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Modelling the effect of $CO₂$ [loading of aqueous potassium](https://www.frontiersin.org/articles/10.3389/fceng.2022.982891/full) glycinate on $CO₂$ [absorption in a](https://www.frontiersin.org/articles/10.3389/fceng.2022.982891/full) [membrane contactor](https://www.frontiersin.org/articles/10.3389/fceng.2022.982891/full)

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 $CO₂$ absorption into aqueous potassium glycinate in a polypropylene membrane contactor was modelled using two alternative models: a 1D model and a 1D-2D model considering axial diffusion in the liquid phase. Models were fitted to experimental data using various fitting parameters, which were compared. Experiments were carried out under industrially relevant conditions characterized by $CO₂$ -loaded absorbent entering the contactor and high degree of reactant conversion over the contactor. The experiments and models were developed to specifically investigate the effect of changes in solution $CO₂$ loading at contactor inlet. This is a key issue rarely reported in the literature, especially for amino acid salt solutions. Unexpectedly, the 1D model was found to explain the experimental results more accurately compared to the more complex 1D-2D model. This was the case for the base models, using only the membrane mass transfer coefficient as a fitting parameter, and the final models introducing secondary fitting parameters. The 1D model was found to show the best experimental fit following fitting of the equilibrium constant used in prediction of the enhancement factor. The 1D-2D model showed the best fit following correction of potassium glycinate diffusivity as a function of solution $CO₂$ loading. The 1D approach was found to result in a computationally effective model with good fit to the present experimental data. This model provides a good basis for further development and could be considered for use in contactor design and optimization studies. It is suggested that various model simplifications led to inability of the 1D-2D model to accurately predict the experimental results.

KEYWORDS

 $CO₂$ capture, $CO₂$ absorption, membrane contactor, amino acid salt, potassium glycinate, modelling

1 Introduction

Carbon dioxide capture processes are considered key technology facilitating the decarbonization of the energy sector and emission-heavy chemical industries. Such processes aim to capture $CO₂$ directly at the emission source followed by long-term storage of $CO₂$ into various geological features [\(Bui](#page-16-0) [et al., 2018](#page-16-0)), or by conversion of $CO₂$ into valuable fuel or chemical products [\(Ampelli et al., 2015](#page-16-1)). Alternatively, $CO₂$ can be captured directly from the atmosphere, making capture location-independent, but resulting in increased energy demand and costs due to the lower initial $CO₂$ concentration ([Goeppert](#page-16-2) [et al., 2012](#page-16-2)).

Various types of processes have been developed for the capture of $CO₂$ at emission sources [\(Boot-Handford et al.,](#page-16-3) [2014\)](#page-16-3). The selection of optimal technology most importantly depends on the $CO₂$ concentration and conditions of the $CO₂$ containing stream to be treated. The technologies can be roughly divided to those more suitable for pre-combustion capture, i.e., capture from high- $CO₂$ concentration (<15%) and highpressure (>25 bar) streams, and those applicable in postcombustion capture, characterized by low $CO₂$ concentration $(<15\%)$ and low total pressure (-1 atm) , representing conditions typical to power plant flue gases ([Feron et al., 2019\)](#page-16-4). For the latter application, absorption of $CO₂$ into aqueous amine solutions is considered the benchmark technology [\(Feron et al., 2020](#page-16-5)).

Membrane contactors have been investigated as alternative gas-liquid contacting equipment for absorption-based postcombustion capture processes [\(Zhao et al., 2016](#page-17-0)). Over conventionally used packed columns, the advantages of using membrane contactors include increased operational flexibility enabled by physical separation of the gas and liquid phases by the membrane, decreased equipment size due to higher specific gasliquid contact area per unit volume, and simple scale-up due to the modular nature of membrane contactors. Unlike membrane gas separation processes, the membrane contactors are nonselective, with selective absorption of $CO₂$ facilitated by chemical interaction between $CO₂$ and the solvent.

To ensure membrane stability and to minimize the additional mass transfer resistance due to the membrane, the compatibility between the membrane material and the type of solvent is vital. A major challenge is the wetting of polymeric membranes by amine solutions, dictating the use of advanced membrane materials, or the use of alternative solutions with lesser wetting tendency ([Mosadegh-Sedghi et al., 2014\)](#page-16-6). A promising approach is the use of aqueous amino acid salt-based absorbents, as such solutions typically do not wet low-cost polymeric membranes due to their high surface tension compared to amine solutions ([Kumar et al., 2002\)](#page-16-7). Other than improved compatibility with membrane contactors, the relevant properties of amino acid salt solutions, including $CO₂$ absorption rates and capacities, are generally comparable to those of amine solutions [\(Hu et al.,](#page-16-8) [2018\)](#page-16-8).

The present paper discusses the modelling of $CO₂$ absorption into the aqueous amino acid salt potassium glycinate. A variety of models of varying complexity have been developed for aqueous amine solutions, mostly monoethanolamine [\(Chabanon et al.,](#page-16-9) [2013](#page-16-9); [Gebremariam, 2017](#page-16-10); [Rivero et al., 2020](#page-16-11)). In summary, relatively simple models are developed in the 1D-domain based on isothermal assumption, empirical mass transfer correlations and use of the enhancement factor to predict the effect of reaction on the mass transfer rate ([Rode et al., 2012;](#page-17-1) [Albarracin Zaidiza](#page-16-12) [et al., 2014\)](#page-16-12). Characteristics of more complex models include the consideration of the axial direction in the liquid (and gas) phase, inclusion of heat effects, detailed calculation of reaction rates and prediction of physical properties, incorporation of rigorous chemical and phase equilibrium calculations, and also multicomponent mass transfer including water and/or amine transfer [\(Rongwong et al., 2013](#page-17-2); [Hoff and Svendsen, 2014;](#page-16-13) [Albarracin](#page-16-14) [Zaidiza et al., 2016;](#page-16-14) [Gebremariam, 2017\)](#page-16-10).

Such models are more scarcely available for amino acid salt solutions such as potassium glycinate ([Eslami et al., 2011;](#page-16-15) [Masoumi et al., 2016](#page-16-16); [Ghasem, 2020](#page-16-17)). Compared to the previous work, the novel approach of the present study is to focus on the prediction of $CO₂$ transfer rate as a result of changes in the lean solvent $CO₂$ loading, i.e., the $CO₂$ content in the solution entering the membrane contactor. At the same time, experiments were designed to approach industrial operating conditions characterized by high reactant conversion over the contactor. The lean loading is considered an important operating parameter as it directly influences the $CO₂$ absorption rate and capacity of the solvent. It is also tied to the overall optimization of the capture process which consists of absorption and solvent regeneration, as regeneration of the solvent to lower loading increases the process energy consumption ([Abu-Zahra et al.,](#page-16-18) [2007](#page-16-18)). With some exceptions [\(Albarracin Zaidiza et al., 2015\)](#page-16-19), model-based analyses on the effect of lean loading have not been reported even for conventional amine solvents, much less amino acid salt solutions. The present paper aims to address this by means of model development combined with experimental validation.

