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# Development of soil type-independent calibration relationships for water content and dry density measurements using time-domain reflectometry

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Soil water content and dry density are critical parameters for assessing loess collapsibility and other geotechnical applications. However, existing time-domain reflectometry (TDR) calibration methods are often constrained by soil-specific limitations. This study aimed to develop soil type-independent calibration relationships for TDR measurements of soil water content and dry density. Laboratory experiments were conducted on four distinct soil types to calibrate and validate the existing TDR models. The results indicated that the current models exhibited suboptimal performance, necessitating parameter calibration for specific soil types. To enhance the accuracy and applicability of TDR measurements, the multi-expression programming (MEP) algorithm was employed to develop a soil type-independent calibration relationship for dry density. The MEP model demonstrated robust performance in both training and validation phases, achieving a slope of 0.925 and an  $R^2$  value of 0.88 for the training dataset, with most validation data points falling within a  $\pm 10\%$  relative error range. Additionally, a soil type-independent calibration relationship for water content was established based on the dry density model, achieving high accuracy, with most predicted values exhibiting absolute errors within  $\pm 0.04$ . The developed calibration relationships were further validated using 64 datasets from the literature, covering various soil types, and through two field *in situ* tests. The validation results demonstrated that the developed model could accurately determine dry density, with relative errors of less than  $\pm 10\%$  for most test points. Water content measurements also showed strong agreement with laboratory oven-drying results, with absolute errors within  $\pm 0.02$  for the majority of test points. This work provides a reference for applying TDR to rapid *in situ* measurement of soil water content and dry density, which is of significant importance for evaluating loess collapsibility and other geotechnical applications.

## KEYWORDS

time-domain reflectometry, soil type-independent calibration relationships, soil gravimetric water content, dry density, machine learning

# 1 Introduction

Loess is distributed worldwide, particularly in northwestern China, where it covers an area of 640,000 km<sup>2</sup> (Li, 2018; Jia et al., 2020; Ji et al., 2021). It is well-known that many geotechnical problems, such as ground subsidence (Rogers et al., 1994; Muñoz-Castelblanco et al., 2011; Zhang et al., 2022) and slope failure (Peng et al., 2018; Wang et al., 2018), occur in loess areas due to wetting-induced collapse. Therefore, evaluating the collapsibility of loess prior to construction is essential. However, the unique structure of loess inevitably becomes disturbed during field sampling and subsequent laboratory testing, which compromises the accuracy of the collapsibility assessments (Atkinson et al., 1992; Mu Q. et al., 2020; Wu et al., 2025). Furthermore, evaluating large-scale or deep loess sites requires extensive drilling and the collection of numerous samples for laboratory analysis, which makes it expensive. In the laboratory experiments, conventional compression tests at constant water content require 24 h of equilibrium at each loading increment, whereas suction-controlled compression tests of unsaturated soil need several days (Ng and Pang, 2000; Mu et al., 2020a; Mu et al., 2023 Q.; 2023c), rendering the evaluation of numerous samples extremely time-consuming. Given these limitations of the existing methods, there is an urgent need to develop novel techniques for the *in situ* evaluation of loess collapsibility.

Implementing *in situ* collapsibility evaluation for loess involves establishing an evaluation model that comprehensively considers the main influencing factors and conducting *in situ* testing to obtain the model parameters. Regarding the evaluation models, Holtz and Hillf (1961) proposed a model based on the void ratio at the liquid limit state and the natural void ratio, successfully evaluating the collapse in various unsaturated soil types. Based on Holtz and Hillf (1961), Gibbs and Bara (1962) utilized the dry density at the liquid limit state and the liquid limit to define a collapse criterion line, effectively assessing collapsibility in loess from a US canal and channel site. Basma and Member (1992) investigated the effects of physical properties, such as dry density, water content, and overburden load, on wetting-induced collapse and subsequently developed an empirical model using multiple regression analysis. Lim and Miller (2004) proposed a new empirical model based on the study by Basma and Member (1992), which was found to have good predictive performance in *in situ* tests. Wang L. et al. (2020) established an exponential equation to simulate the one-dimensional compression behavior of loess under different moisture conditions. Mu et al. (2023b) developed a new and simple method for predicting loading- and wetting-induced collapse of intact loess within an elastoplastic framework. In conclusion, the current models are mainly related to soil dry density and water content, which are consistent with the results of a large number of geotechnical tests based on the theory of unsaturated soil mechanics (Ng et al., 2024). Consequently, the precise and expeditious measurement of soil water content and dry density is imperative for evaluating the collapse susceptibility of *in situ* sites.

Time-domain reflectometry (TDR) is a geophysical technique widely utilized in geological exploration and soil analysis, enabling the measurement of soil apparent permittivity and electrical conductivities. Since its initial application for measuring water content by Topp et al. (1980), TDR has been extensively studied

and applied within the field of geotechnical engineering (Lin et al., 2006; Zhang et al., 2017; Mu et al., 2019; 2020b; 2023b; Bittelli et al., 2021). For instance, Siddiqui et al. (2000) proposed a two-step method to establish a correlation between the apparent dielectric constant and soil parameters such as dry density and water content. This method requires separate testing of the two soil samples on-site, which may introduce errors due to inconsistencies in the state of the two soil samples. Yu and Drnevich (2004) further enhanced the two-step method by incorporating soil electrical conductivity, developing a relationship between water content and conductivity, and introducing a correction equation to account for differences in water conductivity between *in situ* and laboratory conditions. Jung et al. (2013) introduced a new TDR measurement parameter,  $V_1$ , which is termed the first voltage drop, and proposed a novel approach using TDR to directly calculate dry density, followed by water content determination through a normalized apparent permittivity equation, which was validated across various soil types. Curioni et al. (2018) improved the model proposed by Jung et al. (2013), which enhanced precision and accuracy while being less susceptible to multiplexer influence. Bhuyan et al. (2020) developed a model utilizing soil apparent permittivity and electrical conductivity to compute wet density and water content, which is applied for *in situ* detection of subgrade compaction. These studies further emphasize the significant potential of TDR technology for measuring soil dry density and water content. However, the existing calibration relationships are typically limited to specific soil types, requiring different sets of calibration parameters for different soil types.

In Northwest China, the wide variety of soil types (e.g., sandy, silty, and clayey loess) exhibits substantial differences in physical properties. Consequently, it is challenging to use a single set of TDR parameters for rapid *in situ* measurement of dry density and water content across different types of soil. The objectives of this study are to (1) prepare and test four distinct types of soil at different gravimetric water contents and dry densities in the laboratory to calibrate and validate the existing TDR theoretical models; (2) employ machine learning to develop a soil type-independent calibration relationship for water content and dry density; and (3) validate the applicability of the proposed model using two field *in situ* tests. This study innovatively develops a soil type-independent calibration relationship based on the multi-expression programming (MEP) algorithm, eliminating the need for soil-specific calibration parameters. This advancement significantly enhances the applicability of TDR technology for rapid *in situ* measurements across diverse soil types, thereby providing a more efficient and accurate method for assessing soil properties in geotechnical applications.

## 2 Existing calibration relationship for measuring $\rho_d$ and $w$

The one-step TDR method provides a procedure for the *in situ* measurement of soil water content ( $w$ , %) and dry density ( $\rho_d$ , g/cm<sup>3</sup>) using TDR, based on the calibration parameters of a specific soil type obtained from laboratory TDR tests. This method utilizes the apparent permittivity constant ( $\epsilon$ ) and the bulk electrical conductivity ( $EC_b$ , S/m) of the soil to predict  $w$  and  $\rho_d$ . For a

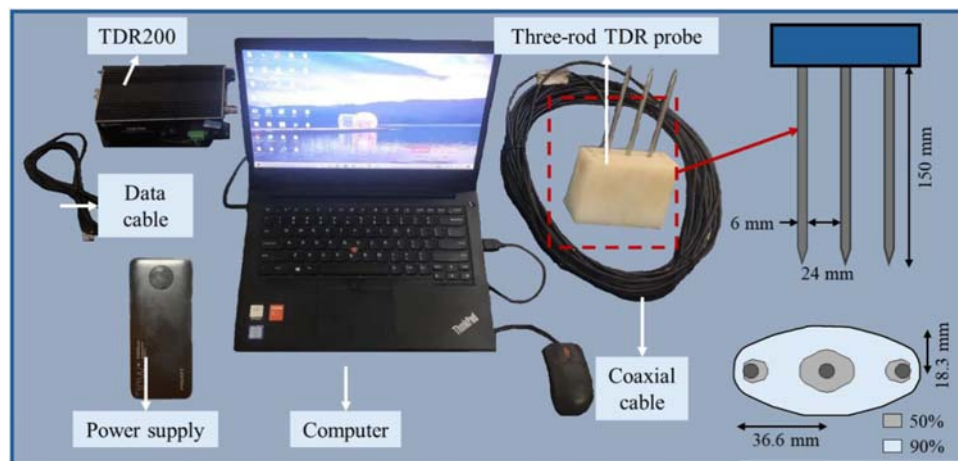


FIGURE 1  
Illustration of the TDR *in situ* measurement.

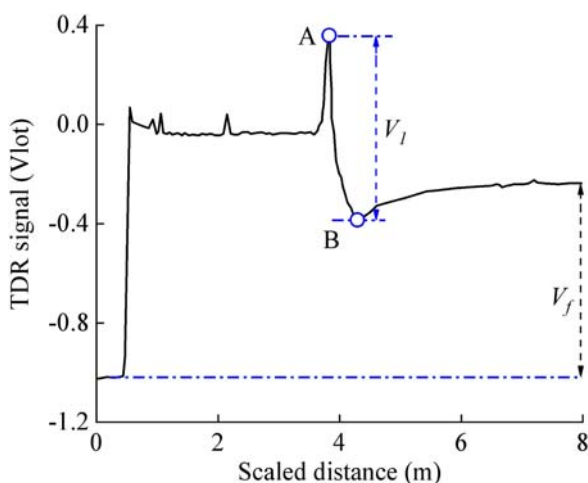


FIGURE 2  
Illustration of a typical TDR waveform.

