.043 30° 0.075 0.4 g 1.000 1.461 1.101	0.5 g 1.000 1.561 1.244 1.083 1.013 0.5 g 1.000 1.503 1.148	0.2 g 1.000 1.405 1.239 1.073 1.020 0.2 g 1.000 1.334 1.147	0.3 g 1.000 1.495 1.237 1.072 1.077 D/W = 0.3 g 1.000 1.395 1.128	0.4 c 1.000 1.540 1.233 1.090 1.034 = 0.100 0.4 c 1.000 1.423 1.156	g 0.5 g 0 1.000 0 1.544 3 1.251 0 1.113 4 1.073 5 1.497
0 1/16 1/8 1/4 1/2 X/W 0 1/16 1/8 1/4	0.2 g 1.000 1.454 1.242 1.018 1.016 0.2 g 1.000 1.395 1.071 1.029	0.3 g 1.000 1.520 1.247 1.019 1.014 D/W = 0.3 g 1.000 1.474 1.080 1.019	0.4 g 1.000 1.559 1.242 1.016 1.009 0.050 0.4 g 1.000 1.498 1.094 1.012	0.5 g 1.000 1.597 1.271 1.058 1.025 0.5 g 1.000 1.524 1.143 1.022	0.2 g 1.000 1.446 1.239 1.049 1.019 0.2 g 1.000 1.334 1.090 1.026	$\begin{array}{c} 0.3 \text{ g} \\ 1.000 \\ 1.513 \\ 1.239 \\ 1.038 \\ 1.011 \\ \theta = \\ D/W = \\ 0.3 \text{ g} \\ 1.000 \\ 1.442 \\ 1.122 \\ 1.018 \end{array}$	0.4 g 1.000 1.556 1.236 1.043 1.043 30° 0.075 0.4 g 1.000 1.461 1.101 1.010	0.5 g 1.000 1.561 1.244 1.083 1.013 0.5 g 1.000 1.503 1.148 1.036	0.2 g 1.000 1.405 1.239 1.073 1.020 0.2 g 1.000 1.334 1.147 1.023	0.3 g 1.000 1.495 1.237 1.072 1.072 1.007 D/W = 0.3 g 1.000 1.395 1.128 1.013	0.4 c 1.000 1.540 1.233 1.090 1.034 0.100 0.4 c 1.000 1.423 1.156 1.017	 9. 0.5 g 1.000 1.544 3. 1.251 3. 1.251 4. 1.073 4. 1.073 5. 0.5 g 1.497 5. 1.203 7. 1.028
0 1/16 1/8 1/4 1/2 X/W 0 1/16 1/8 1/4 1/2	0.2 g 1.000 1.454 1.242 1.018 1.016 0.2 g 1.000 1.395 1.071 1.029 1.024	0.3 g 1.000 1.520 1.247 1.019 1.014 D/W = 0.3 g 1.000 1.474 1.080 1.019 1.019 1.018	0.4 g 1.000 1.559 1.242 1.016 1.009 0.4 g 1.000 0.4 g 1.000 1.498 1.094 1.012 1.003	0.5 g 1.000 1.597 1.271 1.058 1.025 0.5 g 1.000 1.524 1.143 1.022 1.016	0.2 g 1.000 1.446 1.239 1.049 1.019 0.2 g 1.000 1.334 1.090 1.026 1.020	$\begin{array}{c} 0.3 \text{ g} \\ 1.000 \\ 1.513 \\ 1.239 \\ 1.038 \\ 1.011 \\ \theta = \\ D/W = \\ 0.3 \text{ g} \\ 1.000 \\ 1.442 \\ 1.122 \\ 1.018 \\ 1.011 \end{array}$	0.4 g 1.000 1.556 1.236 1.043 1.043 30° 0.075 0.4 g 1.000 1.461 1.101 1.010 1.010	0.5 g 1.000 1.561 1.244 1.083 1.013 0.5 g 1.000 1.503 1.148 1.036 1.010	0.2 g 1.000 1.405 1.239 1.073 1.020 0.2 g 0.2 g 1.000 1.334 1.147 1.023 1.011	0.3 g 1.000 1.495 1.237 1.072 1.072 1.007 D/W = 0.3 g 1.000 1.395 1.128 1.013 1.008	0.4 <u>c</u> 1.000 1.540 1.233 1.090 1.034 c 0.100 0.4 <u>c</u> 1.000 1.423 1.156 1.017 1.017	9 0.5 g 1.000 1.000 1.544 1.541 3 1.251 0 1.113 4 1.073 9 0.5 g 0 1.000 3 1.497 5 1.203 7 1.028 7 1.011
0 1/16 1/8 1/4 1/2 X/W 0 1/16 1/8 1/4 1/2 X/W	0.2 g 1.000 1.454 1.242 1.018 1.016 0.2 g 1.000 1.395 1.071 1.029 1.024	0.3 g 1.000 1.520 1.247 1.019 1.014 D/W = 0.3 g 1.000 1.474 1.080 1.019 1.018	0.4 g 1.000 1.559 1.242 1.016 1.009 0.4 g 1.000 0.4 g 1.000 1.498 1.094 1.094 1.012 1.003	0.5 g 1.000 1.597 1.271 1.058 1.025 0.5 g 1.000 1.524 1.143 1.022 1.016	0.2 g 1.000 1.446 1.239 1.049 1.019 0.2 g 1.000 1.334 1.090 1.026 1.020	$\begin{array}{c} 0.3 \text{ g} \\ 1.000 \\ 1.513 \\ 1.239 \\ 1.038 \\ 1.011 \\ \theta = \\ D/W = \\ 0.3 \text{ g} \\ 1.000 \\ 1.442 \\ 1.122 \\ 1.018 \\ 1.011 \\ \theta = \\ \theta = \\ \end{array}$	0.4 g 1.000 1.556 1.236 1.043 1.008 30° 0.075 0.4 g 1.000 1.461 1.101 1.010 1.002 45°	0.5 g 1.000 1.561 1.244 1.083 1.013 0.5 g 1.000 1.503 1.148 1.036 1.010	0.2 g 1.000 1.405 1.239 1.073 1.020 0.2 g 0.2 g 1.000 1.334 1.147 1.023 1.011	0.3 g 1.000 1.495 1.237 1.072 1.072 1.007 D/W = 0.3 g 1.000 1.395 1.128 1.013 1.008	0.4 <u>c</u> 1.000 1.540 1.233 1.090 1.034 = 0.100 0.4 <u>c</u> 1.000 1.423 1.156 1.017 1.007	9 0.5 g 1.000 1.544 3 1.251 0 1.113 4 1.073 9 0.5 g 0 1.000 3 1.497 5 1.203 7 1.028 7 1.011
0 1/16 1/8 1/4 1/2 X/W 0 1/16 1/8 1/4 1/2 X/W	0.2 g 1.000 1.454 1.242 1.018 1.016 0.2 g 1.000 1.395 1.071 1.029 1.024	0.3 g 1.000 1.520 1.247 1.019 1.014 D/W = 0.3 g 1.000 1.474 1.080 1.019 1.018 D/W =	0.4 g 1.000 1.559 1.242 1.016 1.009 0.4 g 1.000 0.4 g 1.000 1.498 1.094 1.012 1.003	0.5 g 1.000 1.597 1.271 1.058 1.025 0.5 g 1.000 1.524 1.143 1.022 1.016	0.2 g 1.000 1.446 1.239 1.049 1.019 0.2 g 1.000 1.334 1.090 1.026 1.020	$\begin{array}{c} 0.3 \text{ g} \\ 1.000 \\ 1.513 \\ 1.239 \\ 1.038 \\ 1.011 \\ \theta = \\ 0.3 \text{ g} \\ 1.000 \\ 1.442 \\ 1.122 \\ 1.018 \\ 1.011 \\ \theta = \\ D/W = \\ D/W = \\ D/W = \\ 0.3 \text{ g} \\ 0.3$	0.4 g 1.000 1.556 1.236 1.043 1.008 30° 0.075 0.4 g 1.000 1.461 1.101 1.010 1.002 45° 0.200	0.5 g 1.000 1.561 1.244 1.083 1.013 0.5 g 1.000 1.503 1.148 1.036 1.010	0.2 g 1.000 1.405 1.239 1.073 0.2 g 0.2 g 1.000 1.334 1.147 1.023 1.011	0.3 g 1.000 1.495 1.237 1.072 1.072 1.007 D/W = 0.3 g 1.000 1.395 1.128 1.013 1.008	0.4 <u>c</u> 1.000 1.540 1.233 1.090 1.034 0.100 0.4 <u>c</u> 1.000 1.423 1.156 1.017 1.007 1.007	9 0.5 g 1.000 1.544 3 1.251 0 1.113 4 1.073 5 1.203 7 1.203 7 1.011
0 1/16 1/8 1/4 1/2 X/W 0 1/16 1/8 1/4 1/2 X/W	0.2 g 1.000 1.454 1.242 1.018 1.016 0.2 g 1.000 1.395 1.071 1.029 1.024 0.2 g	0.3 g 1.000 1.520 1.247 1.019 1.014 D/W = 0.3 g 1.000 1.474 1.080 1.019 1.018 D/W = 0.3 g	0.4 g 1.000 1.559 1.242 1.016 1.009 0.4 g 1.000 1.498 1.094 1.012 1.003 0.4 g 0.100 0.4 g	0.5 g 1.000 1.597 1.271 1.058 1.025 0.5 g 1.000 1.524 1.143 1.022 1.016	0.2 g 1.000 1.446 1.239 1.049 1.019 0.2 g 1.000 1.334 1.090 1.026 1.020	$\begin{array}{c} 0.3 \text{ g} \\ 1.000 \\ 1.513 \\ 1.239 \\ 1.038 \\ 1.011 \\ \theta = \\ D/W = \\ 0.3 \text{ g} \\ 1.000 \\ 1.442 \\ 1.122 \\ 1.018 \\ 1.011 \\ \theta = \\ D/W = \\ 0.3 \text{ g} \end{array}$	0.4 g 1.000 1.556 1.236 1.043 1.008 30° 0.075 0.4 g 1.000 1.461 1.101 1.010 1.002 45° 0.200 0.4 g	0.5 g 1.000 1.561 1.244 1.083 1.013 0.5 g 1.000 1.503 1.148 1.036 1.010	0.2 g 1.000 1.405 1.239 1.073 0.2 g 0.2 g 1.000 1.334 1.147 1.023 1.011	0.3 g 1.000 1.495 1.237 1.072 1.072 0.3 g 1.000 1.395 1.128 1.013 1.008 D/W = 0.3 g	0.4 c 1.000 1.540 1.233 1.090 1.034 0.100 0.4 c 1.007 1.007 1.007 1.007 0.4 00 0.4 c	g 0.5 g j 1.000 j 1.544 k 1.251 j 1.113 k 1.073 k 1.073 k 1.073 k 1.000 k 1.028 k 1.011 k 1.015

