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# PID control: Resilience with respect to controller implementation

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One of the major drawbacks of the basic parallel formulations of a PID controller is the effects of proportional and derivative kick. In order to minimize these effects, modified forms of parallel controller structures such as PI-D and I-PD are usually considered in practice. In addition, there is a usual servo/regulation tradeoff regarding closed-loop control system operation. Appropriate tuning is needed for each situation. One way of focusing explicitly on load disturbance is by the appropriate selection of a controller equation. A gap is generated here between the conception of a tuning rule and its final application that may need deployment on different controller equations. There is no danger when we go from PI-D to I-PD as we just change reference processing. However, there will be a loss of performance. The potential loss of performance, depending on the final controller equations used, motivates the authors to introduce the idea of resilient PID tuning: minimize the effects of changing the controller equation on the achieved performance/robustness. Today, this can be seen as a complement to the well-known controller fragility concept. On the basis of this scenario, this paper motivates the analysis of a tuning rule from such a point of view and also emphasizes the benefits that a better process model may provide from such an aspect.

#### KEYWORDS

PID, controller structure, process industry, tuning rules, robustness

# 1 Introduction

The proportional-integral-derivative (PID) controller was first proposed in 1922 by Minorsky (1922) and first applied in industrial applications in 1939 (Bennett, 1993). Since then, it has been considered an effective tool and is one of the most common control schemes that have dominated the majority of industrial processes and mechanical systems because of its versatility, high reliability, and ease of operation (Astrom and Hagglund, 2006). PID controllers can be manually tuned appropriately by the operators and control engineers based on the empirical knowledge when the mathematical model of the controlled plant is unknown. Some classical tuning methods, such as Ziegler–Nichols method (Ziegler and Nichols, 1942), Chien–Hrones–Reswick method (Chien et al., 1952), IMC (Rivera et al., 1986), S-IMC (Skogestad, 2003), robust IMC (Vilanova, 2008), and MoReRT (Alfaro and Vilanova, 2016), are applied to the process control, and the performance is then significantly outperformed compared to the one that is manually tuned.

One of the major drawbacks of the basic parallel formulations of PID controllers is the effects of proportional and derivative kick. The changes in the set point cause an impulse signal or sudden change in the controller output as well as in the output response (Johnson, 2005). The controller output is given to the final control elements like control valve, motor, or electronic circuit in which the spikes create serious problems. In order to minimize these effects, modified forms of parallel controller structures such as ID-P and I-PD are usually considered in practice as suggested by Ogawa and Kano (2008) and Ang et al. (2005).

Another motivation for the appropriate selection of the controller structure comes from the differences that arise depending on the mode of operation of the designed closedloop. This is a common factor (O'Dwyer, 2009) that all approaches face: the frequently referred topic of set-point tracking vs. disturbance rejection performance. It is wellknown (Alcantara et al., 2013) that there is an inherent tradeoff between both modes of operation in addition to the also well-known performance/robustness tradeoff. This distinction has made available in recent years a number of research works that analyze and provide tuning solutions to each one of the operational modes under a variety of performance indexes as well as control constraints. However, it has also been recognized (Shinskey, 2002; Vilanova et al., 2017) that disturbance rejection is much more important than set-point tracking for many process control applications, leading set-point tracking to a secondary level of interest. Therefore, a controller design that emphasizes disturbance rejection rather than setpoint tracking is an important design problem that, even if it has been the focus of research, it may have not received the appropriate attention. One way of focusing explicitly on load disturbance is by the appropriate selection of the controller equation. In the ideal PID formulation, all the three modes process the error signal and therefore both the reference and the disturbance signals. However, industrial software packages (Ang et al., 2005) used to offer a choice menu where different implementations are available. One can choose which controller modes are fed with the reference signal. From this aspect, we can go, for example, from PID to PI-D, where the derivative term just acts on the process output, or the I-PD where the error signal is just seen by the integral term.

On the basis of the previous situation, the authors aim to focus on the idea of resilience of PID tuning rules. This is the idea of tuning rules that guarantee appropriate performance and robustness even when applied on a different PID formulation from the one the tuning rule was conceived for. We do not refer in this work to the problem of not appropriately converting the tuning equations and making them consistent with the controller formulation. This has already been addressed by Alfaro and Vilanova (2012a) for what matters to the changes in the PID equation. However, a deep analysis of the implications that the signal processed by each controller mode does have on the resulting closed-loop control performance is still needed. This will serve as a basis for evaluating the resilience of the tuning.

Vilanova et al. (2018a) presented a robust tuning rule for I-PD controllers from the point of view of solving the servo vs. regulation choice for tuning. From this perspective, the I-PD implementation is conceived as an alternative that provides a structural solution to tradeoff tuning. The proposal states that a direct, simple, and efficient solution is found if the controller tuning is addressed for the servo mode but using the I-PD controller structure. The effects of the usual tuning rules implemented as an I-PD controller are analyzed, and the loss of performance of the usual IMC tuning, for example, is reported. However, it is to be noted that the IMC tuning is essentially a servo tuning. Therefore, when implemented as an I-PD controller, the loss of performance is expected because the proportional term does not process the process output. This analysis, however, even if correct, is not general and does not imply that all tunings will underperform when implemented as an I-PD controller. In other words, the lack of resilience should not be taken for granted.

