



An Experimental Examination of Thermal Conductivity Anisotropy in *hcp* Iron

Kenji Ohta^{1*}, Yu Nishihara², Yuki Sato¹, Kei Hirose^{3,4}, Takashi Yagi⁵, Saori I. Kawaguchi⁶, Naohisa Hirao⁶ and Yasuo Ohishi⁶

¹ Department of Earth and Planetary Sciences, Tokyo Institute of Technology, Tokyo, Japan, ² Geodynamics Research Center, Ehime University, Ehime, Japan, ³ Earth-Life Science Institute, Tokyo Institute of Technology, Tokyo, Japan, ⁴ Department of Earth and Planetary Science, The University of Tokyo, Tokyo, Japan, ⁵ National Metrology Institute of Japan, National Institute of Advanced Industrial Science and Technology, Ibaraki, Japan, ⁶ Japan Synchrotron Radiation Research Institute, Hyogo, Japan

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> *Correspondence: Kenji Ohta k-ohta@geo.titech.ac.jp

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Ohta K, Nishihara Y, Sato Y, Hirose K, Yagi T, Kawaguchi SI, Hirao N and Ohishi Y (2018) An Experimental Examination of Thermal Conductivity Anisotropy in hcp Iron. Front. Earth Sci. 6:176. doi: 10.3389/feart.2018.00176 The Earth's core mainly consists of iron, and its thermal transport properties are of vital importance for our understanding of the thermal evolution and the dynamics of the core and the mantle. However, the reported values of thermal conductivity of iron at the core conditions are so far inconclusive. Although hexagonal closed-packed (*hcp*) iron is often studied as a proxy metal to investigate the physical properties not only of the inner core, but also the outer core, the anisotropy of the thermal conductivity of *hcp* iron has never been experimentally examined. Here we report the results of texture analyses by means of synchrotron X-ray diffraction experiments and thermal conductivity measurements on polycrystalline *hcp* iron up to 44.5 GPa and 300 K. These results indicate that the thermal conductivity of single crystal *hcp* iron along *c* axis is about 3–4 times higher than that along *a* axis, which could have partially caused the controversial values of the thermal conductivity of *hcp* iron at the Earth's core conditions.

Keywords: hcp iron, Earth's core, thermal conductivity, XRD, thermoreflectance (TR), diamond anvil cell (DAC)

INTRODUCTION

At some point in the past, the Earth's liquid iron alloy core began to crystallize at Earth's center, resulting in the birth and growth of the solid inner core. Energy considerations indicate that the power delivered to the present-day geodynamo comes mainly from the growth of the solid inner core that induces light element and latent heat releases at the inner core boundary (ICB) (Verhoogen, 1961; Braginsky, 1963; Lister, 2003). On the other hand, before the birth of an inner core, the geodynamo was powered by secular cooling alone, or was possibly helped by an exsolution of MgO and SiO₂ (Badro et al., 2016; O'Rourke and Stevenson, 2016; Du et al., 2017; Hirose et al., 2017). On this note, the birth of the inner core must have been a major event for the geodynamo and could be observed in the paleointensity records (Biggin et al., 2015; Smirnov et al., 2016; Landeau et al., 2017). However, the age of the inner core is still under hot debate, mainly due to controversial estimates of the thermal conductivity of iron that critically affect thermal evolution of the core (e.g., Williams, 2018).

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The conductivity of hexagonal closed-packed (*hcp*) iron has been experimentally determined in a laser-heated diamond anvil cell (DAC) at the pressure (*P*) and temperature (*T*) conditions corresponding to the upper part of Earth's outer core (Konôpková et al., 2016; Ohta et al., 2016). It was surprising to see that the reported thermal conductivity of *hcp* iron showed about septuple difference at 135 GPa and 4,000 K corresponding to the Earth's core-mantle boundary (CMB) condition. Due to the experimental difficulty in measuring thermal conductivity at such extremely high *P*-*T* conditions, conventional studies have measured electrical conductivity (σ , the inverse of electrical resistivity) of iron and iron alloys, and then converted it to the electronic thermal conductivity (κ_{el}) via the Wiedemann-Franz relation,

$$\kappa_{el} = \sigma T L, \tag{1}$$

where T is absolute temperature and L is the Lorenz number. The ideal (i.e., Sommerfeld) Lorenz number L_0 is 2.45 $\times 10^{-8}$ $W\Omega/K^2$. Ohta et al. (2016) likewise measured the electrical resistivity of solid iron to the core pressure and temperature conditions. Their resistivity data demonstrated the κ_{el} of hcp iron to be 226(+71/-31) W/m/K at the CMB when the Wiedemann-Franz relation with L_0 was applied. On the other hand, Konôpková et al. (2016) carried out fast thermal radiation detection experiments and estimated high-P/high-T thermal conductivity of iron on the basis of finite element modeling to reproduce the detected temperature decay in a laser-heated DAC. Their study advocated the thermal conductivity value of iron at the CMB to be 33 \pm 7 W/m/K. What causes the discrepancy between these two studies? One possibility is that the Wiedemann-Franz relation cannot be directly applied at very high P-T conditions corresponding to the core conditions (Dobson, 2016). The Lorenz number might be strongly temperature and pressure dependent. Inelastic electronelectron scattering might be enhanced at the extreme pressures and temperatures, which is not considered in the Wiedemann-Franz law (Pourovskii et al., 2017; Secco, 2017). Indeed, liquid lead (Pb) and tin (Sn) show breakdown of the Wiedemann-Franz law at high temperature conditions (Yamasue et al., 2003).

