



The TTT Curves of the Heterogeneous and Homogeneous Crystallization of Lithium Disilicate – A Stochastic Approach to Crystal Nucleation

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Krüger S and Deubener J (2016) The TTT Curves of the Heterogeneous and Homogeneous Crystallization of Lithium Disilicate – A Stochastic Approach to Crystal Nucleation. Front. Mater. 3:42. doi: 10.3389/fmats.2016.00042 The present study explores the temperature and time dependence of heterogeneous (HET) crystal nucleation in a lithium disilicate glass using the stochastic approach. In particular, a single lithium disilicate sample was repeatedly (284 runs) undercooled to 1173 K in a PtRh-crucible and the crystallization onset time during an isothermal hold was detected in each run. The statistical distribution of the times elapsed before crystallization is described by a first-order reaction with a HET crystal nucleation rate of $(9.19 \pm 0.04) \times 10^{-4} \, \text{s}^{-1}$ while individually shaped crystallization exotherms of each run were recorded, which indicate growth of a single or only few crystals during crystallization of the entire volume. The data were used together with results of previous stochastic experiments and those of double-stage heat treatments to calculate the crystallization time of a fraction of 10^{-4} percent for all temperatures between glass transition and melting. The derived TTT diagram shows a double-nose of crystallization in the volume at large undercoolings (0.53–0.61 T_m) and crystallization at the surface at small undercoolings (0.62–0.92 T_m) initiated by homogeneous and HET crystal nucleation, respectively. The critical cooling rate at the HET nose is approximately 73 K s⁻¹.

Keywords: lithium disilicate glass, time of formation of the first supercritical nucleus, stochastic nature of crystal nucleation, effective nucleation rate, TTT representation, coast-island microstructure

INTRODUCTION

In the last 40 years, crystal nucleation in silicate glasses has been addressed by counting crystal number densities in the volume of glass specimens subjected to double-stage heat treatments (Fokin et al., 2006). The techniques bears the advantage of direct determination of the crystal nucleation rate from calculating the first time derivative of the number density curve but has the drawback that it is limited to a narrow temperature range near the glass transformation temperature ($T_g \leq T \leq 1.2 T_g$) where driving forces are high and crystal nucleation is occurring frequently in the volume. Another drawback is the dissolution of nuclei that are critical at the first stage but subcritical at the second stage. In the case of surface crystallization, the accessible temperature range becomes broader but the time period of crystal nucleation is mostly limited due to fast saturation of active sites. A short nucleation period merely allows for an indirect determination of the crystal nucleation rate. Thus, birth- (from crystal size distribution) (Müller et al., 2000) and impingement-times (Krüger and Deubener, 2015a) of crystals at the surface have been analyzed to deduce

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their rates of nucleation. In each of these methods (and also for analyzing high-temperature X-ray diffraction data (Dressler et al., 2011, 2014), an ensemble of crystals is analyzed in order to derive nucleation parameters. The criterion applies for large undercoolings but becomes ineffective at higher temperatures where crystal grow rates are generally high and the entire liquid volume is shortly consumed by the first nucleated crystal. In consequence, nucleation data for temperatures $T > 1.2 T_g$ are lacking for both binary/ternary model glasses and for technical multi-component glass systems. The occurrence of a substantial gap in the reported nucleation data is surprising and unexpected if one recalls the large number of glasses produced in industrial practice by forming during quench. Furthermore, the analysis of a crystal ensemble does not allow to prove randomness in the nucleation events, a necessary condition in the framework of CNT. By contrast, the observation of single crystal events helps in discriminating partition of long-range diffusion fluxes (Kelton, 2000).

In the light of the above, this study aims at establishing nucleation kinetics by its time average of repeated single crystal nucleation events rather than using the ensemble average of crystals of double-stage heat treatments. The so-called stochastic approach to crystal nucleation has been introduced for undercooled low viscous (mPa s) liquids, such as metals and hydrous suspensions (Toschev and Markov, 1967; Toschev and Gutzow, 1972; Toschev et al., 1972; Toschev, 1973; Morton et al., 1994; Barlow and Haymet, 1995; Uttormark et al., 1997; Heneghan et al., 2001, 2002; Heneghan and Haymet, 2002; Wilson et al., 2005; Wilde et al., 2006, 2009; Yang et al., 2009, 2011, 2013). Our results show that it is applicable to high viscous (kPa s) silicate melts and it results in heterogeneous (HET) crystal nucleation rates from which TTT representations and critical cooling rates can be derived.

