



# Computer simulation of a submerged membrane bioreactor treating high COD industrial wastewater

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A dynamic model was developed to simulate the behavior of the biological processes taking place in a membrane bioreactor (MBR) pilot plant treating industrial wastewater at the Heraklion Industrial Park including the cake development on the membrane surface. The modified extended CES-ASM3 model has been used. Hydrolysis rates of the soluble microbial products have been added. Membrane fouling was taken into account and trans membrane pressure (TMP) was modeled and compared to experimental data. Simulation results are presented for the operation period between February 2012 and May 2013 and the prediction ability of the model is shown through the computation of the mean relative error of each measured state variable. Overall, the model estimates match the experimental data satisfactorily, as they follow similar trends while for all input variables their mean value was used as a constant input in the simulations. The operation of the MBR was conducted at three different sludge retention times.

**Keywords:** Activated Sludge Models, CES-ASM3 model, membrane bioreactor, membrane fouling, trans membrane pressure

## INTRODUCTION

Nowadays Membrane Bioreactor (MBR) technology is widely used for industrial and domestic wastewater treatment. MBR reactor is an activated sludge process (ASP) that uses membranes for wastewater filtration, it can achieve complete solids removal, high organic and nutrients removal at a small bioreactor volume. MBR is becoming the technology of choice due to these favorable characteristics. However, in contrast to their advantages, MBRs have a main drawback, membrane bio-fouling, which can cause many problems during their operation.

For the simulation of an ASP process, Activated Sludge Models ASM1, ASM2, ASM2d, and ASM3 have been developed by Henze et al. (2000). ASM1 is widely used for conventional ASP processes. ASM3 is a modification of ASM1 model that can describe the ASP process with higher accuracy. ASM2 and ASM2d simulate the biological processes including the phosphorus removal (Henze et al., 2000; Bournazou et al., 2011). ASM3 model is selected as it can model realistically the ASP systems and despite its sensitivity on several operational parameters it can be a promising mathematical tool for the study of aerobic biological processes like the MBR systems (Saroj et al., 2008; Sperandio and Espinoza, 2008).

Several studies, based on classic or modified ASM models, have been published simulating MBR performance. Jang et al. (2006) developed a model simulating the kinetics of production and degradation for the extracellular polymeric substances (EPS) simultaneously with soluble microbial products (SMPs) in MBR under steady-state conditions, according to a theory suggested by Lapidou and Rittmann (2002). The aim of their study was the prediction of membrane fouling potential, using the Membrane fouling index (MFI) at steady state operating conditions. Saroj et al. (2008) used a modified ASM3 model to

simulate the dynamic behavior of EPS production, which is considered as a fouling factor. Janus and Ulanicki (2010) developed a combined ASM3-LR model in order to predict the formation and degradation of all microbial products in an MBR at various conditions under steady state operation. Janus (2014) developed an integrated ASM1 model version for MBR systems. This study was focused on the effect of microbial products on membrane fouling and the de-nitrification process in comparison to other models. The trans-membrane pressure was solely compared with the experimental measurements. Tian et al. (2011) studied the development of an ASM-SMP model. They took into consideration the hydrolysis of SMPs, whereas they excluded EPS kinetics. Chen et al. (2012) investigated the biological process in MBR that is based on an extended ASM3 combined with SMPs formation and hydrolysis rates. This work tried to quantify the uncertainty of model parameters at different SRTs using sensitivity analysis; however, the results were not compared to experimental measurements. Insel et al. (2011) investigated a modified ASM model simulating the simultaneous nitrification and de-nitrification (SNdN) taking place in an MBR. They focused on the limitations of oxygen mass transfer.

In this work the dynamic behavior of all biological processes except phosphorous removal occurring in an MBR unit treating high COD influents is simulated. In particular, simultaneous formation and degradation processes for EPS and SMP have been added to the ASM3 model according to Janus and Ulanicki (2010), Tian et al. (2011), and Chen et al. (2012). Additionally, the effect of the activated sludge on oxygen mass transfer limitations was taken into consideration (Insel et al., 2011). The solids cake build up on the membranes' surface was also simulated and the membrane-fouling phenomenon, in terms of changes in

the observed trans-membrane pressure (TMP) was investigated. The model estimates are compared to experimental data obtained from February 2012 to May 2013.

## MATERIALS AND METHODS

### DESCRIPTION OF THE MODEL PROCESSES

Two additional processes, describing the hydrolysis of SMPs that includes the utilization-associated products (UAP) and biomass associated products (BAP) have been added to the CES-ASM3 model according to Chen et al. (2012) as well as the build-up of solids cake on the membrane surface. It is also assumed that the kinetic parameters that govern the mass transfer of dissolved oxygen and affect biomass growth kinetics, depend on activated sludge concentration (Insel et al., 2011). The state variable describing the alkalinity is excluded, as it can be assumed that it is not limiting substrate for microbial growth (Bournazou et al., 2011).

The model has sixteen state variables, which are divided into three groups. The first group includes all the soluble components, whereas the second one consists of the particulate material components. The last group has a single variable describing cake's thickness. All state variables with their symbols are presented in **Table 1**.

Sixteen processes describe the model structure. The first thirteen processes have been described in classic ASM3 model (processes from  $p_1$  to  $p_{13}$  presented in **Table 2**) (Henze et al., 2000). The aerobic and anoxic Storage processes for the SMP and the hydrolysis reaction for EPS were introduced by Janus and Ulanicki (2010), and are described by the processes  $p_{2b}$ ,  $p_{2c}$ ,  $p_{3b}$ ,  $p_{3c}$ , and  $p_{13}$ , presented in **Table 2**. Two additional expressions for the hydrolysis of UAP and BAP have been added (Chen et al., 2012) and are described by the processes  $p_{14}$ ,  $p_{15}$ . In the nitrification process ( $p_{10}$ ) the effect of wall attached autotrophic biomass on growth-kinetics taken into account (Dokianakis et al., 2006). The dynamic behavior of cake growth on the membranes surface is based on classic cake filtration theory.