Anisotropic conductivity in a *hcp* iron sample with strong crystallographic preferred orientation (CPO) is another likely

culprit of the discrepancy in the estimated iron conductivities by Konôpková et al. (2016) and Ohta et al. (2016). Both studies used iron foil as a sample and compressed it to its thickness direction in a DAC. The direction of thermal conductivity measurement performed by Konôpková et al. (2016) was parallel to the compression axis of the DAC, while the direction of electrical resistivity measurement by Ohta et al. (2016) was perpendicular to the DAC compression. If the hcp iron sample used in their studies had strong CPO and the conductivity of hcp iron is crystallographically anisotropic, the measured conductivities would differ from each other. However, to our knowledge, the conductivity anisotropy in hcp iron has never been examined. The hcp phase of iron is stable above 13 GPa and unquenchable to ambient conditions, so that in-situ high-P determination of anisotropic conductivity is imperative. As analog materials of hcp iron, one can review reports of the conductivity anisotropy in other hcp metals that are stable at ambient conditions, which shows that the magnitudes of conductivity anisotropy differ from each other (Hall et al., 1959; Nellis and Legvold, 1969; Spedding et al., 1971; Alderson and Hurd, 1975; Stierman et al., 1983; Sanborn et al., 1989; Balog and Secco, 1999; Secco and Balog, 2001). For instance, the electrical conductivity of hcp scandium (Sc) along the c axis is 2.3 times as high as that along the *a* axis (Spedding et al., 1971), while the conductivity of hcp cobalt (Co) along the a axis is 80% larger than that along the c axis (Sanborn et al., 1989).

As an experimental examination of the thermal conductivity anisotropy in *hcp* iron, we performed synchrotron X-ray diffraction (XRD) and thermal conductivity measurements on polycrystalline *hcp* iron with CPO *in-situ* at high *P* up to 44.5 GPa and 300 K in a DAC. We analyzed the results and found anisotropic thermal conductivity of *hcp* iron single crystal; thermal conductivity along the *c* axis (κ_c) is about 3~4 times higher than that along the *a* axis (κ_a). The anisotropy in the *hcp* iron thermal conductivity could partially be the cause of the discrepancy between the reported iron conductivity values (Konôpková et al., 2016; Ohta et al., 2016). If the observed conductivity anisotropy in *hcp* iron is preserved to the Earth's inner core conditions, it may have a strong influence on the heat transfer in the Earth's inner core.

Run #	Starting material	Pressure, <i>P</i> (GPa)	Thermal diffusivity, <i>D</i> (mm ² /s)	Density, ρ (kg/m ³)	lsobaric heat capacity, C _P (J/kg/K)	Thermal conductivity, κ (W/m/K)	
1 Wire		16.0 (20)	4.7 (4)	8966.4	510.2	21.7 (17)	
2	Foil	18.5 (2)	3.6 (2)	9046.4	502.2	16.5 (7)	
3	Foil	23.1 (11)	4.9 (6)	9191.1	488.1	21.9 (28)	
4	Foil	24.5 (11)	4.4 (2)	9235.4	483.9	19.6 (9)	
5	Powder	39.9 (14)	7.1 (9)	9669.2	444.6	30.4 (40)	
6	Wire	41.2 (23)	9.3 (14)	9704.2	441.6	39.9 (61)	
7	Foil	41.6 (7)	6.8 (5)	9712.3	441.2	29.3 (23)	
8	Wire	44.5 (17)	9.6 (4)	9787.9	434.5	41.0 (17)	

TABLE 1 | Experimental conditions and the results

MATERIALS AND METHODS

We performed eight separate sets of experiments to examine the anisotropy in the thermal conductivity of single crystal *hcp* iron up to 44.5 GPa at 300 K (**Table 1**). Our procedure follows these four steps:



FIGURE 1 [Back-scattered electron (BSE) Image of the *bCc* iron starting materials; (**A**) foil, (**B**) sintered and deformed powder, and (**C**) wire. These images were obtained using a scanning electron microscope equipped with a field emission gun (FE-SEM, JEO JSM-7000F) with accelerating voltage of 10 kV and probe current of 8 nA. Observed cross sections are normal to compression axis in the subsequent DAC experiments. Contrast in gray area is orientation contrast in iron whereas black dots in (**B**) are iron oxide.