2 Materials and methods

2.1 Experimental

CO2 absorption experiments were carried out using 1 M aqueous potassium glycinate as the absorbing solution. The solution was prepared by neutralization of glycine (Sigma-Aldrich, >99%) with equimolar amount of potassium hydroxide (Sigma-Aldrich, >85%) dissolved in purified water. Concentration was verified (within 1% of nominal concentration) by potentiometric titration using 1 M hydrochloric acid. Feed gas consisted of nitrogen (>99.5%) mixed with 10 vol% of $CO₂$ (AGA, >99.99%).

TABLE 1 Membrane contactor properties. Fiber details are omitted as this information is not publicly available from the supplier.

The experimental setup consisted of the membrane contactor (3 M Liqui-Cel 2.5×8 Extra-Flow) as the absorber, a buffer vessel for the absorbing solution, a magnetic drive gear pump (Pulsafeeder Eclipse E12) for solvent circulation, and equipment for controlling the solvent temperature prior to entering the absorber. A flowsheet of the unit is given in [Figure 1](#page-2-0), and details of the membrane contactor are given in [Table 1](#page-2-1). The flow configuration in the contactor was set up with liquid flowing on the lumen side (inside membrane fibers) and gas on the shell side. Liquid flow rate was controlled using a volume flow meter (Litre Meter LMX.48) and verified gravimetrically. Solution temperature was controlled by a heating coil installed within the solution vessel, and a plate heat exchanger (Alfa Laval, 0.2 m²) installed prior to the membrane contactor. Both were connected to circulating water heater/coolers (Lauda).

Inlet gas flows were controlled using mass flow controllers (Bronkhorst EL-FLOW Select). The $CO₂$ concentration in the inlet and outlet gas was measured using infrared analyzers (Vaisala GMP251 probe and Indigo 201 transmitter). Gas pressure was controlled at contactor outlet using a backpressure controller (Bronkhorst EL-PRESS). Liquid pressure was measured by pressure transducers and controlled using a manual needle valve. The pressure at gas outlet was automatically maintained 0.1 bar below the liquid inlet pressure. The control and measurement system was implemented using LabView (2015) software and a data acquisition system (NI cDAQ-

TABLE 2 Operating conditions during absorption experiments.

9189). The control action and data collection frequency were 2000 and 10 Hz, respectively.

The absorption experiments were carried out in batch mode. The system was filled with a batch (4 L) of unloaded solution, which was then circulated for the duration of the experiment, continuously increasing the $CO₂$ loading. Other experimental variables (liquid flow rate and temperature) and parameters (gas flow rate and composition, liquid and gas pressure) were controlled and maintained as close to constant as possible during each run. The operating conditions during the experiments are summarized in [Table 2](#page-3-0). The values given represent nominal or setpoint values. The actual measured values during each experimental run are found in [Supplementary Tables A1](#page-16-20)–[A3](#page-16-20).

By continuous measurement of $CO₂$ concentration in the outlet gas, combined with calculation of $CO₂$ loading from periodically collected liquid samples (lean and rich solution), the $CO₂$ recovery ([Eq. 1\)](#page-3-1) could be correlated with the lean loading during each experiment. The liquid $CO₂$ loading was calculated based on a previously developed correlation with the solution density. The basis of this correlation is the volumetric measurement of $CO₂$ released upon titration with 1 M HCl to neutral pH. The temperatures of lean and rich solution were also measured, and the average of these was taken to represent the temperature at each data point.

$$
\eta = \frac{\dot{n}_{\text{CO}_2,\text{in}} - \dot{n}_{\text{CO}_2,\text{out}}}{\dot{n}_{\text{CO}_2,\text{in}}} \cdot 100\%
$$
 (1)

Where η is the CO₂ recovery (%) and $\dot{n}_{\rm CO_2,in}$ and $\dot{n}_{\rm CO_2,out}$ are the molar flows of $CO₂$ (mol s⁻¹) in the inlet and outlet gas, respectively.

2.2 Modelling

Two separate models were developed and validated using the experimental data. Both models are rating-type models aiming to predict the performance of the membrane contactor, using

contactor sizing and absorbent and inlet gas composition, flow rates, and operating conditions as model inputs. Development of such models would facilitate sizing of the membrane contactor absorber unit, and combined with a solvent regeneration model, the overall optimization of the capture process in terms of energy consumption and overall cost.

The models developed include a simplified 1D model and a 1D-2D model accounting for the convection-diffusion phenomena in the liquid phase. The latter model was created in order to investigate whether the added complexity and detail compared to the 1D model would yield more accurate prediction of the experimental data. The main assumptions taken in development of both models are described in [Table 3.](#page-4-0) Ultimately, the objective of this work was to develop practical and computationally effective models to facilitate design and optimization studies. Detailed and fundamental physical and chemical characterization of the absorption process was thus not targeted. Thus, the 1D-2D model is also based on a relatively simple, empirical approach compared to more rigorous models described in the literature [\(Rongwong et al., 2013](#page-17-2); [Hoff and Svendsen, 2014](#page-16-13); [Albarracin](#page-16-14) [Zaidiza et al., 2016](#page-16-14); [Gebremariam, 2017](#page-16-10)). All modelling was carried out using MATLAB software (R2019a).

When attempting to predict experimental results using the developed absorption models, all model inputs were set exactly as reported for the corresponding experiment and data point, as given in [Supplementary Tables A1](#page-16-20)–[A3.](#page-16-20)

2.2.1 Reaction and physical properties

Within both 1D and 1D-2D models, physical and chemical properties of 1M potassium glycinate and $CO₂$ are calculated using experimental correlations as given in [Table 4](#page-4-1). The models consider a second order irreversible reaction between $CO₂$ and the amino acid salt ([Kumar et al., 2002\)](#page-16-7):

$$
2RNH_2 + CO_2 \rightarrow RNH_3COO^- + RNH_3^* \tag{2}
$$

2.2.2 Gas-liquid equilibrium

The gas-liquid equilibrium of $CO₂$ in 1 M potassium glycinate is modelled using the Henry's law. The Henry's law constant was calculated following ([Portugal et al., 2009\)](#page-16-21). First, the Henry constant for $CO₂$ in water is calculated [\(Versteeg and Van](#page-17-3) [Swaaij, 1988\)](#page-17-3):

$$
H_{CO_2,w} = \frac{e^{-\frac{2044}{T}}}{3.54 \times 10^{-7}}
$$
 (3)

Where $H_{CO_2,w}$ is Henry's law constant (Pa m³ mol⁻¹). The Sechenov model constant for $CO₂$ in potassium glycinate [\(Portugal et al., 2007](#page-16-22)) is calculated from:

$$
K_{CO_2} = \frac{62.183098}{T} - 0.111175\tag{4}
$$

The constant K_{CO_2} (m³ mol⁻¹) gives the ratio between the Henry's law constant of $CO₂$ in aqueous potassium glycinate, and TABLE 3 Main assumptions taken in development of 1D and 1D-2D absorption models.