**Table 1 | Model state variables.**

#### Model components

- Dissolved oxygen,  $S_O$
- Inert soluble COD,  $S_I$
- Readily biodegradable soluble COD,  $S_S$
- Ammonium,  $S_{NH}$
- NOx,  $S_{NOx}$
- Nitrogen gas,  $S_{N_2}$
- Utilization-associated products,  $S_{UAP}$
- Biomass-associated products,  $S_{BAP}$
- Inert particulate COD,  $X_I$
- Slowly biodegradable particulate COD,  $X_S$
- Heterotrophic biomass,  $X_H$
- Cell internal component,  $X_{STO}$
- Autotrophic biomass,  $X_A$
- EPS,  $X_{EPS}$
- MLSS,  $X_{TSS}$
- Cake thickness,  $B$

**Table 2 | Mathematical expression of the model processes.**

Hydrolysis of $X_S$	$p_1 = k_H \left( \frac{X_S/X_H}{K_x + (X_S/X_H)} \right) X_H$
Aerobic storage of readily biodegradable COD, biomass associated products and utilization associated products	$p_{2,a} = k_{STO} \left( \frac{S_O}{K_O + S_O} \right) \left( \frac{S_S}{K_S + S_S} \right) X_H$ $p_{2,b} = k_{STO,BAP} \left( \frac{S_O}{K_O + S_O} \right) \left( \frac{S_{BAP}}{K_S + S_{BAP}} \right) X_H$ $p_{2,c} = k_{STO,UAP} \left( \frac{S_O}{K_O + S_O} \right) \left( \frac{S_{UAP}}{K_S + S_{UAP}} \right) X_H$
Anoxic storage of readily biodegradable COD, biomass associated products and utilization associated products	$p_{3,a} = \eta_{ANOX} k_{STO} \left( \frac{K_O}{K_O + S_O} \right) \left( \frac{S_S}{K_S + S_S} \right) \left( \frac{S_{NOx}}{K_{NOx} + S_{NOx}} \right) X_H$ $p_{3,b} = \eta_{ANOX} k_{STO,BAP} \left( \frac{K_O}{K_O + S_O} \right) \left( \frac{S_{BAP}}{K_S + S_{BAP}} \right) \left( \frac{S_{NOx}}{K_{NOx} + S_{NOx}} \right) X_H$ $p_{3,c} = \eta_{ANOX} k_{STO,UAP} \left( \frac{K_O}{K_O + S_O} \right) \left( \frac{S_{UAP}}{K_S + S_{UAP}} \right) \left( \frac{S_{NOx}}{K_{NOx} + S_{NOx}} \right) X_H$
Aerobic growth of heterotrophs	$p_4 = \mu_H \left( \frac{S_O}{K_O + S_O} \right) \left( \frac{S_{NH_4}}{K_{NH_4} + S_{NH_4}} \right) \left( \frac{X_{STO}/X_H}{K_{STO} + (X_{STO}/X_H)} \right) X_H$
Anoxic growth of heterotrophs (de-nitrification)	$p_5 = \eta_{ANOX} \mu_H \left( \frac{K_O}{K_O + S_O} \right) \left( \frac{S_{NH_4}}{K_{NH_4} + S_{NH_4}} \right) \left( \frac{S_{NOx}}{K_{NOx} + S_{NOx}} \right) \left( \frac{X_{STO}/X_H}{K_{STO} + (X_{STO}/X_H)} \right) X_H$
Aerobic endogenous respiration	$p_6 = b_{H,O} \left( \frac{S_O}{K_O + S_O} \right) X_H$
Anoxic endogenous respiration	$p_7 = b_{H,O} \left( \frac{K_O}{K_O + S_O} \right) \left( \frac{S_{NOx}}{K_{NOx} + S_{NOx}} \right) X_H$
Aerobic endogenous respiration of $X_{STO}$	$p_8 = b_{H,O} \left( \frac{S_O}{K_O + S_O} \right) X_{STO}$
Anoxic endogenous respiration of $X_{STO}$	$p_9 = b_{H,O} \left( \frac{K_O}{K_O + S_O} \right) \left( \frac{S_{NOx}}{K_{NOx} + S_{NOx}} \right) X_{STO}$
Aerobic growth of autotrophs	$p_{10} = \mu_A \left( \frac{S_O}{K_{A,O} + S_O} \right) \left( \frac{S_{NH_4}}{K_{A,NH_4} + S_{NH_4}} \right) \left( X_A + \frac{A_{bior}}{V} \sqrt{\frac{2D_{AOB,biof} Y_{AOB,biof} d_{AOB,biof}}{K_{AOB,biof}} S_{NH_4}} \right)$
Aerobic endogenous respiration of autotrophs	$p_{11} = b_{A,O} \left( \frac{S_O}{K_O + S_O} \right) X_A$
Anoxic endogenous respiration of autotrophs	$p_{12} = b_{A,NOx} \left( \frac{K_{A,O}}{K_{A,O} + S_O} \right) \left( \frac{S_{NOx}}{K_{NOx} + S_{NOx}} \right) X_A$

(Continued)

**Table 2 | Continued**

Hydrolysis of $X_{EPS}$
$p_{13} = k_{H,EPS}X_{EPS}$
Hydrolysis of $S_{UAP}$
$p_{14} = k_{H,UAP} \left[ \left( \frac{S_O}{K_O + S_O} \right) + \eta_{ANOX} \left( \frac{K_O}{K_O + S_O} \right) \left( \frac{S_{NOx}}{K_{NOx} + S_{NOx}} \right) \right] \left( \frac{S_{UAP}}{K_{UAP} + S_{UAP}} \right) X_H$
Hydrolysis of $S_{BAP}$
$p_{15} = k_{H,BAP} \left[ \left( \frac{S_O}{K_O + S_O} \right) + \eta_{ANOX} \left( \frac{K_O}{K_O + S_O} \right) \left( \frac{S_{NOx}}{K_{NOx} + S_{NOx}} \right) \right] \left( \frac{S_{BAP}}{K_{BAP} + S_{BAP}} \right) X_H$

Sludge Retention Time (SRT) is adjusted to 15, 20, and 30 days by regular intermittent sludge removal. The model predicts MLVSS, MLSS, soluble COD,  $NH_4$ ,  $NO_x$  and microbial products (SMP and EPS) concentrations as well as cake development. As soluble COD, which passes through the membrane, is considered the sum of the readily biodegradable COD ( $S_S$ ) and inert soluble COD ( $S_I$ ). The total autotrophic ( $X_A$ ), heterotrophic ( $X_H$ ) microorganisms and the slowly biodegradable particulate COD ( $X_S$ ) express the MLVSS concentration in the MBR. MLSS concentration is expressed by the  $X_{TSS}$  state variable. The  $NO_x$  include the  $NO_3$ -N and  $NO_2$ -N ( $S_{NOx}$ ). SMPs compound is considered the soluble EPS, where the  $X_{EPS}$  concentration expresses the particulate EPS concentration.