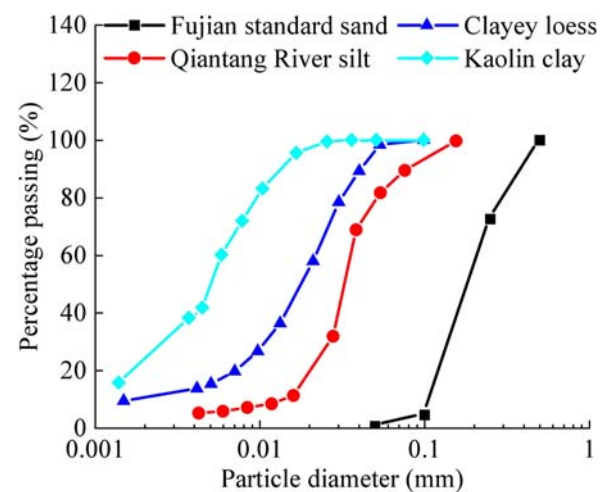


FIGURE 3  
Particle size distributions of the tested soil types.

given probe configuration,  $EC_b$  can be derived from the measured waveform reflection and the characteristic impedance of the cable (Giese and Tiemann, 1975; Dalton et al., 1984; Nadler et al., 1991). Therefore, Yu and Drnevich (2004) proposed relationships between  $\epsilon$ ,  $EC_b$ ,  $\rho_d$ , and  $w$ , as illustrated in Equations 1–3:

$$\sqrt{\epsilon} \frac{\rho_w}{\rho_d} = a + bw, \quad (1)$$

$$\sqrt{EC_b} \frac{\rho_w}{\rho_d} = c + dw, \quad (2)$$

$$\sqrt{EC_{b,adj}} = f + g\sqrt{\epsilon}, \quad (3)$$

where  $a, b, c, d, f$ , and  $g$  are the soil-specific calibration coefficients that are determined from the laboratory calibration tests. The parameter  $\rho_w$  represents water density, and  $EC_{b,adj}$  represents

adjusted bulk electrical conductivity. The model proposed by Yu and Drnevich (2004) demonstrated satisfactory results across various soil types. However, the application of this method may be limited to a narrower range of water content due to inadequate modeling of the relationship between density-normalized  $EC_b$  and  $w$ . Furthermore, the method exhibits sensitivity to variations in compaction energy, which constrains its accuracy in the field. Subsequently, Jung et al. (2013) introduced a new TDR measurement parameter, termed the first voltage drop ( $V_1$ , V). Utilizing  $V_1$  together with the final voltage ( $V_f$ , V) measured by TDR, they established an independent relationship relating the voltage- and density-normalized terms to the TDR-measured  $K_a$ , as expressed in Equation 4:

$$\frac{V_1}{V_f} \frac{\rho_w}{\rho_d} = c_1 + d_1(\epsilon - 1) - c_1 \exp[-f_1(\epsilon - 1)]. \quad (4)$$

TABLE 1 Physical properties of the tested soil types.

Soil parameter	Fujian standard sand	Qiantang River silt	Clayey loess	Kaolin clay
Specific gravity	2.67	2.69	2.67	2.65
Plastic limit (%)	—	23.2	17.4	33.5
Liquid limit (%)	—	31.8	31.8	70.3
Particle-size distribution (ASTM D422-63, 2007)	—	—	—	—
Sand (%)	97.2	10.5	0.8	0
Silt (%)	2.8	82.4	84.2	51.8
Clay (%)	0	7.1	15	48.2
Unified soil classification (ASTM D2487-11, 2011)	SP	ML	CL	CH

The calibration parameters  $c_1$ ,  $d_1$ , and  $f_1$  are obtained through laboratory tests. The soil dry density  $\rho_d$  can be calculated according to Equation 4. This value is then combined with the calibration parameters  $a$  and  $b$  to determine  $w$  in Equation 1. However, the method proposed by Jung et al. was tested only with a specially developed probe (MRP). In some tests, the results obtained using commercially available three-rod TDR probes indicated that the outcomes provided by the method proposed by Jung et al. (2013) were not entirely consistent and were affected by the addition of the multiplexer. Therefore, Curioni et al. (2018) proposed an improved relationship to replace the calibration relationship for dry density. This modification enhanced the precision and accuracy while being less susceptible to multiplexer influence, as shown in Equation 5:

$$\frac{V_1}{V_f} \frac{\rho_w}{\rho_d} = c_2 + d_2 (V_1 \sqrt{\varepsilon})^{f_2}. \quad (5)$$

Equation 5 also contains three calibration parameters ( $c_2$ ,  $d_2$ , and  $f_2$ ). As stated before, using the calibrated parameters  $c_2$ ,  $d_2$ , and  $f_2$ ,  $\rho_d$  can be calculated, and together with the parameters  $a$  and  $b$  in Equation 1,  $w$  can be determined. Curioni et al. (2018) experimentally confirmed the accuracy of  $\pm 5\%$  for the dry density and  $\pm 2\%$  for the water content.

In summary, the existing calibration relationships exhibit a reasonable capacity for predicting soil dry density and water content. However, in practical applications, the soil physical properties can vary significantly, which, in turn, may influence their electrical properties. As demonstrated by Jung et al. (2013), the parameters  $a, b, c, d, f$ , and  $g$  need to be calibrated separately for different types of soil during the laboratory validation of their TDR model. As a result, it becomes challenging to accurately calculate  $\rho_d$  and  $w$  for different soil types using a single set of parameters. This limitation may potentially undermine the advantage of TDR in enabling rapid *in situ* measurement of  $w$  and  $\rho_d$ . Therefore, a soil type-independent calibration relationship needs to be developed to provide a reference for applying TDR to the rapid *in situ* measurement of  $\rho_d$  and  $w$ .

### 3 Test apparatus and TDR waveform processing

As illustrated in Figure 1, the Campbell Scientific TDR200, in conjunction with a three-rod TDR probe, was used to measure the reflection waveforms of soil specimens. The TDR200 was connected to an electric source with a constant voltage of 12 V for the power supply. The three-rod TDR probe consists of three stainless steel rods with a diameter of 6 mm and a length of 150 mm. The distance between two neighboring rods (center to center) is 30 mm. Based on the numerical method proposed by Zhan et al. (2014), Zhan et al. (2015), the sampling area of the three-rod TDR probe is approximately characterized as an ellipse with a major axis of 36.6 mm and a minor axis of 18.3 mm. Furthermore, the blue area in the figure indicates 90% measurement sensitivity, corresponding to an ellipse with a short semi-axis of 18.3 mm and a long semi-axis of 36.6 mm, with an area of approximately 2,141 mm<sup>2</sup>. This area is larger than the representative unit of the soil under test. A coaxial cable with an impedance of 50  $\Omega$  was used to connect the three-rod TDR probe to the TDR200. In addition, a plastic cylinder with a diameter of 150 mm and a height of 200 mm was used to house the soil specimen, where the three-rod probe is inserted. Based on the numerical calculation result, the volume of the plastic cylinder is sufficient to cover the sampling area of the three-rod probe.

During measurement, the TDR200 sends a step voltage pulse (i.e., 1 V) that travels along the coaxial cable and the three-rod TDR probe. The reflections of the step voltage pulse occur at the sections of impedance mismatch and are recorded by the TDR200. A typical TDR waveform is illustrated in Figure 2. The points A and B in the TDR waveform are associated with the first reflections of the step voltage pulse at the surface of the soil specimen and at the end of the three-rod TDR probe, respectively. The TDR waveform beyond point B represents the subsequent multiple reflections of the step voltage pulse in the three-rod TDR probe. Based on previous studies, apparent permittivity ( $\varepsilon$ ) can be calculated based on the time difference ( $\Delta t$ ) between points A and B as follows (Equation 6):

$$\varepsilon = \sqrt{c\Delta t/2L}, \quad (6)$$

TABLE 2 Properties of the soil types used for TDR calibration and validation in this study.

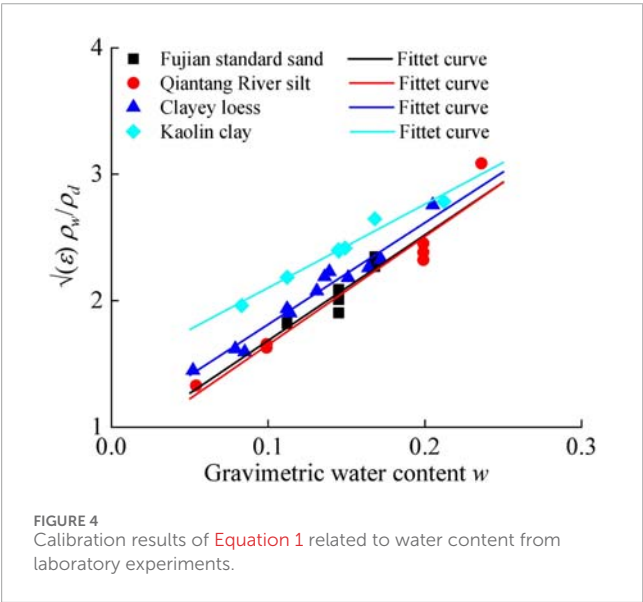
Soil type	$\rho_d$	$w$	$V_1$	$V_f$	$\varepsilon$	$\rho_d$	$w$	$V_1$	$V_f$	$\varepsilon$
	Group I: calibration					Group II: validation				
Fujian standard sand	1.50	11.20	0.04	1.73	7.44	1.50	14.50	0.09	1.68	9.98
	1.50	16.80	0.12	1.64	12.39	1.50	25.60	0.19	1.47	20.39
	1.55	11.20	0.06	1.72	8.04	1.55	7.90	0.02	1.76	5.68
	1.55	14.50	0.10	1.68	10.49	1.55	21.30	0.17	1.57	16.95
	1.55	16.80	0.13	1.64	12.37	1.60	11.20	0.06	1.72	8.01
	1.60	14.50	0.10	1.68	10.32	1.60	16.80	0.14	1.62	13.14
	1.65	14.50	0.11	1.66	9.86	1.65	11.20	0.06	1.70	7.85
	—	—	—	—	—	1.65	16.80	0.15	1.60	13.07
Qiantang River silt	1.30	9.90	0.06	1.50	4.48	1.30	15.00	0.13	1.37	8.96
	1.30	19.90	0.15	1.32	10.17	1.40	9.90	0.08	1.46	5.92
	1.40	5.40	0.02	1.64	3.46	1.40	15.00	0.14	1.33	7.84
	1.40	23.60	0.25	1.12	18.67	1.40	19.90	0.17	1.30	11.28
	1.50	9.90	0.09	1.44	6.17	1.50	5.40	0.02	1.65	3.50
	1.50	19.90	0.19	1.23	12.14	1.50	15.00	0.16	1.27	9.18
	1.60	19.90	0.21	1.20	14.54	1.50	23.60	0.27	1.03	20.06
Clayey loess	1.30	11.20	0.06	1.58	6.33	1.30	13.90	0.07	1.58	7.28
	1.30	15.10	0.09	1.55	8.05	1.35	5.00	0.02	1.72	3.55
	1.35	7.90	0.04	1.66	4.78	1.35	11.20	0.08	1.55	6.64
	1.35	13.90	0.11	1.50	9.05	1.35	17.00	0.14	1.46	10.85
	1.40	5.20	0.03	1.65	4.11	1.40	8.50	0.06	1.59	5.68
	1.40	11.40	0.08	1.56	7.10	1.40	13.90	0.12	1.46	8.41
	1.40	17.20	0.15	1.41	10.61	1.40	20.10	0.23	1.24	15.84
	1.40	32.20	0.28	1.19	24.89	1.45	11.20	0.11	1.49	7.83
	1.45	13.60	0.14	1.44	10.08	1.45	16.70	0.17	1.41	12.17
	1.50	8.50	0.07	1.54	5.72	1.50	11.40	0.11	1.46	7.89
	1.55	16.40	0.18	1.34	12.26	1.55	20.20	0.23	1.24	18.60
	1.60	13.10	0.18	1.28	11.04	1.60	16.90	0.21	1.24	13.15
	1.60	20.50	0.26	1.14	19.47	—	—	—	—	—

(Continued on the following page)

TABLE 2 (Continued) Properties of the soil types used for TDR calibration and validation in this study.

