



# **Graphene-Based Tunable Wideband Metamaterial Absorber With Polarization Insensitivity and Wide Incident Angle**

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A graphene-based tunable wideband metamaterial absorber with polarization insensitivity and wide incident angle is presented in this paper. The results show that the absorption is over 90% from 5 to 8 GHz when the Fermi level of graphene is 0.5 eV, and the absorption can be tuned by electrically changing the Fermi level of graphene. The mechanism of wideband and tunable absorption is explained by calculating the normalized input impedance and monitoring the surface current. Finally, the results adequately verify that the absorption of metamaterial absorber has the advantages of polarization insensitivity and wide incident angle. Thus, it holds great potential application value in many fields such as electromagnetic stealth, electromagnetic shielding, communication, and so on.

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# INTRODUCTION

In recent years, metamaterial, a kind of artificially structured material has attracted wide attention due to its unique electromagnetic properties [1-3]. With the development of research on metamaterial, researchers discovered that metamaterial has great potential in the fields of super lens, electromagnetic stealth, optical black hole, polarization converter, perfect electromagnetic absorption, and many more [4-8]. Among the above applications, metamaterial absorber was proposed by Landy et al. [9]. Since then, the research of metamaterial absorber has attracted extensive attention because of its perfect electromagnetic absorption property, ultrathin microstructure, and great potential in military and civil applications. Currently, the research of metamaterial absorber mainly focuses on the wide incident angle, polarization independency, tunability, and multiband absorption [10-14]. However, the wideband metamaterial absorber is more suitable for the application of practical electromagnetic environment. At present, many methods have been used to expand the absorption bandwidth of metamaterial absorber, such as vertical superposition of different resonant units, fractal structure, and magnetic media and so on [15-18]. Among them, the combination of lumped element, plasma Brewster enhancement, and strong coupling effect with metamaterial absorber is a very effective method to realize wideband metamaterial absorber [19-21].

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Compared with the traditional passive metamaterial absorber, the active metamaterial absorber can realize the active adjustment of its electromagnetic property by changing the parameters of lumped components or the electromagnetic property of the intermediate medium, so it has more application prospects in practice.

Based on the electrically tunable conductivity of graphene, a graphene-based tunable wideband metamaterial absorber with polarization insensitivity and wide incident angle is designed in this paper. The results show that the absorption of metamaterial absorber is more than 90% from 5 to 8 GHz when the Fermi energy level of graphene is 0.5 eV, and the absorption can be tuned by electrically changing the Fermi level of graphene. Further study shows that the absorption property of metamaterial absorber has the advantages of polarization insensitivity and wide incident angle.

# THE ELECTRICALLY TUNABLE CONDUCTIVITY OF GRAPHENE

Graphene is a kind of two-dimensional planar crystal with very high electron and hole mobility. Its conductivity can be regulated by changing the external bias voltage applied on graphene, so graphene is widely used in tunable microwave and terahertz devices. When there is no bias magnetic field applied on graphene, its conductivity from microwave to visible band can be expressed by Kubo formula [22]:

$$\sigma(\omega,\mu_{c}) = \frac{-ie^{2}(\omega+i2\Gamma)}{\pi\hbar^{2}} \{ \frac{1}{(\omega+i2\Gamma)^{2}} \int_{0}^{\infty} \varepsilon \left[ \frac{\partial f_{d}(\varepsilon)}{\partial \varepsilon} - \frac{\partial f_{d}(-\varepsilon)}{\partial \varepsilon} \right] d\varepsilon - \int_{0}^{\infty} \varepsilon \left[ \frac{f_{d}(-\varepsilon) - f_{d}(\varepsilon)}{(\omega+i2\Gamma)^{2} - 4(\varepsilon/\hbar)^{2}} \right] d\varepsilon \}$$
(1)

$$f_d(\varepsilon) = \left[\exp(\varepsilon - \mu_c)/(k_B T) + 1\right]^{-1}$$
(2)

In the formulas (1) and (2),  $k_B$  is the Boltzmann constant,  $\hbar$  is the reduced Dirac constant,  $f_d(\varepsilon)$  is the Fermi Dirac distribution function,  $\mu_c$  is the Fermi level of graphene, *T* is the Kelvin temperature, and  $\Gamma=5 \times 10^{12} Hz$  is the carrier scattering rate. According to formulas (1) and (2), the calculated conductivity of graphene with different Fermi levels is shown in **Figure 1**.