- 1. We used three types of iron starting materials with different CPO and transformed them to *hcp* iron in a DAC.
- 2. We collected XRD data of the *hcp* iron samples in two directions: parallel and orthogonal to the DAC compression axis. The obtained XRD data were analyzed to determine CPO in the *hcp* iron samples as reported in the previous studies (Merkel et al., 2004; Miyagi et al., 2008; Nishihara et al., 2018).



- 3. After the CPO analyses, thermal conductivity measurements were performed on the textured *hcp* iron *in-situ* at high *P*.
- 4. We calculated κ_a and κ_c of single crystal *hcp* iron from the obtained CPO information and measured thermal conductivity of the polycrystalline *hcp* iron sample assuming an aggregate texture.

High Pressure Apparatus and Iron Starting Materials

High-P conditions were generated in a symmetric-type DAC with 300 µm flat culet diamond anvils. Body centered cubic (bcc) to hcp phase transformation of iron occurring around 13 GPa and 300 K is considered to be a prototypical martensitic transition. A number of studies reported that the texture of hcp iron is basically inherited from *bcc* iron across the transition (Merkel et al., 2004; Miyagi et al., 2008; Ishimatsu et al., 2014; Dewaele et al., 2015; Nishihara et al., 2018). Therefore, we anticipated synthesizing hcp iron samples with different textures in a DAC by using various types of textured bcc iron starting material. Here we used three types of bcc iron sample: foil, sintered powder, and wire. A highpurity iron foil (99.99%) with 10 μ m initial thickness was cut into a disk shape and compressed to its thickness direction in a DAC (Figures 1A, 2A). The iron foil has a relatively heterogeneous grain-size distribution, with the largest grains being a few micrometers in size (Figure 1A). This foil sample was also used in the previous studies (Gomi et al., 2013; Ohta et al., 2016). Iron powder (99.9% purity) with a few micro-meters grain size was sintered in a deformation-DIA apparatus (D-DIA), MADONNA-I, at the Geodynamics Research Center, Ehime University. It was sintered at 2 GPa and 600°C for 1 h, then deformed by advancing each differential-ram by 0.4 mm (Figure 1B). We cut a disk (90 µm in diameter and 10 µm initial thickness) out of the sintered and deformed iron batch and loaded it into a DAC (Figure 2B). Compression direction by a DAC is parallel to the deformation direction by a D-DIA. In the sintered iron powder, an array of iron oxide (black dots in Figure 1B) that originally formed on the surface of grains in the powder was observed. The volume fraction of the iron oxide was estimated to be <2%based on the image analysis. The grain size of iron in this starting material is judged to be significantly smaller than that of the original powder (a few hundred nanometers). The bcc iron wire (99.99% purity) with $100 \,\mu$ m in diameter was sliced to about $10\,\mu\text{m}$ thick, and then loaded into the sample chamber of a DAC. The iron wire has a homogeneous microstructure, which consists of very small, wavy grains with about $0.1 \,\mu\text{m}$ width (Figure 1C). The compression direction in a DAC is parallel to the length direction of the bcc iron wire (Figure 2C). We employed the twostage amorphous boron plus Kapton gasket that enabled us to perform radial XRD measurement for sample texture analysis (Merkel and Yagi, 2005) (Figures 3, 4). SiO₂ glass was used as a pressure transmitting medium.

Synchrotron XRD Measurements and Texture Analysis

For phase identification and texture analyses, angle-dispersive two-dimensional XRD measurements were conducted on the



iron samples in a DAC at BL10XU, SPring-8. The wavelengths of the monochromatic incident X-ray beam were $0.247 \sim 0.413$ Å ($30 \sim 50$ keV) and the incident X-ray was collimated to about $10 \,\mu$ m in diameter. The XRD images were recorded on an imaging plate (IP) detector (RIGAKU R-AXIS V⁺⁺) with a typical exposure time of 30 s. The XRD data for the iron sample in a DAC were collected in both axial and radial diffraction geometries where the sample is irradiated with X-rays both parallel and perpendicular to the DAC compression axis, respectively, in order to increase pole figure coverage (**Figure 3A**). In runs 1 and 4, only the axial XRD spectrum was collected. Pressures were determined by using an equation of state (EOS) of *hcp* iron (Yamazaki et al., 2012).

Axial and radial XRD images were quantitatively analyzed for determination of CPO using the Rietveld method as implemented in the software package MAUD (Lutterotti et al., 2014). First, the XRD images were integrated from 0° to 360°



azimuth angles over 5° sectors to produce 72 patterns (**Figure 4**). Sample to the IP distance, wavelength of incident X-ray, and the IP geometry were calibrated with CeO₂ standard. The sample CPO is calculated by the E-WIMV algorithm to produce an orientation distribution function (ODF) with a resolution of 15° . No symmetry constraint was applied in the analysis.