Soil type	$\rho_d$	$w$	$V_1$	$V_f$	$\varepsilon$	$\rho_d$	$w$	$V_1$	$V_f$	$\varepsilon$
	Group I: calibration					Group II: validation				
Kaolin clay	0.80	14.50	0.02	1.74	3.66	0.80	16.80	0.03	1.72	4.89
	0.90	11.20	0.02	1.73	3.87	0.90	14.50	0.03	1.71	4.48
	0.90	16.80	0.03	1.70	5.68	1.00	12.00	0.04	1.68	4.86
	1.00	8.30	0.02	1.73	3.85	1.00	17.70	0.07	1.64	6.41
	1.00	14.90	0.06	1.65	5.84	1.10	11.20	0.07	1.61	5.71
	1.00	21.20	0.09	1.61	7.76	1.10	16.80	0.10	1.57	7.91
	1.10	14.50	0.09	1.57	6.99	—	—	—	—	—

Note:  $\rho_d$ , dry density (g/cm<sup>3</sup>);  $w$ , gravimetric water content (%);  $V_1$ , first voltage drop (V);  $V_f$ , final steady voltage (V);  $\varepsilon$ , apparent permittivity.



where  $c$  is the velocity of the electromagnetic wave in free space (i.e.,  $3 \times 10^8$  m/s),  $L$  is the probe length of the three-rod TDR probe, which is calibrated based on the method described by [Zhan et al. \(2013\)](#). On the other hand, the first voltage drop ( $V_1$ ) and final voltage ( $V_f$ ) represent the voltage difference between points A and B and the voltage of the step voltage pulse after multiple reflections, respectively. These two parameters are related to the electrical conductivity of the tested specimen.

## 4 Test material and specimen preparation

### 4.1 Test material

To develop the soil type-independent relationship, four soil types (i.e., Fujian standard sand, Qiantang River silt, clayey loess,

and kaolin clay) are used for TDR measurements. The particle size distribution curves and physical properties of the tested soil samples are shown in [Figure 3](#) and [Table 1](#), respectively. The chosen soil types represent a broad range of particle size distributions and index properties present in engineering practices. The four selected soil types have a clay content ranging from 0 to 48.2%, a silt content ranging from 2.8% to 84.2%, and a sand content ranging from 0 to 97.2%. On the other hand, the plastic limits and liquid limits range from 17.4% to 35.5% and from 31.8% to 70.3%, respectively. According to [ASTM D2487-11 \(2011\)](#), the Fujian standard sand, Qiantang River silt, clayey loess, and kaolin clay are classified as SP, ML, CL, and CH, respectively. More details regarding the physical properties of the tested soil types are provided in previous studies ([Mu Q. et al., 2023](#); [Mu Q. et al., 2023c](#)).

### 4.2 Specimen preparation

The soil samples are first oven-dried and mixed with water to generate various moisture contents using a plant mister. The prepared wet soils are wrapped in cling film and allowed to equilibrate for 48 h. After moisture equalization, the soil samples are compacted into plastic cylinders with a diameter of 100 mm and a height of 150 mm. The compaction of each specimen was divided into five layers (i.e., 30 mm height for each layer). The top surface of each layer was scarified before the compaction of the subsequent layer to ensure better contact. After compaction, the specimen was left for 24 h to allow the equilibration of pore water across the specimen prior to the TDR measurement. For Fujian standard sand, the compaction dry densities ranged from 1.50 g/cm<sup>3</sup> to 1.65 g/cm<sup>3</sup> in steps of 0.05 g/cm<sup>3</sup>. The compaction dry densities of Qiantang River silt and clayey loess ranged from 1.30 g/cm<sup>3</sup> to 1.60 g/cm<sup>3</sup>, while the kaolin clay had dry densities ranging from 0.80 g/cm<sup>3</sup> to 1.10 g/cm<sup>3</sup>, both in steps of 0.1 g/cm<sup>3</sup>. The soil specimens prepared above were uniformly divided into two groups; group I was used for calibration and training of the machine learning model, and group II was used for

TABLE 3 Summary of the calibration coefficients.

Soli type	<i>a</i>	<i>b</i>	<i>c</i> <sub>1</sub>	<i>d</i> <sub>1</sub>	<i>f</i> <sub>1</sub>	<i>c</i> <sub>2</sub>	<i>d</i> <sub>2</sub>	<i>f</i> <sub>2</sub>
Fujian standard sand	0.85	8.36	−0.024	0.007	0.241	0.004	0.103	0.970
Qiantang River silt	0.80	8.56	−0.001	0.009	0.303	−3.9e-4	0.144	0.788
Clayey loess	1.01	8.05	−0.003	0.008	0.192	−0.002	0.131	0.767
Kaolin clay	1.44	6.61	−0.012	0.012	7.8E-07	2.5e-4	0.169	0.815

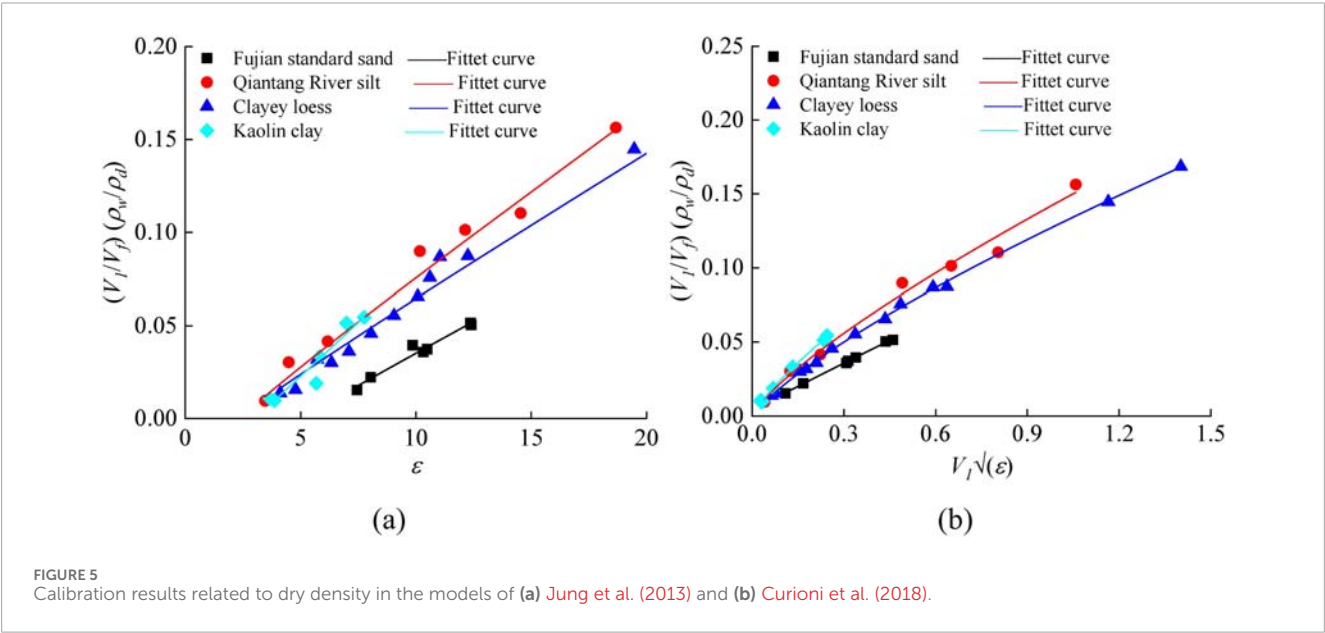


TABLE 4 Optimized MEP parameters.

Genetic operator	Value
Size of the subpopulation	3,000
Number of subpopulations	2
Number of generations	2,000
Length of the code	30
Probability of crossover	0.9
Type of crossover	Uniform
Probability of mutation	0.01
Function set	+, −, ×, ÷, sqrt
Function probability	0.3
Variable probability	0.3
Constant probability	0.4

validation of both the existing model and the developed machine learning model.

Note that the compaction of the soil samples with high water contents is unrealistic to achieve the predefined dry densities mentioned above. To prepare the specimens with high water contents, the relatively dry soil samples were first compacted into plastic cylinders to the predefined dry densities. With the known water content, the volume of the plastic cylinder, and the dry density, the required amount of water was calculated and sprayed into the plastic cylinder to achieve the predefined high water contents. Similar to the specimens with low water contents, the prepared specimens with high water contents were also left for pore water equilibration. Based on the targeted water contents, the specimens with high water contents need 3–10 days for pore water equilibration. To check the uniformity of the prepared specimens, three sub-specimens from the top, middle, and bottom parts of the prepared specimens were collected. The results show that the differences in dry density and water content are less than  $\pm 0.07 \text{ g/cm}^3$  and  $\pm 0.1\%$ , respectively. More details of the soil physical properties of the prepared specimens are provided in Table 2.