In comparison with other studies the saturation values, regarding to  $S_O$  transfer,  $K_O$  and  $K_{A,O}$  are not constants and they depend on activated sludge concentration. According to the approach of Insel et al. (2011) the values of these parameters are given by the equations below:

$$K_O = 0.1 + \frac{0.20}{(1 + e^{-0.5 \cdot (MLSS - 12,000)})} \quad (1)$$

$$K_{A,O} = 0.15 + \frac{0.10}{(1 + e^{-0.5 \cdot (MLSS - 12,000)})} \quad (2)$$

**DESCRIPTION OF THE DYNAMIC MODEL**

A system of 16 ordinary differential equations (ODEs), describing partial mass balances of the MBR unit, have been used to simulate the overall behavior of the system. The general differential equation form that describes the soluble concentrations included in the first group of the model's state variables is:

$$\frac{dS_j}{dt} = D(S_{j,in} - f_{Sj}S_j) + R_{Sj} \quad (3)$$

where

$D$  = dilution rate,  $d^{-1}$

$S_{j,in}$  = concentration of soluble variable  $j$  in the influent stream,  $mg L^{-1}$

$f_{Sj}$  = fraction of  $S_j$  with molecular weight below membrane cutoff molecular weight

$S_j$  = concentration of soluble variable  $j$  in the effluent stream,  $mg L^{-1}$

The term,  $R_j$ , expresses the sum of all reaction rates for the  $j$ th state variable and is given by the equation:

$$R_j = \sum_i v_{ij} p_i, j = 1, 2, \dots, 15 \quad (4)$$

where

$v_{ij}$  = are the stoichiometric coefficients for state variable  $j$  and model process  $i$  as shown in the stoichiometric matrix in **Table 3** except the stoichiometric coefficients for  $S_O$ ,  $S_{NH_4}$  and  $X_{TSS}$  which are provided in **Table 4**.

$p_i$  = model process  $i$  as described in **Table 2**

For example, the reaction rate for readily biodegradable soluble COD ( $S_S$ ) is:

$$R_{S_S} = (1 - f_{S_I}) p_1 + p_{2,a} - p_{3,a} + f_{S_P} p_{13} \quad (5)$$

The compounds  $S_O$ ,  $S_S$ ,  $S_{NH}$  and  $S_{NOx}$  are assumed to be diffused through the cake's layer. Thus, a term expressing the diffusion, for each of these concentrations in the cake, is added. Diffusion rate is follows the Fick's law by:

$$J_{S_j} = -A_S D_j \left. \frac{dS_j}{dx} \right|_{x=0} \quad (6)$$

where

$J_{S_j}$  = the flux,  $mg L^{-1} d^{-1}$

$A_S$  = the total membranes surface,  $mm^2 mm^{-3}$

$D_j$  = effective diffusivity of Substrate  $j$  in cake,  $mm^2 d^{-1}$

The ODE expression for  $S_S$ ,  $S_{NH}$ , and  $S_{NOx}$  is given by the following equation:

$$\frac{dS_j}{dt} = D(S_{j,in} - f_{Sj}S_j) + R_{Sj} - A_S D_j \left. \frac{dS_j}{dx} \right|_{x=0} \quad (7)$$

The ODE expression for dissolved oxygen concentration is:

$$\frac{dS_O}{dt} = K_L a (S_{O,sat} - S_O) + R_{S_O} - A_S D_O \left. \frac{dS_O}{dx} \right|_{x=0} \quad (8)$$

where

$K_L a$  = Dissolved oxygen mass transfer coefficient,  $d^{-1}$

$S_{O,sat}$  = Saturated dissolved oxygen concentration,  $mg L^{-1}$

The general ODE describing dynamic behavior of particulate state variables is given by the following equation:

$$\frac{dX_j}{dt} = D X_{j,in} + R_j \quad (9)$$

The term  $R_j$ , is given by the Equation (4), for  $j = 9, 10, \dots, 15$ .

Cake build up is calculated from the solids deposition on the membrane surface. The mathematical expression relating the flux to the transmembrane pressure is derived from Darcy's law as expressed in the following equation (Lee et al., 2002; Koo et al., 2013).

$$J = \frac{\Delta P}{\eta(r_m + r_c)} \quad (10)$$

where

$J$  = the permeate flux through the membrane surface  $m/d^{-1}$  and is considered to be constant ( $J = Q/A$ )

**Table 3 | Stoichiometric matrix includes all the stoichiometric coefficients ( $v_{ij}$ ).**

Processes, <i>i</i>	Model state variables, <i>j</i>													
	$S_O$	$S_I$	$S_S$	$S_{NH}$	$S_{N2}$	$S_{NOx}$	$S_{BAP}$	$S_{UAP}$	$X_I$	$X_S$	$X_H$	$X_{STO}$	$X_{EPS}$	$X_{TSS}$
$p_{1,1}$ Hydrolysis		$f_{SI}$	$1 - f_{SI}$	$\beta_1$										$Z_1$
$p_{2,a}$ Aerobic storage of $S_S$	$\alpha_{2a}$		-1	$\beta_{2a}$								$Y_{STO,O2}$ $-f_{EPS,STO}$	$f_{EPS,STO}$	$Z_{2a}$
$p_{2,b}$ Aerobic storage of $S_{BAP}$	$\alpha_{2b}$			$\beta_{2b}$			-1					$Y_{STO,SMP,O}$ $-f_{EPS,STO}$	$f_{EPS,STO}$	$Z_{2b}$
$p_{2,c}$ Aerobic storage of $S_{UAP}$	$\alpha_{2c}$			$\beta_{2c}$				-1				$Y_{STO,SMP,O}$ $-f_{EPS,STO}$	$f_{EPS,STO}$	$Z_c$
$p_{3,a}$ Anoxic storage of $S_S$			-1	$\beta_{3a}$	$-\alpha_a$	$\alpha_{3a}$						$Y_{STO,NO}$ $-f_{EPS,STO}$	$f_{EPS,STO}$	$Z_{3a}$
$p_{3,b}$ Anoxic storage of $S_{BAP}$				$\beta_{3b}$	$-\alpha_{3b}$	$\alpha_{3b}$	-1	-1				$Y_{STO,SMP,NO}$ $-f_{EPS,STO}$	$f_{EPS,STO}$	$Z_{3b}$
$p_{3,c}$ Anoxic storage of $S_{UAP}$				$\beta_{3c}$	$-\alpha_{3c}$	$\alpha_{3c}$						$Y_{STO,SMP,NO}$ $-f_{EPS,STO}$	$f_{EPS,STO}$	$Z_{3c}$
$p_4$ Aerobic growth	$\alpha_4$			$\beta_4$				$\gamma_H/\gamma_{H,O}$			$1 - f_{EPS,h}$	$-1/\gamma_{H,O}$	$f_{EPS,h}$	$Z_4$
$p_5$ Anoxic growth				$\beta_5$	$-\alpha_5$	$\alpha_5$		$\gamma_H/\gamma_{H,NO}$			$1 - f_{EPS,h}$	$-1/\gamma_{H,NO}$	$f_{EPS,h}$	$Z_5$
$p_6$ Aerobic endogenous respiration	$\alpha_6$			$\beta_6$			$f_{BAP}$		$f_{XI}$		-1		$f_{EPS,d}$	$Z_6$
$p_7$ Anoxic endogenous respiration				$\beta_7$	$-\alpha_7$	$\alpha_7$	$f_{BAP}$		$f_{XI}$		-1		$f_{EPS,d}$	$Z_7$
$p_8$ Aerobic Respiration of $X_{STO}$	$\alpha_8$											-1		$Z_8$
$p_9$ Anoxic Respiration of $X_{STO}$					$-\alpha_9$	$\alpha_9$						-1		$Z_9$
$p_{10}$ Nitrification	$\alpha_{10}$			$\beta_{10}$		$1/\gamma_A$		$\gamma_A/\gamma_A$				$1 - f_{EPS,a}$	$f_{EPS,a}$	$Z_{10}$
$p_{11}$ Aerobic respiration	$\alpha_{11}$			$\beta_{11}$			$f_{BAP}$		$f_{XI}$			-1	$f_{EPS,d}$	$Z_{11}$
$p_{12}$ Anoxic respiration				$\beta_{12}$	$-\alpha_{12}$	$\alpha_{12}$	$f_{BAP}$		$f_{XI}$			-1	$f_{EPS,d}$	$Z_{12}$
$p_{13}$ Hydrolysis of $X_{EPS}$			$f_S$				$1 - f_S$						-1	
$p_{14}$ Hydrolysis of $S_{UAP}$		$f_{S,SMP}$					$1 - f_{S,SMP}$							
$p_{15}$ Hydrolysis of $S_{BAP}$		$f_{S,SMP}$					$1 - f_{S,SMP}$							