On the basis of the previous scenario, the purpose of this work is to gain insights into such a resilience concept. We analyze the performance and robustness of the implementation of simple robust tuning (SRT) presented by Alfaro and Vilanova (2013) when I-PD and PID formulations are considered both a 1-DoF and a 2-DoF controller. The evaluation is confronted with robust tuning explicitly designed for the I-PD controller as presented by Vilanova et al. (2018a). This comparison is not conducted with the aim of establishing the best tuning but to illustrate the advantages of the resilience with respect to controller implementation.

The following section reviews the concepts of fragility and resilience with respect to robustness and performance as they will be used in the work. Next, the control problem formulation is presented, and the differences between PID controller implementations are stated. Notation is introduced regarding PID implementation in terms of signal processing. Following this, simple robust tuning (SRT) is presented. Section 5 presents an evaluation of a benchmark process and different robustness levels, followed by a discussion on the resilience idea and some concluding remarks.

## 2 Fragility evaluation

Alfaro (2007) presented the concept of controller fragility. Fragility introduces a measure of the change (in fact, the loss) in the controlled closed-loop system robustness due to a change in the controller parameters (changes up to 20% are usually associated to the final fine-tuning of the controller). The loss of robustness caused because of this change in the controller parameters is evaluated by means of the delta 20 fragility index. Values of this index determine if the tuning is fragile (>0.5), non-fragile ( $\geq$ 0.5), or resilient ( $\geq$ 0.1).

Two main differences arise in the idea presented here. First of all, the property that may change is not robustness but the performance. Second, the motivation for such a change is not a change in the controller parameters but a change in the equation that implements the controller.

The notion we introduce in this work refers to controller implementation. In fact, the main difference with respect to the notion of the controller's fragility presented by Alfaro (2007) is the effect generated by an eventual small change on the controller parameters, whereas here the tuning remains fixed, but the controller equations are the ones that may change. The changes in the controller equation that are considered here mainly refer to reference processing. Even one of the degrees of freedom may be lost. What matters here is which controller modes (proportional and/or integral) process the reference signal and in which way (using the set-point weight—2-DoF—or not—1-DoF)<sup>1</sup>. In all such cases, the feedback properties remain unchanged. Therefore, the control system will experience a potential reduction in the tracking performance. Its robustness and regulation properties will remain unchanged.

The classification proposed by Alfaro (2007) as fragile, nonfragile, or resilient, in terms of the delta 20 fragility index, is chosen because the change in the controller parameters may turn a control system with a highly robust controller (with  $M_s$  between 1.2 and 1.4) into one with minimum acceptable robustness ( $M_s \approx 2.0$ )<sup>2</sup>.

In this case, it is not possible to get an idea of relative loss because the change in the controller is structural. It gets difficult to establish a single number as a threshold where we can say whether the performance loss is acceptable or not. This will be process- and application-dependent. In addition, it must be considered that as the effects of the implementation will be just on tracking, the evaluation will depend on the measure that the control system will operate as a regulator or as a servo. There are too many considerations that prevent a single, objective definition to be established. However, even in this different framework, it is the author's opinion to better consider a conceptual extension of the initial fragility index along the same lines as presented by Alfaro and Vilanova (2012b) for the idea of performance fragility with respect to a small variation in the controller parameters.

Therefore, we propose to extend the same classification of performance-fragile, non-fragile, and resilient controllers as presented by Alfaro and Vilanova (2012b), but with respect to a change in the controller implementation rather than a 20% change in its parameters. Of course, this adoption is made with the idea of avoiding to introduce other different and subjective measures. Considering a change in the controller's equation implementation, the delta performance-fragility index,  $PFI_{\Delta}$ , could define the maximum loss of the control system performance with respect to the original equation the controller was conceived for (Alfaro and Vilanova, 2012b):

$$PFI_{\Delta} \doteq \frac{J_{e\Delta}^m}{J_e^o} - 1, \qquad (1)$$

where  $J_e^o$  is the performance measure index evaluated on the nominal system and  $J_{e\Delta}^m$  is the extreme value for the same index evaluated when a  $\Delta$  variation in the controller parameters is introduced. This index usually takes the form of an integral criterion such as IAE, ITAE, ISE, and ITSE. However, it does not need to be constrained to this form. Based on the  $PFI_{\Delta}$ , the controller's performance, its fragility degree is defined as follows:

- Performance-fragile PID controller: A PID controller is performance-fragile if its delta performance fragility index is higher than 0.50,  $PFI_{\Delta} > 0.50$ .
- Performance-non-fragile PID controller: A PID controller is performance-non-fragile if its delta performance fragility index is less than or equal to 0.50,  $PFI_{\Delta} \leq 0.50$ .
- Performance-resilient PID controller: A PID controller is performance-resilient if its delta performance fragility index is less than or equal to 0.10,  $PFI_{\Delta} \leq 0.10$ .

#### 3 Control problem and PID controller formulation

In this section, we revise the control problem formulation as well as the formulation of the PID controller equation and the different options for error, feedback, and reference signal processing. As some of the concepts, especially what matters to the control problem are well-known, the presentation will be succinct.



<sup>1</sup> A second degree of freedom is understood here as the separate processing of the reference signal, usually with a set-point weight ß that modifies the usual error signal e = r - y to  $e = \beta r - y$ .

<sup>2</sup>  $M_S$  is the well-known robustness measure of the closed-loop system in terms of the maximum sensitivity function  $M_S \doteq \max_{\omega} |\frac{1}{1+C(W)P(W)}|$ .

