



Trapped in Out-of-Equilibrium Stationary State: Hot Brownian Motion in Optically Trapped Upconverting Nanoparticles

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Kumar S, Kumar A, Gunaseelan M, Vaippully R, Chakraborty D, Senthilselvan J and Roy B (2020) Trapped in Out-of-Equilibrium Stationary State: Hot Brownian Motion in Optically Trapped Upconverting Nanoparticles. Front. Phys. 8:570842. doi: 10.3389/fphy.2020.570842 Upconverting nanoparticles typically absorb low frequency radiation and emit at higher frequencies relying upon multiphoton processes. One such type of particle is NaYF₄:Yb,Er, which absorbs at 975 nm while emitting in visible radiation. Such particles have routinely been optically trapped. However, we find that trapping at the absorption maximum induces non-equilibrium features to the system. When we ascertain the Mean Square Displacement (MSD) of the axial motion, we find features that resemble Hot Brownian Motion (HBM) in active particles. We characterize the HBM observed here and find that the effective translational velocity of the system is 36 nm/s, small enough to be compensated by the optical tweezers. Thus, we have a system which is optically confined and stationary but in non-equilibrium, which we can also use to study non-equilibrium fluctuations.

Keywords: optical tweezers, hot Brownian motion, upconverting nanoparticles, active matter, nanophotonics

1. INTRODUCTION

The study of non-equilibrium system thermodynamics and active matter as emerged as a topic of intense interest in the recent decades [1–3], necessiated by the need to study the physics of microscopic systems where athermal fluctuations pay a crucial role [4, 5] and of living matter which is inherently far from equilibrium [6, 7]. Active matter, comprised of active agents, has the ability to transform energy to motion. Such study is important keeping in mind that biological systems are active in nature. In this context a key question is to use thermodynamic parameters to explain active systems [8–10].

One of the first active systems used an active Brownian particle moving at a constant speed in a medium with a direction determined by rotational diffusion [11]. Earlier, Boltzmann distribution was used to model the position of an active swimmer while in motion, with the effective temperature being higher than the ambient temperature. However, recent research showed that such assumptions fail when such a system is considered in confinement [12, 13]. Further, Argun et al. also showed that when a set of tracer particles is placed in a bacterial bath, the motion of the tracers show deviation from the mean field theory [8]. When and how the Boltzmann statistics fails for the active swimmers is an open question [7].

1

Here, we present a new system of an Upconverting Nanoparticle (UCNP) optically trapped [14, 15] on the absorption resonance that generates a thermal gradient across the particle due to preferential absorption of 975 nm light and emission of visible light on one side that propels the particle into a HBM [16]. We find that the MSD of the axial motion of the particle bears a signature that deviates from the effective temperature picture and instead follows HBM. The experimental system is much simpler than what has previously been attempted to generate an optically trapped active system, not to mention, there being an equilibrated directed motion inside the trap as opposed to being half the time along one direction and other half another direction [17]. The position distribution function is also simpler to analyse here than in the earlier case because of a clear preference for direction. There have been reports of estimation of instantaneous ballistic velocity [18] of such UCNP but active motion never reported.

2. THE EXPERIMENT

The experiment was performed on a setup made from the optical tweezers kit OTKB/M (Thorlabs) in the inverted configuration [19-21]. A linearly polarized 400 mW, 975 nm butterfly laser (Thorlabs) is inserted into the set-up to trap the upconverting particles. The objective used was an Olympus 100X, 1.3 NA oil immersion objective with the illumination aperture being overfilled and the condenser being a 10x, 0.25 NA Nikon airimmersion one. The power at the sample plane was about 30 mW, with the schematic being shown in Figure 1. There are a set of two dichroic mirrors, one at the input while one is at the output. An LED lamp illuminates the sample from the top via the output dichroic and passes through the bottom dichroic into a CMOS camera (Thorlabs). The 975 nm laser passes through the sample chamber and the forward scattered light is selected using the top dichroic into the Quadrant Photodiode (QPD). Only the 975 nm infra-red trapping light is used to infer positional information from the set-up.

The hexagonal upconversion disks (NaYF₄:Yb,Er) were prepared using a modified hydrothermal method [22]. 1.26 g of yttrium nitrate and 1.23 g of sodium citrate were dissolved in 14 ml of deionized water and stirred for 10 min. Then, 0.38 g of Yb(NO₃)₃ and 0.037 g of $Er(NO_3)_3$ were added in 21 ml of aqueous solution and mixed into the above solution. The white solution converted into a clear solution by adding 1.411 g of NaF (67 ml aqueous solution). The transparent solution was heated to 200 C for 12 h using a 200 ml teflon lined autoclave. The white colored powders were collected after washing with ethanol/water, followed by drying at 100 C about 12 h.