The formation of supercritical nuclei is a stochastic process. Nucleation events occur randomly and independent from each other. Already in the 1960s, Toschev and Markov (1967) showed that the electrolytic deposition of cadmium on platinum single crystal electrodes follows a Poisson distribution. Thereby, both the number of nuclei in a given time interval and the time necessary to form a certain number of nuclei are linked to probability distributions (Toschev and Gutzow, 1972; Toschev et al., 1972; Toschev, 1973).

Later probability distribution functions in the formation of the first supercritical nucleus have been studied for other liquid metals, such as niobium and zirconium (Morton et al., 1994), aluminum (Uttormark et al., 1997), gold and copper (Wilde et al., 2006, 2009), and tin (Yang et al., 2009, 2011, 2013) but also in water (pure and seeded) (Barlow and Haymet, 1995; Heneghan et al., 2001, 2002; Heneghan and Haymet, 2002; Wilson et al., 2005) and in gas hydrates (Maeda et al., 2011, 2012). In all these experiments, a single sample was repeatedly undercooled from above the melting temperature, while either the time (at an isothermal hold) or the temperature (at an isochronal cooling) of crystallization was detected. These experiments provided primary information on the average lag time and the mean undercooling, from which the crystal nucleation rate and the critical cooling rate can be derived. Secondary information include the activity of seeds and the purification of the liquid upon thermal cycling. Especially the ALTA ("automated lag time apparatus") concept

developed for studying the freezing behavior of water (Barlow and Haymet, 1995) is acknowledged since it has been designed to permit time-saving through a feed-back control that heats the sample immediately upon freezing.

In the past years, non-adiabatic fast scanning calorimetry has been developed to *in situ* measure the response of single metallic drops to temperature changes in a large range of cooling rate spanning four orders of magnitude (Yang et al., 2009, 2011, 2013). In these experiments, a small drop (volume $\approx 10^{-6}$ mm³) is repeatedly heated and cooled on a thin film sensor with rates up to 10^4 K s⁻¹. Unfortunately, current technology of the so-called flash- or chip-calorimeters is limited to a maximum sensor temperature of about 700 K, which is much lower than the liquidus temperature of lithium disilicate glass [1306 K (Kracek, 1930)].

Glasses in the binary Li₂O-SiO₂ system, such as lithium disilicate (Li₂Si₂O₅) have been the object of extensive research (see, for example, Tomozawa, 1972, 1973; Matusita and Tashiro, 1973; James, 1974, 1985; Fokin et al., 1981; Weinberg and Neilson, 1985; Barker et al., 1988; Deubener et al., 1993; Ota et al., 1997; Burgner and Weinberg, 2001; Nascimento et al., 2011) since their crystal nucleation and growth rates are relatively low at high undercoolings ($T < 1.2 T_g$) and thus conveniently measurable from crystal number densities and crystal sizes of optical microscopy images (James, 1974, 1989; Rowlands and James, 1979). Furthermore, detailed thermodynamic data are available for this system (Takahashi and Yoshio, 1973) which allow to test the validity of basic nucleation models from comparisons of predicted rates with measured data (Neilson and Weinberg, 1979; Rowlands and James, 1979; Zanotto and James, 1985; Weinberg and Zanotto, 1989; Fokin et al., 2010a).

Li₂Si₂O₅ crystals nucleate homogeneously in the volume (James et al., 1978; James, 1985; Zanotto and James, 1985; Zanotto, 1987; Barker et al., 1988) disregarding the controversy of metastable phase formation prior to the crystallization of stable Li₂Si₂O₅ crystals (Hench et al., 1971; Tomozawa, 1972; Barker et al., 1988; Deubener et al., 1993; Zanotto, 1997; Burgner et al., 1999; Iqbal et al., 1999) but also heterogeneously at suspended particles, such as platinum (Cronin and Pye, 1986; Narayan et al., 1996; Ray and Day, 1996; Ray et al., 1996; Mishima et al., 2006; Ranasinghe et al., 2007) and at the surfaces with the surrounding gas atmosphere (James, 1989; Ray and Day, 1996; Ray et al., 1996; Ranasinghe et al., 2007; Fokin et al., 2010b). Ranasinghe et al. (2007) performed heat treatments on pure and platinum doped Li₂Si₂O₅ glasses and found that the critical cooling rate increases and the activation energy of crystallization decreases when Li₂Si₂O₅ glass is heated in a container as compared to containerless processing (levitation) and that in both cases platinum promotes the crystallization of lithium disilicate glasses. However, the temperature dependence of preferred HET crystal nucleation leading to observable "coast-island" microstructures [see Fig. 1C in Krüger and Deubener (2015a) and Fig. 14 in Fokin et al. (2010b)] is not well understood with respect to isothermal heat treatments and for ramping at constant rates from above melting temperature and below glass transformation temperature, respectively.

