

# Analysis of Runner Dynamics of Reversible Hydraulic Turbine by Alternating Fluid–Solid Action

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In order to study the effect of alternating fluid-solid action on the dynamic characteristics of the runner of a reversible hydraulic turbine, a reversible hydraulic turbine model is used as the research object, and the two-way fluid-solid coupling method is used to iteratively calculate and analyze the fluid and structural equations to obtain the effect of the reversible hydraulic turbine on the runner under the two-way fluid-solid coupling action of the runner of the reversible hydraulic turbine under typical operating conditions. The results showed that under the influence of a high-speed water ring area under a certain working condition, the incoming flow direction forms a certain impulse angle with the blade, and under the joint action of the runner rotating at high speed, the vortex structure is generated in the blade area, and the speed change in the inlet area has a large random fluctuation, which is not conducive to the stability of the runner area and causes a strong pressure pulsation at the inlet. Under different working conditions, the runner stress area phenomenon is obvious, concentrated in the runner blade inlet side and the upper crown, lower ring connection. The maximum deformation region appears in the lower region of the middle of the blade inlet. The comparison of the modal analysis shows that the dynamic stress frequency caused by the dynamic interference is very unlikely to trigger the resonance of the runner.

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# INTRODUCTION

With the proposal of the goal of "a carbon peak" in 2030 and the vision of "carbon neutralization" in 2060, green and low carbon has become synonymous with current industrial development (Li et al., 2021; Li et al., 2022). Hydraulic machinery with clean and efficient characteristics is attracting much attention. Reversible hydraulic turbine high head, ultra-high head, and other performance indicators become the need of industrial development. However, there is a complex coupling vibration problem of solid blades submerged in fluid. The internal turbulence excitation of the unit operation is intense, and the instability is very prominent. The runner is prone to fatigue fracture, which affects the safe and stable operation of the unit (Zhu et al., 2012; Wang et al., 2012) . Therefore, it is important to reveal the dynamics of hydraulic turbine rotor blades and establish a sound theoretical system (Zheng et al., 2016; Zhang et al., 2021; Yue et al., 2017).

Fluid-solid coupling mainly studies the fluid-solid interaction and the interference phenomenon of interaction. Researching so far, for different theoretical problems, many solutions have been developed. Some scholars use Newton's method to study the overall solution of strong coupling with large displacement, which is expensive and time-consuming and not suitable for solving complex

1



practical engineering problems (Heil, 2003; Wood et al., 2010). For example, using the boundary element-based method and considering the damping effect of the surrounding water flow, the deformation problem is studied using the time-domain FSI analysis method (Lee et al., 2014).

The high reliability of experimental studies in the research method is also essential to test the results of theoretical and numerical analysis. Many experts and scholars use advanced measurement techniques and equipment to observe deformation problems in fluid-solid coupling tests (Kalmbach and Breuer, 2013), and the remote sensing device composed of different damping caused by the vibration aspects are taken into account for in-depth exploration and research (Seidel et al., 2012). However, due to the diversity of water flow and the complexity of the internal structure of hydraulic machinery, direct observation of the internal coupling of hydraulic machinery seems impractical (Li et al., 2021), which hinders the research on the fluid-solid mechanism of hydraulic machinery by scientific researchers. With the development of computer technology and image processing technology, a new independent discipline computational fluid dynamics (CFD) is gradually derived on the basis of classical fluid dynamics and numerical calculation methods (Li et al., 2021). It replaces the continuous physical quantities in the time domain and space domain of the original physical field with the set of physical quantities of finite discrete points and applies certain principles and methods to establish algebraic equations about the relationship between physical quantities of discrete points. The approximate solution of the flow field is obtained by solving the algebraic equations. Due to its small investment, short time-consuming, and visualization of the internal flow characteristics of fluid machinery, CFD has quickly become an important means to study the cavitation characteristics of hydraulic machinery (Liang et al. 2020). Zheng et al. (2016). In order to study the influence of runner dynamic characteristics and internal flow field of cross-flow hydraulic turbine under fluid-solid coupling, the coupling solution of its solid domain and fluid domain is performed by using CFX and ANSYSAPDL, and compared with the measured values, and it is found that the coupling effect will reduce the hydraulic performance of the runner to

TABLE 1 | Model reversible turbine geometry parameters.