$\Delta P$  = is the transmembrane pressure, kPa  
 $\eta$  = the viscosity of filtrate solution, kPa d<sup>-1</sup>  
 $r_c$  = is the cake resistance due to the particles deposition, m<sup>-1</sup>  
 $r_m$  = is the membrane resistance including pore blocking, m<sup>-1</sup>  
 The cake resistance is given by the following equation.

$$r_c = ad_c B \tag{11}$$

where

- $a$  = the specific cake resistance, m kg<sup>-1</sup>
- $B$  = the cake thickness, B, mm
- $d_c$  = the cake density, kg m<sup>-1</sup>

The membrane resistance is continuously increasing due to pore blocking and it is estimated by the following equation (Mondal and De, 2010)

$$r_m = r_{m0}(1 + Jkt) \tag{12}$$

where

- $J$  = the permeate flux (constant at all times), m d<sup>-1</sup>
- $r_{m0}$  = membrane resistance without pore blocking, m<sup>-1</sup>
- $k$  = pore blocking constant, m<sup>-1</sup>
- $t$  = time of membrane of operation, d

The pore-blocking constant is a parameter, which depends on the concentration of soluble EPS (SMP). For simplicity, in this study, the following relationship for the pore-blocking constant is used.

$$k = k_0 \left( \frac{SMP}{SMP_0} \right) \tag{13}$$

where,  $k_0$  and  $SMP_0$  are reference values obtained from the operation of the MBR at SRT = 30 days. Under this assumption, only one parameter,  $k_0$ , was estimated for the model and was used at all SRTs.

The total cake thickness development is given by

$$\frac{dB}{dt} = J - k_b B \tag{14}$$

where

$k_b$  = the cake removal rate due to bubbling action of the air, d<sup>-1</sup>

**MBR CHARACTERISTICS AND OPERATING CONDITIONS**

The nominal wastewater flow rate in the MBR was 10 m<sup>3</sup>/d; the bioreactor's volume was about 7 m<sup>3</sup>, and membranes' surface was 20 m<sup>2</sup>. The characteristics of the wastewater at the inlet are shown in **Table 5**. Although the input COD varied with time, the mean value of 2000 mg/L was used for the total dissolved COD.

The values of all biochemical kinetic constants and stoichiometric parameters used are in the range of values reported in the literature. Some parameters were slightly adjusted in order to simulate more realistically the biological processes. All the calibrated parameters values are presented in **Table 6**.

**Table 4 | Stoichiometric coefficients for  $S_O$ ,  $S_{NH4}$  and  $X_{TSS}$  which are presented in Table 3.**

Stoichiometric coefficients for $S_O$	Stoichiometric coefficients for $S_{NH4}$	Stoichiometric coefficients for $X_{TSS}$
$\alpha_{2,\alpha} = 1 - Y_{STO,O}$ $\alpha_{2,b} = \alpha_{2,c} = 1 - Y_{STO,SMP,O}$	$\beta_1 = i_{N,XS} - f_{SI}i_{N,SI} - (f_{SI} - 1)i_{N,SS}$	$z_1 = i_{TSS,XS}$
$a_{3,a} = -0.35(1 - Y_{STO,NOx})$ $a_{3,b} = a_{3,c} = -0.35(1 - Y_{STO,SMP,NOx})$	$\beta_{2,a} = \beta_{3,\alpha} = i_{N,SS} - f_{EPS,STO}i_{N,XEPS}$ $\beta_{2,b} = \beta_{2,c} = i_{N,SBAP} - f_{EPS,STO}i_{N,XEP}$ $\beta_{2,c} = \beta_{3,c} = -f_{EPS,STO}i_{N,XEPS}$	$z_{2,a} = (Y_{STO,O} - f_{EPS,STO})i_{TSS,STO} + f_{EPS,STO}i_{TSS,EPS}$ $z_{2,b} = z_{2,c} = (Y_{STO,SMP,O} - f_{EPS,STO})i_{TSS,STO} + f_{EPS,STO}i_{TSS,EPS}$
$\alpha_4 = (\gamma_H + Y_{H,O} - 1)/Y_{H,O}$	$\beta_4 = \beta_5 = (f_{EPS,h} - 1)i_{N,BM} - f_{EPS,h}i_{N,XEPS}$	$z_{3,a} = (Y_{STO,NOx} - f_{EPS,STO})i_{TSS,STO} + f_{EPS,STO}i_{TSS,EPS}$
$\alpha_5 = (\gamma_H + Y_{H,NO} - 1)/Y_{H,NOx}$	$\beta_6 = \beta_7 = i_{N,BM} - f_{XI}i_{N,XI} - f_{EPS,a}i_{N,XEPS} - f_{BAP}i_{N,SBAP}$	$z_{3,b} = z_{3,c} = (Y_{STO,SMP,NOx} - f_{EPS,STO})i_{TSS,STO} + f_{EPS,STO}i_{TSS,EPS}$
$\alpha_6 = \alpha_{11} = f_{BAP} + f_{XI} + f_{EPS,d} - 1$	$\beta_{10} = (f_{EPS,a} - 1)i_{N,BM} - f_{EPS,a}i_{N,XEPS} - 1/Y_A$	$z_4 = -(1 - f_{EPS,h})i_{TSS,BM} - (i_{TSS,STO}/Y_{H,O}) + f_{EPS,h}i_{TSS,XEPS}$
$\alpha_7 = \alpha_{12} = 0.35a_6$	$\beta_{11} = \beta_{12} = i_{N,BM} - f_{EPS,d}i_{N,XEPS} - f_{XI}i_{N,XI} - f_{BAP}i_{N,SBAP}$	$z_5 = -(1 - f_{EPS,h})i_{TSS,BM} - (i_{TSS,STO}/Y_{H,NOx}) + f_{EPS,h}i_{TSS,XEPS}$
$\alpha_8 = -1$	$\beta_{13} = i_{N,XS}$	$z_6 = z_7 = z_{11} = z_{12} = f_{XI}i_{TSS,XI} - i_{TSS,BM} - f_{EPS,d}i_{TSS,EPS}$
$\alpha_9 = 0.35\alpha_8$	$\beta_{14} = \beta_{15} = i_{N,SBAP} - f_{SI,SMP}i_{N,XI}$	$z_8 = z_9 = i_{TSS,STO}$
$\alpha_{10} = (-4.57 + \gamma_A + Y_A)Y_A$		$z_{10} = (1 - f_{EPS,a})i_{TSS,BM} + f_{EPS,a}i_{TSS,XEPS}$  $z_{13} = i_{TSS,XEPS}$