The present paper reports on novel experiments of HET crystal nucleation, which have been performed by the stochastic approach under isothermal conditions at small undercooling (1.6 $T_{\rm g}$). In

particular, the time elapsed before the formation of the first supercritical nucleus is detected from repeated measurements in a PtRh-crucible and the HET steady-state nucleation rate is derived from the first-order kinetics of the probability distribution function. Using previous data (Krüger and Deubener, 2014, 2015a), a TTT diagram is produced from which the HET and homogeneous (HOM) crystallization can be clearly distinguished. The TTT curves of lithium disilicate help in understanding the development of coast-island microstructures observed in practice during cooling from above the liquidus temperature. We assume that the here established method is able to clarify also the crystallization mechanisms in other glass-forming systems.

EXPERIMENTAL

A glass of nominal composition Li₂Si₂O₅ was prepared by melting a batch of the raw materials SiO₂ and Li₂CO₃ (both of analytical grade). The batch was mixed and melted three times in a platinum crucible at 1673 K for 1 h under ambient conditions. The melt was subsequently quenched between two steel plates, which resulted in cooling rates of ~150–250 K min⁻¹. The glass was analyzed by X-ray fluorescence (S4 Pioneer; Bruker AXS, Karlsruhe, Germany) while the Li₂O content was determined by atomic emission spectroscopy (ICP-OES Vista MPX; Varian). The analyzed chemical composition was 77.4 SiO₂, 21.0 Li₂O, and 1.6



FIGURE 1 | Scheme of the DSC protocol for two subsequent cooling-dwelling runs (*N* and *N* + 1) in the isothermal operating mode ($\Delta T = 133$ K). The red dashed-dotted line shows the progression of the temperature of the heating-dwelling-cooling-dwelling cycles. The black horizontal dashed lines are T_m and the nucleation temperature of the runs *N* and *N* + 1 with $T_N = T_{N+1} = 1173$ K, thus $\Delta T = 133$ K (black double arrow). The black vertical dashed lines show the times of the beginning of the isothermal hold of the runs *N* and *N* + 1 with $t_{\text{b}(N)}$ and $t_{\text{b}(N+1)}$, respectively and the times of the start of the crystallization of both runs with t_N and t_{N+1} . Herein, the beginning of the crystallization equals the onset of the extinemation of the first supercritical nucleus in each run (black horizontal double arrows) δ_N (for run *N*) and δ_{N+1} (for run *N* + 1) is calculated by $t_N - t_{\text{b}(N)}$ and $t_{N+1} - t_{\text{b}(N+1)}$, respectively.

impurities (all in percent by weight), which slightly deviates from the nominal stoichiometry of $\rm Li_2Si_2O_5.$

A chip (= 21.4 mg) of the glass was inserted in a lidded PtRhcrucible and subjected to high-temperature differential scanning calorimetry (DSC 404 F3 Pegasus; Netzsch, Selb, Germany) under nitrogen atmosphere. A scheme of the operating mode of the DSC with the characteristic repeatedly performed heatingdwelling-cooling-dwelling cycles (red dashed-dotted line) is shown in Figure 1. In particular, the glass chip was heated at 0.167 K s^{-1} to a temperature of 1353 K, which is 47 K above $T_{\rm m}$ $[T_m = 1306 \text{ K} \text{ (Kracek, 1930)}]$, dwelled for 300 s to ensure fully melting of the sample, cooled by $\sim 1.25 \text{ K s}^{-1}$ to the dwell temperature of 1173 K (undercooling $\Delta T = 133$ K) and dwelled for 3360 s [the dwell time was set to ca. 1 h, a reasonable time in accordance with the results of Krüger and Deubener (2014)]. After dwelling the sample was immediately heated again to start the next run. In total 284 ($= N_0$) runs were performed. In each run, the time elapsed before the first supercritical nucleus is formed $(\delta_N \text{ and } \delta_{N+1})$ was calculated by subtracting the beginning of the isothermal hold $(t_{b(N)} \text{ and } t_{b(N+1)})$ from the crystallization onset time (t_N and t_{N+1}) of the isothermal exothermal DSC signal (blue solid line in Figure 1). We assume that the recorded crystallization onset times follow the same distribution as δ_N and δ_{N+1} since the time for crystal growth is negligible at this high temperature.