Parameter name	Numerical value		
Number of blades/pc	9		
Active guide leaf/pc	20		
Rotor high-pressure side diameter/mm	473.6		
Worm shell inlet diameter/mm	315		
Height of guide lobe bo/mm	66.72		
Number of fixed guide vane/pc	20		
Height of guide leaf/mm	66.72		
Rotor low-pressure side diameter/mm	300		
Tailpipe outlet diameter/mm	660		

some extent, which provides a reference for the blade transient response and runner hydraulic performance prediction in practical engineering. Hu et al. (2016) used the finite volume method for the fluid domain and the finite element method for the solid domain to study the fluid-solid coupling of the flexible airfoil under the action of water flow. It is found that the blade deformation caused by the fluid-solid coupling will lead to the change of the dynamic pressure frequency of the blade, and its airfoil impulse angle and water flow velocity will have some influence on the blade deformation. Zhu et al. (2012) took a mixed-flow hydraulic turbine as an example and carried out process simulation to calculate the blade stress distribution, based on which fatigue analysis was performed and optimized to reduce the maximum stress to improve the fatigue life. Wang et al. (2012) predicted the fatigue life of a hydraulic turbine runner during start-up, steady operation, and stopping and optimized the leaf root area where the stress is concentrated to improve the fatigue life.

Therefore, this study takes a reversible hydraulic turbine runner as the research object and analyzes the influence of alternating fluid–solid coupling on the dynamic characteristics of the runner blade under the variable operating conditions of the reversible hydraulic turbine and obtains the conclusions related to the stress, strain, and vibration of the runner area. This study provides a theoretical reference for the design of reversible hydraulic turbine blades.

# MODEL ESTABLISHMENT AND MESHING

The object of this study is a reversible hydraulic turbine model, and the overflow components consist of a worm shell, fixed guide vane, movable guide vane, runner, and tailpipe, and the schematic diagram is shown in **Figure 1**, and the specific parameters are shown in **Table 1**.

In order to ensure that the numerical calculation results are feasible and reliable, this meshing is performed using the subfunction ICEM of commercial software ANSYS for full flow channel hexahedral meshing. In order to eliminate the errors arising from the number of meshes, mesh-independence verification is required. Seven different sets of meshes are generated by choosing different mesh scales. The calculation conditions (a0 = 33 mm, Q11 =  $0.66 \text{ m}^3/\text{s}$ , and n11 = 70.8 r/

#### TABLE 2 | Mesh division of each component.

Project	Worm housing and fixed guide vane	Active guide leaf	Rotating wheel	Tailpipe
Number of grid cells	1894316	1218511	1605320	1556111
Number of nodes	316,841	1028423	1217820	1432144
Minimum angle/(°)	18	29	30	36
Minimum grid mass	0.45	0.5	0.50	0.65



TABLE 3   Model reversible turbine geometry parameters.					
Working condition point	Q1	Q2	Q3	Q4	Q5
Flow rate Q <sub>11</sub> (m <sup>3</sup> /s) Rotational speed n <sub>11</sub> (r/min)	0.83 56.8	0.76 65.6	0.66 70.8	0.54 72.3	0.3 67.4

min) are taken, and the constant calculation is performed. By comparing the efficiency characteristics, it is found that the efficiency basically does not change with the increase of grid number, and the runner blade y + under this working condition meets the turbulence model requirements, and finally the grid quality of minimum 0.4 or more is adopted, and the total number of grids is about 6.1 million for calculation. The mesh quality is shown in **Table 2** the finite element mesh of the solid region is generated in transient structure, and the number of mesh cells is 289,230. The mesh division results are shown in **Figure 2**.