#### 3.1 Control problem

Consider a closed-loop control system, as shown in Figure 1, where P(s) is the controlled process model and  $C_r(s)$  and  $C_y(s)$  are the transfer functions of the set-point controller and the feedback controller, respectively. In this system, r(s) is the set point, u(s) is the controller output signal, d(s) is the load disturbance, and y(s) is the controlled process variable.

The control system output is

$$y(s) = M_{yr}(s)r(s) + M_{yd}(s)d(s),$$
 (2)

where the *servo-control* and the *regulatory control* closed-loop transfer functions are

$$M_{yr}(s) = \frac{C_r(s)P(s)}{1 + C_y(s)P(s)}$$
(3)

and

$$M_{yd}(s) = \frac{P(s)}{1 + C_y(s)P(s)},$$
(4)

respectively, that are related by

$$M_{yr}(s) = C_r(s)M_{yd}(s).$$
<sup>(5)</sup>

As the control system closed-loop characteristic polynomial is

$$p(s) = 1 + C_y(s)P(s),$$
 (6)

the control system relative stability depends on the controlled process model and the feedback controller parameters but not on the set-point controller parameters that are not included in the feedback controller transfer function.

Given a controlled process model P(s) and the controller  $C(s) = \{C_r(s), C_y(s)\}$ , control algorithm parameters must be selected considering the control system robustness—relative stability—and its performance under a selected design metric.

#### 3.2 PID controllers

As a general controller, the two-degree-of-freedom (2-DoF) proportional integral derivative control algorithm,

$$u(t) = K_p \left\{ \beta r(t) - y(t) + \frac{1}{T_i} \int_0^t [r(\xi) - y(\xi)] d\xi + T_d \frac{d[\gamma r(t) - y(t)]}{dt} \right\},$$
(7)

is considered that can be expressed in the s domain as

$$u(s) = K_p \left\{ \beta r(s) - y(s) + \frac{1}{T_i s} [r(s) - y(s)] + \frac{T_d s}{\alpha T_d s + 1} [\gamma r(s) - y(s)] \right\}, \quad (8)$$

where  $K_p$  is the controller proportional gain,  $T_i$  is the integral time,  $T_d$  is the derivative time,  $\alpha$  is the derivative filter constant,  $\beta$  is the proportional set-point weight factor, and  $\gamma$  is the derivative set-point weight factor. It is to be noted that in Eq. 8, as usual practice, a first-order filter has been added to the derivative term.

#### TABLE 1 PID controller "family."

	β	Г
PID <sub>e2</sub>	$\geq 0$	[0…1]
$PI_eD_{y2}$	$\geq 0$	0
$PID_{e1}$	1	1
$PI_eD_{y1}$	1	0
$PI_eD_{y1}$ $I_ePD_{y1}$	0	0



Controller output Eq. 8 can be expressed as

$$u(s) = C_r(s)r(s) - C_y(s)y(s),$$
(9)

and the control system error signal is

$$e(s) = r(s) - y(s).$$
 (10)

Selection of the set-point weight factors  $\beta$  and  $\gamma$  allows to obtain the different members of the PID controller "family": the general 2-DoF PID controller  $PID_{e2}$ —control modes act on different weighted error signals; the 2-DoF PID controller  $PI_eD_{y2}$ —derivative mode acts only on the feedback signal; the basic one-degree-of-freedom (1-DoF) PID controller  $PID_{e1}$ —all control modes act on the error signal; the 1-DoF  $PI_eD_{y1}$  controller—proportional and integral control modes act on the error; and the 1-DoF  $I_ePI_{y1}$  controller—only the integral control acts on the error signal, as listed in Table 1. Figure 2 shows a generic block diagram of a 2-DoF PID controller, showing the role of the  $\beta$  and  $\gamma$  weights according to this table.

From Eq. 8 and Table 1, it is found that all the aforementioned PID control algorithms provide the same feedback controller but different regulatory controllers as follows—considering here only controllers with no derivative "kick" ( $\gamma = 0$ ):

• Feedback controller of all the *PID* algorithms:

$$C_{y}(s) = K_{p} \left( 1 + \frac{1}{T_{i}s} + \frac{T_{d}s}{\alpha T_{d}s + 1} \right).$$
(11)

• Set-point controller of the  $PI_eD_{y2}$ :

$$C_r(s) = K_p \left(\beta + \frac{1}{T_i s}\right). \tag{12}$$

• Set-point controller of the  $PI_eD_{y1}$ :

$$C_r(s) = K_p \left( 1 + \frac{1}{T_i s} \right). \tag{13}$$

• Set-point controller of the  $I_e PD_{y1}$ :

$$C_r(s) = \frac{K_p}{T_i s}.$$
 (14)

In the I-PD controller structure, all three parameters contribute to the disturbance attenuation as all three parameters process the output signal. On the other hand, only the integral time constant contributes to the tracking performance. Therefore, the final allocation of the controller gains should result in different controller tunings depending on the use of an I-PD or a PID. Questions such as the following ones naturally arise: will the performance of the I-PD degrade significantly from the PID one? Will it be beneficial to elaborate tuning rules specifically for the I-PD configuration?

#### 4 Simple robust tuning

As presented, the simple robust tuning (SRT) method by Alfaro and Vilanova (2013) is considered for evaluation with respect to the different PID controller implementations. In this section, the SRT formulation, tuning equations, and robustness characterization are presented. The SRT equations for the 2-DoF PID controllers ( $PI_eD_{y2}$ ) are obtained on the basis of a performance/robustness tradeoff analysis.