TABLE 5 Scaling factor F_g for $\theta = 5^\circ$, $\theta = 10^\circ$, $\theta = 15^\circ$, $\theta = 30^\circ$, and $\theta = 45^\circ$ with varying *D/W* and *PGA*.

(Continued on following page)

X/W	$\theta = 45^{\circ}$											
		D/W =	0.100			D/W =	0.200		D/W = 0.400			
	0.2 g	0.3 g	0.4 g	0.5 g	0.2 g	0.3 g	0.4 g	0.5 g	0.2 g	0.3 g	0.4 g	0.5 g
1/16	1.321	1.391	1.415	1.470	1.224	1.316	1.336	1.420	1.181	1.308	1.322	1.393
1/8	1.117	1.118	1.119	1.185	1.113	1.104	1.103	1.183	1.104	1.102	1.100	1.174
1/4	1.021	1.010	1.017	1.026	1.017	1.011	1.012	1.015	1.014	1.006	1.011	1.012
1/2	1.005	1.008	1.006	1.009	1.008	1.003	1.010	1.004	1.006	1.004	1.006	1.010

TABLE 5 (*Continued*) Scaling factor F_q for $\theta = 5^\circ$, $\theta = 10^\circ$, $\theta = 15^\circ$, $\theta = 30^\circ$, and $\theta = 45^\circ$ with varying *D/W* and *PGA*.



1.6 $\theta = 15^{\circ}, PGA = 0.5 \text{ g}$ 1.5 -D/W = 0.050 $- - \circ - D / W = 0.075$ 1.4 $\cdot \Delta \cdot D / W = 0.100$ Basin width (W 1.0 Z Basin 0.9 depth (D) 0.8 X/W 0.3 0.1 0.2 0.4 0.5 1.6 $\theta = 30^\circ$, PGA = 0.5 g 1.5 -D/W = 0.050--0 - D / W = 0.0751.4 $\cdots \bigtriangleup D / W = 0.100$ 1.0 Basin width (W) 7 Basin 0.9 depth (D) 0.8 X/W 0.3 0.5 0.1 0.2 0.4 FIGURE 12 Scaling factor F_{DW} for $\theta = 15^{\circ}$ and $\theta = 30^{\circ}$ at PGA = 0.5 g.