High-Pressure Thermal Conductivity Measurement

Thermal conductivity (κ) is a function of thermal diffusivity (D), density (ρ), and isobaric heat capacity (C_P): $\kappa = D\rho C_P$. The D of hcp iron at high P was measured by means of the pulsed light heating thermoreflectance technique in a DAC at Tokyo Institute of Technology (**Figure 3B**). Details of the measurement system and the analytical methods of this technique have been described in the literature (Yagi et al., 2011; Ohta et al., 2017). The density (ρ) of hcp iron was determined from the present XRD data. The isobaric specific heat capacity (C_P) was calculated from the thermodynamic relations and the reported thermoelastic parameters of hcp iron (Yamazaki et al., 2012).

RESULTS

Crystallographic-Preferred Orientation of Iron Samples

Prior to the high-*P* experiments, we investigated the CPO of *bcc* iron starting materials loaded into a DAC at ambient conditions. **Figure 4** presents the variations in the diffraction intensity for (110), (200), (211), and (220) diffractions of the three-types of *bcc* iron starting material. We used these four XRD peaks for texture analyses with the MAUD program, and acquired pole figures of the *bcc* samples (**Figure 5**). Pole densities are expressed in multiples of random distribution (m.r.d.). The *bcc* iron foil

showed a single crystal-like CPO with an alignment of <111> along its compression axis and an alignment of <110> on the radial plane (Figure 5A). Since the foil included large grains, as shown in Figure 1A, the number of grains in a diffraction volume might be limited. This would be the reason for the single crystal-like CPO of this sample. Although the CPO of bcc iron foil was only determined in Run 3, the CPO could be entirely different in each run due to the limited number of grains in a sample volume of a DAC experiment. The sintered and deformed bcc iron powder showed an almost axi-symmetric CPO pattern with concentrations of <100> and <111> along its compression axis (Figure 5B). This is consistent with reports by Merkel et al. (2004) and Nishihara et al. (2018), where similar CPO was formed by uniaxial compression of randomly textured bcc iron. The bcc iron wire had an almost random texture as shown in Figure 5C.

The polycrystalline bcc iron starting materials loaded into a DAC were squeezed to transform them into hcp iron. In all eight runs, we collected XRD data for hcp iron and obtained their CPO patterns. Figure 6 shows the representative XRD data for hcp iron obtained at 41.6 GPa in both axial and radial geometries. Five XRD peaks from the (1010), (0002), (1011), (1012), and (1120) diffractions were used for texture analyses. The obtained pole figures of hcp iron clearly show that the CPO of *hcp* iron differs depending on the texture of the starting materials (Figure 7). The CPO of hcp phase derived from powder bcc iron is characterized by an alignment of $<11\overline{2}0>$ parallel to the compression axis and <0001> on the radial plane (Figure 6B). This is largely consistent with the Burgers orientation relationship, $\{110\}_{bcc}//\{0001\}_{hcp}$ and $<111>_{bcc}//<11\overline{2}0>_{hcp}$, for a martensitic transformation between bcc and hcp phases. The orientation of <0001> is not axisymmetric, but lies along a particular direction (Figure 7B);



although the orientation of <110> in the *bcc* starting material is nearly axi-symmetric (**Figure 5B**). This is presumably due to strong variant selection in the *bcc* to *hcp* phase transformation under high deviatoric stress in a DAC. The CPO pattern of *hcp* iron from *bcc* wire is characterized by a strong concentration of <0001> parallel to its compression axis (**Figure 7C**), and this pattern is accompanied by a weaker concentration of <0001> along the radial direction at lower *P* (Run 1). This observation is reasonably interpreted as follows. The <111> (and <100>) is aligned parallel to the compression axis from initial random texture by compression of *bcc* phase at low pressure. The *bcc* to *hcp* phase transformation yields an alignment of <0001> along the radial direction following the Burgers relationship, and subsequent uniaxial compression to higher pressure gradually aligns <0001> along the compression axis through the basal slip dominant viscous creep (e.g., Merkel et al., 2004; Nishihara et al., 2018). In *hcp* iron that was transformed from *bcc* foil, completely different CPO patterns were observed depending on the run: $<10\overline{10}>$ was aligned along the compression axis in Runs 2 and 7 (**Figure 7A**), whereas <0001> was aligned along the compression axis in Runs 2 and 7 (**Figure 1A**). However, the CPO of *bcc* iron foil was different in each run due to its large grain size (**Figure 1A**). However, the CPO of the *bcc* phase is not perfectly inherited by the *hcp* phase along with the Burgers orientation relationship. In reality, the situation is complicated by the existence of internal stresses between grains that develop during the phase transformation. They also influence the orientation relations and variant selection and their effects cannot be deduced from simple crystallographic considerations.



measured in axial (blue) and radial (black) geometries. Wavelength of incident X-ray was 0.247 Å.

Figure 8 indicates the emergence distributions of crystals with angle θ between the DAC compression axis and <0001> of *hcp* iron, which means the frequency of *hcp* iron grains with angles between the c axis and compressional axis. This was calculated from <0001> pole figure (hence from ODF), and a distribution is normalized such that its integration in the hole interval to be unity.