Such powder was suspended in double distilled de-ionized water and used for the experiment by placing in the sample chamber. The sample chamber consisted of a glass slide at the top (Blue Star, 75 mm length, 25 mm width, and a thickness of 1.1 mm) and a cover slip at bottom (Blue Star, number 1 size, English glass). For the air-water interface experiment, we used a long cover slip (Blue Star, number 1 size, English glass) over which the suspension was directly dropped, as reported in [21]. The system is room temperature controlled by the air-conditioner of the room, set at 25 C.



3. THE THEORY

An UCNP that absorbs in 975 nm and emits in visible typically has the light incident from one side of the particle [23]. It is on that backscattered direction itself that a large amount of visible light is also emitted. There is some light escaping in the forward scattered direction too but is much lower in intensity. This kind of configuration generates a temperature differential across the UCNP with the bottom part being hotter than the top. Such a configuration typically pushes the particle forward along the direction of propagation of the trapping beam.

In order to derive the MSD, lets consider the Langevin equation (Equation 1).

$$\frac{d\vec{r}}{dt} + \frac{k\vec{r}}{\gamma} = v_0\vec{n} + \frac{\vec{\eta}}{\gamma} \tag{1}$$

Here, the k is the trap stiffness, γ is the drag coefficient, \vec{n} is the unit vector along the activity direction, v_0 is the velocity with which the particle is moving and η the Gaussian distributed random noise due to Brownian motion. From here, the MSD is derived to be

$$<\Delta r^{2}(\Delta t) > = v_{0}^{2} \int_{0}^{t} dt' \int_{0}^{t} dt'' < \vec{n}(t')\vec{n}(t'')$$

$$> e^{-\frac{k}{\gamma}(t-t')} e^{-\frac{k}{\gamma}(t-t'')}$$

$$+ \frac{1}{\gamma^{2}} \int_{0}^{t} dt' \int_{0}^{t} dt'' < \eta(t')\eta(t'')$$

$$> e^{-\frac{k}{\gamma}(t-t')} e^{-\frac{k}{\gamma}(t-t'')}$$
(2)



In 2-dimensions,

$$<\eta(t')\eta(t'')>=4k_BT\gamma\delta(t'-t'')$$
(3)

and the correlation function between the normal vectors assuming D_r is the rotational diffusion coefficient of the particle in 2 dimensions,

$$<\vec{n}(t')\vec{n}(t'')>=e^{-2D_r|t'-t''|}$$
(4)

Thus the MSD, in the presence of the confining potential with trapping stiffness k is given by the expression

$$<\Delta r^{2}(\Delta t) > = \frac{2k_{B}T}{\gamma} (1 - e^{-2kt/\gamma}) + v_{0}^{2} \frac{(1 - exp(-2k\Delta t/\gamma))}{2k/\gamma} \frac{4D_{r}}{4D_{r}^{2} - (k/\gamma)^{2}} + v_{0}^{2} \frac{1 + exp(-2k\Delta t) - 2exp((-k/\gamma + 2D_{r})\Delta t)}{(k/\gamma)^{2} - 2D_{r}^{2}}$$
(5)

This simplifies to the expression, in the limit of very small k and D_r replaced as $\frac{1}{2\tau_r}$,

$$<\Delta r^{2}(\Delta t)>=4D\Delta t+\frac{\nu_{0}^{2}\tau_{r}^{2}}{2}(\frac{2\Delta t}{\tau_{r}}+e^{-\frac{2\Delta t}{\tau_{r}}}-1) \qquad (6)$$

where, v_0 is the velocity with which the particle is moving, τ_r is the timescale associated with the rotational motion of the particle, D is the diffusion coefficient and Δt is the elapsed time. This MSD expression corresponds to Hot Brownian Motion (HBM) [16, 24] and comprises a normal translational diffusion term with an extra term giving the rotational diffusion.

When Δt is much smaller than τ_r , the Equation (6) reduces to

$$<\Delta r^2(\Delta t)>=4D\Delta t+v_0^2(\Delta t)^2\tag{7}$$

In order to calibrate the motion of the UCNP particle, we can use the PSD of the motion of the particle in the axial direction. The fit to the PSD is a lorentzian of the form (Equation 8).

$$PSD = \frac{A}{\omega^2 + B} \tag{8}$$

The calibration factor can then be ascertained using the expression [25].

$$\beta = \sqrt{\left(\frac{k_B T}{\gamma A}\right)} \tag{9}$$

Here, γ is the drag coefficient for an oblate spheroid, T is the ambient room temperature and k_B is the Boltzmann constant. The drag coefficient is assumed for that of an oblate spheroid, given as [26],

$$\gamma = \frac{8}{6} \gamma_0 e^3 [e(1-e^2)^{(1/2)} - (1-2e^2) sin^{-1}(e)]^{-1}$$
(10)

For a typical UCNP which has a 5 μ m major axis and 1 μ m minor axis, the e = 0.2. Then the drag coefficient become $\gamma = \frac{2}{3} \gamma_0$. Here γ_0 is the drag coefficient of a sphere with the same radius as the semimajor axis as the spheroid, for the particle placed away from any other surfaces in water.