**Table 5 | Influent wastewater composition\*.**

Process parameter (mg L <sup>-1</sup> )	Average value ± SD	Minimum value	Maximum value
COD total	2440 ± 1288	730	7600
COD dissolved	1897 ± 1108	480	5400
BOD <sub>5</sub>	1353 ± 570	600	2400
TOC	554 ± 333	145.6	1487.4
TSS	952 ± 630	390	3604
VSS	570 ± 380	25.62	2205
TN	30 ± 13.7	8.86	72.91
NH <sub>4</sub> -N	14.1 ± 9.1	0.2	41.65
NO <sub>3</sub> -N	1.94 ± 2.5	0.08	12.3
PO <sub>4</sub> -P	11.6 ± 13.8	0.184	54.2

\*Source: Babatsouli et al. (2014).

**EXPERIMENTAL METHODS**

The influent industrial wastewater and permeate were sampled once a week and analyzed for total and volatile suspended solids (TSS and VSS), total and dissolved COD, BOD, TOC, N-NH<sub>4</sub>, N-NO<sub>3</sub>, TN, P-PO<sub>4</sub>. All these analyses were performed according to standard methods and details are provided by Babatsouli et al. (2014).

The mixed liquor from bioreactor (biomass) was sampled weekly for determination of total and volatile suspended solids according to Standard methods. Dissolved oxygen concentration (DO), pH, temperature, and reactor levels are continuously recorded.

Extracellular Polymeric substances (EPS) were obtained with an extraction method using a Cation Exchange Resin (CER) Dowex 20–50 mesh in the sodium form. The sludge and the CER were stirred for 16 h at 900 rpm and the amount of CER used was 70 g CER/g VSS. Sludge was firstly centrifuged at 5000 g for 15 min at 4°C, in order to separate the supernatant EPS (or soluble microbial products- SMP) from the solid where the bound EPS were to be subsequently extracted. Both EPS and SMP were analyzed in terms of proteins, carbohydrates, and humic acids.

The carbohydrates content in EPS was measured by the Anthrone method (Gaudy, 1962) with glucose as the standard. The protein and humic content in EPS were measured by the modified Lowry method (Frolund et al., 1996) using bovine Serum Albumin and Humic acid as the respective standards.

**CALIBRATION OF THE MODEL**

The values of all biochemical kinetic constants and stoichiometric parameters used are in the range of values reported in the literature. Some parameters were slightly adjusted in order to simulate more realistically the biological processes. All the calibrated parameters values are presented in **Table 6**.

**RESULTS AND DISCUSSION**

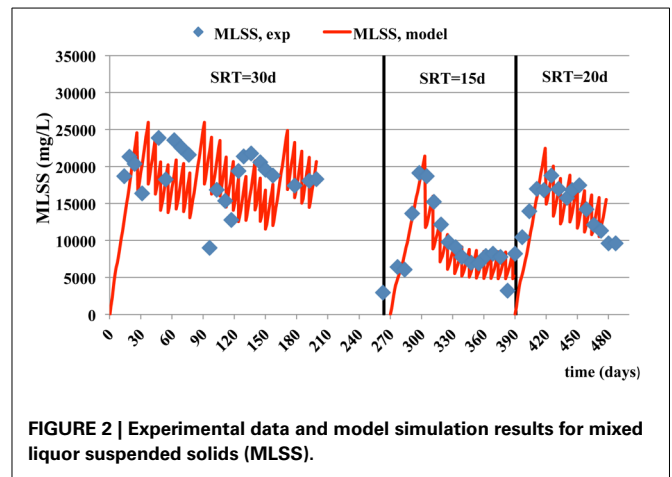
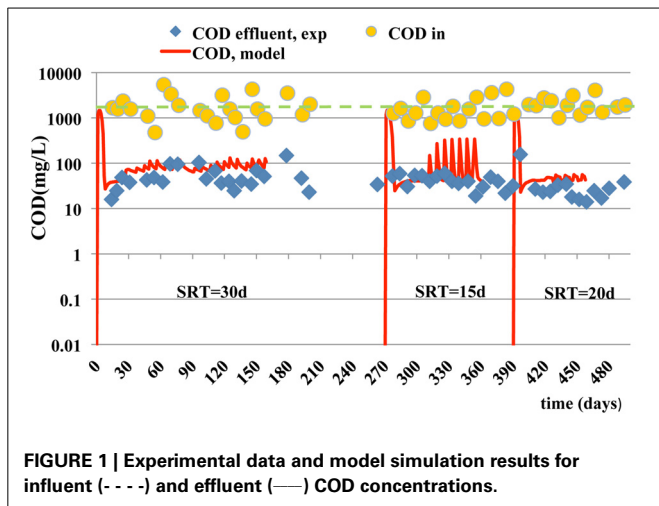
The estimated state variables by the calibrated dynamic model were compared to the experimental data obtained from the pilot MBR unit. **Figures 1–7** show respectively the observed measurements for COD in the effluent, MLSS, MLVSS,  $S_{NOx}$ , EPS and SMPs in the bioreactor and ammonium in the effluent. The estimated state variables are shown at SRTs of 15, 20, and 30 days. For