Thermal Conductivity of the Polycrystalline hcp Iron

After the XRD experiments and the subsequent CPO analyses, we measured high-P thermal conductivity of the polycrystalline *hcp* iron by means of the pulsed light heating thermoreflectance technique (**Table 1**). The transient temperature change in a *hcp* iron sample by pulse laser heating was recorded at high P as shown in Figure 9A. The obtained temperature history curve was analyzed considering the one-dimensional heat diffusion in iron and pressure medium (SiO₂ glass):

$$T(t) = \overline{T} \sqrt{\frac{\tau}{\pi t}} \sum_{n=0}^{\infty} \gamma^{2n} exp\left[-\frac{(2n+1)^2}{4}\frac{\tau}{t}\right], \qquad (2)$$

where T(t) is temperature, \overline{T} is a constant, t is time, and γ expresses heat effusion to pressure medium (Yagi et al., 2011). τ is the heat diffusion time across the iron sample. We obtained \overline{T} , γ , and τ by fitting the measured curves to Equation (2). The sample thickness (d) was measured in a sample recovered from the DAC. Its cross section was prepared by using the focused ion beam (FIB) apparatus, and the thickness of the iron sample was measured under a scanning microscope (SEM) (Figure 9B). The effect of lattice volume expansion due to decompression and transformation from hcp to bcc phase was corrected to determine *d* by using the EOSs of *hcp* iron (Yamazaki et al., 2012). The τ and *d* gives high-*P* thermal diffusivity;

$$D = d^2 / \tau. \tag{3}$$

Multiplication of the D, ρ , and C_P yields the high-P thermal conductivity of *hcp* iron.

The obtained thermal conductivity of hcp iron at high P and 300 K is shown in Figure 10. The hcp iron samples from the wire starting material show higher conductivity than those from the foil and powder samples at similar pressures. The aforementioned CPO analyses showed that hcp iron from bcc wire shows a strong orientation of <0001> parallel to the compression axis, while *hcp* iron from powder and foil tends to show an alignment of <0001> on the radial plane. This CPO information and polycrystalline hcp iron conductivity imply that the thermal conductivity of *hcp* iron along the *c* axis (κ_c) is higher than that along the *a* axis (κ_a). For comparison, we calculated high-*P*/room- $T \kappa_{el}$ of polycrystalline *hcp* iron from the reported electrical resistivity (Gomi et al., 2013) and the Wiedemann-Franz law with the L_0 (Equation 1) (Figure 10). The present values of thermal conductivity of hcp iron are about half of the calculated κ_{el} . Such a difference could be due to anisotropy in the thermal conductivity of hcp iron because (Gomi et al., 2013) measured the high-P resistivity during decompression after squeezing the iron foil up to 100 GPa at 300 K. The measurement direction of the high-P resistivity was perpendicular to that of the present thermal conductivity. Since all the compared data are at 300 K, the influence of electron-electron scattering on thermal conductivity should be negligible (Pourovskii et al., 2017).



DISCUSSION

Estimation of Single Crystal Thermal Conductivity Anisotropy in *hcp* Iron

Here we quantitatively evaluate the anisotropy in the crystallographic thermal conductivity of *hcp* iron single crystal based on the present results of CPO analyses and thermal conductivity measurements (**Figures 7**, **8**, **10**). The thermal conductivity of polycrystalline *hcp* iron we measured can be regarded as the effective thermal conductivity of a *hcp* iron single crystal aggregate along the obtained CPO (**Figure 10**). First, we define the effective thermal conductivity of a *hcp* crystal along a direction θ ($\kappa(\theta)$) as follows:

$$\kappa\left(\theta\right) = \kappa_a \sin^2\theta + \kappa_c \cos^2\theta \tag{4}$$

where θ is an angle between the heat flow direction and the *c* axis (**Figure 8** inset) (see **Appendix**). In this study, the heat flow direction is parallel to the DAC compression direction (**Figure 3B**). Then, we calculated the anisotropy in thermal conductivity of a *hcp* iron crystal assuming two-types of $\kappa(\theta)$ mixing model as described below.

Approach I: Layered Texture Solved by Parallel and Series Models

We consider a layered structure in which each layer consists of *hcp* iron crystals having the same θ value. When the heat flow and DAC compression directions are perpendicular to the stacking direction, the effective thermal conductivity of the layered *hcp* iron aggregate along the heat flux can be expressed by an equivalent equation of the parallel resistor model (**Figure 11A** inset):



FIGURE 8 Distribution of angle between <0001> and DAC compression axis in three *hcp* iron samples. Red triangles; *hcp* iron from foil starting material, blue circles; *hcp* iron from sintered powder, green squares; *hcp* iron from wire sample. Black line shows randomly oriented *hcp* iron. θ is defined as an angle between DAC compression direction and *c* axis of *hcp* iron (inset).