RESULTS

The basic result of our experiment is a histogram of the time of the formation of the first supercritical nucleus for each run δ_N in dependence of the run number *N* (**Figure 2**). This histogram provides the following information: first, 26 runs were crystallized before the dwell temperature at $\Delta T = 133$ K was reached ($\delta_N < 0$ s,





blue dashed-dotted line of Figure 2) and 21 runs remained uncrystallized due to the programmed maximum dwell time of 3360 s $(\delta_{\rm N} > 3360$ s, red dashed-dotted line of **Figure 2**). Second, the histogram shows a random distribution of δ_N which indicates that the preferred HET nucleation site is continuously active during the entire experiment. A fast Fourier transformation (not shown) proved absence of any diurnal or other periodic behavior. One may assume that the crystal nucleates at the three-phase boundary between the silicate melt, the crucible wall, and the nitrogen atmosphere, but this is not known. Furthermore, the silhouette of Figure 2 (black outline of the time elapsed before the first supercritical nucleus is formed) seems to be horizontal, which indicates that compositional changes of the melt due to possible nitrogen dissolution and lithium evaporation at the surface are negligible. Furthermore, no shift in the integrated signal values was observed (not shown) which confirms the absence of any traceable mass loss during the entire period of the experiment.

In order to determine the HET steady-state nucleation rate $I_{0 (\text{HET})}$ from this isothermal experiment, the relative frequencies of the number of runs remained unfrozen after a certain time are calculated. The procedure is similar to the calculation of the survival curve in Barlow and Haymet (1995) and Krüger and Deubener (2014). The δ_N data of Figure 2 are first arranged according to their length. At the shortest δ_N (=0s), there are 258 runs uncrystallized (26 runs crystallized during cooling to the dwell temperature). In all other runs, crystallization occurred at larger δ_N . For $\delta_N = 0$, the uncrystallized fraction is $N(\delta_{\rm N}=0)/N_0 = 258/284 = 0.908$. For the second shortest $\delta_{\rm N}$, the fraction uncrystallized is 257/284 = 0.905 and so on. The last $N(\delta_{\rm N})/N_0$ fraction calculated in that way is 21/284 = 0.074 at $\delta_{\rm N} = 3342$ s since 21 runs were still uncrystallized at the end of the programmed isothermal hold. This fraction is set to 0. The calculated fractions $N(\delta_N)/N_0$ are plotted as a function of δ_N (Figure 3). The distribution curve shows a simple exponential decay that illustrates an increase in the nucleation probability with longer δ_N . The nucleation probability can be described by a simple first-order rate equation

$$\frac{N(\delta_{\rm N})}{N_0} = A \exp(-I_{0(\rm HET)} \delta_{\rm N}) \tag{1}$$

and its logarithmic form

$$\ln\left(\frac{N(\delta_{\rm N})}{N_0}\right) = \ln(A) - I_{0(\rm HET)}\delta_{\rm N}$$
(2)

where the constant *A* accounts for the initially crystallized fraction at $\delta_N = 0$. Equation 2 is shown by the insert of **Figure 3**. The apparently linear dependence of the data on δ_N confirmed first-order reaction kinetics, and fitting the data (green solid line in **Figure 3**) results in a HET crystal nucleation rate of I_0 (HET) = $(9.19 \pm 0.04) \times 10^{-4} \text{ s}^{-1}$. We note that exclusion of the 26 runs crystallized before the isothermal hold is reached results in the same value of I_0 (HET) but the parameter *A* of Eq. 1 will become unity. However, we think that the consideration of all data points in the probability distribution as shown in **Figure 3** is the most appropriate linking to the stochastic experiment.



FIGURE 3 | Probability distribution of the fraction of runs uncrystallized ($N(\delta_N) N_0^{-1}$) in dependence of δ_N . The ovals (blue and red) correspond to the dashed-dotted lines of Figure 2. The insert shows the logarithmic Eq. 2. I_0 (HET) is given as the slope of the linear dependence. The green solid line is the best linear fit through the data with a regression coefficient $R^2 = 0.995$.