# METHODS

### **Test Device and Reliability Verification**

In this study, the model reversible hydraulic turbine with movable guide vane  $a_0 = 33$  mm was selected for numerical calculation reliability verification. Five operating points are selected as shown in **Table 3**, for which constant numerical calculations are performed. **Figure 3** shows the reversible hydraulic turbine experimental setup. The results of the numerical calculations



FIGURE 3 | Reversible hydraulic turbine experimental setup.

are converted to unit speed and unit flow rate with the following equations:

$$n_{11} = \frac{nD_2}{\sqrt{H}},\tag{1}$$

$$Q_{11} = \frac{Q}{D_2^2 \sqrt{H}},$$
 (2)

where  $n_{11}$  is the unit speed (rpm),  $Q_{11}$  is the unit flow rate (L/s), n is the speed (rev/min), Q is the flow rate (L/s), H is the working head (m), and  $D_2$  is the nominal diameter of the runner (m).

 $Q_{11}$  and  $n_{11}$  were obtained by conversion, and then the  $n_{11}-Q_{11}$  characteristic curve was plotted. The  $n_{11}-Q_{11}$  characteristic curve obtained by the conversion is compared



with the test curve, and the results are shown in **Figure 4**. Through comparison, the two have a high degree of agreement and the error value is kept near 4%, which meets the requirements of engineering research. **Figure 5** shows the comparison of efficiency for different working conditions, and the difference between the experimental and calculated efficiency is around 1.4%. Therefore, the model selected for this numerical calculation has high reliability.

# **Reliability Analysis of Pressure Pulsation**

The pressure pulsations are measured over all operating ranges of turbine operating conditions and at the cavitation factor of the power plant unit. It is necessary to measure the amplitude and frequency of pressure pulsations between the worm shell, runner, and guide vane as well as between the top cover and the upper crown of the runner. The sensor arrangement should be located where the maximum pressure pulsation amplitude can be measured. The pressure pulsations are recorded and analyzed. Spectrum analysis of the collected data should be performed to determine the main frequency and amplitude of the pressure pulsation.  $\Delta H$  is used to represent the degree of pressure pulsation in the turbine/pump, and H is the amplitude of the turbine/pump, and H is the turbine head/pump head, which is the characteristic amplitude. According to the IEC60193-1999 "hydraulic turbine, storage pump, and pump turbine model acceptance test," 18 characteristic amplitude values using statistics were recorded, and given probability range (for example, 97%) values beyond this probability range will be ignored, so the pressure pulsation peak is derived by the confidence method, and the confidence level is consistent with the model test as far as possible. Since the turbine pressure pulsation test is performed in the full range of operating conditions, the corresponding pressure pulsation amplitude is 97% of the peak confidence level. Each operating point and each measurement signal were analyzed, and the test results are shown in Table 4.



# **Turbulence Model and Boundary Conditions**

Reversible turbines have frequent changes under operating conditions and complex and variable flow conditions. The application of SST k-w in ANSYS can accurately capture surface vortices and near-wall flow, which is applicable to a wide range of applications (Liang et al., 2020). Therefore, this turbulence model is selected for numerical calculation. The inlet and outlet pressures are 404300 pa and 101325 pa, respectively. Interface coupling and SIMPLEC velocity pressure coupling algorithm are used to solve the time-averaged N-S equation. The residual value is set to  $10^{-6}$ , and the iteration time step is set to  $10^{-4}$ s. The steady-state numerical calculation of the whole flow field of pump turbine is carried out first, and the convergent steady-state result is taken as the initial value of transient calculation. During transient numerical calculation, the time step is set to  $3.867 \times 10^{-4}$  s, and 120 steps are required for one rotation, and each time step is rotated by 3°. In terms of a solid domain, normal temperature clean water is used as the medium, the density is  $1 \text{ g/cm}^3$ , and the viscosity is  $1c_p$ ; the model material of pump turbine runner is structural steel, the density is 7850kg/m<sup>3</sup>, and the elastic modulus is 166.67 Gpa. Poisson's ratio is 0.3. Fixed constraints are imposed on the central part of the runner, the centrifugal force is applied through the angular velocity counterclockwise around the z-axis, the gravity direction is the negative direction of the z-axis, and the fluid domain acts on the water pressure of the structure by increasing the fluid-structure coupling surface.