It can be seen from **Figure 1** that the conductivity of graphene increases with the increasing of its Fermi level. The main method of changing the Fermi level of graphene is applying bias voltage on it. The Fermi level of graphene under different bias voltages applied on can be expressed as:

$$E_{bias} = \frac{e}{\varepsilon_0 \pi \hbar^2 v_F^2} \int_0^\infty \varepsilon [f_d(\varepsilon) - f_d(\varepsilon + 2\mu_c)] d\varepsilon$$
(3)

In formula (3),  $E_{bias}$  is the bias voltage applied on graphene,  $v_F = 10^6 m/s$  is the velocity of the electron. Graphene can be set as a material with the thickness of 0.001 µm, and the conductivity as shown in **Figure 1**.

# **MODEL DESIGN**

The unit cell of our graphene-based tunable wideband metamaterial absorber with polarization insensitivity and wide incident angle is presented in **Figure 2**. The unit cell consists of five layers: fractal tree metal loaded with graphene, FR4 medium ( $\varepsilon$ =4.3,tan  $\delta$  = 0.025), cross metal, FR4 medium, and metallic ground, in which the fractal tree metal and cross metal layer are connected by passing metal rods through the middle FR4 layer, as illustrated in **Figure 2**. The metal part of unit cell is composed of copper (). The optimized parameters of the unit cell are a = b = 9 mm, c = d = e = 0.6 mm, f = 8.5 mm,  $t_1 = 0.6$  mm,  $t_2 = 2$  mm,  $t_3 = 0.1$  mm. Doped silicon is used as the electrode to apply bias voltage on graphene.

The modeling and numerical simulation of metamaterial absorber is performed with Microwave Studio CST. At the simulation process, the boundary conditions of x and y directions are set as unit cell, the z direction is set as open, All+Floquet ports are used to simulate the incoming and outgoing waves. The electromagnetic parameters are calculated by using frequency domain electromagnetic solver.

# **RESULTS AND DISCUSSION**

When the incident electromagnetic waves enter into the proposed metamaterial absorber, the magnetic and electric resonances will be produced independently. The electromagnetic power of incident waves gets absorbed gradually by the dielectric loss and the loss of lumped graphene. When the absorption of metamaterial absorber reaches near perfect absorption, it obtains a state such that the permittivity equals the permeability and at the same time matches the impedance to free space. In a more direct perspective, the absorption of metamaterial absorber can be expressed as:

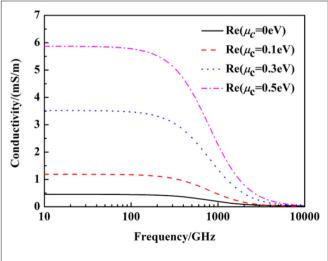


FIGURE 1 | The conductivity of graphene under different Fermi levels.