DISCUSSION

The most striking feature of the results is that the found exponential decay of Figure 3 is similar to those reported for seeded water (Barlow and Haymet, 1995; Heneghan et al., 2001, 2002). This underlines the fundamental character of crystal nucleation as a stochastic process obeying first-order reaction kinetics. However, one should note that due to the experimental constraints, such as the limited cooling rate to reach the dwell temperature and the restricted dwell time of 3360 s, 47 of the 248 runs are not captured by the probability distribution. Thus, a second crystal nucleation mechanism might be active with characteristic time scales $t_{\rm N} < t_{\rm b (N)}$ and $t_{\rm N} > \delta_{\rm N}$ (3360 s). This assumption is supported by the fact that the long time fractions of Figure 3 show a negative deviation from the proposed linearity. On the other hand, the negative deviation can also arise from an insufficient number of cooling runs preventing good statistics and, therefore, underestimating $N(\delta_N)/N_0$ at long times.

In order to exclude memory effects between adjacent runs of the histogram (**Figure 2**), a Pearson correlation test (Barlow and Haymet, 1995; Heneghan et al., 2001) was performed (not shown). A Pearson correlation coefficient r = 0.01 was obtained, which confirms that the probability of having correlation between adjacent runs is close to 0. The exclusion of memory effects is illustrated by different onset times of adjacent runs (**Figure 4**). Herein, the runs 6 and 7 exhibit significantly different crystallization onset times. Moreover, the individual evolution of the heat release of each run of **Figure 4** reveals growth of one or only few crystals (Krüger and Deubener, 2014). A larger ensemble of growing crystals would lead to an averaged signal shape (Gaussian) as it is typical for heating lithium disilicate glasses in DTA/DSC experiments



from temperatures below glass transformation (Krüger et al., 2013).

Additionally to the visual inspection of the signal's shape the broadness is analyzed. As an example, the signal of run 249 exhibits a broadness of 600 s (Figure 4). Assuming only one growing crystal and a crystal size that corresponds to the circumference of the crucible (the final geometry of the crystal after 284 runs is ring-shaped due to wetting of the crucible walls by the Li₂Si₂O₅ melt) leads to a crystal growth rate of $3.4 \times 10^{-5} \,\mathrm{m \, s^{-1}}$. The approximated growth rate from the signal's length is very close to the reported value $(5.1 \times 10^{-5} \text{ m s}^{-1})$ of Burgner and Weinberg (2001) for the same temperature that supports the assumption that the entire liquid volume is consumed by only one or few crystals. Few crystals would result in a somewhat smaller broadness (see, e.g., run 126 of Figure 4). A low number of crystals growing simultaneously at the surface are further supported by the observations of Ranasinghe et al. (2007). They found that only up to two crystals were simultaneously growing at the surface of levitated Li₂Si₂O₅ drops. Thus, in accordance with our DSC protocol (Figure 1), assigning the onset time of the crystallization peak to the time of the formation of the first supercritical nucleus seems to be reasonable.

In order to link $I_{0 \text{ (HET)}}$ to our previous stochastic experiment (Krüger and Deubener, 2014), which was run under constant cooling conditions (cooling rate = 0.083 K s⁻¹), nucleation rate data have to be derived from the undercooling-dependent $N(\Delta T)/N_0$ vs. ΔT distribution curve (**Figure 5**). In this case, the probability curve with the fractions of runs remaining unfrozen $N(\Delta T)/N_0$ at a certain undercooling is deconvoluted considering the temperature-dependent $I_{0 \text{ (HET)}}$:

$$I_{0(\text{HET})} = \frac{C_1}{\eta} \exp\left(-\frac{C_2}{T\Delta T^2}\right)$$
(3)



uncrystallized ($N(\Delta T) N_0^{-1}$) in dependence of the undercooling taken from Krüger and Deubener (2014) and deconvoluted to determine the temperature-dependent nucleation rate curve (insert). The green solid line of the insert shows the best fit of Eq. 4 through the data points using the adjustable parameters $C_1 = 391$ Pa and $C_2 = 2 \times 10^8$ K³. Note the renaming $\tau_N \equiv \delta_{N}$.