# **Dynamic Mesh Solving Method**

For the bi-directional fluid-solid coupling study of hydraulic turbine conditions of reversible hydraulic turbine, dynamic treatment of the runner basin is required, so the dynamic mesh update method of spring smoothing and local reconstruction is needed for the runner area mesh. The fluid domain and the solid domain are iterated several times, and the node non-boundary in the computational domain undergoes relative displacement changes and reaches a new equilibrium. The spring smooth method is based on the principle given in **Eqn. 3**. The original is replaced by the newly generated mesh, backward to the newly generated mesh difference.

#### TABLE 4 | Hydraulic turbine working condition pressure pulsation test.

Location	Operating condition	Test result (∆H/H)	Guaranteed value (△H/H)
of measurement point			
Worm shell import	At rated operating conditions	2.02	<3%
	Partial working condition operation	2.14	<3%
Movable guide vane-between runners	At rated operating conditions	2.64	<7%
	Partial working condition operation	5.76	<7%
Between the top cover and runner	At rated operating conditions	3.45	<7%
	Partial load or no-load operation	5.22	<7%
Tailpipe	Optimum operating conditions	1.10	<2%
	Part-load or no-load operation	6.39	<7%



$$\vec{F} = \sum_{j}^{n} k_{ij} \Big( \Delta \vec{x}_{j} - \Delta \vec{x}_{i} \Big), \tag{3}$$

$$k_{ij} = \frac{k_f}{\sqrt{\left|\vec{x}_i - \vec{x}_j\right|}},\tag{4}$$

where  $\vec{F}$  is the resistance on the node,  $k_{ij}$  is the elastic constant between two nodes,  $\Delta X_i$  is the move distance for the node,  $X_i$  is the node location, and  $X_f$  is the elastic factor.

# CALCULATION RESULTS AND ANALYSIS

# Effect of Water Flow in the Leaf-Free Zone on the Leaf Area

When the reversible turbine is operating under the optimal working condition, the direction of water flow at the inlet of the runner is close to its inlet angle, and the relative resistance of water flow becomes smaller. But in the case of partial working condition Q5 (larger unit speed and smaller flow rate), the water flow state is relatively complex, and the water flow and blade placement angle will produce a rush angle, which will cause the effective flow rate to be reduced, forming a more obvious high-speed water ring phenomenon. Not only the phenomenon, but it will also cause this chaotic water flow state wave to the rotor blade. From the blade inlet section, vortex development can be seen in Figure 6, in the impulse angle, stronger centrifugal force and blade coupling under the composite effect, blade working surface, and blade between the formation of unstable vortex structure. The existence of the vortex causes the instability of the water flow, making the blade by the water repeatedly hit the intensity of the increase; cavitation performance due to the vortex generation also produces a certain degree of decline. There is a separation flow-complex flow where chaotic water flow filled in the leafless area and between the rotor blades.





As the velocity distribution of the blade inlet section is extremely uneven, in order to study the impact of the velocity of the incoming impulse angle on the rotor blade inlet, the velocity extraction line is established in the vertical direction of the blade profile tangent line, and the incoming impulse angle is triangulated according to the fluid flow velocity. Two runner blade inlet velocities are selected for calculation and analysis, as shown in **Figure 7**. There is a certain impulse angle in the blade under this condition; at the same time, the blade inlet velocity change law analysis found: when a regional velocity fluctuation of the blade is larger, there is an obvious trough; when two regional velocity fluctuations are smaller, in this region, there is no more obvious peak and trough. Not only that but also both did not appear at the same time point to increase or decrease the same or common peak and valley values, that in the runner high-speed rotation, no leaf area and blade between the existence of a large speed difference and strong static and dynamic interference make the blade inlet area speed and direction change fluctuations, and there is strong randomness. This effect on the blade inlet area of the blade will not only produce a relatively larger force and ensure the safety of the runner from producing harm but also have the possibility of partial resonance.