$$\kappa_{parallel} = \int_{0}^{90} p(\theta) \kappa(\theta) \, d\theta, \tag{5}$$

where $\kappa_{parallel}$ is an effective thermal conductivity assuming the parallel model and $p(\theta)$ is the emergence distribution of angles between the <0001> axis and heat flow (DAC compression) direction (e.g., **Figure 8**). When the heat flow (DAC compression) direction is parallel to the stacking direction, the effective thermal conductivity can be regarded as the series resistor model (**Figure 11B** inset):

$$\frac{1}{\kappa_{series}} = \int_0^{90} p(\theta) \frac{1}{\kappa(\theta)} d\theta, \tag{6}$$

where κ_{series} denotes an effective thermal conductivity considering the series model. Using these models (Equations 4–6) and pairs of the present thermal conductivity of polycrystalline *hcp* iron at similar *P*, we found the κ_a and κ_c of *hcp* iron at high *P* (**Table 2** and **Figures 11A,B**). Based on the mixing theory (Guéguen and Palciauskas, 1994), the solution of the parallel model gives the lower limit, while the series model provides the upper bound limit. The results clearly indicate anisotropy in the single crystal thermal conductivity of *hcp* iron.

The solutions of the parallel model indicate that κ_c is about four-fold higher than κ_a . And, the values of κ_c are comparable to the κ_{el} of *hcp* iron from the electrical resistivity data reported by Gomi et al. (2013) (**Figure 11A**). The series model also shows a similar trend, although the absolute values of the κ_a and κ_c are different from the solutions of the parallel model (**Figure 11B**).



obtained at 18.5 GPa and 300 K (Run #2) and (B) SEM image of a cross section of the recovered sample prepared by the FIB apparatus. The transient temperature curve was fitted by Equation (2) (yellow curve). In this case, we set n = 5. The obtained fitting parameters are shown in (A). Note that this SEM image has been acquired from an oblique direction to sample stage, and thus the apparent thickness shown in this figure is different from the actual sample thickness.

Approach II: Random Distribution Texture Solved by Effective Medium Approximation

This is a realistic case in which each *hcp* iron crystal with the same orientation (i.e., the same θ) is randomly distributed in the polycrystalline aggregate sample, rather than forming the laminated structure considered above (**Figure 11C** inset). We thus employ effective medium approximation to calculate the thermal conductivity anisotropy in a *hcp* iron crystal that is



randomly distributed in polycrystal (Landauer, 1952):

$$\sum_{i=1}^{n} \frac{\kappa_{random} - \kappa_i}{2\kappa_{random} + \kappa_i} v_i = 0, \tag{7}$$

where κ_{random} , κ_i , and v_i are the effective thermal conductivity assuming a random texture, thermal conductivity of *i* component, and its volume fraction, respectively. As well as the parallel and series models, the effective medium approximation also shows strong anisotropy in the single crystal thermal conductivity of *hcp* iron (**Figure 11C**). In this case, the κ_c is about three times as high as κ_a , at least up to 43.1 GPa.

All the crystal mixing models indicate strong anisotropy in the thermal conductivity of *hcp* iron at high *P* and room *T* (**Table 2** and **Figure 11**). The obtained results of κ_c of *hcp* iron are comparable or higher than the κ_{el} (Gomi et al., 2013), indicating that the thermal and electrical conductivity of polycrystalline *hcp* iron would show variation up to a factor of four, depending on the CPO of the *hcp* iron sample in a DAC. Indeed, the measured electrical resistivities (or resistance) of *hcp* iron show considerable variation, especially at the onset of *bcchcp* transition that is about 13 GPa, but all of the experimental data obtained above 40 GPa are consistent with each other (Reichlin, 1983; Jaccard et al., 2002; Deng et al., 2013; Gomi et al., 2013; Seagle et al., 2013; Zhang et al., 2018). The discrepancy among them could be derived from difference in CPO of *hcp* iron samples just after the transition, since they have used various



FIGURE 11 | Thermal conductivities of single crystal *hcp* iron along *a* and *c* axes (κ_a and κ_c) as a function of *P* at 300 K. (A) Solutions of the parallel model (Equation 5). (B) The series model solutions (Equation 6). (C) Random distribution model calculated by the effective medium approximation (Equation 7) (Landauer, 1952). Circles; κ_a , triangles; κ_c . Black line with gray band is κ_{el} of *hcp* iron as shown in **Figure 10**. Inset figures show schematic illustrations of the parallel, series, and random models, respectively.

Run pair	<i>P</i> (GPa)) Parallel			Series			Random		
		<i>κ</i> a (W/m/K)	κ _c (W/m/K)	κ _c /κ _a	<i>κ</i> a (W/m/K)	κ _c (W/m/K)	κ _c /κ _a	<i>κ</i> a (W/m/K)	κ _c (W/m/K)	κ _c /κ _a
1, 2	17.3	10.4	44.5	4.3	14.9	64.5	4.3	10.7	49.8	4.7
3, 4	23.8	12.5	36.2	2.9	14.8	80.6	5.4	12.8	37.9	3.0
5,6	40.6	15.6	69.7	4.5	27.9	85.8	3.1	21.9	64.8	3.0
7,8	43.1	16.6	70.5	4.2	27.9	105.3	3.8	21.5	69.9	3.3

TABLE 2 | Thermal conductivities of *hcp* iron along each axis.

types of *bcc* iron starting materials. The CPO of such samples might become similar due to uniaxial compression of the DAC, resulting in similar resistivity values at higher *P*. Although Secco and Balog (2001) have selected Gd as the best analog material to predict the anisotropy in the conductivity of *hcp* iron, the electrical conductivity of Gd along the *c* axis is only 30% larger than that along the *a* axis at ambient conditions.