TABLE 4 Physical property and reaction rate correlations or values used in 1D and 1D-2D absorption models. PG: potassium glycinate.

that in water, as a function of the potassium glycinate concentration:

$$
\log\left(\frac{H_{CO_2}}{H_{CO_2,w}}\right) = K_{CO_2}C_{PG}
$$
 (5)

Where H_{CO_2} is the Henry's law constant of CO_2 in aqueous potassium glycinate (Pa m³ mol⁻¹), and C_{PG} is the solution potassium glycinate concentration (mol m³). The Henry's constant is used to calculate the dimensionless gas-liquid partition coefficient for $CO₂$ in 1M potassium glycinate:

$$
m = \frac{1}{H_{CO_2}} RT \tag{6}
$$

Where R is the universal gas constant $(m^3 Pa K^{-1} mol^{-1})$ The partition coefficient relates the equilibrium $CO₂$ concentration at the gas-liquid interface to the $CO₂$ concentration in the (bulk) liquid phase

$$
C_{CO_2, int} = m C_{CO_2,l} \tag{7}
$$

Where $C_{CO_2, int}$ is the interfacial CO_2 concentration (mol m³), and $C_{CO_2,l}$ is the CO_2 concentration in liquid bulk (mol m³).

2.2.3 1D model

To take into account the evolution of mass transfer phenomena along the axial coordinate of the contactor, the 1D model developed in this study considers three separate mass transfer domains, i.e., $CO₂$ transfer from the bulk phase to the gas-membrane interface, $CO₂$ transfer through the membrane to the membrane-liquid interface and $CO₂$ absorption in the liquid phase enhanced by the occurring chemical reaction between $CO₂$ and potassium glycinate. The effective local mass transfer coefficient, K, is determined following the resistance in series model based on the film theory:

$$
\frac{1}{K} = \frac{1}{k_g} + \frac{1}{k_m} + \frac{1}{mEk_l}
$$
 (8)

Where k_q , k_l and k_m are the mass transfer coefficients for CO_2 transfer in the gas phase, liquid phase and the membrane $(m s^{-1})$, m is the $CO₂$ gas-liquid partition coefficient, and E is the enhancement factor, which accounts for the contribution of the chemical reaction occurring in the liquid phase. The correlations applied for calculation of the mass transfer coefficients for gas and liquid phases are provided in [Supplementary Appendix B1.](#page-16-20)

Apart from neglecting axial and radial dispersion in the liquid and gas phases, the 1D model also assumes isothermal conditions, thermodynamic equilibrium at the gas-liquid interface and constant membrane mass transfer coefficient. In accordance with the experimental work performed in this study, in the gas phase, the model considers only $CO₂$ and $N₂$ species. It is also worth mentioning that N_2 does also pass the membrane, but its mass transfer flux is negligible compared to $CO₂$.

Therefore, $CO₂$ mass balance in the gas phase is described with the following equation ([Rode et al., 2012\)](#page-17-1):

$$
d(Q_g C_{CO_2,g}) = -Ka C_{CO_2,g} S_{shell} dz
$$
 (9)

Where Q_g is the gas flowrate $(m^3 s^{-1})$, $C_{CO_2,g}$ is the CO_2 concentration in the gas phase (mol m⁻³), *a* is gas-liquid interfacial area (m² m⁻³), S_{shell} is the module area without fiber (m^2) and z is the axial coordinate (m) .

The changes in the potassium glycinate concentration due to the chemical reaction in the liquid phase are considered through the following stoichiometric constraint:

$$
d(Q_l C_{PG}) = -2d(Q_g C_{CO_2,g})
$$
\n(10)

Where Q_l is the liquid flowrate (m³ s⁻¹) and C_{PG} is the potassium glycinate concentration in the liquid phase (mol m⁻³).

The changes in the volumetric gas flowrate due to the $CO₂$ absorption are considered with the following global mass balance expression for the inert component:

$$
Q_{g}^{in} \frac{P_{g}^{in}}{RT} \left(1 - y_{CO_2}^{in} \right) = Q_{g} \frac{P_{g}}{RT} \left(1 - y_{CO_2} \right) \tag{11}
$$

Where Q_g^{in} is the gas flowrate at the inlet (m³ s⁻¹), P_g^{in} and P_g are pressure in the gas phase at the inlet and inside the contactor, respectively (Pa), $y_{\text{CO}_2}^{in}$ and y_{CO_2} are CO_2 molar fraction in the gas phase at the inlet and inside the contactor, respectively, R is the universal gas constant (J mol⁻¹ K⁻¹) and T is temperature, K.

The gas phase pressure drop is determined with the Kozeny equation:

$$
-\frac{dP_g}{dz} = \frac{4k\mu}{r_{ext}^2} \frac{\varphi^2}{\left(1-\varphi\right)^2} u \tag{12}
$$

Where k is the Kozeny coefficient, μ is the gas viscosity (Pa s), r_{ext} is the external fiber radius (m), φ is the packing factor and u is the superficial gas velocity $(m s^{-1})$.

To determine the effect of the potassium glycinate diffusion on the $CO₂$ absorption, Hatta number, Ha, and the infinite enhancement factor, E_{inf} , were calculated based on the following expressions:

$$
Ha = \frac{\sqrt{D_{CO_2}, k_r C_{PG}}}{k_l} \tag{13}
$$

Where $D_{CO_2,l}$ is the CO_2 diffusion coefficient in the liquid phase (m² s⁻¹) and k_r is the rate constant of the reaction occurring between the potassium glycinate and CO_2 (m³ mol⁻¹ s⁻¹). The infinite enhancement factor, corresponding to the situation where reaction rate is limited by reactant diffusion, was calculated using the following equation. This modified equation includes the apparent equilibrium constant K_{eq} which essentially constitutes a fitting parameter improving the enhancement factor prediction under conditions of reversible reaction and high reactant conversion [\(Hoff and Svendsen, 2014](#page-16-13)).

$$
E_{inf} = \left(\frac{D_{CO_2,l}}{D_{PG}}\right)^{1/3} + \left(\frac{D_{PG}}{2D_{CO_2,l}}\right)^{2/3} \frac{K_{eq}C_{PG}}{1 + K_{eq}C_{CO_2, int}} \tag{14}
$$

Where D_{PG} is potassium glycinate liquid diffusion coefficient $(m^2 s^{-1})$ and $C_{CO_2, int}$ is the CO_2 concentration at the gas-liquid interface (mol m[−]³), which is determined following the Henry law.