The SRT method regards a controlled process as a generic SOPDT model, given by the following transfer function:

$$P(s) = \frac{Ke^{-Ls}}{(Ts+1)(aTs+1)},$$
  

$$0 \le a \le 1, \quad 0.1 \le \tau_L = \frac{L}{T} \le 2,$$
(15)

covering first- and second-order plus dead-time overdamped processes.

The control system performance is optimized under the *integrated absolute error* (IAE) cost functional

$$J_{e} \doteq \int_{0}^{\infty} |e(t)| dt = \int_{0}^{\infty} |r(t) - y(t)| dt,$$
(16)

and its robustness is measured with the maximum sensitivity

$$M_{S} \doteq \max_{\omega} |S(j\omega)| = \max_{\omega} \frac{1}{|1 + C_{y}(j\omega)P(j\omega)|}.$$
 (17)

As additional performance evaluation metrics, the *control effort total variation* 

$$TV_u \doteq \sum_{k=1}^{\infty} |u_{k+1} - u_k|,$$
 (18)

and the *controller output instant change* to a set-point step change

$$\Delta u_0 \doteq \beta \ K_p \ \Delta r, \tag{19}$$

can be used.

Analysis of the regulatory control performance and robustness shows that for a model with a given time constant ratio *a*, increasing the control system target robustness  $M_S^t$  results in a substantial reduction in the controller gain  $K_p$  but has a negligible effect on the controller integral time  $T_i$  and the derivative time  $T_d$ . As a result, tuning equations that are independent of the desired robustness are obtained for the  $T_i$ and  $T_d$  controller parameters. On the other hand,  $K_p$  is used to match the control system target robustness level and becomes the only robustness-dependent controller parameter. As the controller gain depends on the control system robustness, the proportional set-point weight factor  $\beta$  depends on it as well.

The SRT equations are of the general form<sup>3</sup>:

$$K_p = \mathbf{H}(T, \tau_L, a; M_S^t), \tag{20}$$

$$T_i = \mathbf{F}(T, \tau_L, a), \tag{21}$$

$$T_d = \mathbf{G}(T, \tau_L, a), \tag{22}$$

$$\beta = \mathbf{Q}(\tau_L; M_S^t). \tag{23}$$

SRT equations *H*, *F*, *G*, and *Q* for four target robustness levels,  $M_S^t \in \{\text{minimum (2.0)}, \text{low (1.8)}, \text{intermediate (1.6)}, \text{high (1.4)}\}$ , and controlled process models with five time constant ratios,  $a \in \{\text{fopdt (0.0)}, \text{sopdt (0.25}, 0.50, 0.75), \text{dppdt (1.0)}\}$ , can be found in Alfaro and Vilanova (2013).

#### 5 Performance evaluation

Having presented the SRT tuning equations, now it is time to evaluate their performance regarding the operation of the closedloop control system with the PID controller implemented under different variations, say  $PI_eD_{y2}$ ,  $PI_eDy1$ , and  $I_ePD_{y1}$ . Performance is evaluated with respect to regulatory control and servo-control operation. Also, robustness of the control system should be taken into account. The evaluation will be conducted by considering a usual benchmark process model from Åström and Hägglund (2000) and also considering the robust I-PD tuning from

<sup>3</sup> Derivative filter constant  $\alpha = 0.1$  is used in all controllers.

TABLE 2 FOPDT and SOPDT models.

K	T [s]	а	L [s]	$ au_L$
a' = 0.4				
1.25	11.49	_	5.17	0.450
1.25	8.56	0.704	1.47	0.172
a' = 0.8				
1.25	17.57	_	13.37	0.761
1.25	11.15	1.0	7.71	0.691

Vilanova et al. (2018a) to have a reference of robust tuning regarding  $I_e PD_{v1}$  implementation.

The evaluation is conducted using the following steps: first of all, the process models are obtained, and the corresponding controllers are adjusted according to the presented SRT tuning rule. Next, the regulatory control performance is analyzed, and evaluation of the robustness/performance tradeoff in terms of the process model used (FOPDT and SOPDT) is presented. Next, we proceed with the servo-control performance. The effects of losing the reference signal processing (either because of a 1-DoF or  $I_ePD_{y1}$  implementation) are discussed. Those evaluations provide an idea of the effects of changing the controller implementation with respect to the SRT tuning rule itself. As a final step, in order to get an idea of the achievable performance of SRT compared with a specific  $I_ePD_{y1}$  tuning, the robustness/performance tradeoff of the SRT tuning is faced with that of the tuning presented by Vilanova et al. (2018a).

#### 5.1 Controlled process and models

As controlled processes, the four-order test system from Astrom and Hagglund (2000)

$$P_0(s) = \frac{K}{(T's+1)(a'T's+1)(a'^2T's+1)(a'^3T's+1)},$$
 (24)

with K = 1.25, T' = 10 s, and  $a' \in \{0.4, 0.8\}$  is used.

For controller tuning purposes, these processes are approximated by FOPDT and SOPDT models

$$P_1(s) = \frac{K e^{-Ls}}{Ts+1},$$
 (25)

$$P_2(s) = \frac{Ke^{-Ls}}{(Ts+1)(aTs+1)},$$
(26)

using the three-point 123*c* identification method (Alfaro, 2006). The parameters of the identified low-order models are listed in Table 2. At this point, it is important to highlight that both FOPDT and SOPDT are considered, mainly because even though SRT can be based on both FOPDT and SOPDT, the robust  $I_ePD_{y1}$  method by Vilanova et al. (2018a) just considers FOPDT process models.