**Table 6 | Model parameter values.**

Parameter	Calibrated value*	Parameter	Calibrated value*
Saturated DO concentration, $S_{O,sat}$	7 mgO/L	Active tank area, $A_t$	10 m <sup>2</sup>
Flow rate, $Q$	10 m <sup>3</sup> /d	Dilution rate, $D$	1.47 d <sup>-1</sup>
Flux through the membrane	2 m/d	Pore blocking constant, $k_0$	5 m <sup>-1</sup> *
Volume of MBR, $V$	6.8 m <sup>3</sup>	$S_f$ fraction below the critical molecular weight, $f_f$	0.5
Total membrane surface, $A$	20 m <sup>2</sup>	$S_s$ fraction below the critical molecular weight, $f_s$	1
Hydrolysis rate constant for BAP, $k_{H,BAP}$	0.04 d <sup>-1</sup> *	$S_{NH4}$ fraction below the critical molecular weight, $f_{NH4}$	1
Storage rate constant, $k_{STO}$	1 d <sup>-1</sup>	$S_{N2}$ fraction below the critical molecular weight, $f_{N2}$	1
BAP storage rate constant, $k_{STO,BAP}$	0.1 d <sup>-1</sup>	$S_{NOx}$ fraction below the critical molecular weight, $f_{NOx}$	1
Heterotrophic maximum growth rate, $\mu_{Het}$	0.5 d <sup>-1</sup> *	$S_{UAP}$ fraction below the critical molecular weight, $f_{UAP}$	0.1
Aerobic endogenous respiration rate of $X_H$ , $b_{H,O}$	0.25 d <sup>-1</sup> *	$S_{BAP}$ fraction below the critical molecular weight, $f_{BAP}$	0.1
Anoxic endogenous respiration rate of $X_H$ , $b_{h,NOx}$	0.25 d <sup>-1</sup> *	Cake removal rate, $k_b$	1.5 d <sup>-1</sup> *
Aerobic respiration rate of $X_{STO}$ , $b_{STO,O}$	0.05 d <sup>-1</sup> *	DO mass transfer coefficient, $K_L a$	390 d <sup>-1</sup> *
Anoxic respiration rate of $X_{STO}$ , $b_{STO,NOx}$	0.05 d <sup>-1</sup> *	Yield for ammonia utilization by AOBs in biofilm, $Y_{AOB,biof}$	0.20*
Autotrophic maximum growth rate, $\mu_A$	0.5 d <sup>-1</sup> *	AOBs maximum growth rate, $k_{AOB,biof}$	0.2 d <sup>-1</sup> *
Aerobic endogenous respiration rate of $X_A$ , $b_{A,O}$	0.25 d <sup>-1</sup> *	Fick's diffusion coefficient for substrate, $D_S$	200 mm <sup>2</sup> /d
Anoxic endogenous respiration rate of $X_A$ , $b_{A,NOx}$	0.25 d <sup>-1</sup> *	Fick's diffusion coefficient for dissolved oxygen, $D_O$	230 mm <sup>2</sup> /d
EPS hydrolysis rate, constant, $k_{H,EPS}$	1.6 d <sup>-1</sup> *	Fick's diffusion coefficient for ammonia, $D_{NH4}$	100 mm <sup>2</sup> /d
Aerobic yield of stored product per $S_s$ , $Y_{STO,O}$	0.8 d <sup>-1</sup> *	Fick's diffusion coefficient for nitrate/nitrite, $D_{NOx}$	200 mm <sup>2</sup> /d
Anoxic yield of stored product per $S_s$ , $Y_{STO,NOx}$	0.7 d <sup>-1</sup> *	Membrane surface area, $A_s$	0.003 mm <sup>2</sup> /mm <sup>3</sup>
Aerobic yield of heterotrophic biomass, $Y_{H,O}$	0.63*	Hydrolysis saturation constant, $K_X$	0.1 d <sup>-1</sup>
Anoxic yield of heterotrophic biomass, $Y_{H,NO}$	0.45*	Saturation constant for $S_O$ , $K_O$	0.1 mgO/L
Yield of autotrophic biomass (AOB), $Y_A$	0.40 d <sup>-1</sup>	Saturation constant for substrate $S_s$ , $K_S$	0.7 mgCODsS/L
Fraction of SUAP produced during heterotrophic growth	0.05*	Fraction of $S_{UAP}$ produced during autotrophic growth, $\gamma_A$	0.12*
Saturation Constant for $S_{UAP}$ , $K_{UAP}$	100 mgS <sub>UAP</sub> /L	Fraction of $S_{UAP}$ produced during Cell lysis, $f_{UAP}$	0.05
Fraction of XEPS produced during Cell decay, $f_{EPS,d}$	0.04*	Fraction of SBAP produced during Cell lysis, $f_{BAP}$	0.04*
Specific cake resistance, $\alpha$	1.5 · 10 <sup>8</sup> m kg <sup>-1</sup> *	Saturation constant for $S_{BAP}$ , $K_{BAP}$	100 mgS <sub>BAP</sub> /L
Membrane resistance, $R_m$	1.9 · 10 <sup>9</sup> m <sup>-1</sup> *	BAP's hydrolysis saturation constant, $K_{H,BAP}$	0.5 mgS <sub>BAP</sub> /L
UAP's Hydrolysis saturation constant, $K_{H,UAP}$	0.65 mgS <sub>UAP</sub> /L	Saturation constant for $X_{STO}$ , $K_{STO}$	1
Saturation constant for $S_{NOx}$ , $K_{NOx}$	0.25 mgNO <sub>3</sub> -N/L*	Saturation constant for $S_{NH4}$ , $K_{SNH4}$	0.01 mgN/L
Saturation constant for $S_{NH4}$ , $K_{A,SNH4}$	0.1 mgN/L	Saturation constant for $SO$ for Nitrifiers, $K_{A,O}$	0.15 mgO/L
Saturation constant for SNOX for Nitrifiers, $K_{A,NOx}$	0.25 mgNO <sub>3</sub> -N/L	Hydrolysis rate constant, $k_H$	1 d <sup>-1</sup>
Fraction of $S_s$ produced during XEPS hydrolysis, $f_S$	0.6*	Hydrolysis rate constant for UAP, $k_{H,UAP}$	0.08 d <sup>-1</sup> *
Fraction of $X_i$ produced during endogenous respiration, $f_{X_i}$	0.1	Fraction of $S_i$ produced during Hydrolysis, $f_{S_i}$	0
N content of $S_i$ , $i_{N,S_i}$	0.01	Fraction of $S_i$ produced during the SMPs Hydrolysis, $f_{S_i,SMP}$	0.11
N content of $X_{EPS}$ , $i_{N,XEPS}$	0.04	N content of biomass, $i_{N,BM}$	0.05
N content of $S_{BAP}$ , $i_{N,SBAP}$	0.04	N content of $X_i$ , $i_{N,X_i}$	0.02
N content of $S_s$ , $i_{N,SS}$	0.02	TSS/COD of $X_S$ , $i_{TSS,XS}$	0.75 mgS <sub>S</sub>
TSS/COD of $X_{EPS}$ , $i_{TSS,EPS}$	0.9 mgS <sub>S</sub>	TSS/COD of $X_{STO}$ , $i_{TSS,STO}$	0.6 mgS <sub>S</sub>
TSS/COD of $X_i$ , $i_{TSS,X_i}$	0.75 mgS <sub>S</sub>	TSS/COD of $X_A$ & $X_H$ , $i_{TSS,BM}$	0.9 mgS <sub>S</sub>
Anoxic yield of stored product per $SMP$ , $Y_{STO,SMP,NOx}$	0.7 d <sup>-1</sup>	Fraction of XEPS produced during Cell growth of $X_A$ , $f_{EPS,a}$	0.1
Aerobic yield of stored product per $SMP$ , $Y_{STO,SMP,O}$	0.7 d <sup>-1</sup>	Fraction of $X_{EPS}$ produced during Storage of internal substrates, $f_{EPS,STO}$	0.1
Fraction of XEPS produced during cell growth of $X_H$ , $f_{eps,h}$	0.1		