# Analysis of Transient Flow Field Pressure Pulsation in the Rotor Blade Area

The Q2 and Q5 working conditions were selected for the nonconstant pressure pulsation analysis. In order to obtain the pressure changes in the flow field, three fluid domain measurement points are set for the bi-directional fluid–solid coupling rotor blade area, and the monitoring points are shown in **Figure 8**.

Figure 9 shows the frequency domain waterfall plots of pressure pulsations at each monitoring point on the blade area of the runner area under the two operating conditions of the turbine under bi-directional fluid-solid coupling calculation. The pressure pulsations are mostly dominated by low frequencies, as shown in Figure 9A. The first main frequency reaches 78.7 at 5f<sub>n</sub>, and the second main frequency reaches 51.4 at  $13f_n$ , which is 34.6% lower than the first main frequency amplitude. Near the inlet of the rotor, i.e., near the bladeless area, there is a strong dynamic interference, and the branch water flow coming out through the movable guide vane gathers in this part and then diverges again after the rotor blades. Therefore, the flow pattern here is complex, with a large number of vortices and more violent pressure pulsation. When the two-way fluid-solid coupling is considered, the slight deformation of the runner blade area also produces a certain degree of disturbance to the flow field, which intensifies the pressure pulsation of the reversible turbine and has a certain influence on the fundamental frequency of the pressure



pulsation, so the pressure pulsation amplitude in this part of 25f<sub>n</sub>-60f<sub>n</sub> produces some fluctuation phenomenon, as shown in Figure 9B. Under Q5 working condition, compared with Q2 working condition, the pressure pulsation in the first 15f<sub>n</sub> is much intense, the first main frequency reaches 99.4 at 3f<sub>n</sub>, the second main frequency is 38.6 at 7fn, and the main frequency increases by 26.3%. Compared with Q2 working condition, the flow rate in this working condition is reduced but the speed is relatively high, the water flow into the rotor is much complicated, and the velocity flow line distribution is extremely uneven, which increases the flow field. The random and instability of the flow field, which will make the runner blade under this working condition by the water pressure to become larger, are not conducive to the safe operation of the runner blade. ZL1 monitoring point in the two working conditions of the pressure pulsation amplitude is significantly greater than the other two monitoring points and there are strong fluctuations. ZL2 is in the middle of the blade position, the water flow channel is reduced, the effective overflow is less, there is a structural steel blade before and after the restraint of water movement, and the water in the front blade and after the reaction force of the blade there is a certain amount of mutual resistance to the filling situation. ZL3 resistance to the filling effect exists and is in the connection with the tailpipe, and the pressure difference between the front and rear is larger, so the pressure pulsation of the monitoring point will be less than that of ZL1. Pressure pulsation will also be less than that of the ZL1 situation.