However, note that the strength of conductivity anisotropy obtained above highly depends on the strength of the CPO determined based on the XRD data. The ODF (and hence CPO) in this study was calculated using the E-WIMV algorithm, which is an improved version of WIMV. Determination of the ODF is a kind of inversion which does not have a unique solution, and WIMV algorithm (as well as E-WIMV) gives the smoothest positive solution with maximum entropy for ODF (Kocks et al., 2000; Lutterotti et al., 2007). This means that the CPO determined from XRD data with a limited pole figure coverage gives a lower bound in texture strength. Therefore, the single crystal thermal conductivity anisotropy of *hcp* iron presented in this study is considered to be the upper bound and the real anisotropy might be smaller.

Geophysical Implications

An open question raised above is whether the discrepancy in experimentally determined thermal conductivity of iron at the core conditions can be explained by anisotropy in the conductivity of single crystal hcp iron (Konôpková et al., 2016; Ohta et al., 2016). As a matter of fact, both studies did not determine the room-T conductivity of iron from their own experiments. Ohta et al. (2016) measured T dependence of electrical resistance of iron samples at high P and referred to the high-P/room-T resistivity of hcp iron from Gomi et al. (2013) to calculate high-P/high-T resistivity. The κ_{el} of hcp iron at 135 GPa and 300 K was obtained as 165(+56/-22) W/m/K. The method employed in Konôpková et al. (2016) cannot determine high-P/room-T conductivity in principle, as they acquired time-dependent thermal radiation spectra from a laser-heated iron sample. To construct a model of high-P/high-T thermal conductivity of hcp iron, they referred to a value of electrical resistivity of hcp iron at 135 GPa and 300 K inferred from the experimental results of Seagle et al. (2013) and converted it to κ_{el} of 120(+20/-30) W/m/K via the Wiedemann-Franz law with an unusual Lorenz number of $1.9 \times 10^{-8} \text{ W}\Omega/\text{K}^2$. In this study, we found highly anisotropic thermal conductivity of hcp iron at least up to 44.5 GPa and 300 K based on the present XRD and thermal conductivity measurements. Based on the pressure derivatives $\left(\frac{d\kappa}{dP}\right)$ of the obtained κ_a and κ_c of *hcp* iron



FIGURE 12 | Linear extrapolation of the obtained κ_a and κ_c at 300 K. Values of κ_{el} of *hcp* iron at 135 GPa and 300 K are also plotted that were estimated from the resistivity of *hcp* iron (Gomi et al., 2013) and the WF law with L_0 (open diamond), and from the *hcp* iron resistivity (Seagle et al., 2013) and the WF law with $L = 1.9 \times 10^{-8} \text{ W}\Omega/\text{K}^2$ (open hexagon).

that are 0.43 and 0.98 W/m/K/GPa, respectively, we estimated κ_a and κ_c of *hcp* iron at higher *P*, indicating the anisotropy in the conductivity is maintained to the core pressures (Figure 12). At 135 GPa, the pressure of the Earth's core-mantle boundary, $\kappa_{\rm a}$ and $\kappa_{\rm c}$ of *hcp* iron are 61.4 \pm 8.9 and 157.3 \pm 72.6 W/m/K, respectively, and κ_c/κ_a is 2.6. Therefore, thermal conductivity anisotropy in single crystal hcp iron can explain the discrepancy in the reference conductivities at 135 GPa and 300 K (Figure 12). However, the reported values of the thermal conductivity of *hcp* iron at 135 GPa and high T conditions shows about a sevenfold difference (Konôpková et al., 2016; Ohta et al., 2016). It remains unclear whether the conductivity anisotropy of single crystal hcp iron is kept to a few thousand K. In some hcp analog metals, their κ_c/κ_a was getting smaller with increasing T (Nellis and Legvold, 1969; Alderson and Hurd, 1975; Secco and Balog, 2001). Only for magnesium, its κ_c/κ_a increases with increasing T, but the T response of κ_c/κ_a was examined only from 3 to 300 K. Unless hcp iron shows strongly positive T dependence of κ_c/κ_a , the conductivity anisotropy is unlikely to

be the main cause of the controversial reports (Konôpková et al., 2016; Ohta et al., 2016). In this context, T enhanced electronelectron scattering in compressed iron would be a key factor as shown in Pourovskii et al. (2017). Within their calculations, the thermal conductivity is depressed by 39% by electron-electron scattering. For more detailed discussion, further studies for direct determination of both electrical and thermal conductivities are required at extremely high *P*-*T* conditions.