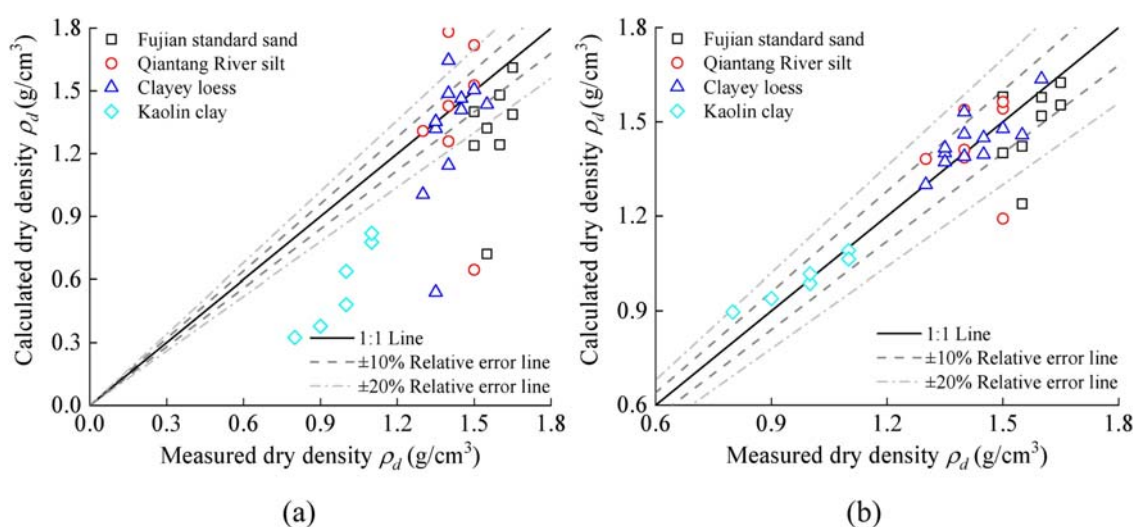


FIGURE 6 Performance in measuring soil dry density using the models proposed by (a) Jung et al. (2013) and (b) Curioni et al. (2018).

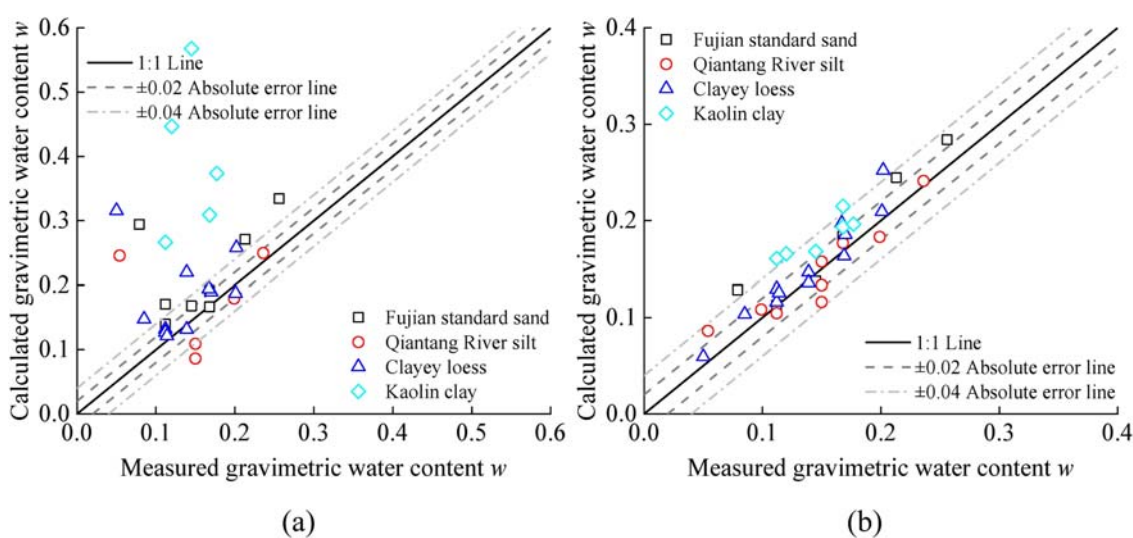


FIGURE 7 Performance in measuring soil water content using the models proposed by (a) Jung et al. (2013) and (b) Curioni et al. (2018).

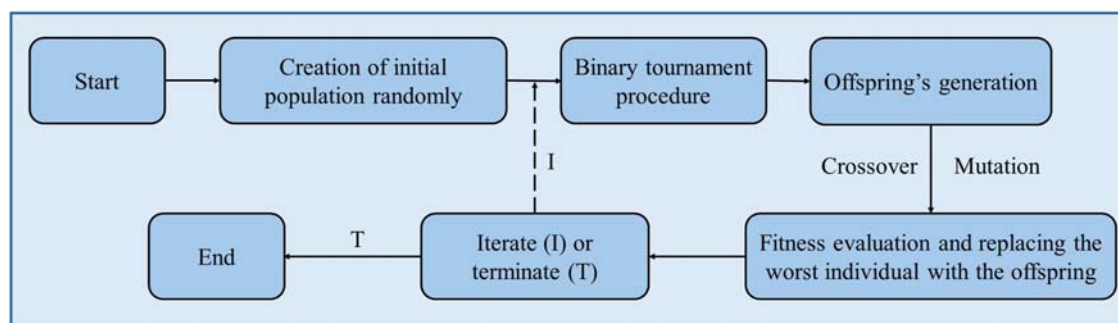


FIGURE 8 Illustration of the computational flow chart of MEP.

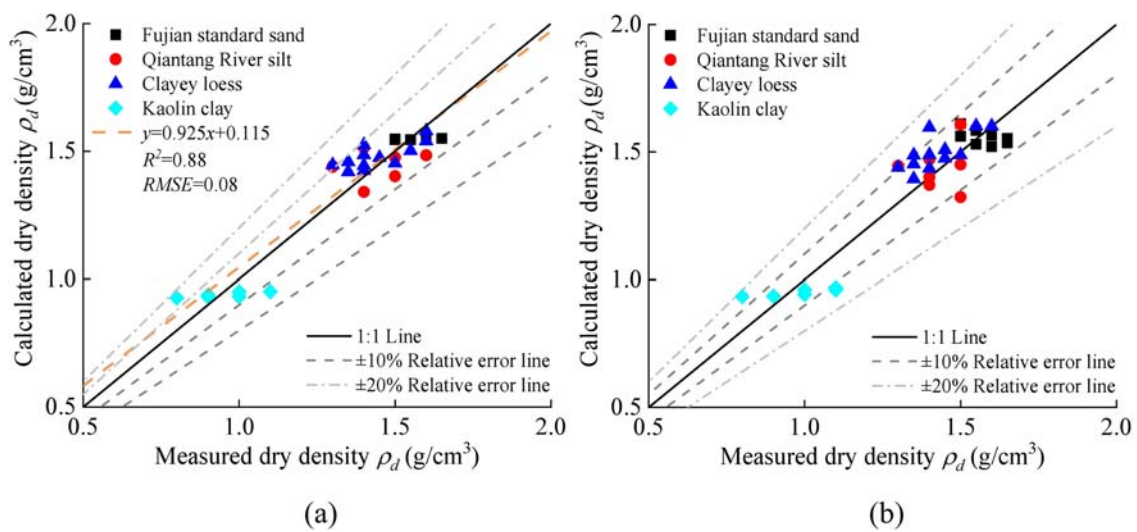


FIGURE 9  
Soil type-independent calibration relationship for dry density based on MEP: (a) model development and (b) model validation.

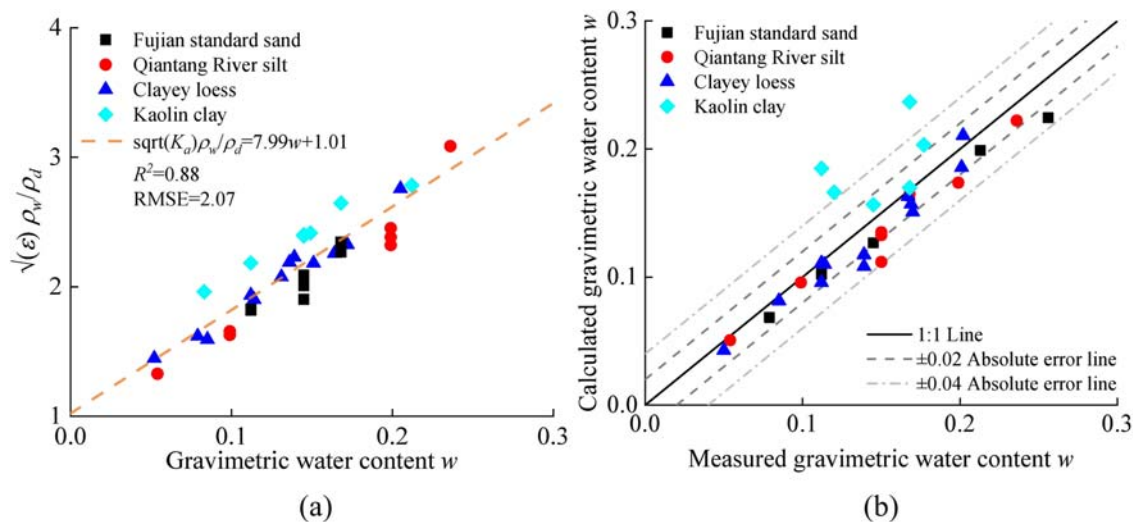


FIGURE 10  
Soil type-independent calibration relationship for gravimetric water content based on Equation 1: (a) parameter calibration and (b) model validation.

## 5 Calibration and calculation of the existing models

In this research, the calibration relationships proposed by Jung et al. (2013) and Curioni et al. (2018) were utilized to assess the dry density and water content of soil, respectively. The calibration of Equation 1 involves two soil constants, which are denoted as  $a$  and  $b$ . The measured parameters, including water content, dry density, and apparent permittivity, were represented in the  $w - \sqrt{\epsilon} \rho_d / \rho_w$  plane, as depicted in Figure 4. Based on Equation 1, a linear regression analysis was carried out and presented in Table 3. It is clear that the coefficient of determination ( $R^2$ ) for Equation 1 exceeds 0.95, indicating a strong correlation between  $w$  and  $\sqrt{\epsilon} \rho_d / \rho_w$  across the four soil types, with values closer to 1 suggesting a better fit.

The calibration of Equation 4, as proposed by Jung et al. (2013), incorporates the three soil parameters  $c_1$ ,  $d_1$ , and  $f_1$ . The TDR test results for the four soil samples, which have varying water contents and dry densities, were computed and plotted in the  $\epsilon - (V_1/V_f)/\rho_d$  plane. A nonlinear fitting was performed using the least-squares method in accordance with the relationship defined in Equation 4, with the calibration results for the soil parameters shown in Figure 5a and Table 4. The  $R^2$  values obtained from the calibration of Equation 4 during the laboratory experiments are greater than 0.94, indicating a robust correlation among dry density, apparent permittivity, and voltage drop.