This way, if the $CO₂$ capture is not limited by reactant diffusion, the value of the enhancement factor E approximately equals the Hatta number. In case of potassium glycinate diffusion significantly limiting the $CO₂$ capture process, the infinite enhancement factor is considered ([Rode et al., 2012\)](#page-17-1).

$$
\begin{cases}\n\frac{E_{inf}}{Ha} > 50 \to E = Ha \\
\frac{E_{inf}}{Ha} < 0.02 \to E = E_{inf}\n\end{cases}
$$
\n(15)

In case of the intermediate situation, i.e., partial diffusion limitation of potassium glycinate, the enhancement factor is evaluated with the equation developed by [DeCoursey \(1974\):](#page-16-24)

$$
E = \frac{-Ha^2}{2(E_{inf}-1)} + \sqrt{\frac{Ha^4}{4(E_{inf}-1)^2} + \frac{E_{inf}Ha^2}{(E_{inf}-1)} + 1}
$$
 (16)

To solve the obtained system of equations, the following boundary conditions were applied:

$$
\begin{cases}\nC_{CO_2,g}|_{z=0} = C_{CO_2,g}^{in} \\
P_g|_{z=0} = P_g^{in} \\
C_{PG}|_{z=L} = C_{PG}^{in}\n\end{cases}
$$
\n(17)

To solve the boundary value problem and determine $CO₂$ concentration at the outlet, $C_{CO_2,q}|_{z=L}$, the iterative shooting method was applied ([Kiusalaas, 2010\)](#page-16-25). The system of ordinary differential equations was solved in MATLAB with explicit nonstiff solver ode23 ([Kiusalaas, 2010](#page-16-25)), the use of which was found to result in stable and quick (<1 min) solution of the problem over the investigated operational range.

2.2.4 1D-2D model

In contrast to the 1D model, the developed 1D-2D model takes account of the radial diffusion phenomena in the liquid phase and explicitly simulates the reaction between potassium glycinate and dissolved $CO₂$. Therefore, for the liquid phase, the general form of the differential mass balance equation is considered, and no enhancement factor is required. This provides an opportunity to explicitly resolve diffusion in the radial direction together with mass transfer and reaction in the boundary layer. A grid independence study was conducted to ensure sufficient grid density and address the potential inaccuracies due to the sharp changes in the radial concentration profiles. More details on the grid independence study are provided in [Supplementary Appendix C1.](#page-16-20)

Considering the negligible mass transfer resistance in the gas phase, the 1D assumption for this domain is consistent. This assumption is further corroborated by the physical properties of the membrane contactor–the wider shell side incites more turbulent flow in the gas phase, while the small inner diameter of a fiber leads to laminar liquid flow in the liquid phase. Therefore, axial convection and radial diffusion are modeled for the liquid phase, while constant velocity and perfect plug flow is assumed for the gas phase. Furthermore, the model also assumes isothermal conditions, thermodynamic equilibrium at the gas-liquid interface and constant membrane mass transfer coefficient.

While $CO₂$ transfer phenomena occurring in the gas phase are modeled in the same way as in the 1D model, mass conservation equations for $CO₂$ and potassium glycinate in the liquid phase are expressed in the following way:

$$
v_l \frac{\partial C_{PG}}{\partial z} = D_{PG} \left(\frac{1}{r} \frac{\partial C_{PG}}{\partial r} + \frac{\partial^2 C_{PG}}{\partial r^2} \right) + 2R_{CO_2}
$$
 (18)

$$
v_l \frac{\partial C_{CO_2,l}}{\partial z} = D_{CO_2,l} \left(\frac{1}{r} \frac{\partial C_{CO_2,l}}{\partial r} + \frac{\partial^2 C_{CO_2,l}}{\partial r^2} \right) + R_{CO_2}
$$
 (19)

Where v_l is the interstitial velocity in the liquid phase (m s⁻¹), $C_{CO_2,l}$ is the CO_2 concentration in the liquid phase (mol m⁻³), R_{CO_2} is the reaction rate of CO_2 with potassium glycinate (mol m⁻³ s⁻¹) and r is the radial coordinate (m).

The transmembrane flux of $CO₂$ is considered as a part of the boundary conditions applied in the radial direction:

$$
\left\{\n\begin{array}{c}\n\frac{\partial C_{CO_2,l}}{\partial r}\bigg|_{r=0} = 0 & D_{CO_2,l} \frac{\partial C_{CO_2,l}}{\partial r}\bigg|_{r=r_{int}} = k_{ext} \Big(C_{CO_2,g} - C_{CO_2,int}\Big) \\
\frac{\partial C_{PC}}{\partial r}\bigg|_{r=0} = 0 & \frac{\partial C_{PC}}{\partial r}\bigg|_{r=r_{int}} = 0\n\end{array}\n\right\}
$$
\n(20)

Where k_{ext} is the external mass transfer coefficient (m s⁻¹), i.e., a lumped parameter describing the transfer of $CO₂$ from the bulk of the gas phase to the gas-membrane interface and through the membrane. This coefficient is expressed with the following equation:

$$
\frac{1}{k_{ext}} = \frac{1}{k_g} + \frac{1}{k_m} \tag{21}
$$

The rate of reaction between $CO₂$ and potassium glycinate is determined with the following equation:

$$
R_{CO_2} = k_r C_{PG} C_{CO_2,l} \tag{22}
$$

Accounting for the laminar flow of the liquid inside the hollow fibers, the parabolic velocity profile is assumed:

$$
v_l = 2v_{l,av} \left[1 - \left(\frac{r}{r_{int}} \right)^2 \right] \tag{23}
$$

Where $v_{l,av}$ is the average liquid velocity (m s⁻¹) and r_{int} is the internal radius of a fiber (m).

The obtained system of differential equations was solved in MATLAB with the same boundary conditions applied in the axial direction ([Eq. 20\)](#page-6-0). Numerical method of lines was applied to discretize the obtained system of partial differential equations into a system of ordinary differential equations. More specifically, the first order radial derivatives were approximated with the fourth order finite difference approximation (dss004 algorithm as in [\(Schiesser, 2016\)](#page-17-4), while the second order approximation (dss042 algorithm as in [\(Schiesser and Grif](#page-17-5)fiths, 2009) was applied to the second order radial derivatives. Accounting for the sharp concentration fronts in close vicinity to the gas-liquid interface, a very fine discretization was applied to ensure numerical stability of the solution. More specifically, the liquid phase domain was discretized into 1,000 compartments in both radial and axial directions. As highlighted by the results of the grid independence study ([Supplementary Appendix](#page-16-20)), no changes in the model's accuracy were observed with a more refined discretization. The obtained system of ordinary differential equations is solved with a stiff, variable-step solver ode15s ([Wouwer et al., 2014](#page-17-6)). Similar to the 1D model, the boundary value problem was solved iteratively via shooting method.