where C_1 and C_2 are temperature-independent constants and η is the viscosity of the Li₂Si₂O₅ melt. In order to determine C_1 and C_2 from the isochronal experiment, Eq. 3 is inserted in Eq. 1 and the parameter *A* is set to unity. By doing so, we assume that the crystal nucleation process is independent on the cooling rate. Rearranging the equation and taking the logarithm results in:

$$\ln\left[\frac{\eta}{\delta_{\rm N}}\ln\left(\frac{N_0}{N(\Delta T)}\right)\right] = \ln(C_1) - \frac{C_2}{T\Delta T^2}.$$
 (4)

By applying Eq. 4 to the already published data of Krüger and Deubener (2014) and the temperature-dependent viscosity of Krüger and Deubener (2015b), the adjustable parameter $C_1 = 391$ Pa and $C_2 = 2 \times 10^8$ K³ were determined (green solid line in the insert of **Figure 5**). We note the small deviation from the fitted trend of the runs of $\Delta T < 120$ K that is either an artifact of an insufficient number of cooling runs or an indication of a second crystal nucleation mechanism as already discussed in case of the isothermal experiment.

Plotting together the HET nucleation rate curve of the above calculation in the range 0.62–0.92 $T_{\rm m}$ (red solid line), $I_{0 (\rm HET)}$ of the isothermal experiment at $T = 0.898 T_{\rm m}$ (red circle), $I_{0 (\rm HET)}$ of single-stage experiments in the range 0.64–0.68 $T_{\rm m}$ (Krüger and Deubener, 2015a) (red squares), and the HOM nucleation rates of double-stage experiments in the range 0.53–0.61 $T_{\rm m}$ (James, 1974; Zanotto and James, 1985; Barker et al., 1988; Deubener et al., 1993) (blue circles) on the reduced temperature scale $T/T_{\rm m}$ reveals that the HET nucleation rate curve is well separated from the HOM one. Maximum nucleation rates are found at $T_{\rm max (HOM)} = 0.55 T_{\rm m}$ and $T_{\rm max (HET)} = 0.82 T_{\rm m}$ for the HOM and

the HET crystal nucleation, respectively (**Figure 6**). The equations of the classical nucleation theory and the material-specific input parameters listed in **Tables 1** and **2** were used to fit these experimental data (OriginPro 9.0.0G; OriginLab Corp.). In order



to calculate crystal nucleation rates (blue and red dashed-dotted lines in Figure 6) in the dimension of a frequency, HOM and HET nucleation rates were multiplied by the sample volume and the surface area, respectively. The liquid-crystal interfacial energy was treated as an adjustable parameter for which a linear temperature dependence in accordance with James (1985) was anticipated (Tables 1 and 2). The coordination number of the moving particle (CN = 2) and the number of atoms in a structural unit (n = 9)both entering the Eyring equation to adopt diffusivity to viscous flow where utilized from a previous study (Krüger and Deubener, 2015b). In case of the HET nucleation rate curve, additionally the number of active nucleation sites $n_{\rm S} = (0.023 \pm 0.001) \text{ m}^{-2}$ and the wetting angle $\theta = (26.4 \pm 0.1)^{\circ}$ were adjusted to fit the data best. The resulting curves emphasize that at T_{max} the HET crystal nucleation rate is about two orders of magnitude smaller than the HOM one. The sum of both rates is the effective crystal nucleation rate that is highlighted by the black solid line in Figure 6. We note that possible sources of the small deviation between $I_{0 (\text{HET})}$ of the isothermal and the isochronal statistical experiment are differences in the glass composition and changes in the quality of the crucible used in the two studies.

With regard to the large difference in T_{max} between surface and volume crystal nucleation in lithium disilicate, it is interesting to compute a TTT diagram for the crystalline fraction $\alpha = 10^{-6}$ (Uhlmann, 1972) using the following two equations (Zanotto, 1996):

$$t_{\rm V} = \left(-\frac{3\ln(1-\alpha)}{\pi I_{0({\rm HOM})} U^3} \right)^{\frac{1}{4}}$$
(5)

and

$$t_{\rm S} = \left(-\frac{\ln(1-\alpha)}{I_{0({\rm HET})}U^2}\right)^{\frac{1}{3}}.$$
 (6)