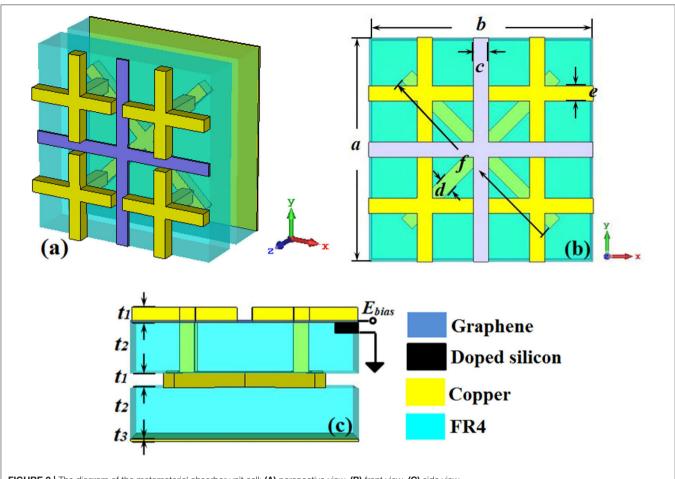
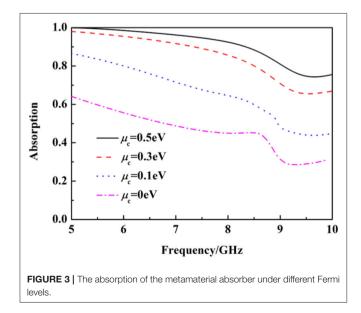
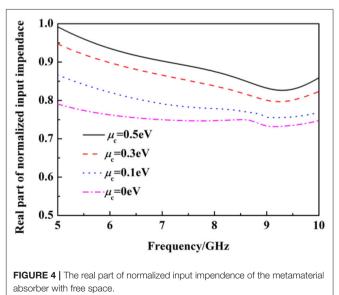
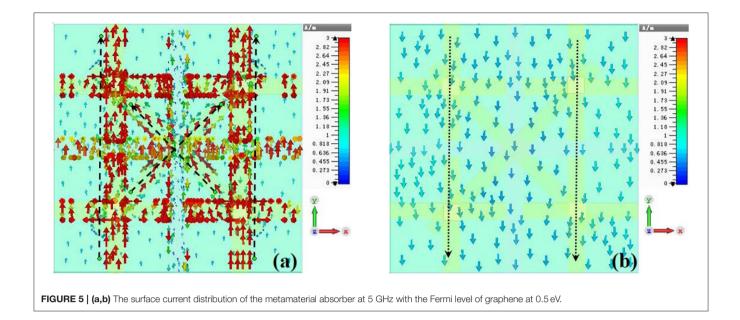
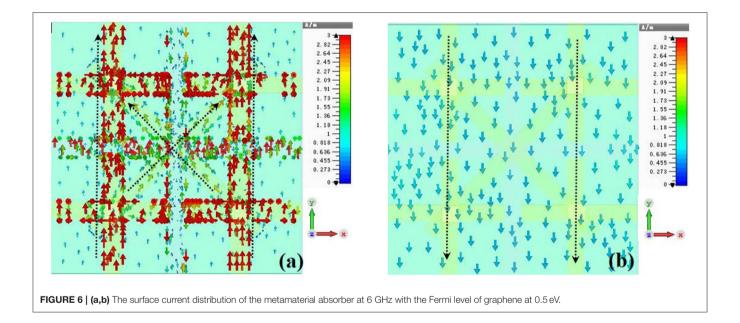


FIGURE 2 | The diagram of the metamaterial absorber unit cell: (A) perspective view, (B) front view, (C) side view.









$$A(\omega) = 1 - R(\omega) - T(\omega) = 1 - |S_{11}(\omega)|^2 - |S_{21}(\omega)|^2$$
(4)

Since the metallic ground of unit cell prevents the incident electromagnetic wave transmission, the above calculation formula of absorption can be simplified as:

$$A(\omega) = 1 - R(\omega) = 1 - |S_{11}(\omega)|^2$$
(5)

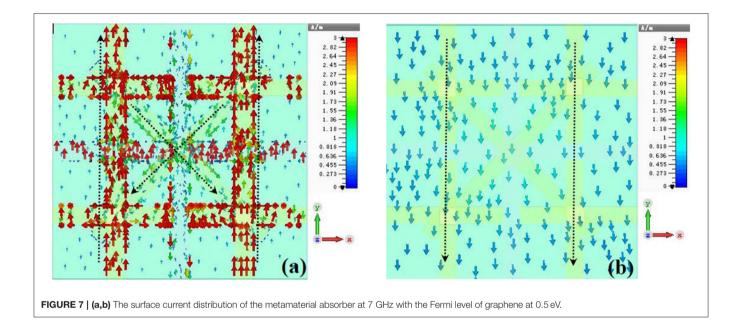
According to formula (5), we calculate the absorption of metamaterial absorber under different Fermi levels, as shown in **Figure 3**. It can be seen from **Figure 3** that the absorption