# Analysis of Transient Stress and Its Deformation in the Rotor Area

Influenced by many secondary flows, different moments under the blade stress distribution have changed, there is an uneven stress distribution in the blade inlet, the stress area is concentrated in the blade inlet in the front of the high-pressure area, and the maximum stress in the blade is near the lower ring connection place, as shown in Figure 10. Figure 11 shows the stress and deformation diagram of the runner under Q2 working condition. Figure 12 shows the maximum stress and deformation fluctuation curve under this condition. So, in the upper ring under the crown of the T-shaped connection, a part of the stress exists leading to abrupt change of the situation. Due to the periodically repeated action of the water in the runner blade, the blade formed a different degree of stress distribution and selected different moments under the fluid on the blade surface as maximum stress, taken as the deformation situation for analysis. The 1 S results were selected to perform the analysis. Figure 11 shows the two working conditions of the runner blade stress; the blade working surface stress distribution trend from the inlet side to the middle of the blade gradually reduced, and this pressure distribution trend is in line with the hydraulic machinery blade pressure law. In the Q2 working condition, the runner blade stress presents "a C"-type distribution, the stress is concentrated in the upper and lower side of the blade inlet, the middle stress is small, and the blade tail end stress tends to zero. The maximum stress in 0.1-0.3 s changes drastically and then appears as slight up and down fluctuations. For the blade deformation, the inlet position directly impact gravity, centrifugal force, and high-pressure high-speed fluid on the thin blade, and there is a big stress difference in the middle and the two ends; the middle of the blade inlet has no restraint, making deformation maximum parts concentrated in the middle of the blade; because of the model structure material reasons, the overall deformation variable is small. The maximum deformation is only about 0.01 mm, and the trend of change and the maximum stress changes are roughly the same but there is a certain hysteresis. The deformation in the middle is the largest and gradually spreads to the surrounding area and gradually decreases.

Xin et al.







under this working condition].

Figure 13 shows the stress and deformation diagram of the runner under Q5 working condition. Figure 14 shows the maximum stress and deformation fluctuation curve under this condition. Under the Q5 working condition, the runner blade

stress is a "D"-type distribution, that is, the stress is concentrated in the middle of the blade inlet and the upper and lower side of the stress is small, but the maximum stress part is still in the lower side of the blade and the same will undergo sudden change of





stress situation. The stress distribution with the time change is not big, but this condition stresses maximum value change more strongly, changes amplitude more than 15%, and in the subsequent time the maximum stress value in 55 MPa fluctuates up and down; the stress value is greater than that of Q2 condition. The deformation position is concentrated in the middle of the blade inlet, but the overall variation is larger than that of the Q2 condition, and the maximum value of deformation shows a large and small phenomenon, which is not conducive to the safe operation of the reversible hydraulic turbine.

# **Comparison of Rotor Area Modal Analysis**

In order to obtain the inherent frequencies of the reversible turbine runner, the existing models were analyzed in dry mode, prestressed mode, and wet mode for the sixth-order nodal modal analysis, respectively. In **Figure 15**, it can be seen that the difference between the dry mode and the dry mode vibration frequency under pre-stress in the rotor blade area is very small, and to some extent, the rotor blade is not affected by the pre-stress on its fixed frequency. The overall vibration trend increases with the increase of the order. The first- and secondorder and the fifth- and sixth-order vibration frequencies have similar regular changes. Due to the additional mass force of the water medium in the wet mode and the damping diffusion effect, the vibration frequency of the wet mode starts to differ from the dry mode in the fourth order, and the increasing rate of frequency in the wet mode becomes smaller by about 5.1%. Because the influence of water on the vibration becomes larger in the higherorder cases, the frequency difference is about 11% at the sixth order, which has a tendency to increase gradually.

Since the study involves the submerged reversible turbine runner, the wet mode analysis is more suitable for the actual operating environment of the reversible turbine runner so that the numerical calculation results are closer to the actual situation. Therefore, it is necessary to further analyze the modal vibration pattern of the reversible hydraulic turbine runner under wet mode. **Figure 16** shows the first six orders of the wet mode vibration pattern of the reversible hydraulic turbine runner. The first- and second-order formations are left-right and front-back oscillations, respectively. The deformation is symmetrically



the runner.

distributed, and the maximum deformation is at the farthest point of the runner oscillation. The third-order vibration pattern is rotation around the axis left up, and the largest variable is located at the lower ring. The fourth-order model is up-and-down vibration along the central axis, the deformation is centrally symmetric at the main axis, and the largest deformation is at the upper crown of the runner. The fifth- and sixth-order mode vibration pattern is more similar, producing larger bending deformation at the center, with smaller deformation at the upper part, and the larger deformation is concentrated at the upper and lower crown and lower ring areas. The first-, second-, third-, and fourth-order modal vibration patterns are all vibration phenomena of the whole structural part of the runner, while the fifth- and sixth-order modal vibration patterns are bending deformation at a certain position. Since the connection between the upper crown and the main shaft is specified as a fixed constraint, the deformation in the area near it is low. The larger deformation area is concentrated at the edge of the upper crown and lower ring. The deformation of the runner blade is



FIGURE 16 | Sixth-order modal vibration pattern of the runner of a reversible hydraulic turbine. [(A-F) are the first, second, third, fourth, fifth and sixth order mode vibration patterns respectively].