2.2.5 Parameter fitting

Both the 1D and 1D-2D models were fitted to the experimental data by means of empirical parameter fitting. Parameter fitting was carried out in MATLAB (R2019a) using the "fmincon" constrained non-linear equation solver to minimize the objective function. The objective function consisted of the summed error squared between the experimental and model results over all experimental runs. The parameter estimation procedure was found computationally effective with the 1D model (<5 min per estimation case) but slow (hours per case) and somewhat difficult to converge with the 1D-2D model. During the estimation, initial values and bounds for variables were manually refined in a trial-and-error fashion to assist quick solution. The presence of local optimums was not explicitly checked but no signs of multiple minima for the objective function were observed during the described estimation procedure.

The membrane mass transfer coefficient was used as the primary fitting parameter. This approach has been suggested as the accurate prediction of the membrane mass transfer coefficient is difficult and would require very detailed knowledge of the membrane pore size distribution and geometry that is generally not available [\(Chabanon et al.,](#page-16-9) [2013\)](#page-16-9).

In addition to the membrane mass transfer coefficient k_m , both models were tested using various secondary fitting parameters to improve the overall fit. These second fitting parameters were used for empirical adjustment of either component diffusivities or reaction rate predictions. Both constitute key model components affecting the predicted $CO₂$ absorption rates and $CO₂$ recoveries over the contactor. First, the rate constant for the second order reaction between CO₂ and potassium glycinate, k_r , was fitted using a correction factor, yielding the apparent reaction rate constant $k_{r,app}$:

$$
k_{r,app} = f k_r \tag{24}
$$

Where f is the fitted correction factor, and k_r is the original temperature-dependent reaction rate constant. The apparent equilibrium constant K_{eq} , used in the calculation of the infinite enhancement factor ([Eq. 14](#page-5-0)), was selected as an alternative reaction rate-related fitting parameter for the 1D model. This equilibrium constant has specifically been introduced to improve the enhancement factor prediction at high reactant conversion, i.e., loading [\(Hoff and Svendsen, 2014](#page-16-13)). As a simplification, this parameter was fitted without a temperature dependence.

Correction of potassium glycinate diffusivity in solution was also considered. This was done via empirical correlation of the apparent diffusivity with the loading. It should be noted that the apparent diffusivity constitutes the overall or mean diffusivity of free potassium glycinate and ionic reaction products. The latter are not included in the present simplified models but are considered in rigorous models implementing chemical speciation and equilibrium calculations. In case of amines such as monoethanolamine, the diffusivity of the reaction products is known to be lower compared to free amine ([Hoff,](#page-16-26) [2003\)](#page-16-26). Thus, it is feasible to consider a decrease in the apparent diffusivity with increasing amine conversion. In the present work, various forms of correlation were tested, and the exponential correlation of the following form was found to yield the best model fit:

$$
D_{PG,app} = D_{PG} \left(1 - a^f \right) \tag{25}
$$

Where $D_{PG,app}$ is the corrected apparent diffusivity, D_{PG} is the temperature-dependent diffusivity of potassium glycinate in the unloaded solution, a is the solution $CO₂$ loading, and f is the fitted correction exponent.

3 Results

The results of this study consist of the resulting fits of 1D and 1D-2D model to the experimental data using various fitting parameters, and analysis of contactor performance using the fitted models.

3.1 1D model

3.1.1 Parameter fitting

[Figure 2](#page-8-0) presents the 1D model fits to experimental data using alternative fitting parameters as described in [Section 2.2.5.](#page-6-1) For each experimental run and at each data point, model parameters were set to match corresponding experimental data ([Supplementary Tables A1](#page-16-20)–[A3\)](#page-16-20). In the base model, only the membrane mass transfer coefficient is fitted. Other fits consider second fitting parameters in addition to the membrane mass transfer coefficient. The introduction of secondary parameters was found to improve the model fit by increasing the predicted effect of $CO₂$ loading on the $CO₂$ recovery, i.e., making the curves shown in [Figure 2](#page-8-0) steeper. The difference between the various models is most prominent in prediction of results from the third experiment, at 30° C and 0.21 L min[−]¹ .

[Table 5](#page-8-1) compares the resulting 1D model fits with the alternative fitting parameters. In terms of coefficient of determination (R^2) , the best fit to experimental data was found with the combination of the membrane mass transfer coefficient and the equilibrium constant K_{eq} as fitting parameters.

3.1.2 Contactor performance and profiles

 $CO₂$ absorption in the membrane contactor was investigated using the 1D model with K_{eq} fitted. [Figure 3](#page-9-0) presents the normalized concentrations of $CO₂$ in the gas phase and potassium glycinate in the liquid phase over the contactor length. The model results are shown for replicated experimental cases, using the corresponding experimental conditions as model inputs in each case. Detailed operating conditions for the corresponding runs are given in [Supplementary Tables A1](#page-16-20)–[A3.](#page-16-20) The left-hand plot shows predicted concentrations during a single run at varied lean loading, and the right-hand plot compares the results of different runs at nearly identical lean loading.

[Figure 4](#page-9-1) presents the variation in volumetric $CO₂$ flux transferred from gas to liquid over the contactor length. The volumetric flux corresponds to the $CO₂$ flux per overall contactor volume. The results are shown for replicated experimental cases. Detailed operating conditions for the corresponding runs are given in [Supplementary Tables](#page-16-20) [A1](#page-16-20)–[A3](#page-16-20). The left-hand plot shows predicted concentrations

TABLE 5 Fitting parameters tested for the $1D CO₂$ absorption model.

during a single run at varied lean loading, and the right-hand plot compares the results of different runs at nearly identical lean loading.

[Figure 5](#page-10-0) presents the variation in calculated enhancement factor for chemical absorption over the contactor length. Enhancement factor was calculated following [Eqs 13](#page-5-1)–[16.](#page-5-2)

FIGURE 3

Normalized concentration of CO₂ in gas and potassium glycinate (PG) in liquid over the contactor length, as predicted by the 1D absorption model. Left: variation of lean loading at constant liquid flow rate and temperature. Right: variation of liquid flow rate and temperature at (nearly) constant lean loading. Liquid inlet at $z = 0$, gas inlet at $z = 0.16$.

constant liquid flow rate and temperature. Right: variation of liquid flow rate and temperature at (nearly) constant lean loading. Gas inlet at $z = 0$, liquid inlet at $z = 0.16$.

The equilibrium constant K_{eq} for calculation of the infinite enhancement factor ([Eq. 14\)](#page-5-0) was fitted to experimental data. The fitting procedure is discussed in [Section 2.2.5](#page-6-1) and results of the parameter estimation are discussed in [Section 3.1.1.](#page-7-0) The results in [Figure 5](#page-10-0) are shown for replicated experimental cases. Detailed operating conditions for the corresponding runs are given in [Supplementary Tables A1](#page-16-20)–[A3](#page-16-20). The left-hand plot shows predicted concentrations during a single run at varied lean loading, and the right-hand plot compares the results of different runs at nearly identical lean loading.