Additionally, the calibration of Equation 5 for dry density, as proposed by Curioni et al. (2018), also includes three parameters ( $c_2$ ,  $d_2$ , and  $f_2$ ). The measured dry density, apparent

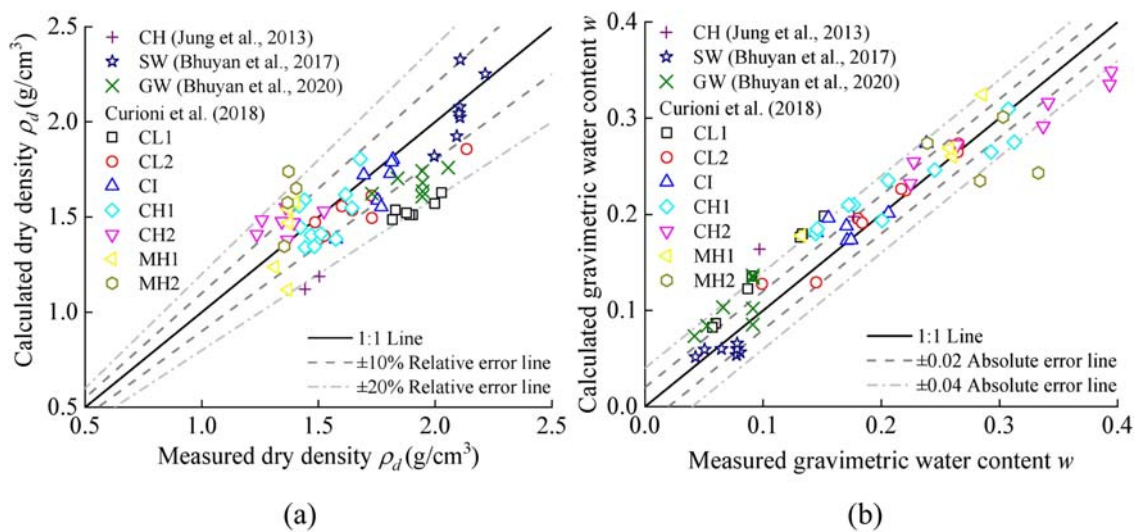


FIGURE 11 Validation of the developed soil type-independent calibration relationships with the data from the literature: (a) dry density; (b) gravimetric water content.

permittivity, and voltage drop of the soil were plotted in the  $V_1 \sqrt{\epsilon} - (V_1/V_f)/\rho_d$  plane, as illustrated in Figure 5b. A subsequent nonlinear fitting was performed based on the relationship outlined in Equation 5, with the fitting results ( $R^2 > 0.99$ ) summarized in Table 3.

Once the parameters  $c_1$ ,  $d_1$ , and  $f_1$  (or  $c_2$ ,  $d_2$ , and  $f_2$ ) have been estimated for a specific soil, the measured values of  $V_1$ ,  $V_f$ , and  $\epsilon$  can be directly utilized to determine the dry density ( $\rho_d$ ) of soil types. At this stage, Equations 4, 5 could be transformed into the following forms:

$$\rho_d = \frac{V_1/V_f}{c_1 + d_1(\epsilon - 1) - c_1 \cdot \exp[-f_1(\epsilon - 1)]} \rho_w, \quad (7)$$

$$\rho_d = \frac{V_1/V_f}{c_2 + d_2(V_1 \sqrt{\epsilon})^{f_2}} \rho_w. \quad (8)$$

Once  $\rho_d$  is obtained from Equations 7, 8, Equation 1 can be solved for the soil gravimetric water content ( $w$ ) (Equation 9) using the TDR-measured  $\epsilon$  and the parameters  $a$  and  $b$  specific to the tested soil.

$$w = \frac{1}{b} \left( \frac{\sqrt{\epsilon}}{\rho_d} - a \right). \quad (9)$$

Figure 6a presents the performance of the models proposed by Jung et al. (2013) in measuring the soil dry density. The results reveal that the dry densities computed using the model proposed by Jung et al. (2013) exhibit suboptimal performance compared to the direct measurements derived from the oven-drying method (ASTM D2216, 2010), with a relative error exceeding  $\pm 20\%$  for 14 out of 33 test points, particularly in the case of kaolin clay. This deviation can be attributed to the model's inability to account for the interference effects of the multiplexer, which distort the test waveforms and consequently affect the precise calculation of electrical properties such as  $V_1$ ,  $V_f$ , and

$\epsilon$ , thereby influencing the estimation of  $\rho_d$ . Conversely, the dry densities predicted by the model proposed by Curioni et al. (2018) demonstrate a higher degree of accuracy, as illustrated in Figure 6b. Among the four soil types that were tested, the majority of the data points exhibited relative errors of less than  $\pm 10\%$ , with only two points exceeding  $\pm 20\%$ , which indicates a strong correlation with the direct measurements obtained through the oven-drying method.

The gravimetric water content of the soil was assessed using Equation 9 combined with the calculated dry densities from Equation 7, as illustrated in Figure 7a. It was found that the gravimetric water content derived from the model proposed by Jung et al. (2013) demonstrated limited agreement with the results obtained from the oven-drying method, exhibiting an absolute error greater than  $\pm 0.04$  at 15 out of the 33 test points. This may be attributed to the requirement of integrating the calculated dry density from Equation 7 into Equation 9 during the calculation of gravimetric water content, which consequently propagates errors from the dry density estimation into the outcomes of gravimetric water content. Figure 7b illustrates a comparison between the gravimetric water content calculated from the model proposed by Curioni et al. (2018) and the results obtained from the oven-drying method. As shown in Figure 7b, with the exception of a few points, most data points fall within an absolute error of  $\pm 0.04$  relative to the results obtained by the drying method. This observation is attributed to the improved accuracy of the dry density calculated using the model proposed by Curioni et al. (2018) (Equation 8). It emphasizes that the application of Equation 9 facilitates a more accurate prediction of gravimetric water content when underpinned by more reliable dry density estimation. Therefore, in the forthcoming development of soil type-independent calibration relationships, the primary emphasis will be on refining the model of dry density while maintaining the existing model of gravimetric water content.

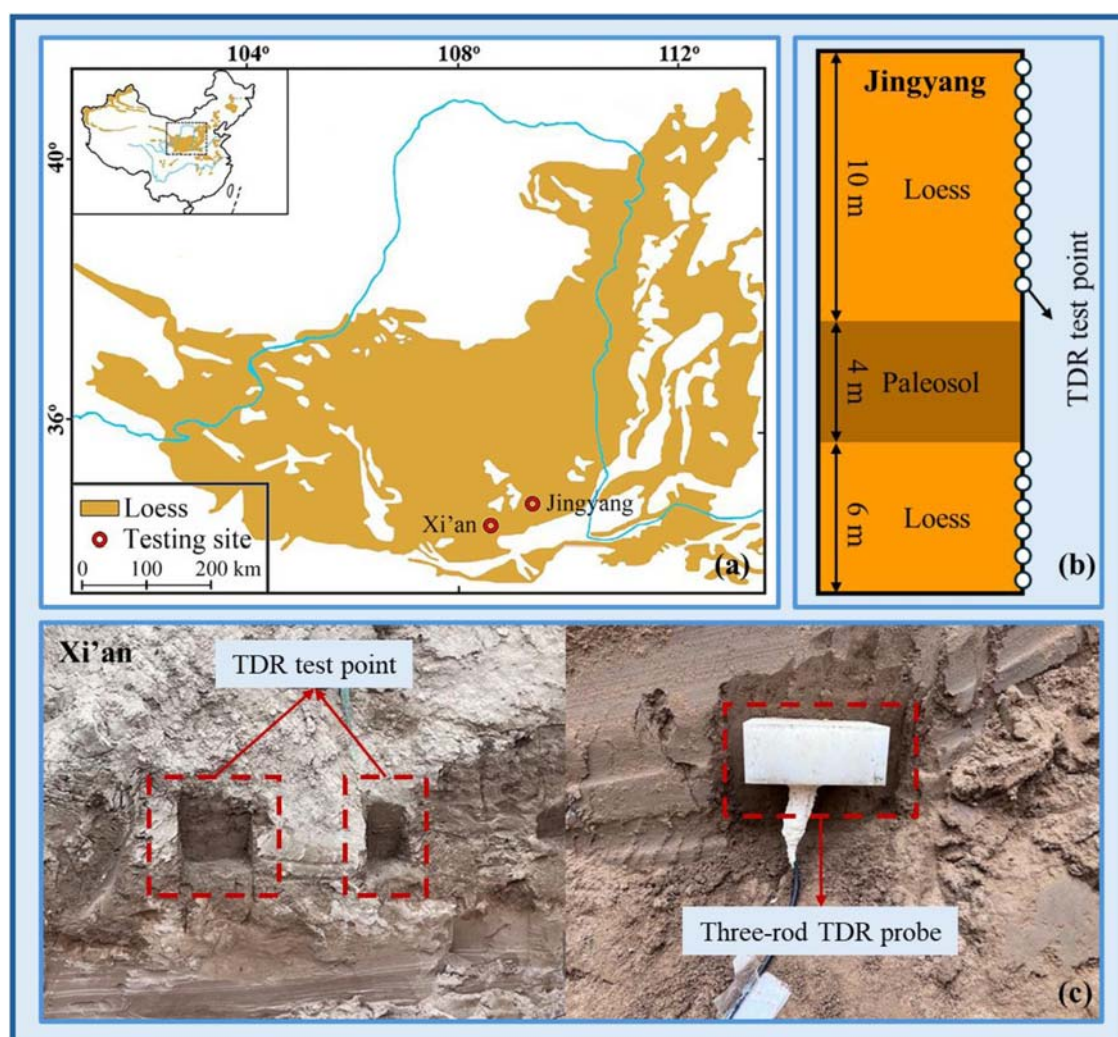


FIGURE 12 Overview of the *in situ* test site: (a) testing site; (b) schematic diagram of the *in situ* test point in Jingyang; (c) *in situ* test in Xi'an.