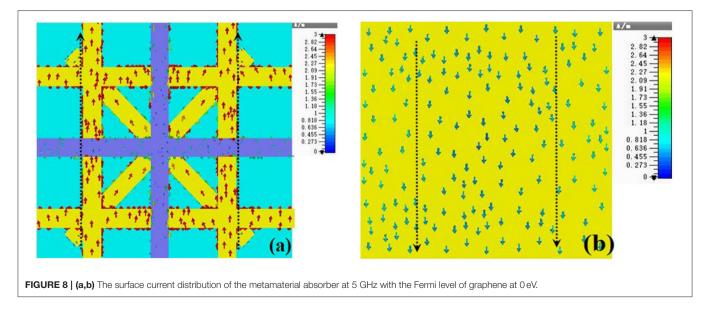
of metamaterial absorber exceeds 90% from 5 to 8 GHz when the Fermi level of graphene is at 0.5 eV, and the absorption of metamaterial absorber from 5 to 8 GHz gradually decreases with the decreasing of the Fermi level of graphene.

At present, the theory of equivalent medium can effectively explain the physical mechanism of metamaterial absorber [23]. According to the theory of equivalent medium, the metamaterial absorber can be regarded as an equivalent medium, which can be characterized by the equivalent permittivity  $\varepsilon(\omega)$  and equivalent permeability  $\mu(\omega)$ . According to the calculation, formula of normalized input impedance  $Z(w)/Z_0 = \sqrt{u(w)/\varepsilon(w)}$ , when the equivalent permittivity  $\varepsilon(\omega)$  and the equivalent

permeability  $\mu(\omega)$  of metamaterial absorber are identical, the normalized input impedance of metamaterial absorber with free space equals one, and then the reflection of metamaterial absorber to the incident wave reaches zero. As an outcome, the perfect absorption of metamaterial absorber will be realized. According to the  $S_{11}$  and  $S_{21}$  parameters extracted by simulation, the normalized input impedance  $Z_1(\omega)$  ( $Z_1(\omega)=Z(\omega)/Z_0$ ) of metamaterial absorber under different Fermi levels is calculated using the scattering parameter method [24], as shown in **Figure 4**. It can be seen from **Figure 4** that the real part of the normalized input impedance of metamaterial absorber with free space is close to one from 5 to 8 GHz with the Fermi energy level of graphene at 0.5 eV. This indicates that the metamaterial absorber has a good impedance matching with free space and achieves the condition of perfect absorption. At the same time, the real part of the normalized input impedance of metamaterial absorber with free space decreases gradually with the increasing of frequency, which leads to the decreasing of absorption.

In order to analyze the mechanism of wideband absorption, the surface current distribution of metamaterial absorber at 5, 6, and 7 GHz with the Fermi level of graphene at 0.5 eV is monitored, as shown in **Figures 5**, 7. It can be seen from **Figures 5A**, **6A**, **7A** that the generated surface current at the top fractal tree metal layer and the middle cross metal layer flows upward (although the surface current of the cross metal structure at 7 GHz is downward, it is very weak). This will lead



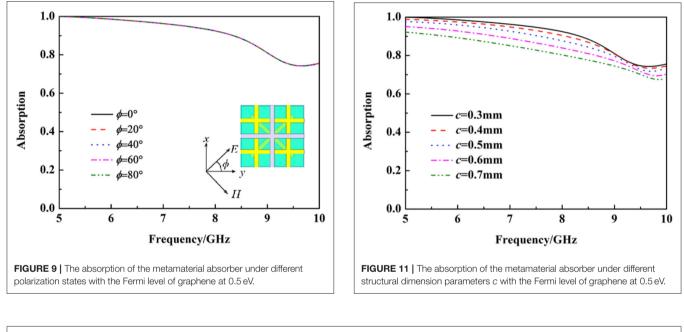


to the alternating accumulation of charges in the *y* direction, and then form electric dipole resonance [25]. It can be seen from **Figures 5B**, **6B**, **7B** that the generated surface current at the bottom metal substrate flows downward, which is opposite to the current direction of the top fractal tree metal layer and the cross metal layer. This antiparallel current forms a current circuit, which can cause a strong magnetic response resonance [26]. The magnetic resonance and electrical resonance are realized simultaneously at 5, 6, and 7 GHz and achieve the condition of perfect absorption. The wideband absorption is caused by the overlay of different resonance frequencies.