TABLE 3 SRT  $PI_eD_{y2}$  controllers; process with a'=0.4

$M_S^t$	2.0	1.8	1.6	1.4
Tuning with the	FOPDT model			
$K_p$	1.59	1.41	1.19	0.90
$T_i$ [s]	7.88			
$T_d$ [s]	2.28			
ß	0.62	0.67	0.75	0.95
$M^m_S$	2.01	1.80	1.60	1.40
$J_{ed}/\Delta d$	6.56	7.39	8.67	11.11
$TV_{ud}/\Delta d$	1.53	1.49	1.43	1.34
Tuning with the	sOPDT model			
$K_p$	5.07	4.39	3.56	NA†
$T_i$ [s]	6.72			
$T_d$ [s]	2.85			
ß	0.54	0.56	0.58	0.71
$M_S^m$	2.00	1.80	1.61	_
$J_{ed}/\Delta d$	1.59	1.93	2.55	_
$TV_{ud}/\Delta d$	2.07	1.87	1.76	_

† Valid only for  $\tau_L \ge 0.25$  if  $a \ge 0.50$ .

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TABLE 4 SRT  $PI_eD_{y2}$  controllers; process with a' = 0.8

$M_S^{\iota}$	2.0	1.8	1.6	1.4
Tuning with the	e FOPDT model			
$K_p$	1.05	0.93	0.79	0.60
$T_i$ [s]	16.37			
$T_d$ [s]	5.46			
ß	0.68	0.76	0.89	1.16
$M_S^m$	2.02	1.81	1.61	1.41
$J_{ed}/\Delta d$	20.08	22.02	24.89	30.58
$TV_{ud}/\Delta d$	1.46	1.37	1.27	1.14
Tuning with th	e SOPDT model			
$K_p$	1.37	1.21	1.01	0.77
$T_i$ [s]	16.19			
$T_d$ [s]	7.56			
ß	0.67	0.74	0.86	1.11
$M_S^m$	1.98	1.79	1.59	1.40
$J_{ed}/\Delta d$	15.17	17.11	20.17	25.35
$TV_{ud}/\Delta d$	1.41	1.33	1.25	1.18

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# 5.2 SRT controller parameters and regulatory control performance

The SRT  $PI_eD_{y2}$  controller parameters for four target robustness levels  $M_s^t$  using the FOPDT and the SOPDT controlled process models are listed in Table 3 for the process



TABLE 5 Servo-control response; process with a' = 0.4 and tuning using the FOPDT model.

$M_S^t$	2.0	1.8	1.6	1.4
Controller PI <sub>e</sub> D <sub>y2</sub>				
$J_{er}/\Delta r$	12.40	12.93	13.66	14.71
$TV_{ur}/\Delta r$	2.57	2.39	2.15	1.87
$\Delta u_0 / \Delta r$	0.99	0.94	0.89	0.86
Controller $PI_eD_{y1}$				
$J_{er}/\Delta r$	12.84	13.24	13.78	14.71
$TV_{ur}/\Delta r$	3.62	3.16	2.60	1.92
$\Delta u_0 / \Delta r$	1.59	1.41	1.19	0.90
Controller I <sub>e</sub> PD <sub>y1</sub>				
$J_{er}/\Delta r$	15.45	16.20	17.28	19.14
$TV_{ur}/\Delta r$	1.96	1.83	1.66	1.41
$\Delta u_0/\Delta r$	0	0	0	0

TABLE 6 Servo-control response; process with a' = 0.4 and tuning using the SOPDT model.

$M_S^t$	2.0	1.8	1.6
Controller PI <sub>e</sub> D <sub>y2</sub>			
$J_{er}/\Delta r$	7.56	8.15	9.21
$TV_{ur}/\Delta r$	8.28	6.91	5.67
$\Delta u_0 / \Delta r$	2.74	2.56	2.06
Controller $PI_eD_{y1}$			
$J_{er}/\Delta r$	8.60	9.23	10.30
$TV_{ur}/\Delta r$	14.63	11.70	9.06
$\Delta u_0 / \Delta r$	5.07	4.39	3.56
Controller I <sub>e</sub> PD <sub>y1</sub>			
$J_{er}/\Delta r$	9.65	10.2	11.26
$TV_{ur}/\Delta r$	4.29	3.85	3.48
$\Delta u_0 / \Delta r$	0	0	0

with the time constant ratio a' = 0.4 and in Table 4 for the process with a' = 0.8. These tables also include the obtained control system robustness  $M_S^m$  and the regulatory control behavior—performance  $J_{ed}$  and controller output total variation  $TV_{ud}$ . The control system robustness  $M_S^m$  is evaluated using the controlled process low-order models Eqs. 25, 26, in a real industrial application, and it cannot be obtained directly with the controlled process. However, the system performance in terms of  $J_{ed}$  and  $TV_{ud}$  is evaluated with the original processes Eq. 24 as it may correspond to an application of the tuned controller and the corresponding recording of the closed-loop signals.

Regarding the achieved robustness and its effects on the control system performance, the first thing noticed in these tables is that all the controllers—based on four different models—achieve the target robustness levels within 1%. It is also noticed that an inverse relation exists between the control system robustness and its performance. If the target robustness is increased  $-M_S^t \downarrow$ -, the control system performance decreases— $J_{ed} \uparrow$ —but the control effort is smoother— $J_{ud} \downarrow$ .