\*The value of the parameter was obtained by minimizing the mean relative error (MRE).





estimation of the overall accuracy of the model, the mean relative error (MRE) of all measured state variables was used, namely,

$$MRE = \frac{1}{N \times N_y} \sum_{j=1}^N \sum_{i=1}^{N_y} \left| \frac{\hat{y}_i(t_j) - y_i(t_j)}{\hat{y}_i(t_j)} \right| \quad (15)$$

where

$N$  = number of measurements taken over time ( $t_j$ ,  $j = 1, \dots, N$ )

$N_y$  = number of measured state variables

$y_i(t_j)$  = model prediction of variable  $y_i$  ( $i = 1, \dots, N_y$ ) at time  $t_j$

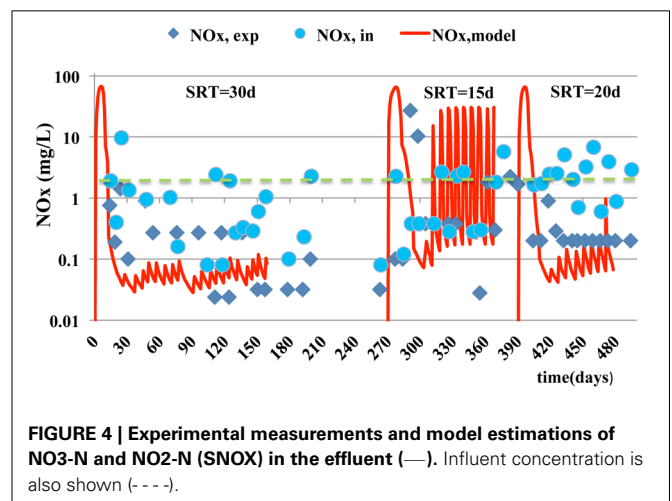
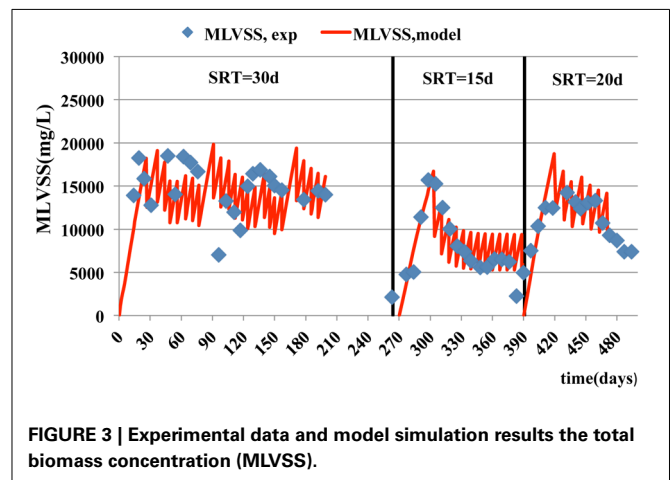
$\hat{y}_i(t_j)$  = measured value of variable  $y_i$  ( $i = 1, \dots, N_y$ ) at time  $t_j$

The calibration of the adjustable model parameters (indicated by a \* in Table 6) was performed by minimizing the value of MRE. The parameter estimation was based on a sequential approach for estimating parameters in models described by sets of ordinary differential equations (Kalogerakis, 2002). On the other hand, in order to quantify the performance of the model with respect to a particular variable, the mean relative error of each state variable,  $MRE_i$ ,  $i = 1, \dots, N_y$ , was also computed by

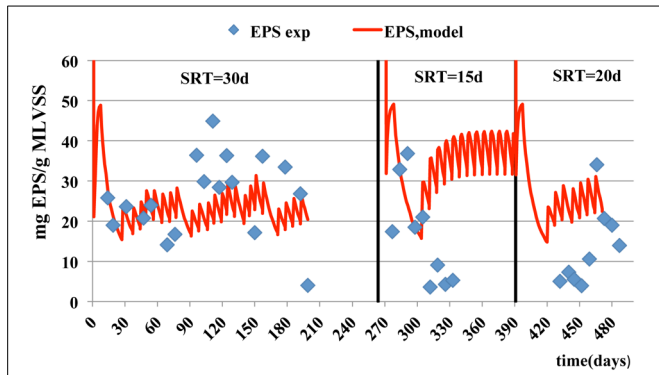
$$MRE_i = \frac{1}{N} \sum_{j=1}^N \left| \frac{\hat{y}_i(t_j) - y_i(t_j)}{\hat{y}_i(t_j)} \right| \quad (16)$$

Figure 1 exhibits the COD influent (orange dots), COD effluent (blue diamond signs) and COD predicted concentrations (continuous red line). The model matches sufficiently well the COD removal although as COD in the influent stream a constant value of 2500 mg/L was used. The COD of the outlet stream, simulation line follows the inert COD behavior, because it is the fraction of soluble COD with the bigger concentration. The MRE is estimated to 3.15, 1.07, and 0.19 at the SRTs of 15, 20, and 30 days. The prediction ability decreases at shorter SRTs.