TABLE 5 | Comparison of the first six orders of vibration frequency of the runner of reversible hydraulic turbine.

Modal order	First	Second	Third	Fourth	Fifth	Sixth
Dry mode (Hz)	625.32	625.34	735.8	1,061.6	1,291.6	1,291.8
Wet mode (Hz)	633.98	633.98	749.69	1,021.33	1,153.6	1,153.6
Q2 work conditions (Hz)	636.13	636.14	744.26	1,073.6	1,291.6	1,296.62
Q5 work conditions (Hz)	636.46	636.46	744.28	1,073.6	1,291.6	1,296.29

relatively uniform and decreases gradually along the runner from the inlet. The stress concentration area is distributed near the connection of the runner blade with the upper crown and lower ring, which is easy to produce fatigue damage and creates a hidden danger to the safety of the reversible hydraulic turbine.

**Table 5** shows reversible hydraulic turbine runner's first six orders of vibration frequency comparison and hydraulic excitation force-frequency comparison. The hydraulic turbine speeds to get the runner rotational frequency  $f_n$  were 17.2 Hz and 21.4 Hz, while the blade passing frequencies  $9f_n$  were 154.8 Hz and 192.648 Hz. The guide vane passing frequencies  $20f_n$  were 344 Hz and 428 Hz. The main frequencies of pressure pulsation at the internal flow field monitoring points are  $3f_n$ ,  $5f_n$ ,  $7f_n$ , and  $13f_n$ . Compared with the inherent frequency of the runner, there is a big difference. The minimum residual (guide vane passing frequency  $20f_n$ ) is also at 46.03%, far exceeding the safety residual threshold of 20%, so the possibility of a resonance phenomenon of dynamic stress is very small.

### CONCLUSION

- 1 Under high-speed and small flow conditions by the influence of high-speed water ring region, there is a large random fluctuation of speed change in the inlet region. The vortex structure is generated in the blade area, which is not conducive to the stability of the runner area, and the gradual development of the vortex also reduces the blade cavitation performance, and there is a certain safety risk.
- 2 In the case of considering the two-way fluid–solid coupling, the pressure pulsation in the fundamental frequency region exacerbates the pressure pulsation fluctuations. The blade inlet is influenced by the pressure pulsation of the static and dynamic interference in the bladeless area, which gradually decreases along the flow path direction. The water flow state is more complex under Q5 conditions, and the pressure pulsation is high and unstable, which increases the risk of runner blade fatigue.

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- 3 Through the two-way fluid–solid coupling analysis of the runner area, it can be seen that the hydraulic turbine stress is concentrated at the inlet of the runner blade and distributed in the area near the connection between the runner blade and the upper crown and lower ring; the maximum deformation is concentrated in the middle of the blade, which is prone to fatigue damage.
- 4 Using the acoustic-solid coupling technique, the inherent frequencies of the runner in the three cases were obtained and compared with the pulsation frequencies in the main frequency region of the blade passage frequency, guide vane passage frequency, and its pressure pulsation analysis, and it was found that the difference was large and the possibility of resonance was small.

## DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material; further inquiries can be directed to the corresponding author.

## **AUTHOR CONTRIBUTIONS**

LX wrote and improved the manuscript. QL provided guidance and advice on writing the manuscript. ZL provided guidance on the analysis of the study. ZL provided guidance on handling the test apparatus, and GX provided guidance on the tests.

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