In Equations 5 and 6, t_V and t_S are the times necessary to crystallize 10^{-4} percent of the glass in the volume and at the surface, respectively. *U* is the crystal growth rate that is utilized from

| Parameter | ном | HET | Reference |
|---|----------------------------------|-----------------------|-----------------------------|
| Number of formula units per unit volume n_V (m ⁻³) | 9.43 × 10 ²⁷ | _ | Neilson and Weinberg (1979) |
| Density of the supercooled liquid ρ_{liquid} (g cm ⁻³) ^b | 2.350 | | Schmelzer et al. (2004) |
| Molar mass M (g mol ⁻¹) | 150.05 | | |
| Number of active nucleation sites per unit surface area $n_{\rm S}$ (m ⁻²) | - | 0.023 ± 0.001^{a} | |
| Interfacial energy parameter a (J m ⁻²) | $(2885 \pm 8) \times 10^{-5a,c}$ | | |
| Interfacial energy parameter $b (Jm^{-2}K^{-1})$ | $(1655 \pm 8) \times 10^{-7a,c}$ | | |
| Molar volume $V_{\rm M}$ (m ³ mol ⁻¹) | 6.15×10^{-5} | | Krüger and Deubener (2015b) |
| Crystal density $\rho_{crystal}$ (g cm ⁻³) | 2.438 | | Deubener et al. (1993) |
| Molar enthalpy of melting $\Delta H_{\rm m}$ (J mol ⁻¹) | 61090 | | Takahashi and Yoshio (1973) |
| Thermodynamic ratio ω | 0.34 | | Takahashi and Yoshio (1973) |
| Contact angle θ (°) | 180 | 26.4 ± 0.1^{a} | |
| Atomic jump distance λ (m) | 4.68×10^{-10} | | Krüger and Deubener (2015b) |
| VFT parameter A _{VFT} | -2.37 | | Krüger and Deubener (2015b) |
| VFT parameter B _{VFT} (K) | 3248.62 | | Krüger and Deubener (2015b) |
| VFT parameter T_0 (K) | 500.24 | | Krüger and Deubener (2015b) |
| Coordination number CN | 2 | | Krüger and Deubener (2015b) |
| Number of atoms per formula unit n | | 9 | |

^aAdjustable parameter.

^bGlass density at room temperature. Thermal expansion of the liquid volume is neglected.

^cInterfacial energy parameters of James (1985): $a = 2911 \times 10^{-5} Jm^{-2}$, $b = 1617 \times 10^{-7} Jm^{-2} K^{-1}$ were used as initial values for the fitting.

TABLE 2 | Equations of the calculation of the homogeneous (HOM) and heterogeneous (HET) crystal nucleation rate.

| Equation | ном | HET | Reference |
|--|---|---|---|
| Number of formula units per volume $n_{\rm V} =$ | $ ho_{liquid} N_A/M$ | | James (1985, 1989) |
| Molar volume $V_{\rm m} =$ | <i>Μ</i> /ρ _{crystal} | | James (1985, 1989) |
| Liquid–crystal interfacial energy $\sigma =$ | a+bT | | James (1985, 1989) |
| Atomic jump distance $\lambda =$ | $\left(\frac{V_{M}}{N_{A}}\right)^{\frac{1}{3}}$ | | James (1985, 1989) |
| Viscosity $lg(\eta) =$ | $A_{\rm VFT} + rac{B_{\rm VFT}}{\overline{T-T_0}}$ | | Vogel (1921), Fulcher (1925), and Tammann and Hesse (1926) |
| Gibbs energy of crystallization $\Delta G =$ | $\Delta H_{\rm m} \left(1 - \frac{T}{T_{\rm m}}\right) \left[1 - \frac{\omega}{2} \left(1 - \frac{T}{T_{\rm m}}\right)\right]$ with | $\omega = \frac{\Delta C_{\rm p}(T_{\rm m})}{\Delta S_{\rm M}}$ | Gutzow and Schmelzer (1995) |
| Diffusion coefficient $D =$ | $\frac{kT}{\eta} \frac{1}{CN} \left(\frac{nN_A}{V_M} \right)^{\frac{1}{3}}$ | | Eyring et al. (1982) |
| Kinetic barrier $\frac{\Delta G_{\rm D}}{kT}$ = | $\ln\left(\frac{kT\lambda^2}{hD}\right)$ | | James (1985, 1989) |
| Thermodynamic barrier $\frac{W}{kT} =$ | $\frac{16\pi\sigma^3 V_{M}^2}{3\Delta G^2} \frac{2\!-\!3\cos(\theta)\!+\!\cos^3(\theta)}{4}$ | | Gutzow and Schmelzer (1995) |
| Prefactor $A_{\rm I} =$ | $\frac{kT}{h}N_V$ | $\frac{kT}{h}n_{s}$ | James (1985, 1989) |
| Nucleation rate $I_0 =$ | $A_{\rm I} \exp\left(-rac{W+\Delta G_{\rm D}}{kT} ight)$ | | Turnbull (1956) |