4. RESULTS AND DISCUSSIONS

The UCNP used in this experiment is the hexagonal one which has an absorption resonance at 975 nm and emits in red and green bands [27]. The scanning electron microscopy image for the particles is shown in **Figure 2A**. The particles are hexagonal in shape with diagonals about 5 μ m and a thickness of about 1 μ m. The **Figure 2B** represents the Power Spectral Density (PSD) for such a hexagonal shaped particle trapped using optical tweezers. The particle tends to align side on preferentially [28] and the motion along the axial direction

Kumar et al.



is recorded using the QPD in the forward scattered direction. The PSD is for a laser power of 20 mW and fits well to a Lorentzian in the high frequency limit. However, at lower frequencies, there is a deviation from the Lorentzian which may indicate the HBM characteristics. The local temperature of the UCNP surface can be probed with the spectrum of emission [29]. The spatial distribution of the particles are reported in **Figure 2C**.

Optical trapping of such individual particles is routinely performed and can easily be visualized in a 100x objective. We have shown one such trapped particle in **Figure 1** with the visible glow when the trapping is performed at 975 nm.

Using the lorentzian parameters, we get $\beta = 20 \text{ nm/V}$.

We go on to carefully study the MSD characteristics of the axial motion and find that the conventional Fluctuation-Dissipation theorem holds good to yield a exponent of 1 for the relation between MSD and lag time, as indicated by the green curve in **Figure 3**, which is taken at a trapping wavelength of 1064 nm. However, as soon as the trapping wavelength is changed to 975 nm, there are major variations from the exponent of 1. Here, a fit of the form Equation (6) fits better, thereby indicating HBM.

We go on to plot the histograms for the time series at three different 975 nm laser powers of 20, 40, and 50 mW, shown in **Figure 4**, and find a gradual skewing of the histogram to one side. This indicates that the particle is getting pushed axially and spends more time on the far side than the near side. The effect is more pronounced at higher powers. The histograms have been calibrated for the different powers of the laser and normalized to have the total area under the curve as 1.



FIGURE 4 [I his figure represents the calibrated and normalized histogram for the time series data for axial motion of a hexagonal UCNP trapped with 975 nm light at three different powers, namely, 20 mW (pink), 40 mW (red), and 50 mW (blue). Here, the negative side is the far side in the axial direction for the laser injected from the bottom.



We can also note that the maximum probability of the peak of the distribution becomes higher at higher values of power due to increased trap stiffness.

We also calibrate the MSD for a particle trapped at 20 mW laser power at 975 nm and find the curve in **Figure 5**, fitted to



Equation (6). The relaxation time and velocity calculated from the fit parameters are 2.76 s and 36 nm/s, respectively.

The corresponding drag force encountered by the 5 μ m diameter hexagonal shaped UCNP particle moving with an effective velocity of 36 nm/s is about 1 fN, which can be easily compensated by the optical tweezers.

In order to confirm heating effects, we place such a particle on the side edge of an air-water interface. When the 975 nm light is illuminated on the edge, there i.e., no effect, as reported in **Figure 6a**. However as soon as the particle is illuminated with 975 nm light, there is water vapor bubble formation on the interface, shown in **Figure 6b**. That confirms local heating due to the particle. This is also the proof that heating is performed when the particle is illuminated by 975 nm light, and not directly by absorption of the laser by water. Thus trapping of the particle at other wavelengths like 800 nm is not required. Thermometry

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using the spectrum emitted by the particle has been proven to be problematic [30], and thus has not been used.

Further, the confirmation of directional heating required a more imaginative configuration where the 975 laser was inserted just in front of QPD (reported in **Figure 1**), to propagate in the backward direction. When the light was illuminated on a cluster of UCNP placed on the surface, there was no visible glow, shown in **Figure 6c**. This indicates that very little visible light is radiated in the forward scattered direction. Nonetheless, the accessibility of the forward scattered light in our configuration is harder as the camera is located in the backscattered direction while the condenser is just 10 X and will lose much of the light in the forward scattered direction.

5. CONCLUSIONS

Thus, we describe a new kind of active motion where the particle is trapped in optical tweezers while exhibiting what we believe is HBM, simultaneously. An UCNP trapped optically at the absorption resonance absorbs more light at the near end from the trapping light while also emitting preferentially in the backscattered direction. This generates a higher temperature at the near end than the far end, thereby creating a temperature differential that leads to the HBM. The MSD of the axial motion bears signature of the HBM. A typical velocity due to the HBM was found to be 36 nm/s with a force exerted of 1 fN which can be easily compensated by optical tweezers. Such a system can be used to study controlled interactions of active particles while confined in optical tweezers.

DATA AVAILABILITY STATEMENT

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

AUTHOR CONTRIBUTIONS

This project was designed by BR and JS while the UCNP particles were made by MG and JS. The experiments performed by AK, RV, and SK. The theory was done by DC. The manuscript was written by BR, AK, and SK.

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Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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