3.2 1-D modeling

The 1-D wave propagation modeling was conducted using D-MOD 2000. This program requires several soil parameters, namely, shear modulus, maximum shear modulus (G_{max}), shear wave velocity, and unit weight. In addition, for defining the bedrock, the D-MOD 2000 needs V_s and γ . This program applies the MKZ non-linear stress-strain model. The MKZ

model relates initial shear stress (τ_{mo}) and initial shear modulus (G_{mo}) based on the reference shear strain (γ_r) of 2.44 × 10⁻³, as shown in the following equation:

$$\tau_{mo} = G_{mo} \times \gamma_r. \tag{5}$$

Equation 1 shows the MKZ non-linear stress-strain model (Matasovic and Vucetic, 1995). In this equation, normalized shear stress (τ^*) is a function of curve-fitting parameters of the

TABLE 6 Scaling factor F_{DW} for $\theta = 10^{\circ}$, $\theta = 15^{\circ}$, $\theta = 30^{\circ}$, and $\theta = 45^{\circ}$ with varying PGA and D/W.

X/W		$ heta = 10^{\circ}$											
	Р	GA = 0.2	2 g	Р	<i>GA</i> = 0.3	g	F	PGA = 0.4	g	P	GA = 0.5	g	
	0.050		0.075	0.050		0.075	0.050		0.075	0.050		0.075	
0	1.000		1.000	1.000		1.000	1.000		1.000	1.000		1.000	
1/16	1.297		1.284	1.308		1.293	1.373		1.364	1.445		1.430	
1/8	1.274		1.260	1.294		1.258	1.338		1.289	1.384		1.339	
1/4	1.094		1.058	1.099		1.062	1.103		1.063	1.159		1.151	
1/2	1.029 1.021		1.034		1.023	1.045		1.022	1.058		1.030		
X/W						$\theta =$	15°						
	P	CGA = 0.	2 g	P	GA = 0.3	g	F	PGA = 0.4	g	F	<i>CGA</i> = 0.5	g	
	0.050	0.075	0.100	0.050	0.075	0.100	0.050	0.075	0.100	0.050	0.075	0.100	
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	
1/16	1.454	1.446	1.405	1.520	1.513	1.495	1.559	1.556	1.540	1.597	1.561	1.544	
1/8	1.242	1.239	1.239	1.247	1.239	1.237	1.242	1.236	1.233	1.271	1.244	1.251	
1/4	1.018	1.049	1.073	1.019	1.038	1.072	1.016	1.043	1.090	1.058	1.083	1.113	
1/2	1.016	1.019	1.020	1.014	1.011	1.007	1.009	1.008	1.034	1.025	1.013	1.073	
X/W					$\theta = 30^{\circ}$								
	Р	GA = 0.	2 g	Р	GA = 0.3	g	P	PGA = 0.4	g	Р	GA = 0.5	g	
	0.050	0.075	0.100	0.050	0.075	0.100	0.050	0.075	0.100	0.050	0.075	0.100	
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	
1/16	1.395	1.334	1.334	1.474	1.442	1.395	1.498	1.461	1.423	1.524	1.503	1.497	
1/8	1.071	1.090	1.147	1.080	1.122	1.128	1.094	1.101	1.156	1.143	1.148	1.203	
1/4	1.029	1.026	1.023	1.019	1.018	1.013	1.012	1.010	1.017	1.022	1.036	1.028	
1/2	1.024	1.020	1.011	1.018	1.011	1.008	1.003	1.002	1.007	1.016	1.010	1.011	
X/W						$\theta =$	45°						
	P	CGA = 0.	2 g	P	GA = 0.3	g	F	PGA = 0.4	g	F	<i>GA</i> = 0.5	g	
	0.100	0.200	0.400	0.100	0.200	0.400	0.100	0.200	0.400	0.100	0.200	0.400	
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	
1/16	1.321	1.224	1.181	1.391	1.316	1.308	1.415	1.336	1.322	1.470	1.420	1.393	
1/8	1.117	1.113	1.104	1.118	1.104	1.102	1.119	1.103	1.100	1.185	1.183	1.174	
1/4	1.021	1.017	1.014	1.010	1.011	1.006	1.017	1.012	1.011	1.026	1.015	1.012	
1/2	1.005	1.008	1.006	1.008	1.003	1.004	1.006	1.010	1.006	1.009	1.004	1.010	