TABLE 8 Servo-control response; process with a' = 0.8 and tuning

using the SOPDT model.

$M_S^t$	2.0	1.8	1.6	1.4	$M_S^t$	2.0	1.8	1.6	1.4
Controller PI <sub>e</sub> D	0 <sub>y2</sub>				Controller PI <sub>e</sub> L	$D_{y2}$			
$J_{er}/\Delta r$	28.74	29.30	29.96	30.90	$J_{er}/\Delta r$	26.72	27.74	29.08	30.78
$TV_{ur}/\Delta r$	1.89	1.73	1.56	1.34	$TV_{ur}/\Delta r$	2.20	2.04	1.86	1.65
$\Delta u_0 / \Delta r$	0.71	0.71	0.70	0.70	$\Delta u_0 / \Delta r$	0.92	0.90	0.87	0.85
Controller PI <sub>e</sub> D	0 <sub>y1</sub>				Controller PIeL	$D_{y1}$			
$J_{er}/\Delta r$	29.49	29.66	30.01	31.15	$J_{er}/\Delta r$	27.71	28.45	29.38	30.65
$TV_{ur}/\Delta r$	2.44	2.07	1.69	1.22	$TV_{ur}/\Delta r$	3.01	2.56	2.08	1.52
$\Delta u_0 / \Delta r$	1.05	0.93	0.79	0.60	$\Delta u_0 / \Delta r$	1.37	1.21	1.01	0.77
Controller I <sub>e</sub> PD	0 <sub>y1</sub>				Controller I <sub>e</sub> PI	$D_{y1}$			
$J_{er}/\Delta r$	35.37	36.72	38.65	42.44	$J_{er}/\Delta r$	33.07	34.55	36.72	40.08
$TV_{ur}/\Delta r$	1.44	1.30	1.16	0.98	$TV_{ur}/\Delta r$	1.52	1.41	1.27	1.10
$\Delta u_0 / \Delta r$	0	0	0	0	$\Delta u_0 / \Delta r$	0	0	0	0

TABLE 7 Servo-control response; process with a' = 0.8 and tuning using the FOPDT model.



There is a conflict between the control system robustness and its performance, but it cannot be considered an industrial control system design tradeoff. The control system design robustness level is process-dependent. It is a requirement imposed by the controlled process non-linearity—changes in the process dynamic characteristics in the control system operation range. Then, the required control system robustness level is a must and its performance should be sacrificed.

As all the controllers considered— $PI_eD_{y2}$ ,  $PI_eD_{y1}$ , and  $I_ePD_{y1}$ —have the same feedback controller transfer function Eq. 11, their closed-loop regulatory control transfer functions as well as their robustness and performance are all the same as listed in Tables 3, 4. In fact, robustness is a feedback property, and having the same closed-loop regulatory control transfer functions, the three controller implementations provide the same robustness.

For both controlled processes— $a \in \{0.4, 0.8\}$ —two low-order models were obtained—FOPDT and SOPDT—and used for tuning purposes. From the control system evaluation, it is clear that for the same robustness level, the control systems designed using the SOPDT models provide better performance, but with a less smooth control effort, than the corresponding systems designed using the FOPDT models.

From the designer's point of view, the marginal extra effort needed to obtain a SOPDT low-order model to represent the controlled process in the controller design procedure pays for itself with the higher performance obtained. The regulatory control responses for the process Eq. 24 with a' = 0.4 are shown in Figure 3. It shows the robustness/performance conflict, but more important is the performance increase obtained by designing the control system using the SOPDT



TABLE 9 VAGG robust *I<sub>e</sub>PD<sub>y</sub>* tuning

	a' = 0.4		a' = 0.8		
$M_S^t$	2.0	1.6	2.0	1.6	
$K_p$	1.81	1.35	1.25	0.94	
$T_i$ [s]	8.17	7.80	17.34	15.85	
$T_d$ [s]	1.86	2.03	4.13	4.72	
$M_S^m$	2.19	1.70	2.35	1.78	
$J_{ed}/\Delta d$	5.83	7.74	18.80	22.50	
$TV_{ud}/\Delta d$	1.65	1.536	1.83	1.52	
$J_{er}/\Delta r$	14.44	16.36	33.75	36.70	
$TV_{ur}/\Delta r$	2.14	1.86	1.77	1.52	
$\Delta u_0 / \Delta r$	0	0	0	0	

model instead of the FOPDT one. As a complementary view of the better regulatory capabilities, we can look at the integral gain. This is defined as  $K_i = K_p/T_i$ . We can observe that larger values are obtained for designs based on an SOPDT process model. Therefore, better capacity of the controller is needed to reduce the load disturbance effect.

#### 5.3 SRT servo-control performance

The obtained servo-control performance with the three different controllers for the controlled process with a' = 0.4 is listed in Table 5—tuned with the FOPDT model—and in Table 6—tuned with the SOPDT model.

Corresponding performance data for the controlled process with a' = 0.8 are listed in Table 7 (FOPDT) and in Table 8 (SOPDT).

As in  $PI_eD_{y1}$  and  $I_ePD_{y1}$  controllers, the second degree of freedom of the  $PI_eD_{y2}$  controller is lost, and its servo-control performance is lower than the performance obtained with the latter. As shown in Table 1, the  $PI_eD_{y1}$  controller is equivalent to a  $PI_eD_{y2}$  controller with  $\beta = 1$ , and the  $I_ePD_{y1}$  controller is equivalent to a  $PI_eD_{y2}$  controller with  $\beta = 0$ . The drop in the servo-control performance obtained using the 1-DoF controllers depends on the controlled process, the model used for controller tuning, and its target robustness level can be related with the proportional set-point weight factor  $\beta$ .