3.2 1D-2D model

3.2.1 Parameter fitting

[Figure 6](#page-11-0) compares the experimentally determined $CO₂$ recovery values and corresponding results obtained with the 1D-2D model. For each experimental run and at each data point, model parameters were set to match corresponding experimental data ([Supplementary Tables A1](#page-16-20)–[A3](#page-16-20)). It can be noted that the 1D-2D model exhibits poor accuracy in description of the experimental results if membrane mass

transfer coefficient is used as the only adjustable parameter. Introduction of secondary fitting parameters results in a considerable improvement in the agreement between experimental and simulation results. [Table 6](#page-12-0) compares the resulting 1D-2D model fits with the alternative fitting parameters. Correction of the potassium glycinate diffusivity resulted in the most improved accuracy. Even with the resulting model, the fit remains poor for the third experiment carried out at 30°C and 0.21 L min[−]¹ .

3.2.2 Concentration profiles

Since the 1D-2D model explicitly simulates concentrations of $CO₂$ and potassium glycinate in the liquid phase, it enables visualization of the actual concentration profiles of these species inside the fiber. This way, for the purpose of improved understanding of the $CO₂$ capture process, [Figures 7](#page-12-1), [8](#page-12-2) illustrate concentration profiles of potassium glycinate and dissolved CO₂, respectively.

It is worth mentioning that due to reaction between potassium glycinate and $CO₂$ concentration of dissolved $CO₂$ is almost negligible for the most part. Relatively high concentrations of dissolved $CO₂$ can be observed only at the gas inlet point, where potassium glycinate solution is comparatively low. Therefore, to illustrate the dissolved CO2 concentration, [Figure 8](#page-12-2) is focused on the region located in the close vicinity to liquid-membrane interface near the gas inlet. To highlight the changes in the $CO₂$ concentration at the gas-liquid interface with variation in solution $CO₂$ loading, [Figure 9](#page-13-0) gives the same profiles in average concentration over the fiber length.

4 Discussion

Discussion of results presented above is divided into two sections. First, fitting of model parameters and resulting fits to experimental data are explained and potential model limitations identified. Next, the contactor modelling results obtained with the best-fit models are analyzed.

4.1 Model development and parameter fitting

Empirical parameter fitting was carried out to improve the fit of models to the experimental data. The membrane mass transfer coefficient was selected as the primary fitting parameter. This approach has been suggested as the accurate estimation of the mass transfer coefficient would require the characterization of gas diffusivities and membrane properties at such detail that is difficult to realize in practice [\(Chabanon et al., 2013\)](#page-16-9). Furthermore, the membrane mass transfer coefficient is strongly affected by partial wetting of the membrane via much reduced diffusivity of $CO₂$ in liquid-filled as opposed to gas-filled pores [\(Mosadegh-Sedghi et al., 2014\)](#page-16-6). It is noted that the primary motivation of utilizing amino acid salt-based absorbents (such as potassium glycinate) instead of more common amine solutions is the much reduced membrane wetting tendency due to higher surface tension of the ionic salt solutions [\(Kumar et al., 2002](#page-16-7)).

With such parameter fitting, the membrane mass transfer coefficient is reduced to a lumped parameter that adjusts the

model predictions not only via membrane properties, but also corrects for various effects including changes in operating conditions (flow rates, temperature, pressure), phenomena not captured by the model due to various simplifications, and also experimental error. For this reason, direct comparison of mass transfer coefficient values between different experimental and modelling studies may not be very meaningful. However, the values obtained here (approximately 2×10^{-4} m s⁻¹) are consistent with experimental studies with polypropylene contactors ([Franco et al., 2008](#page-16-27); [Lin et al., 2009](#page-16-28)). Furthermore,

TABLE 6 Fitting parameters tested for the $1D-2D CO₂$ absorption model.

 $r = 1$.

CO₂ concentration profiles in the liquid phase. Heatmaps denote CO₂ concentration in mol m⁻³. Fiber wall at r = 1. Note limited x- and y-axis.

the obtained values are nearly identical between the 1D and 1D-2D models. This gives us some confidence in the ability of both models to capture the major mass transfer effects taking place in the contactor.

On the other hand, the fit of both models to experimental data remains unsatisfactory with only the membrane mass transfer coefficient fitted (1D model: [Figure 2](#page-8-0); 1D-2D: [Figure 6\)](#page-11-0). In summary, the model fits are found relatively good at low $CO₂$ loading, but deteriorate as the loading increases. Thus, the base models are not able to sufficiently predict the effect of $CO₂$ loading. Somewhat surprisingly, the simpler 1D model is found to give better predictions over the loading range investigated. Potential explanations for this are discussed below. Due to the insufficient model fits, the inclusion of second fitting parameters in addition to the membrane mass transfer coefficient was considered. These parameters were selected to adjust either the reaction rate between $CO₂$ and potassium glycinate, or potassium glycinate diffusivity in the liquid phase, having identified these as key phenomena affecting the overall absorption rate.

One of the key differences between the two models is the approach used to estimate the effect of reaction between $CO₂$ and potassium glycinate on $CO₂$ absorption. In the 1D model, this is done via estimation of the enhancement factor by means of literature correlations. Two distinct reaction regimes are identified: when reaction is limited by intrinsic rate of reaction, the enhancement factor is given by the Hatta number ([Eq. 13\)](#page-5-1); and when reaction is limited by reactant diffusion, the corresponding infinite enhancement factor is calculated ([Eq. 14](#page-5-0)). In the present model, an edited version of the infinite enhancement factor is used to potentially improve the prediction at high reactant conversion ([Hoff and Svendsen,](#page-16-13) [2014](#page-16-13)). This formulation is also suitable for reversible reactions *via* introduction of the apparent equilibrium constant K_{eq} . In the intermediate regime (partial diffusion limitation), the DeCoursey equations is used to estimate the enhancement factor [\(Eq. 16\)](#page-5-2). It should be noted that in the modelling cases considered in this study, the $\frac{E_{inf}}{Ha}$ ratio is at the low end of the intermediate regime (in the order of 0.1), suggesting relatively significant diffusion limitation.

The reaction rate constant and the apparent equilibrium constant K_{eq} were tested as reaction-rate related fitting parameters in the 1D model. The latter was found to result in a better fit to data ([Table 5](#page-8-1)). It is suggested that based on the $\frac{E_{inj}}{Ha}$ ratio, there is somewhat significant diffusion limitation especially at higher $CO₂$ loading. Thus, the reaction rate is not as strongly affected by the intrinsic reaction rate, and correction of the infinite enhancement factor via the equilibrium constant has a more significant effect on the model results. As a result of fitting both the equilibrium constant and the membrane mass transfer coefficient, a model with a rather good fit to the experiments over the entire loading range is obtained. The fitted membrane mass transfer coefficient remains in a reasonable range considering literature references. It is noted that the fit could be further improved by introducing a temperature dependence to this constant, as suggested in the reference [\(Hoff and Svendsen,](#page-16-13) [2014](#page-16-13)). However, a reasonable temperature fit would call for more experiments carried out at a wider temperature range.