non-linear hysteretic MKZ model (β and s), normalized initial shear modulus (G^*_{mo}), and normalized initial shear stress (τ^*_{mo}). Each superscript asterisk (*) indicates that the corresponding parameter is normalized by initial vertical effective stress (σ'_{vc}). The example of D-MOD 2000 input parameters for the MKZ model is shown in Eq. 9:

$$\tau^* = f^*(\gamma) = \frac{G_{mo}^* \times \gamma}{1 + \beta \left(\frac{G_{mo}}{\tau_{mo}}\gamma\right)^s}.$$
(6)

The β and *s* parameters can be evaluated by performing manual trial–error or using curve fitting based on the refereed G/G_{max} and damping ratio curves.



The Rayleigh damping coefficients are expressed by mass damping constant (α_r) and stiffness damping constant (β_r). These coefficients are a function of the soil's natural period (*T*), a constant (*n*), and viscous damping (ξ in %). The *T* value is a function of soil layer thickness and *V*_s. In this study, *n* and ξ were taken as 5% and 0.2%, respectively.

The soil parameters, including saturated unit weight of soil (γ_{sat}) and moist unit weight of soil (γ_{wet}), in D-MOD 2000 are summarized in Table 3.

3.3 2-D modeling

The 2-D wave propagation modeling was carried out using FLAC. This program allows input motion of acceleration time histories or stress-time histories depending on the base rock assumption (i.e., rigid and flexible bases). A rigid base demands an input motion of acceleration time history, whereas a flexible base requires an input motion of stress time history. A rigid base stipulates that the waves are completely reflected from the base and no waves are absorbed by the base. Thus, a quiet boundary is not needed in the rigid base model. In contrast, the flexible base demands that half of the waves are absorbed by the base model.

Table 4 presents ground parameters, such as V_s , G, ρ , c_u , and K, in FLAC 2-D modeling for base rock and soft soil (site class SE) based on the Mohr–Coulomb soil model.

The FLAC 2-D also requires additional input parameters. These parameters include Rayleigh damping coefficients, grid dimensions, and computational time steps.

The Rayleigh damping is used to dampen the natural oscillations of the model similar to the 1-D analysis. Fourier amplitude shows that the maximum amplitude occurs at a frequency of 2.51 Hz (Figure 5). This maximum value was selected as the Rayleigh β_r parameter. The Rayleigh α_r parameter of 0.02 was taken based on a recommended value by FLAC 2-D.

Hysteretic damping was also used in FLAC 2-D based on a sigmoidal model with three parameters (Sig3 models). The Sig3 model is presented in Eq. 7:

$$M_s = \frac{a}{1 + e^{\left(-(L-x_0)/b\right)}},$$
(7)

where

 M_s represents the secant modulus; *L* represents the logarithmic strain; *a* is 1.014; *b* is -0.4792; and