## 6 Soil type-independent calibration relationships and their verifications

Machine learning methods have an advantage in solving nonlinear mathematical problems with multiple variables and data sources (Yin et al., 2017; Zhang et al., 2021; Qin et al., 2023; Onyelowe et al., 2024; Velastegui et al., 2024; Vatin et al., 2025). MEP, a type of genetic algorithm inspired by genetics and natural selection principles, is a computational technique used for symbolic regression and modeling purposes, and it can generate explicit mathematical expressions (Oltean and Groşan, 2003; Severcan, 2012; Jesswein and Liu, 2022; Rehman et al., 2022). MEP has been effectively applied in diverse fields such as predicting the compressive and tensile strength of concrete (Asif et al., 2024), a shallow foundation's ultimate bearing capacity (Zhang and Xue, 2022), air entry value (Wang H.-L. et al., 2020), soil compaction parameters (Wang and Yin, 2020), and the collapse susceptibility of loess (Mu et al., 2024). Consequently, this study proposes using MEP to establish a calibration relationship for dry

density, given the complex nonlinear relationship between dry density and electrical properties within different soil types.

A dataset comprising 67 data points was constructed based on the physical and electrical properties of four soil types measured by TDR tests and laboratory experiments, as detailed in Section 4. The properties include the first voltage drop ( $V_1$ ), final voltage drop ( $V_f$ ), apparent permittivity ( $\epsilon$ ), plastic limit ( $PL$ ), and clay content ( $Clay$ ). For more details, refer to Tables 2, 3. The first three parameters align with those in the models proposed by Jung et al. (2013) and Curioni et al. (2018), while the latter two represent the difference in soil texture, which significantly impacts the electrical properties of soil types (Bhuyan et al., 2020). Furthermore, this study adopts the form of  $V_1 \sqrt{\epsilon}$  from Curioni's model, resulting in four input variables for the machine learning model, which are  $A = V_f$ ,  $B = V_1 \sqrt{\epsilon}$ ,  $C = PL$ , and  $D = Clay$ . As described in Section 4, data in group I were used for training the machine learning model, and data in group II were reserved for model validation.

This study employed the MEP algorithm as shown in Figure 8. The method randomly creates an initial population using the

TABLE 5 Physical and electrical properties of the *in situ* tested soil types.

Soil parameter	Xi'an loess	Jingyang loess	Xi'an sand
Specific gravity	2.70	2.71	2.64
Plastic limit (%)	18.8	17.4	—
Liquid limit (%)	31.1	31.8	—
Particle-size distribution (ASTM D422-63, 2007)	—	—	—
Sand (%)	43.7	0.8	94.6
Silt (%)	31.5	84.2	5.4
Clay (%)	24.8	15.0	0
Unified soil classification (ASTM D2487-11, 2011)	CL	CL	SP
Gravimetric water content (%)	14.0~19.7	14.6~23.8	4.4~8.9
Dry density (g/cm <sup>3</sup> )	1.51~1.78	1.34~1.43	1.38~1.58
Apparent permittivity	9.83~16.34	6.50~17.38	5.00~8.32
First voltage drop (V <sub>i</sub> )	0.107~1.565	0.005~0.572	0.418~0.331
Final steady voltage (V <sub>f</sub> )	0.376~0.998	1.721~1.789	1.458~1.960

replacement sampling method from the training database. After that, two parents are selected from the initial population using a fitness-based binary tournament, and two offspring are generated from the selected parents through crossover and mutation. Following that, the worst individual is replaced with the superior one identified in the existing population. Finally, the above steps are repeated until the target number of generations is reached (Wang and Yin, 2020; Wang H.-L. et al., 2020; Asif et al., 2024).

The effectiveness of establishing a calibration relationship for dry density using the MEP model largely depends on parameter selection and adjustment (Farooq et al., 2021). Initially, the model was trained on the training dataset and was subsequently evaluated on the testing dataset. Parameters were iteratively adjusted to enhance the model's performance, enabling it to produce results closer to the optimal solution. The process continued until the established fitness function (e.g., *RMSE* or *R*<sup>2</sup>) achieved a state of standstill. Furthermore, the process was repeated with expanded subpopulations, while the model outputs were not accurate. Finally, the result with the lowest *RMSE* and highest *R*<sup>2</sup> was chosen as the optimal solution (Asif et al., 2024). The population size and code length affect the number of programs generated

per chromosome and the length of the resulting mathematical expression. Although larger values may slow convergence, they can yield more accurate results. Table 4 summarizes the optimized parameters for the MEP model.

This study used MEPX software to develop a closed-form mathematical formula for a soil type-independent calibration relationship for dry density, as shown in Equation 10. The parameter settings and basic arithmetic operators are listed in Table 4, and symbols are defined as before.

$$\rho_d = 0.85 \left( 1 + \frac{1}{A} - B + \frac{1}{5} \sqrt{1 + \frac{1}{A} - \frac{1}{10} C - 2BD} \right) - (BD)^2. \quad (10)$$

Figure 9a presents the comparison of the measured and predicted values of the MEP model for dry densities of various soil types during the training phase. It is widely accepted in the literature that an efficient model should exhibit *R*<sup>2</sup> and slope values exceeding 0.8 (Khan et al., 2023). In this study, the MEP model demonstrated a slope of 0.925 and an *R*<sup>2</sup> of 0.88 for the training data, indicating a robust correlation between the predicted and actual values. The data points were found to closely align with the 45-degree lines (1:1), with the majority exhibiting relative errors within ±10%, which is a strong indicator of effective model training (Khan et al., 2021; Nazar et al., 2022). Figure 9b illustrates the model validation of the developed MEP model across different soil types. The findings reveal a close alignment between the predicted and measured values, with most of the 33 validation data points falling within a ±10% relative error, which confirms the performance of the developed soil type-independent calibration relationship for dry density. Overall, the MEP model demonstrated strong performance in both the training and validation phases, showing great potential as a reliable tool for predicting dry density across various soil types.

As discussed in Section 5, the calibration relationship for water content as depicted in Equation 1 could present a good performance when underpinned by more reliable dry density estimation. Thus, a soil type-independent calibration relationship for water content was established using Equation 1. As shown in Figure 10a, the calibration parameters for the four soil types were consistent. The calibrated *a* and *b* values from Equation 1 were 1.01 and 7.99, respectively, with an *R*<sup>2</sup> exceeding 0.88, indicating a good fit. Then, the soil type-independent calibration relationship for water content was developed as follows:

$$w = \frac{1}{7.99} \left( \sqrt{\varepsilon \frac{\rho_w}{\rho_d}} - 1.01 \right). \quad (11)$$

The water content of different soil types was calculated based on the measured electrical properties and Equation 11. Figure 10b shows a comparison of the predicted and measured water content. It reveals that only three of the 33 predicted data points had absolute errors exceeding ±0.04, which highlights the accuracy of the soil type-independent calibration relationship for water content.

Additionally, 64 sets of data from the literature, covering various soil types (CL, CI, CH, MH, SW, and GW), were collected to validate the developed soil type-independent calibration relationships for dry density and water content. Figure 11a shows the comparison between the dry densities calculated from Equation 10 and those obtained from the literature, showing that most data points had relative errors within ±20% of the measured values. This demonstrates the applicability of the calibration relationship for dry

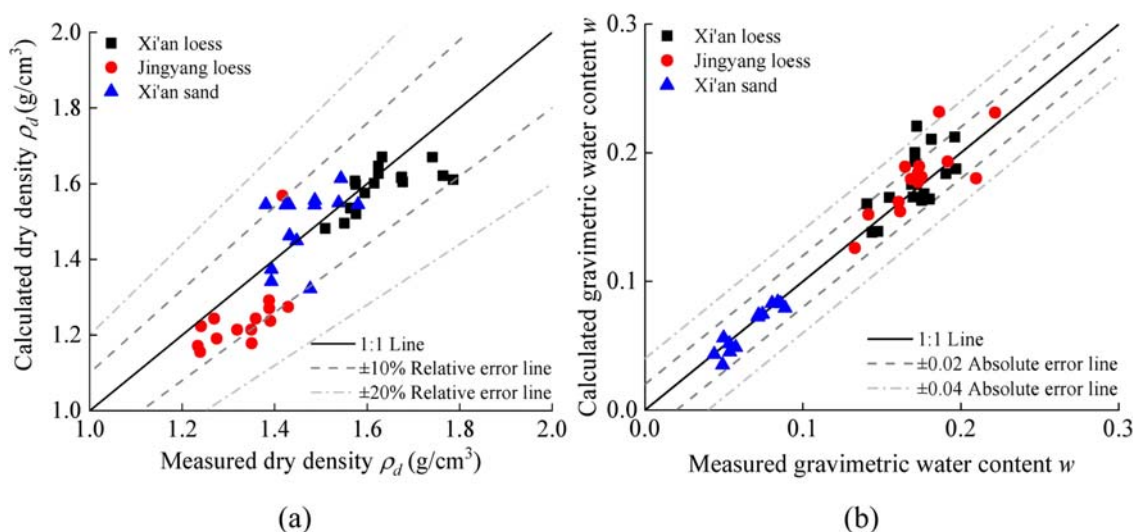


FIGURE 13

Performance for the developed soil type-independent calibration relationships of (a) dry density and (b) gravimetric water content.

density across different soil types. Figure 11b presents a comparison of the results calculated from Equation 11 and measured water content. It shows the high accuracy of Equation 11, with most data points having calculation errors within  $\pm 0.04$  compared to the measured values. This indicates the good performance of the soil type-independent calibration relationship for water content across different soil types. In summary, the calibration relationships developed using the MEP model can rapidly determine water content and dry density for different soil types through TDR measurements and physical properties, without the need for parameter calibration for a specific soil type. This work provides a reference to assist ASTM D6780/D6780M – 19 (2019) in predicting soil properties.

## 7 Verification of the new model using *in situ* measurements

To further verify the practical applicability of the developed soil type-independent calibration relationships, this study preformed two *in situ* TDR tests. Specifically, the TDR test sites were situated in Xi'an and Jingyang, Shaanxi Province, as illustrated in Figure 12a. Notably, at the site in Jingyang, 16 *in situ* TDR test points and corresponding laboratory oven-drying tests were conducted on loess specimens from varying depths within an exploratory well profile (Figure 12b). The oven-drying results revealed that the dry density of the Jingyang loess in the exploratory well profile ranged from  $1.34 \text{ g/cm}^3$  to  $1.43 \text{ g/cm}^3$ , while the gravimetric water content fluctuated within the range of 14.6%–23.8%. Notably, the detailed physical properties of the tested Jingyang loess are same as that of the clayey loess, as mentioned in Table 2. Additionally, a total of 32 TDR *in situ* and laboratory oven-drying tests were carried out at a site in Xi'an, Shaanxi Province (Figure 12c), including two soil types, Xi'an loess and Xi'an sand. The laboratory tests show that the dry densities of the loess specimens range from  $1.51 \text{ g/cm}^3$  to

$1.78 \text{ g/cm}^3$ , with gravimetric water content spanning from 14.0% to 19.7%. Following the ASTM D4318-17 (2010), the liquid limit and plastic limit of Xi'an loess were determined to be 31.1% and 18.8%, respectively. Furthermore, the particle size distribution of Xi'an loess was 43.7% sand, 31.5% silt, and 24.8% clay. In contrast, the dry densities of the Xi'an sand were observed to vary between  $1.38 \text{ g/cm}^3$  and  $1.58 \text{ g/cm}^3$ . Additionally, the natural water content of the Xi'an sand was found to be less than 10%, which is attributed to a sand content of 94.6%. More details of the physical and electrical properties of the *in situ* tested soil types are summarized in Table 5.