In order to further analyze the mechanism of tunable absorption, the surface current of metamaterial absorber at 5

GHz with the Fermi level of graphene at 0 eV is monitored, as shown in **Figure 8**. It can be seen from **Figure 8** that the metamaterial absorber generates electric resonance and magnetic resonance under the action of incident microwave [25, 26]. However, the excited surface currents on the fractal tree metal layer and the cross metal layer are weaker than the one at Fermi level of 0.5 eV (**Figure 5**), so the generated electromagnetic resonance is very weak, this results in lower absorption.

The absorption of metamaterial absorber under different polarization angles with the Fermi level of graphene at 0.5 eV is calculated, as shown in **Figure 9**. It can be seen from **Figure 9** that the absorption of the metamaterial absorber under different



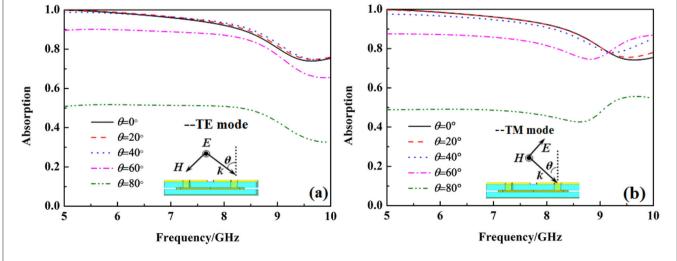
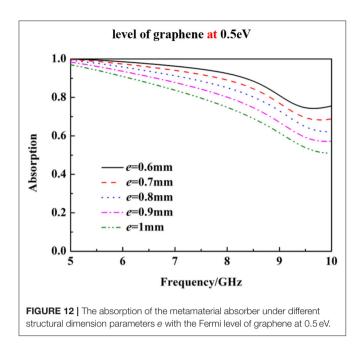


FIGURE 10 | The absorption of the metamaterial absorber under different incident angles with the Fermi level of graphene at 0.5 eV: (a) transverse electric (TE) mode, (b) transverse magnetic (TM) mode.



polarization angles is the same due to the rotational symmetry of the unit cell.

The absorption of the metamaterial absorber under different incident angles with the Fermi level of graphene at 0.5 eV is calculated, as shown in **Figure 10**. It can be seen from **Figure 10** that the absorption of the metamaterial absorber from 5 to 8 GHz gradually decreases with the incident angle increasing from 0 to  $60^{\circ}$  at transverse electric (TE) mode and transverse magnetic (TM) mode, but it can still be up to 90% from 5 to 8 GHz when the incident angle is  $60^{\circ}$ . The results show that the absorption of metamaterial absorber has the advantage of wide incident angle.

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The structural size of the metamaterial absorber has an important influence on its absorption. The absorption of the metamaterial absorber under different graphene width c and fractal tree metal linewidth e with the Fermi level of graphene at 0.5 eV is calculated, as shown in **Figures 11**, **12**. It can be seen from **Figures 11**, **12** that the absorption of the metamaterial absorber gradually decreases with the increasing of structure size parameters c and e.

# SUMMARY

To summarize, a graphene-based tunable wideband metamaterial absorber with polarization insensitivity and wide incident angle is presented in this paper. The metamaterial absorber provides >90% absorption from 5 to 8 GHz when the Fermi level of graphene is 0.5 eV. The absorption of the metamaterial absorber can be tuned electrically by applying an external bias voltage on graphene. Simulation results unveil that the response of the absorber presents a remarkably high absorption for a wide range of incident angles and is insensitive to polarization angle but has a relationship with its structure size parameters. The metamaterial absorber delivers the advantages of wideband, tunable, polarization insensitivity, and wide incident angle. It has great potential application value in the fields of electromagnetic stealth, electromagnetic shielding, communication, and so on.

# DATA AVAILABILITY STATEMENT

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

# **AUTHOR CONTRIBUTIONS**

All authors listed have made a substantial, direct and intellectual contribution to the work, and approved it for publication.

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**Conflict of Interest:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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