X/W		D/W = 0.025										
	F	PGA = 0.2	g		<i>PGA</i> = 0.3	g	Р	GA = 0.4 g	9		PGA = 0.5	g
	5°	10°	15°	5°	10°	15°	5°	10°	15°	5°	10°	15°
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
1/16	1.292	1.262	1.195	1.322	1.288	1.218	1.372	1.317	1.221	1.436	1.396	1.296
1/8	1.199	1.122	1.054	1.195	1.125	1.056	1.244	1.147	1.063	1.324	1.244	1.088
1/4	1.060	1.038	1.002	1.073	1.041	1.002	1.106	1.051	1.006	1.196	1.078	1.009
1/2	1.004	1.003	1.000	1.006	1.002	1.001	1.012	1.005	1.003	1.016	1.008	1.003
X/W						D/W =	0.050					
	F	PGA = 0.2	g		PGA = 0.3	g	P	GA = 0.4 g	9		PGA = 0.5	g
	10°	15°	30°	10°	15°	30°	10°	15°	30°	10°	15°	30°
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
1/16	1.297	1.454	1.395	1.308	1.520	1.474	1.373	1.559	1.498	1.445	1.597	1.524
1/8	1.274	1.242	1.071	1.294	1.247	1.080	1.338	1.242	1.094	1.384	1.271	1.143
1/4	1.094	1.018	1.029	1.099	1.019	1.019	1.103	1.016	1.012	1.159	1.058	1.022
1/2	1.029	1.016	1.024	1.034	1.014	1.018	1.045	1.009	1.003	1.058	1.025	1.016
X/W						D/W	= 0.075					
			PG.	4 = 0.2 g					PGA	= 0.3 g		
	10°	15	5°	30°	45°	60°	10°	15°	9 3	30°	45°	60°
0	1.000	1.0	00	1.000	1.000	1.000	1.000	1.00	0 1	.000	1.000	1.000
1/16	1.284	1.4	46	1.334	1.252	1.247	1.293	1.51	3 1	.442	1.256	1.395
1/8	1.260	1.2	39	1.090	1.057	1.039	1.258	1.23	9 1	.122	1.063	1.156
1/4	1.058	1.0	49	1.026	1.023	1.009	1.062	1.03	8 1	.018	1.016	1.014
1/2	1.021	1.0	19	1.020	1.012	1.001	1.023	1.01	1 1	.011	1.004	1.014
X/W						D/W :	= 0.075					
			PG	A = 0.4g					PGA	= 0.5g		
	10°	15	5°	30°	45°	60 °	10°	15	° 3	80°	45°	60°
0	1.000	1.0	000	1.000	1.000	1.000	1.000	1.00	0 1	.000	1.000	1.000
1/16	1.364	1.5	56	1.461	1.269	1.163	1.430	1.56	1 1	.503	1.382	1.401
1/8	1.289	1.2	36	1.101	1.065	1.040	1.339	1.24	4 1	.148	1.103	1.058
1/4	1.063	1.0	043	1.010	1.007	1.002	1.151	1.08	3 1	.036	1.029	1.014
1/2	1.022	1.0	008	1.002	1.000	1.000	1.030	1.01	3 1	.010	1.004	1.004
X/W						D/W =	0.100					
	ŀ	PGA = 0.2	g		<i>PGA</i> = 0.3	g	<i>PGA</i> = 0.4 g			<i>PGA</i> = 0.5 g		
	15°	30°	45°	15°	30°	45°	15°	30°	45°	15°	30°	45°
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000

TABLE 7 Scaling factor F_{θ} for D/W = 0.025, D/W = 0.05, D/W = 0.075, and D/W = 0.1 with varying PGA and θ .

(Continued on following page)

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TABLE 7 (Continued) Scaling factor F_{θ} for D/W = 0.025, D/W = 0.05, D/W = 0.075, and D/W = 0.1 with varying PGA and θ .

X/W	<i>D/W</i> = 0.100											
	F	PGA = 0.2 q	9	<i>PGA</i> = 0.3 g			<i>PGA</i> = 0.4 g			<i>PGA</i> = 0.5 g		
	15°	30°	45°	15°	30°	45°	15°	30°	45°	15°	30°	45°
1/16	1.405	1.334	1.321	1.495	1.395	1.391	1.540	1.423	1.415	1.544	1.497	1.470
1/8	1.239	1.147	1.117	1.237	1.128	1.118	1.233	1.156	1.119	1.251	1.203	1.185
1/4	1.073	1.023	1.021	1.072	1.013	1.010	1.090	1.017	1.017	1.113	1.028	1.026
1/2	1.020	1.011	1.005	1.007	1.008	1.008	1.034	1.007	1.006	1.073	1.011	1.009



 x_0 is -1.249.

a, *b*, and x_0 values were selected based on Sun et al. (1988).

Maximum grid dimension (Δl_{max}) is required by FLAC 2-D to yield a convergent solution. The maximum grid dimension was calculated using V_s of the medium and the maximum wave frequency (f_{max}), as shown in Eq. 8:

$$\Delta l_{max} = \frac{V_s}{10^* f_{max}}.$$
(8)

Timestep calculation was carried out according to the corresponding mesh dimensions. The maximum timestep (Δt_{crit}) was calculated using Eq. 9:

$$\Delta t_{crit} = \frac{A_z}{L_d} \sqrt{\frac{\rho}{K + \frac{4}{3}G'}},\tag{9}$$

where

 A_z represents the mesh zone area;

 L_d represents the logarithmic strain.