In the 1D-2D model, the reaction rate is explicitly calculated using the second order rate equation [\(Eq. 22](#page-6-2)). This approach should in principle yield more accurate results as the reaction rate depends on the actual reactant concentrations and is not implicitly calculated via correlations for the enhancement factor. However, the accuracy of reaction rate calculations may suffer from the simplification to consider only "apparent" concentrations of free potassium glycinate and molecular $CO₂$ instead of including the actual ionic reactants and products in solution. The rigorous approach would be to calculate the chemical equilibrium between the solution species and then calculate both the reaction rate and the mass transfer driving force based on these concentrations ([Hoff, 2003](#page-16-26)). Also, instead of the simple second order relation used here, more complex reaction rate equations could be used following calculation of all species concentrations. Reversible reaction could also be considered to potentially improve the predictions at higher loading. It is noted that in the 1D approach, reversibility is implicitly considered in calculation of the infinite enhancement factor via the fitted equilibrium constant.

It is noted that the Astarita formulation [\(Astarita et al., 1983\)](#page-16-29), based on shared extent of reaction between the individual equilibrium reactions within the system, has been employed as a computationally effective method to introduce chemical species calculations for amine systems. It would be interesting to

use this approach for amino acid salts, as this has apparently not been done in the literature. Alternative approaches have, however, been developed to calculate the chemical speciation in aqueous amino acid salt-CO₂ systems ([Portugal et al., 2009](#page-16-21); [Mondal et al., 2015\)](#page-16-30).

Alternatively, fitting a correlation to correct the potassium glycinate diffusivity as a function of $CO₂$ loading was tested for both models. The exponential form of this correlation is purely empirical and was obtained after testing various formulations. This correction improves the fit for both models. It is suggested that the improvement in the 1D case is again due to the limiting effect of diffusion on the reaction rate under the investigated conditions. Thus, this is essentially an indirect correction of the reaction rate, which is now decreased at increasing $CO₂$ loading. In the 1D model, the liquid and gas mass transfer coefficients are not directly affected by the potassium glycinate diffusivity ([Supplementary Appendix B1\)](#page-16-20).

In the 1D-2D model, the diffusion of potassium glycinate in the liquid is explicitly modelled. In the absence of chemical species calculations, the added diffusivity correlation results in an apparent diffusivity value that should be understood to represent the "average" for both free potassium glycinate and the ionic reaction products. In the case of amine solutions, the diffusivity of products is known to be lower compared to free amine ([Hoff, 2003\)](#page-16-26). Assuming the same holds for potassium glycinate solutions, this would provide a physically consistent basis for correction the apparent diffusivity as a function of $CO₂$ loading. The 1D-2D model fit is significantly improved with introduction of this correction but remains poor compared to the 1D model.

In summary, the 1D approach appears much more promising of the two models considered in this study. This model is both significantly faster to compute and yields more accurate predictions when compared to the present experimental data. In the literature, 1D models are generally found suitable for design and optimization studies while not providing the same accuracy as more rigorous 2D models [\(Chabanon et al., 2013](#page-16-9); [Hoff and Svendsen, 2014;](#page-16-13) [Albarracin Zaidiza et al., 2016](#page-16-14)). The present 1D model should be further developed and tested with a more comprehensive set of experimental data under a wider range of operating conditions. To further approach the industrial operating conditions, investigations should be carried out at higher amino acid salt concentration and at higher absorption temperature. For better prediction over a wider temperature range, adiabatic instead of isothermal modelling should likely be carried out as the temperature changes over the contactor due to heat of absorption can be significant [\(Albarracin Zaidiza et al.,](#page-16-19) [2015\)](#page-16-19).

The 1D-2D model developed here would require significant improvement to justify its use over the simpler model. It appears that the various simplifications taken result in a model that fails to capture the relevant effects taking place under the investigated operating conditions. Besides the isothermal assumption and omitting chemical speciation, a number of potential limitations can be identified. These include more rigorous phase equilibrium calculations (e.g., using equations of state), more detailed calculations of physical properties as function of both temperature and composition, and multicomponent mass transfer. As amino acid salts are non-volatile, the latter would probably consider the evaporation and transfer of water and possibly resulting complications such as membrane wetting by condensation.

4.2 Fitted model results

The contactor performance was investigated using both the 1D and 1D-2D models. For both models, the fitting parameters resulting in the best fit to experimental data [\(Tables 5](#page-8-1), [6\)](#page-12-0) were selected, representing the final version of each model developed within this study.

The concentration, $CO₂$ flux, and enhancement factor profiles generated using the 1D model were presented ([Figures](#page-9-0) $3-5$ $3-5$ $3-5$) to show the effects of the major operating parameters: $CO₂$ loading, liquid flow rate, and temperature. Within the studied range of operating conditions, the concentration and flux profiles lead to the following conclusions: the $CO₂$ flux is increased with increasing liquid flow rate, decreased with increasing loading, and not significantly affected by the temperature. Decreasing the liquid flow rate results in a decrease in the liquid mass transfer coefficient [\(Supplementary Appendix B1\)](#page-16-20). More importantly, reduction of the liquid flow rate, while keeping the gas flow rate constant, results in a more significant increase in $CO₂$ loading over the contactor. For reference, the modelled rich loading at 0.10 L min[−]¹ is 0.46, and that at 0.21 L min[−]¹ (both at 20 and 30°C) is 0.33. At higher loading, free glycinate is more significantly depleted, which leads to a decrease in the reaction rate, as indicated by the enhancement factor. The same is seen when comparing the data obtained at varying lean loading but constant flow rate at 0.21 L min[−]¹ . In this case, from low to high lean loading, the modelled rich loading is 0.37, 0.41, 0.46, respectively.

Effects of changing the liquid temperature are not as straightforward to characterize. On the other hand, increase in temperature increases both the reaction rate and diffusivity. However, it also affects the vapor-liquid equilibrium, with the absorption capacity of the solvent decreased with increasing temperature. In the present case, the various effects seem to offset as the difference between $CO₂$ recovery (both experimental and calculated) at 20°C or 30°C is minor. Looking at [Figure 2](#page-8-0), the recovery at 30°C seems to be higher at the higher end of the $CO₂$ loading range (above 0.3). Above, it was suggested that at high loading, reaction (and absorption) become increasingly limited by reactant diffusion. It could be that the diffusion limitation is somewhat reduced at the higher temperature due to increased potassium glycinate diffusivity. It is noted that careful conclusion

about the effect of temperature should be made from this work due to limited number of experiments carried out in narrow temperature range, and the isothermal assumption made in model development.