For the controlled processes used for the evaluation, the setpoint weight factor  $\beta$ -values vary from 0.54 to 1.16. Then, as the required  $\beta$ -value approaches 1.0, the  $PI_eD_{y1}$  servo-control performance losses decrease, but the performance corresponding to the  $I_ePD_{y1}$  controller increases (this implementation corresponds to a  $\beta = 0$  2-DoF controller).

The SRT proportional set-point weight factor ß as a function of the normalized model dead-time  $\tau_L = L/T$  and the different robustness target levels  $M_S^t$  are shown in Figure 4. As for all models  $\beta > 0.50$ , the servo-control performance lost with a  $PI_eD_{y1}$ controller is lower than the one lost with an  $I_ePD_{y1}$  controller. A performance reduction in the tracking operation is therefore expected. Some of the robust servo-control responses (a' = 0.4,  $M_S^t = 1.6$ ) are shown in Figure 5. For a given robustness level, the  $PI_eD_{y2}$  controller output is "optimal"—has the lowest  $J_{er}$ . The  $I_ePD_{y1}$  controller loses 22% less performance than the  $PI_eD_{y2}$ 



controller, but its control effort is smoother—has the lowest  $TV_{ur}$ and, more importantly, has no proportional "kick"— $\Delta u_0 = 0$ .

#### 5.4 Robust $I_e PD_y$ tuning performance

To the best of the authors' knowledge, the method proposed by Vilanova et al. (2018b) is one of the few robust tuning procedures available specifically designed for  $I_ePD_{y1}$ controllers. Herein, it is denoted as the VAGG method. It optimizes the  $I_ePD_{y1}$  control system servo-control response—using the IAE cost functional—assuring at the same time a specific robustness level— $M_S \in \{2.0 \ (tight), 1.6 \ (smooth)\}$ —for FOPDT-controlled process models. The VAGG controller parameters and performance indices for the controlled process Eq. 24 using models Eq. 25 are listed in Table 9. 1.50

1.28

	<i>a'</i> = 0.4		a' = 0.8		
$M_S^t$	2.0	1.6	2.0	1.6	
$K_p^*$	1.67	1.22	1.08	0.80	
$M_S^{m'}$	2.01	1.60	2.00	1.60	
$J_{ed}/\Delta d$	6.31	8.50	20.46	25.00	
$TV_{ud}/\Delta d$	1.61	1.49	1.61	1.38	
$J_{er}/\Delta r$	14.92	16.99	34.91	38.31	

TABLE 10 VAGG robust  $I_e PD_v$  tuning with reduced gain.

2.02

 $TV_{ur}/\Delta r$ 

TABLE 11 Servo-control performance  $J_{er}/\Delta r$  (a' = 0.4, SOPDT model, and  $M_{\rm S}^{\rm f} =$  1.6).

1.75

Controller	$PI_eD_{y2}$	$PI_eD_{y1}$	$I_e PD_{y1}$
W/o noise	9.21	10.30	11.26
Run 1	9.898	10.991	11.767
Run 2	9.584	10.626	11.755
Run 3	9.683	10.480	11.998
Run 4	9.436	10.463	11.697
Run 5	9.711	10.868	11.375
Average	9.62	10.69	11.72

As it can be noticed, the obtained closed-loop control system robustness  $(M_S^m)$  is in the range of 6.25%–11.5% lower than the corresponding target levels. Therefore, the resulting control system is less robust than expected. Then, to have a fair comparison, the VAGG controller proportional gains  $K_p$  are reduced in the range of 8%–15%—without changing the controller integral times  $T_i$  and derivative times  $T_d$ —to increase the control system robustness up to the target levels. The new controller's proportional gains  $K_p^*$  and the performance obtained are listed in Table 10.

The VAGG  $I_ePD_{y1}$  controller performances are very similar to the ones obtained with the FOPDT model-based SRT  $I_ePD_{y1}$ controllers,  $\Delta J_{ex\%} \in [-3.8 \cdots + 1.9]$ , and with smoother control efforts but not better than the ones obtained with the SOPDT model-based SRT  $I_ePD_{y1}$  controllers. Then, additional investigation is needed on the performance of the robustly tuned  $I_ePD_{y1}$  controllers using SOPDT models to see if a new tuning rule is needed or if one of the existing optimal and robust regulatory control tunings for 1-DoF or 2-DoF  $PI_eD_y$  controllers can be used with an  $I_ePD_{y1}$  controller without a significant loss of performance<sup>4</sup>.

<sup>4</sup> For example, the RoPe tuning method (Alfaro et al., 2011).

# 5.5 Servo-control performance for a controlled variable with noise

As a complementary evaluation, additional controller performance tests are conducted for a controlled process variable corrupted with a measurement noise. The servocontrol normalized performances  $J_{ern}$  for five simulation runs, and their averages values are listed in Table 11 for different controller configurations. The servo responses for a noisy signal (Run 2) are shown in Figure 6. As the change in the controller configurations is relevant for what matters to the tracking operation, the load disturbance is not evaluated or shown here. We can see that the effect of the noise with respect to the ideal situation can be considered negligible. Table 6 shows the values obtained in the ideal case.