In the 1-D and 2-D models, the first 30 m was set as soft soil. At a greater depth to the base rock elevation, interpolated soil data from soft soils and base rock were used, as shown in Figure 6.

4 Result and discussion

Spectral acceleration values for both 1-D and 2-D methods at several points were evaluated. These observation points were a function of location X relative to basin edge and basin width (W), namely, X/W of 0, 1/16, 1/8, 1/4, and 1/2. The basin geometry and observation points can be seen in Figure 7. In this model, a basin width of 1,000 m was used. To evaluate the effect of basin width on the spectral acceleration values, W of 500 m, 2,000 m, and 4,000 was also used.

Figure 8 presents spectral acceleration values based on 1-D and 2-D methods at the basin edge or X/W = 1/16. A comparison of the 1-D and 2-D spectral acceleration values shows significant differences, particularly at periods below 0.1 s and 0.6 s–3 s. Figure 9 shows the spectral acceleration values from the 1-D and 2-D methods at the central part of the basin (i.e., X/W = 1/2). The spectral acceleration values from both methods are quite similar. These results confirmed (Bard and Gariel, 1986) that 1-D and 2-D methods resulted in similar spectral acceleration values at the basin center, whereas they yielded different spectral acceleration values at the basin edge.

The spectral acceleration values of the 1-D and 2-D methods at a period near 0 s were compared to estimate the scaling factors. The scaling factor describes a multiplier that can be implemented to the 1-D spectral acceleration so that it is equivalent to that of the 2-D

method. A variety of parameters, such as PGA values, D/W, θ , and W, were evaluated to propose the corresponding scaling factors.

4.1 Scaling factor due to PGA (F_q)

Variations in the PGA affect the scaling factor, particularly at the basin edge (X/W = 1/16). The greater the PGA value, the greater the scaling factor is. For example, in a basin with $\theta = 10^{\circ}$, D/W = 0.05, and X/W = 1/16, the F_g values are 1.44, 1.29 for PGA of 0.5 g, and 0.2 g, respectively. It is observed that if the X/Wvalue moves from the edge to the center, the F_g becomes closer to 1 (Figure 10). This pattern was also found in the other θ and D/Wvalues (Table 5).

4.2 Scaling factor due to D/W (F_{DW})

Variation in the D/W value also impacts the scaling factor. The smaller the D/W value, the greater the F_{DW} at the same X/W is. This is observed in basins with θ of 10° and 45° (Figure 11). However, a comparison between D/W = 0.075 and D/W = 0.1, at θ of 15° and X/W of 1/4, showed that D/W increased with F_{DW} (Figure 12). This occurrence may be attributed to the fact that F_{DW} is still affected by the θ at X/W = 1/4. For the same D/W = 0.075 and 0.1, similar findings were also found at θ of 30° and X/W = 1/8. Nevertheless, at D/W = 0.05, the effect of the basin slope to the F_{DW} is reduced. Based on parametric studies on D/W, F_{DW} is still affected by certain θ (i.e., 15° and 30°), particularly at X/W between the edge and the middle of the basin, resulting in a scaling factor that increases with D/W. The study results of the effect of D/W on the scaling factor F_{DW} are summarized in Table 6.

4.3 Scaling factor due to θ (F_{θ})

The scaling factor is also affected by the basin angle. Figure 13 shows the relationship of θ with scaling factor F_{θ} with various X/W for D/W = 0.025, 0.05, 0.075 and 0.1. Observations at the basin edge (X/W = 1/16) indicate that a smaller θ yielded a lower scaling factor than that of larger θ . However, observations at a point farther from the basin edge (e.g., X/W = 1/8) showed that smaller θ resulted in a higher scaling factor. These figures also show that a smaller θ yielded a higher scaling factor. Table 7 summarizes the study results of the effect of θ on the scaling factor F_{θ} .

4.4 Scaling factor due to $W(F_W)$

The effect of basin width on the scaling factor was also evaluated. For this purpose, a study was performed by varying basin widths to 500 m, 1 km, and 2 km, whereas the other basin geometry parameters were fixed (i.e., $\theta = 15^{\circ}$, D = 50 m or 100 m).