The dry densities derived from Equation 10 and those obtained using the oven-drying method are depicted in Figure 13a. It is observed that the developed model for calculating dry density demonstrates a better performance. At both testing sites, the relative error compared to that of the oven-drying results was less than  $\pm 10\%$  for the majority of the 48 test points, indicating the feasibility of soil type-independent calibration relationships for dry density in *in situ* testing. Figure 13b presents the comparison results between *in situ* TDR testing and the laboratory oven-drying method for soil gravimetric water content. As illustrated in the figure, the gravimetric water content calculated using Equation 11 in this study exhibits strong agreement with the results obtained from the oven-drying method. A total of 41 out of 48 test points have absolute errors within  $\pm 0.02$ , indicating that the soil type-independent calibration relationship for water content calculated by Equation 11 has applicability in field testing.

## 8 Conclusion

Accurate assessment of soil water content and dry density is crucial for evaluating the collapsibility of loess and other geotechnical applications. However, existing TDR calibration methods are constrained by soil-specific limitations. This study successfully developed soil type-independent calibration

relationships for TDR measurements of soil water content and dry density. The following conclusions are drawn:

1. Laboratory experiments were conducted on four distinct soil types to calibrate and validate the existing TDR models. Curioni's model demonstrated superior accuracy for dry density measurement, with most data points exhibiting relative errors within  $\pm 10\%$ . In contrast, Jung's model showed relative errors exceeding  $\pm 20\%$  for several test points.
2. A soil type-independent calibration relationship for dry density was successfully developed using the MEP algorithm. The MEP model exhibited robust performance in both the training and validation phases, achieving a slope of 0.925 and an  $R^2$  value of 0.88 for the training database. Most validation data points fell within a  $\pm 10\%$  relative error range. Building upon this model, a soil type-independent calibration relationship for water content was established, demonstrating high accuracy, with most predicted values exhibiting absolute errors within  $\pm 0.04$ .
3. The developed calibration relationships were further validated using 64 datasets from the literature, covering various soil types, and through two field *in situ* tests conducted in Xi'an and Jingyang, Shaanxi Province. The *in situ* validation demonstrated that the developed model could accurately determine dry density with relative errors less than  $\pm 10\%$  for most test points. Water content measurements showed strong agreement with laboratory oven-drying results, with absolute errors within  $\pm 0.02$  for the majority of test points.

This research provides a valuable tool for rapid *in situ* assessment of soil properties, particularly for evaluating loess collapsibility, without requiring soil-specific calibration. The proposed soil type-independent calibration relationships based on MEP and TDR technology offer a reference to assist [ASTM D6780/D6780M – 19 \(2019\)](#) in geotechnical applications.

## Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

## Author contributions

Z-YZ: Writing – original draft. LL: Investigation, Methodology, Writing – original draft. W-TY: Investigation, Methodology, Validation, Writing – original draft. R-SZ: Investigation,

Methodology, Validation, Writing – original draft. HT: Investigation, Methodology, Supervision, Writing – original draft. Q-YM: Conceptualization, Supervision, Writing – review and editing.

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## Conflict of interest

Authors Z-YZ and LL were employed as an Engineer at Shandong Electric Power Engineering Consulting Institute Co., Ltd. Author W-TY was employed as an Engineer at the State Grid Corporation of China, Extra High Voltage Construction Branch. Authors R-SZ and HT were employed as an Engineer at China Jikan Research Institute of Engineering Investigations and Design, Co., Ltd.

The remaining author declares that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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## References

- Asif, U., Javed, M. F., Alyami, M., and Hammad, A. W. (2024). Performance evaluation of concrete made with plastic waste using multi-expression programming. *Mater. Today Commun.* 39, 108789. doi:10.1016/j.mtcomm.2024.108789
- ASTM D2216 (2010). Test methods for laboratory determination of water (Moisture) content of soil and rock by mass. doi:10.1520/D2216-10
- ASTM D2487-11 (2011). *Practice for classification of soils for engineering purposes Unified Soil Classification System*. Conshohocken, PA. ASTM International. doi:10.1520/D2487-11
- ASTM D422-63 (2007). Test method for particle. *Size Analysis Soils*. doi:10.1520/D0422-63R07E02
- ASTM D4318-17 (2010). Standard test methods for liquid limit, plastic limit, and plasticity index of soils.
- ASTM D6780/D6780M – 19 (2019). Test method for water content and density of soil *in situ* by time Domain Reflectometry (TDR). doi:10.1520/D6780\_D6780M-19
- Atkinson, J. H., Allman, M. A., and Böese, R. J. (1992). No AccessInfluence of laboratory sample preparation procedures on the strength and stiffness of intact