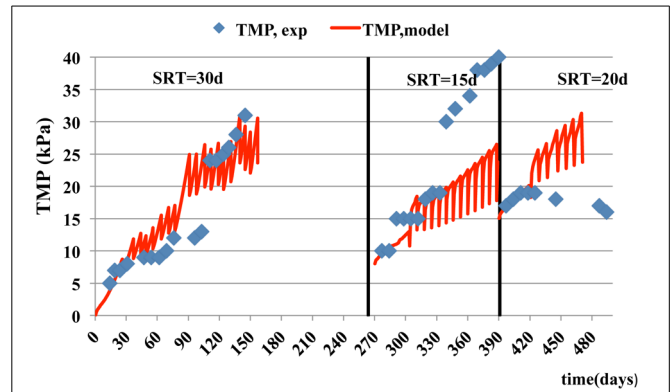
Similar trends are observed for MLSS and MLVSS concentrations (Figures 2, 3) where the model predictions are accurate enough. The mean relative error of the model for MLSS and



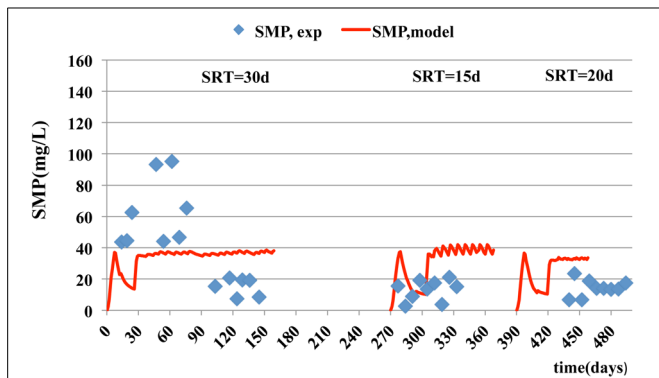
MLVSS is 0.29 and 0.32 respectively, at SRT of 15 days. If SRT increases, the model accuracy for the MLSS and biomass is improved. The MRE for MLSS is 0.22 at SRT of 20 days and 0.11 at the SRT of 30 days. The respective error for MLVSS is 0.25 and 0.11. Only the MLVSS, at the SRT of 15 days, is



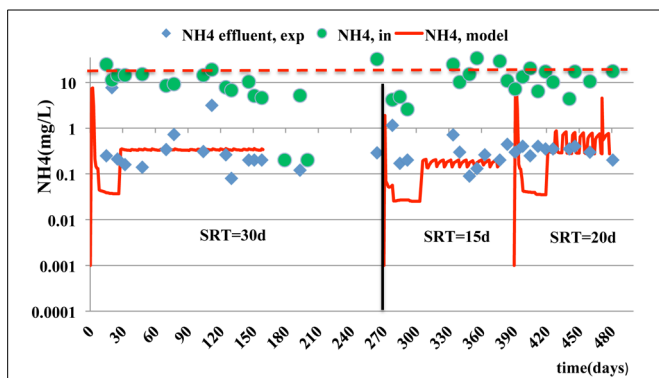
**FIGURE 5 |** Experimental data and model estimations of particulate EPS concentration per mass of MLVSS.



**FIGURE 8 |** Experimental data and model estimations of trans-membrane pressure vs. time at three different SRTs.



**FIGURE 6 |** Experimental data and model estimations of soluble EPS (SMP) concentration.



**FIGURE 7 |** Experimental measurements and model estimations for  $\text{NH}_4$  effluent (—).  $\text{NH}_4$  influent concentration is also shown (---).

not in good agreement with the measurements. Chen et al. (2012) suggested that the SRT impacts on microbial growth and death rate parameters and contributes to the uncertainty of their estimation. The parameters associated with kinetics of the biomass, which are difficult to be estimated at each SRT and hence, they were kept the same for all SRTs. The de-nitrification process simulations as shown in Figure 4 exhibit

a better match to experimental data as the SRT increases. The MRE for  $\text{NO}_x$  is 23.94 at the SRT of 15 days, 1.40 at SRT of 20 days and 0.54 at the SRT of 30 days. It should be noted that the experimental measurements for  $\text{NO}_x$  do not include measurements of  $\text{NO}_2$  (only  $\text{NO}_3$  was measured) and hence, the differences between data should be smaller than the model estimates.

In case of particulate microbial products, the accuracy of model prediction decreases as the SRT becomes smaller. The best predictions for SMPs and EPS are at the SRT of 30 days with a corresponding estimated mean relative error of 2.54 and 0.13 respectively (Figures 5, 6). The simulation results, for the SMPs, are similar to those reported by Chen et al. (2012), where a slight decrease of SMPs occurs when SRT increases and then the SMPs concentration increases with SRT increase. Additionally, as it was mentioned by Tian et al. (2011), the hydrolysis rates of SMPs characterized by uncertainty due to the SRT changes. In the case of ammonium removal, the model fits adequately the nitrification process (Figure 7).

In case of fouling phenomenon prediction ability, as the cake layer on the membrane was not measured, the transmembrane pressure in the MBR simulated and compared with the respective measured TMPs (Figure 8). As it shown, in Figure 8, the modeled TMP describes the operating conditions in MBR accurately, especially at the SRT of 30 days, where the mean relative error is 0.13. However, in two other SRTs fails to match adequately the experimental data. This occurs due to inadequate prediction of SMPs as mentioned earlier. In comparison to a previous study by Janus (2014), this model had a relative good TMP prediction ability at different SRTs.

Overall, model predictions of the state variables follow a similar trend to the observed measurements over time, except the case of de-nitrification process and ammonium removal, where the effect of regular sludge removal on the dynamics of the system is significant. In particular, the MRE of all measured state variables is 4.40, 1.16, and 0.57 at an SRT of 15, 20, and 30 days respectively. The mean estimated error, at the SRT of 15 days is due to an inadequate prediction of de-nitrification process at these operating conditions.



## CONCLUSIONS

The developed MBR model can simulate with sufficient accuracy the general behavior of the MBR unit, characterized by a high COD wastewater input with significant fluctuations, for activated sludge, biomass, COD and ammonia effluents concentrations and the membrane fouling potential at the range of SRTs between 1 and 30 days. It fails to predict the production of microbial products, except the case of SRT of 20 days for the SMPs and the SRT of 30 days for the EPS. Examining the simulation results for TMP and SMP production, SMPs appear to be the main factor for fouling. However, as also pointed out in several previous studies (Ahn et al., 2006; Janus and Ulanicki, 2010; Chen et al., 2012), the model predictions are very sensitive to changes in the kinetic and stoichiometric parameters; and hence, their values match be carefully chosen. Furthermore, some processes such as the production and degradation of EPS and SMPs seem to be affected by changes in sludge retention time and hence, they could impact on prediction ability of the model (Chen et al., 2012). The mathematical descriptions of the SMP kinetics need to be improved in order to describe more realistically the mechanisms of their production and degradation. The model succeeds in simulating satisfactorily the dynamic behavior of transmembrane pressure at different operating conditions.

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