Figure 14 presents the variation in F_w with X where $\theta = 15^\circ$, D = 50 m, and D = 100 m. For $\theta = 15^\circ$ and D = 50 m, this figure shows that, around the basin edge, between X = 62.5 m and 125 m,

variations in basin width yield relatively small differences in F_{W} , only up to 1.5%. In addition, for $\theta = 15^{\circ}$ and D = 100 m, this figure shows a variation of *B* from 500 m, 1 km, and 2 km. This figure shows that around the basin edge, between X = 62.5 m and 125 m, a relatively small difference was observed in F_{w} up to 1.7% with varying *W*.

4.5 Bandung Basin

An example of the application of the proposed scaling factors is demonstrated using the Bandung Basin case. This basin is 13 km wide, 200 m deep, $\theta = 5^{\circ}$, and D/W = 0.015. The selected locations of interest are Cicadas and Soekarno–Hatta, as shown in Figure 2. Cicadas, as observation point 1, has an *X* value of 1 km or X/W = 0.08. Soekarno–Hatta, as observation point 2, has an X = 5 km and X/W value of 0.4.

Scaling factors for Cicadas and Soekarno–Hatta can be found in Table 5 (i.e., D/W = 0.0125). This table shows the scaling factor values for observation points 1 and 2 of 1.275 and 1.05, respectively. These scaling factors are multiplied to the acceleration value on the surface obtained from the Indonesian national hazard map. Based on this map, the surface acceleration (S_{PGA}) in the Bandung Basin area is 0.478 g. Thus, the surface accelerations on observation points 1 and 2, which consider the effect of the Bandung Basin on the spectral acceleration, are as follows:

- Scaled PGA at Cicadas = $F_g \cdot S_{PGA} = 1.275 \cdot 0.478 \text{ g} = 0.609 \text{ g}$
- Scaled PGA at Soekarno–Hatta = $F_g \cdot S_{PGA} = 1.05 \cdot 0.478 \text{ g} = 0.502 \text{ g}$

5 Summary and conclusion

A basin containing soft soil is known to influence the ground surface response due to earthquakes, particularly in areas around the basin edge. This study shows and also confirms the previous studies' results, that is,

- 1-D and 2-D wave propagation analyses yielded substantial amplification differences at the basin edge.
- The 1-D analysis, which is popular in practical applications, may not capture the effect of the basin on the spectral acceleration.
- The 2-D method is better than the 1-D method in considering basin geometry.

However, the link between 1-D and 2-D responses has not been studied for engineering practices. Based on practical considerations, it is necessary to estimate the scaling factor for the 1-D analysis by considering the basin presence, particularly for that containing soft soil. These scaling factors can be used to facilitate engineering practice to evaluate the ground response located around the basin, where the 1-D method is immediately available, but 2-D and 3-D methods are not accessible. These are a novelty of the study.

Furthermore, a series of 1-D and 2-D analyses were conducted to evaluate the spectral amplification differences between these two

methods and to conclude the scaling factors. This study investigates the relationship between PGA, basin angle, basin depth, and basin width to the spectral acceleration in several observation points on the ground surface. Moreover, this parametric study also shows that

- The farther from the basin edge, the closer the scaling factor is to 1.
- At the basin edge, the scaling factor is larger than 1.
- At the basin edge, the greater the input motion PGA, the greater the scaling factor is.
- At the basin edge, the smaller the basin angle, the greater the scaling factor is, except for the basin angle of 10°.
- The smaller the basin angle, the higher the scaling factor is at the observation point away from the basin edge.
- The smaller the *D*/*W*, the larger the scaling factor for the basin angles of 10° and 45°.
- In between X/W = 1/8 and $X/W = \frac{1}{4}$ at the angle range of $15^{\circ}-30^{\circ}$, the greater the D/W value, the greater the scaling factor is.
- The basin width, particularly at the basin edge, has relatively little effect on the scaling factor at the same observation point.

Finally, the proposed scaling factors can be used to introduce the effect of basin geometry on ground spectral acceleration. Examples of the application of this scaling factor have been demonstrated using two sites located on the Bandung Basin.

Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material; further inquiries can be directed to the corresponding author.

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DA: conceptualization, methodology, supervision, writing-original draft, and writing-review and editing. AM: software and writing-original draft. AS: writing-review and editing. YB: visualization, supervision, and writing-review and editing. WS: visualization, supervision, and writing-review and editing. AH: visualization and writing-review and editing.

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Conflict of interest

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