Constants: Avogardo $N_A = 6.0221 \times 10^{23} \text{ mol}^{-1}$, Boltzmann $k = 1.3806 \times 10^{-23} \text{ JK}^{-1}$ and Planck $h = 6.626 \times 10^{-34} \text{ Js}$. Parameters: $\Delta S_M = \text{molar entropy of melting}$, $\Delta C_p(T_m) = \text{difference in the molar heat capacity between the liquid and crystalline state at the melting point.$



(green dotted line).

the data compilation of Burgner and Weinberg (2001). **Figure 7** shows that crystallization initiated by HET surface nucleation (red dashed-dotted line) and HOM volume nucleation (blue dashed-dotted line) overlap only partially. In order to calculate the overall crystallization time, Eq. 6 was used, while I_0 (HOM) was converted to a surface nucleation rate $[I_0$ (HOM, S) = I_0 (HOM, V)^{2/3} × t_V ^{-1/3} (Krüger and Deubener, 2015a), the uncertainty of the conversion is less than 1%] and added to the HET nucleation rate. The shape of

the overall time with a "double-nose" (black solid line) resembles those of an aqueous lithium chloride solution (MacFarlane et al., 1983) and of polybutylene terephthalate (Androsch et al., 2015). The double-nose diagram helps to explain the formation of a coast-island microstructure if lithium disilicate glass is heated at low rates from below T_g in practice. In agreement with the microstructures shown for different heating rates in Krüger and Deubener (2015a), larger heating rates suppress HOM volume nucleation of crystals and allow for surface crystallization only. By contrast, if a lithium disilicate glass sample is subjected at the first stage of the double-stage heat treatment to a temperature in the HOM nucleation range dwelling will form initially crystal nuclei in the volume (James, 1974). Additionally, the distinct HET nose of the TTT diagram emphasizes that cooling a lithium disilicate melt from above $T_{\rm m}$ always leads to a crystallized surface and dictates the critical cooling rate in this system. The latter is estimated by the so-called nose method using the simple calculus $R_{\rm c} = (T_{\rm n} - T_{\rm m})/t_{\rm n}$ (Uhlmann, 1972). With the coordinates of the nose $T_n = 1122$ K and $t_n = 2.51$ s, the critical cooling rate is ca. 73 K s^{-1} (green dotted line in **Figure 7**).

We are fully aware that R_c is overestimated by the TTT representation (Xu et al., 2013). A TTT diagram has to be converted to a CCT diagram to calculate the critical cooling rate more exactly (Grange and Kiefer, 1941; Zhu et al., 2006). However, it was shown by Davies (1976), Ramachandrarao et al. (1977), Uhlmann and Yinnon (1983), and Scherer (1991) that R_c calculated from a TTT diagram meets the experimental result within one order of magnitude. A first attempt to determine TTT and CCT diagrams in lithium disilicate was performed by Zhu et al. (2006) 10 years ago. They spotted a small glass volume on the tip of a Pt-thermocouple and measured the onset temperature and time of the crystallization peak in isochronal and isothermal mode of operation. By comparison to **Figure 7**, their single nose can be clearly identified as the HET part of the overall crystallization leading to exclusively surface crystallization.

CONCLUSION

The most striking outcome of the present study is the "doublenose" TTT diagram of lithium disilicate due to a decoupling of the nucleation mechanisms of HOM volume nucleation of crystals at large undercoolings ($0.53-0.61 T_m$) and HET surface nucleation of crystals at smaller undercoolings ($0.62-0.92 T_m$). This behavior is the origin for the evolution of coast-island microstructures of lithium disilicate in practice. Due to the stochastic experiments at small undercoolings HET nucleation is measurable and the corresponding rate with a maximum at 1071 K is quantified for the first time. Based on the calculated TTT diagram the critical cooling rate is about 73 K s⁻¹.

The results emphasize that exploring the time average of nucleation events by thermal cycling is a novel and highly attractive

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route to study HET crystal nucleation in silicate glasses. In particular, they point out that the rare data on HET nucleation rates and critical cooling rates that are based on one-time cooling experiments have to be reconsidered to include statistical certainty.

AUTHOR CONTRIBUTIONS

SK performed experiments. SK and JD prepared manuscript.

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