#### 6 Discussion

The previous section provided the performance evaluation of the SRT under different scenarios. It is evident that the comparison is process- and robustness-dependent. However, some general conclusions can be drawn.

According to the performance measures shown in Tables 5, 6, it is possible to evaluate the performance loss with respect to the following two implementation changes:

- $PI_eD_{y2} \rightarrow PI_eD_{y1}$ : In this case, the second degree of freedom is lost, and a 2-DoF-tuned controller is implemented in a 1-DoF form. If we evaluate the performance losses and the corresponding  $PFI_{\Delta}$ , it turns out that they are <0.1 for all tunings carried out using an FOPDT model. Therefore, we face resilient tuning. For the design concurred with a better SOPDT model, the  $PFI_{\Delta}$  is also <0.1 for the process with a' = 0.4 and slightly higher than 0.1 for a' = 0.8 but in any case far from 0.5. Therefore, we can say that SRT tuning is resilient and non-fragile.
- $PI_eD_{y2} \rightarrow I_ePD_{y1}$ : As we move to  $I_ePD_{y1}$  implementation, the change is more drastic because just the integral term processes the reference signal. Therefore, a larger performance drop is expected for reference changes. In fact, in this case, for both FOPDT and SOPDT-based tuning, the resulting  $PFI_{\Delta}$  is very similar: slightly greater than 0.2 but in any case far from 0.5. Therefore, we can say that SRT tuning is non-fragile.

The previous classification of the SRT rule as resilient in almost all cases is a rather qualitative evaluation that, in any case, provides an idea of the low sensitivity of the tuning with respect to the implementation of the reference processing term. It is important to bear in mind here that when tuning the three (or four in the 2-DoF case) parameters of a PID controller, distribution of the controller gain is carried out among the different parameters. Therefore, assigning how those gains take care of the two essential signals that do generate the error: the reference signal—for tracking purposes—and the feedback signal—for regulation purposes—altered because of potential disturbances. Depending on how those gains are distributed, the loss of performance in one of the operating modes can be really higher. Therefore, even qualitatively, the fact that the SRT tuning rule is almost in all cases resilient stands as a proof of a balanced gain distribution.

If we focus on a more quantitative evaluation, the only option is to compare the achieved performance on the implemented configuration with respect to a tuning designed specifically for such controller implementation. In this respect, we conducted an evaluation of the VAAG tuning (Vilanova et al., 2018b) performance. As this is a tuning optimized for the  $I_ePD_{y1}$ controller implementation and includes at the same time robustness considerations, it provides a perfect scenario to quantitatively evaluate the degraded performance of the SRT tuning.

Table 10 shows the VAAG performance for a fair comparison. For the two robustness levels considered in Vilanova et al. (2018b), as observed in the previous subsection, the results show that the performance of an  $I_ePD_{y1}$  controller tuned with the VAGG is very similar to the one obtained with the FOPDT model-based SRT (even SRT is not originally optimized for  $I_ePD_{y1}$ ). If we start with SOPDT model-based SRT tuning, in this case, even the SRT's degraded performance is better than the one achieved by the VAAG. This quantitative evaluation raises the question about the potential interpretation of the previously categorized non-fragility of SOPDT-based SRT tuning as really resilient with respect to structural changes in the controller implementation.

# 7 Conclusion

This work has presented a position work regarding the importance of the PID controller structure. Most of the tuning rules are conceived for a PID controller where the reference signal is processed by both the integral and the proportional term (either with or without a reference weighting factor).

One of the major drawbacks of the basic parallel formulations of the PID controllers is the effects of proportional and derivative kick. The changes in the setpoint cause an impulse signal or a sudden change in the controller output as well as the output response. The controller output is given to the final control elements like control valve, motor, or electronic circuit in which the spikes create serious problems. In order to minimize these effects, modified forms of parallel controller structures such as PI-D and I-PD are usually considered in practice. Therefore, it turns out that tuning may finally be applied to an I-PD controller.

The considered simple robust tuning (SRT) allows to tune a PI/PID controller for an FOPDT as well as an SOPDT process model. The advantages of using a better process model have been outlined, and the use of SOPDT models instead of FOPDT models is greatly encouraged. This fact may allow minimizing the loss of performance when the final implementation is an I-PD instead of a PID as usual. This fact will make the tuning rule resilient with respect to the PID implementation.

This issue is not usually considered when presenting new tuning rules or when comparing with existing, wellestablished tunings. Modern tunings use approaches driven by advanced multi-objective algorithms that provide the final tuning values for the controller parameters. The optimality of such a design is not discussed at all. However, other more practical constraints should also be taken into account. This is a similar situation as the one with the fragility of tuning (Alfaro, 2007). Fragility and resilience, taken together, are concepts of great utility for the final practitioner as this will generate more confidence into the provided tuning.

In this work, only simple robust tuning was evaluated as an example. The purpose was to present a situation where a robust design based on FOPDT and SOPDT process models can be evaluated with respect to different PID controller implementations— $PI_eD_{y2}$ ,  $PI_eDy1$ , and  $I_ePD_{y1}$ . This helped shed light on the robustness/performance tradeoff, effect of the process model, and loss of performance because of controller implementation, as well as quite different evaluation issues that are not usually taken into account.

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#### Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material; further inquiries can be directed to the corresponding authors.

## Author contributions

All authors listed have made a substantial, direct, and intellectual contribution to the work and approved it for publication.

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# **Conflict of interest**

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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