- Bothkennar soil recovered using the Laval sampler. *Géotechnique* 42, 349–354. doi:10.1680/geot.1992.42.2.349
- Basma, A. A., and Member, A. (1992). Evaluation and control of collapsible soils. *J. Geotechnical Eng.* 118, 1491–1504. doi:10.1061/(ASCE)0733-9410(1992)118:10(1491)
- Bhuyan, H., Scheuermann, A., Bodin, D., and Becker, R. (2020). Soil moisture and density monitoring methodology using TDR measurements. *Int. J. Pavement Eng.* 21, 1263–1274. doi:10.1080/10298436.2018.1537491
- Bittelli, M., Tomei, F., Anbazhagan, P., Pallapati, R. R., Mahajan, P., Meisina, C., et al. (2021). Measurement of soil bulk density and water content with time domain reflectometry: algorithm implementation and method analysis. *J. Hydrology* 598, 126389. doi:10.1016/j.jhydrol.2021.126389
- Curioni, G., Chapman, D. N., Pring, L. J., Royal, A. C. D., and Metje, N. (2018). Extending TDR capability for measuring soil density and water content for field condition monitoring. *J. Geotech. Geoenviron. Eng.* 144, 04017111. doi:10.1061/(ASCE)GT.1943-5606.0001792
- Dalton, F. N., Herkelrath, W. N., Rawlins, D. S., and Rhoades, J. D. (1984). Time-Domain reflectometry: simultaneous measurement of soil water content and electrical conductivity with a single probe. *Science* 224, 989–990. doi:10.1126/science.224.4652.989
- Farooq, F., Ahmed, W., Akbar, A., Aslam, F., and Alyousef, R. (2021). Predictive modeling for sustainable high-performance concrete from industrial wastes: a comparison and optimization of models using ensemble learners. *J. Clean. Prod.* 292, 126032. doi:10.1016/j.jclepro.2021.126032
- Gibbs, H. J., and Bara, J. P. (1962). *Predicting surface subsidence from basic soil tests Special Technical Publication*, 322. Conshohocken, PA: ASTM International, 231–247.
- Giese, K., and Tiemann, R. (1975). Determination of the complex permittivity from thin-sample time domain reflectometry improved analysis of the step response waveform. *Adv. Mol. Relax. Process.* 7, 45–59. doi:10.1016/0001-8716(75)80013-7
- Holtz, W. G., and Hillf, J. W. (1961). “Settlement of soil foundations due to saturation,” in *Proceedings of the 5th international conference on soil mechanics and* (Paris: Foundation Engineering).
- Jesswein, M., and Liu, J. (2022). Using a genetic algorithm to develop a pile design method. *Soils Found.* 62, 101175. doi:10.1016/j.sandf.2022.101175
- Ji, W., Xiao, J., Toor, G. S., and Li, Z. (2021). Nitrate-nitrogen transport in streamwater and groundwater in a loess covered region: sources, drivers, and spatiotemporal variation. *Sci. Total Environ.* 761, 143278. doi:10.1016/j.scitotenv.2020.143278
- Jia, X., Shao, M., Wei, X., Zhu, Y., Wang, Y., and Hu, W. (2020). Policy development for sustainable soil water use on China's loess Plateau. *Sci. Bull.* 65, 2053–2056. doi:10.1016/j.scib.2020.09.006
- Jung, S., Drnevich, V. P., and Abou Najm, M. R. (2013). New methodology for density and water content by time domain reflectometry. *J. Geotech. Geoenviron. Eng.* 139, 659–670. doi:10.1061/(ASCE)GT.1943-5606.0000783
- Khan, S., Ali Khan, M., Zafar, A., Javed, M. F., Aslam, F., Musarat, M. A., et al. (2021). Predicting the ultimate axial capacity of uniaxially loaded CFST columns using multiphysics artificial intelligence. *Materials* 15, 39. doi:10.3390/ma15010039
- Khan, M., Nassar, R.-U.-D., Khan, A. U., Houda, M., El Hachem, C., Rasheed, M., et al. (2023). Optimizing durability assessment: machine learning models for depth of wear of environmentally-friendly concrete. *Results Eng.* 20, 101625. doi:10.1016/j.rineng.2023.101625
- Li, Y. (2018). A review of shear and tensile strengths of the malan loess in China. *Eng. Geol.* 236, 4–10. doi:10.1016/j.enggeo.2017.02.023
- Lim, Y. Y., and Miller, G. A. (2004). Wetting-induced compression of compacted Oklahoma soils. *J. Geotech. Geoenviron. Eng.* 130, 1014–1023. doi:10.1061/(ASCE)1090-0241(2004)130:10(1014)
- Lin, C., Tang, S., and Chung, C. (2006). Development of TDR penetrometer through theoretical and laboratory investigations: 1. Measurement of soil dielectric permittivity. *Geotechnical Test. J.* 29, 306–313. doi:10.1520/GTJ14093
- Mu, Q. Y., Zhou, C., Ng, C. W. W., and Zhou, G. D. (2019). Stress effects on soil freezing characteristic curve: equipment development and experimental results. *Vadose Zone J.* 18, 1–10. doi:10.2136/vzj2018.11.0199
- Mu, Q. Y., Dong, H., Liao, H. J., Dang, Y. J., and Zhou, C. (2020a). Water-retention curves of loess under wetting–drying cycles. *Géotechnique Lett.* 10, 135–140. doi:10.1680/jgele.19.00025
- Mu, Q. Y., Zhan, L. T., Lin, C. P., and Chen, Y. M. (2020b). Non-invasive time domain reflectometry probe for transient measurement of water retention curves in structured soils. *Eng. Geol.* 264, 105335. doi:10.1016/j.enggeo.2019.105335
- Mu, Q., Zhou, C., and Ng, C. W. W. (2020c). Compression and wetting induced volumetric behavior of loess: macro- and micro-investigations. *Transp. Geotech.* 23, 100345. doi:10.1016/j.trgeo.2020.100345
- Mu, Q., Meng, L., Lu, Z., and Zhang, L. (2023a). Hydro-mechanical behavior of unsaturated intact paleosol and intact loess. *Eng. Geol.* 323, 107245. doi:10.1016/j.enggeo.2023.107245
- Mu, Q. Y., Dai, B. L., Zhou, C., Meng, L. L., Zheng, J. G., Zhang, J. W., et al. (2023b). A new and simple method for predicting the collapse susceptibility of intact loess. *Comput. Geotechnics* 158, 105408. doi:10.1016/j.compgeo.2023.105408
- Mu, Q. Y., Meng, L. L., and Zhou, C. (2023c). Stress-dependent water retention behaviour of two intact aeolian soils with multi-modal pore size distributions. *Eng. Geol.* 323, 107233. doi:10.1016/j.enggeo.2023.107233
- Mu, Q., Song, T., Lu, Z., Xiao, T., and Zhang, L. (2024). Evaluation of the collapse susceptibility of loess using machine learning. *Transp. Geotech.* 48, 101327. doi:10.1016/j.trgeo.2024.101327
- Muñoz-Castelblanco, J., Delage, P., Pereira, J. M., and Cui, Y. J. (2011). Some aspects of the compression and collapse behaviour of an unsaturated natural loess. *Géotechnique Lett.* 1, 17–22. doi:10.1680/geolett.11.00003
- Nadler, A., Dasberg, S., and Lapid, I. (1991). Time domain reflectometry measurements of water content and electrical conductivity of layered soil columns. *Soil Sci. Soc. Amer. J.* 55, 938–943. doi:10.2136/sssaj1991.0361599500550040007x
- Nazar, S., Yang, J., Ahmad, W., Javed, M. F., Alabduljabbar, H., and Deifalla, A. F. (2022). Development of the new prediction models for the compressive strength of nanomodified concrete using novel machine learning techniques. *Buildings* 12, 2160. doi:10.3390/buildings12122160
- Ng, C. W. W., and Pang, Y. W. (2000). Experimental investigations of the soil-water characteristics of a volcanic soil. *Can. Geotechnical J.* 37, 1251–1264. doi:10.1139/t00-05
- Ng, C. W. W., Zhou, C., and Ni, J. (2024). Advanced unsaturated soil mechanics: theory and applications.
- Oltean, M., and Groşan, C. (2003). A comparison of several linear genetic programming techniques. *Complex Systems* 14, 285–313. doi:10.25088/ComplexSystems.14.4.285
- Onyelowe, K. C., Ebid, A. M., Fernandez Vinuesa, D. F., Estrada Brito, N. A., Velasco, N., Buñay, J., et al. (2024). Estimating the compressive strength of lightweight foamed concrete using different machine learning-based symbolic regression techniques. *Front. Built Environ.* 10, 1446597. doi:10.3389/fbuil.2024.1446597
- Peng, J., Tong, X., Wang, S., and Ma, P. (2018). Three-dimensional geological structures and sliding factors and modes of loess landslides. *Environ. Earth Sci.* 77, 675. doi:10.1007/s12665-018-7863-y
- Qin, S., Xu, T., Cheng, Z.-L., and Zhou, W.-H. (2023). Analysis of spatiotemporal variations of excess pore water pressure during mechanized tunneling using genetic programming. *Acta Geotech.* 18, 1721–1738. doi:10.1007/s11440-022-01728-w
- Rehman, Z. U., Khalid, U., Ijaz, N., Mujtaba, H., Haider, A., Farooq, K., et al. (2022). Machine learning-based intelligent modeling of hydraulic conductivity of sandy soils considering a wide range of grain sizes. *Eng. Geol.* 311, 106899. doi:10.1016/j.enggeo.2022.106899
- Rogers, C. D. F., Dijkstra, T. A., and Smalley, I. J. (1994). Hydroconsolidation and subsidence of loess: studies from China, Russia, North America and Europe. *Eng. Geol.* 37, 83–113. doi:10.1016/0013-7952(94)90045-0
- Severcan, M. H. (2012). Prediction of splitting tensile strength from the compressive strength of concrete using GEP. *Neural Comput. & Applic.* 21, 1937–1945. doi:10.1007/s00521-011-0597-3
- Siddiqui, S., Drnevich, V., and Deschamps, R. (2000). Time domain reflectometry development for use in geotechnical engineering. *Geotechnical Test. J.* 23, 9–20. doi:10.1520/GTJ11119
- Topp, G. C., Davis, J. L., and Annan, A. P. (1980). Electromagnetic determination of soil water content: measurements in coaxial transmission lines. *Water Resour. Res.* 16, 574–582. doi:10.1029/WR016i003p00574
- Vatin, N. I., Hematibahar, M., and Gebre, T. H. (2025). Chopped and minibars reinforced high-performance concrete: machine learning prediction of mechanical properties. *Front. Built Environ.* 11, 1558394. doi:10.3389/fbuil.2025.1558394
- Velastegui, L., Velasco, N., Sanchez Quispe, H. R., Barahona, F., Onyelowe, K. C., Hanandeh, S., et al. (2024). Predicting the impact of adding metakaolin on the flexural strength of concrete using ML classification techniques – a comparative study. *Front. Built Environ.* 10, 1434159. doi:10.3389/fbuil.2024.1434159
- Wang, H.-L., and Yin, Z.-Y. (2020). High performance prediction of soil compaction parameters using multi expression programming. *Eng. Geol.* 276, 105758. doi:10.1016/j.enggeo.2020.105758
- Wang, J., Xu, Y., Ma, Y., Qiao, S., and Feng, K. (2018). Study on the deformation and failure modes of filling slope in loess filling engineering: a case study at a loess Mountain airport. *Landslides* 15, 2423–2435. doi:10.1007/s10346-018-1046-5
- Wang, H.-L., Yin, Z.-Y., Zhang, P., and Jin, Y.-F. (2020a). Straightforward prediction for air-entry value of compacted soils using machine learning algorithms. *Eng. Geol.* 279, 105911. doi:10.1016/j.enggeo.2020.105911
- Wang, L., Shao, S., and She, F. (2020b). A new method for evaluating loess collapsibility and its application. *Eng. Geol.* 264, 105376. doi:10.1016/j.enggeo.2019.105376

- Wu, X.-J., Dang, F.-N., and Li, J.-Y. (2025). Research on structural parameters of loess and its experimental determination method. *Front. Built Environ.* 11, 1529204. doi:10.3389/fbuil.2025.1529204
- Yin, Z.-Y., Jin, Y.-F., Shen, S.-L., and Huang, H.-W. (2017). An efficient optimization method for identifying parameters of soft structured clay by an enhanced genetic algorithm and elastic-viscoplastic model. *Acta Geotech.* 12, 849–867. doi:10.1007/s11440-016-0486-0
- Yu, X., and Drnevich, V. P. (2004). Soil water content and dry density by time domain reflectometry. *J. Geotech. Geoenviron. Eng.* 130, 922–934. doi:10.1061/(ASCE)1090-0241(2004)130:9(922)
- Zhan, L., Mu, Q., Chen, Y., and Chen, R. (2013). Experimental study on applicability of using time-domain reflectometry to detect NAPLs contaminated sands. *Sci. China Technol. Sci.* 56, 1534–1543. doi:10.1007/s11431-013-5211-8
- Zhan, L., Mu, Q., and Chen, C. (2014). Analysis and experimental verification of sampling area of three-rod time-domain reflectometry probe. *Chin. J. Geotechnical Eng.* 36, 757–762. doi:10.11779/CJGE201404022
- Zhan, T. L., Mu, Q., Chen, Y., and Ke, H. (2015). Evaluation of measurement sensitivity and design improvement for time domain reflectometry penetrometers. *Water Resour. Res.* 51, 2994–3006. doi:10.1002/2014WR016341
- Zhang, R., and Xue, X. (2022). Determining ultimate bearing capacity of shallow foundations by using multi expression programming (MEP). *Eng. Appl. Artif. Intell.* 115, 105255. doi:10.1016/j.engappai.2022.105255
- Zhang, N., Yu, X., and Pradhan, A. (2017). Application of a thermo-time domain reflectometry probe in sand-kaolin clay mixtures. *Eng. Geol.* 216, 98–107. doi:10.1016/j.enggeo.2016.11.016
- Zhang, P., Yin, Z.-Y., and Jin, Y.-F. (2021). State-of-the-Art review of machine learning applications in constitutive modeling of soils. *Arch. Comput. Methods Eng.* 28, 3661–3686. doi:10.1007/s11831-020-09524-z
- Zhang, H., Zeng, R., Zhang, Y., Zhao, S., Meng, X., Li, Y., et al. (2022). Subsidence monitoring and influencing factor analysis of Mountain excavation and valley infilling on the Chinese loess Plateau: a case study of Yan'an new district. *Eng. Geol.* 297, 106482. doi:10.1016/j.enggeo.2021.106482

Nomenclature

<i>a, b, c, d, f, g</i>	Calibration parameters
$\rho_w$	Density of water (g/cm <sup>3</sup> )
<i>EC<sub>b</sub></i>	Bulk electrical conductivity (S/m)
<i>c</i>	Velocity of the electromagnetic wave in free space (i.e., $3 \times 10^8$ m/s)
<i>V<sub>1</sub></i>	First voltage drop (V)
<i>L</i>	Probe length of the three-rod TDR
<i>Clay</i>	Clay content
<i>w</i>	Gravimetric water content (%)
$\rho_d$	Dry density of soil (g/cm <sup>3</sup> )
$\epsilon$	Permittivity constant
<i>V<sub>f</sub></i>	Final voltage (V)
$\Delta t$	Time difference
<i>PL</i>	Plastic limit