To illustrate the more detailed results obtained from the 1D-2D model, the two-dimensional concentration profiles of potassium glycinate and $CO₂$ in the liquid phase are presented in [Figures 7,](#page-12-1) [8,](#page-12-2) respectively. Owing to the parabolic velocity profile in the liquid phase, the changes in both concentration profiles bear a parabola-like shape. As $CO₂$ comes through the liquid-membrane interface, the rate of decrease in potassium glycinate concentration is the highest in close vicinity to the membrane. In contrast, the potassium glycinate concentration in the center of the fiber remains comparatively unaffected in light of the relatively slow diffusion in the liquid phase. However, as the reaction proceeds and potassium glycinate is being consumed, its concentration gradually decreases across the entire fiber width. This is particularly evident in case of high lean loading of the potassium glycinate concentration ([Figure 7](#page-12-1), right).

At the same time, the concentration profile of dissolved CO2 follows the reversed pattern. More specifically, higher $CO₂$ concentrations in the liquid phase are caused by low potassium glycinate concentrations. This is explicable considering that dissolved CO₂ species are consumed in the reaction with potassium glycinate. As the reaction perishes due to the low potassium glycinate concentration, more $CO₂$ gets dissolved into the liquid phase. This trend is particularly noticeable when comparing [Figures 7](#page-12-1), [8](#page-12-2). The changes in $CO₂$ concentration profile at the gas-liquid interface, located at fiber wall, are highlighted in [Figure 9](#page-13-0). The very sharp profile at low loading is broadened when the reaction rate slows down with increasing loading. This decrease in the concentration gradient is consistent with the decrease in enhancement factor as found with the 1D model.

5 Conclusion

 $CO₂$ absorption into aqueous potassium glycinate in a polypropylene membrane contactor was modelled using two alternative models: a 1D model and a 1D-2D model considering axial diffusion in the liquid phase. While the latter represents a slightly more rigorous approach, both models are empirical in nature and simplified compared to more detailed models presented in the literature for various absorbent systems, mostly aqueous amines. Both models were fitted to experimental data, with experiments carried out under the industrially relevant conditions characterized by $CO₂$ -loaded absorbent entering the contactor, and high degree of reactant conversion over the contactor. In addition, experiments were developed to specifically investigate the effect of changes in solution $CO₂$ loading on the $CO₂$ absorption rate, a key issue that seems to be rarely reported in the literature, especially for amino acid salt solutions.

Somewhat surprisingly, the 1D model was found to explain the experimental results more accurately compared to the more complex 1D-2D model. This was the case for the base models, using only the membrane mass transfer coefficient as a fitting parameter, and the final models with secondary fitting parameters introduced. The 1D model was found to show the best experimental fit following fitting of the apparent equilibrium constant, introduced to improve the enhancement factor prediction for reversible reactions at high reactant conversion. The 1D-2D model showed the best fit with empirical correction of potassium glycinate diffusivity as a function of solution $CO₂$ loading. It is suggested that the various simplifications taken lead to inability of the 1D-2D to accurately predict the experimental results. On the other hand, the 1D model provides a computationally effective model with good fit to the present experimental data. This model warrants further development and testing against further experiments carried out under a wider range of operational conditions.

Data availability statement

The original contributions presented in the study are included in the article/[Supplementary Material,](#page-16-20) further inquiries can be directed to the corresponding author.

Author contributions

HN: ideation and planning, experimental work, model development and calculations, manuscript preparation. PM: model development and calculations, manuscript preparation. AL: model development, manuscript editing. TK: manuscript editing, supervision.

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Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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Supplementary material

The Supplementary Material for this article can be found online at: [https://www.frontiersin.org/articles/10.3389/fceng.](https://www.frontiersin.org/articles/10.3389/fceng.2022.982891/full#supplementary-material) [2022.982891/full#supplementary-material](https://www.frontiersin.org/articles/10.3389/fceng.2022.982891/full#supplementary-material)

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Nomenclature

Abbreviations

a Gas-liquid interfacial area, m² m⁻³ $C_{CO_2,q}$ CO₂ concentration in the gas phase, mol m⁻³

 $C_{CO_2, int}$ CO₂ concentration at gas-liquid interface, mol m⁻³

 C_{CO_2} , CO₂ concentration in the liquid phase, mol m⁻³

 C_{PG} Potassium glycinate concentration in the liquid phase, mol m⁻³

 D_{CO_2} , CO_2 diffusivity in 1M in 1M aqueous potassium glycinate, $m^2 s^{-1}$

 D_{PG} Potassium glycinate diffusivity, m² s⁻¹

 $D_{PG,app}$ Apparent potassium glycinate diffusivity, m² s⁻¹

E Enhancement factor, -

 E_{inf} Infinite enhancement factor, -

f Correction factor, -

 H_{CO} . Henry's law constant for $CO₂$ in 1M aqueous potassium glycinate, Pa m³ mol⁻¹

 $H_{CO₂,w}$ Henry's law constant for CO₂ in water, Pa m³ mol⁻¹ Ha Hatta number, -

 K_{CO} , Sechenov model constant for CO2 in aqueous potassium glycinate, m^3 mol⁻¹

 K_{eq} Equilibrium constant for calculation of infinite enhancement factor, m^3 mol⁻¹

k Kozeny coefficient, -

 k_{ext} External mass transfer coefficient, m $\rm s^{−1}$

 k_q Gas-phase mass transfer coefficient, m s⁻¹

 k_l Liquid-phase mass transfer coefficient, m s⁻¹

 k_m Membrane mass transfer coefficient, m s⁻¹

 k_r Second order reaction rate constant, m³ mol⁻¹ s⁻¹

 $k_{r,app}$ Apparent second order reaction rate constant, m³ mol⁻¹ s⁻¹ m Gas-liquid partition coefficient for $CO₂$ in 1M aqueous potassium glycinate, -

 P_a Gas phase pressure inside the membrane contactor, Pa

 P_g^{in} Gas phase pressure at membrane contactor inlet, Pa

 Q_g Gas volumetric flow rate, m³ s⁻¹

Qⁱⁿ Gas volumetric flowrate at membrane contactor inlet, m³ s⁻¹

 Q_l Liquid volumetric flow rate, m³ s⁻¹

R Universal gas constant, J mol⁻¹ K⁻¹

 $R_{\rm CO_2}$ Reaction rate of CO₂ with potassium glycinate, mol m⁻³ s⁻¹

r Radial coordinate, m

 r_{ext} External fiber radius, m

Sshell Membrane contactor cross-sectional area not including membrane fibers, m²

T Temperature, K

u Superficial gas velocity, m s⁻¹

 v_l Interstitial velocity in the liquid phase, m s^{−1}

 y_{CO} , Gas phase $CO₂$ mole fraction inside the membrane contactor, -

 $y_{{\rm CO}_2}^{in}$ Gas phase CO₂ mole fraction at membrane contactor inlet, -

z Axial coordinate, m

 a CO₂ loading in liquid, mol mol⁻¹

 η CO₂ recovery, -

μ Gas dynamic viscosity, Pa s

φ Packing factor, -