If the thermal conductivity anisotropy in hcp iron single crystal is preserved to the Earth's inner core conditions, it may have important implications for evolution and dynamics there. The seismological exploration of the Earth's inner core has revealed its structural complexities (e.g., Tkalčić, 2015; Romanowicz and Wenk, 2017). One of the main features in the inner core is that a seismic wave along the polar direction propagates by about 3% faster than one along the equatorial direction (Poupinet et al., 1983; Morelli et al., 1986). The preferred alignment of *hcp* iron alloy crystals with the *c* axis parallel to the fast-seismic axis has been repeatedly suggested to explain the cause of the seismic anisotropy in the inner core (Yoshida et al., 1996; Bergman, 1997; Karato, 1999; Buffett and Wenk, 2001), although a consensus has not reached among theoretical studies to calculate sound velocity difference between a and c axes of hcp iron. Early theoretical calculations at 0 K showed that c axis was the faster direction than a axis in hcp iron (e.g., Stixrude and Cohen, 1995), but later studies at high temperatures showed that the sense of anisotropy changes, and the *a* axis becomes the fast direction (Steinle-Neumann et al., 2001), or nearly isotropic (Sha and Cohen, 2010). If the c axis of hcp iron alloy preferentially aligns along the Earth's rotational axis in the inner core, strong anisotropy of the thermal conductivity in *hcp* iron as observed in this study implies an anisotropic thermal conductivity of the inner core with higher conductivity in the polar direction and lower conductivity in equatorial radial directions. In addition, recent first-principles calculations showed that incorporation of silicon and nickel into iron enhances anisotropy in the conductivity (Gomi et al., 2016). The Taylor column type outer core convection extracts more heat away from the ICB in equatorial regions than in polar regions, even in the absence of anisotropic thermal conductivity. As a result, greater heat loss and lower thermal conductivity of the inner core along the equatorial direction than the polar direction would produce large temperature heterogeneity at the ICB, which would enhance the directionality of inner core growth and keep the crystallographic origin of the inner core anisotropy through the geological timescale via the plastic core flow mechanism (Yoshida et al., 1996). In the recent years, detailed modeling of the inner core evolution and dynamics have been reported, but

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no study considered the thermal conductivity anisotropy in the inner core (e.g., Alboussière and Deguen, 2012; Deguen, 2012). The magnitude of thermal conductivity anisotropy in *hcp* iron (iron alloy) at the ICB conditions needs to be confirmed for more detailed discussion about the inner core evolution and dynamics.

CONCLUSIONS

In this paper, we presented the results from the synchrotron XRD experiments and the thermal conductivity measurements on polycrystalline hcp iron up to 44.5 GPa and 300 K. Analyses of the XRD data yielded the CPO of hcp iron samples, which revealed variable CPO of hcp iron depending on the CPO of bcc iron starting materials. The obtained CPO information and thermal conductivity value of hcp iron samples were used to evaluate the anisotropy in the thermal conductivity of *hcp* iron single crystal. Assuming a randomly distributed aggregate texture in hcp iron polycrystal, we found $\kappa_c/\kappa_a \sim 3$ at 44.5 GPa and 300 K. Such strong anisotropy could be maintained to the Earth's core conditions and cause the discrepancy between recent experimental determinations of the thermal conductivity of hcp iron. Thermal conductivity anisotropy of hcp iron under Earth's actual core conditions should thus be investigated in future work to provide tighter constraints on the thermal evolution and dynamics of Earth's core and mantle.

AUTHOR CONTRIBUTIONS

KO and YN are responsible for project design and wrote the manuscript. KO, YN, and YS are responsible for sample preparation, XRD experiments, and texture analyses. KO and TY are responsible for thermal conductivity measurements. KH, SK, NH, and YO helped with XRD experiments at BL10XU, SPring-8. All authors contributed to the discussion and final manuscript.

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Conflict of Interest Statement: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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APPENDIX

Derivation of the Thermal Conductivity of a *hcp* Crystal Along a Direction θ (κ (θ))

The Fourier's law of thermal conduction shows that the local heat flux density (J), is equal to the product of the local temperature gradient (grad T) and thermal conductivity (κ):

$$J = -\kappa \operatorname{grad} T. \tag{A1}$$

Let the effective thermal conductivity be the ratio of the heat flux components in the same direction caused by the temperature gradient of the direction. Here, we consider a temperature gradient having a component only in the x_3 direction:

$$\operatorname{grad} T = \begin{pmatrix} 0\\ 0\\ \frac{\partial T}{\partial x_3} \end{pmatrix},$$
 (A2)

the J_3 component can be written as follow:

$$J_3 = -\kappa_{33} \frac{\partial T}{\partial x_3}.$$
 (A3)

Therefore, in this case, the effective thermal conductivity is κ_{33} . The thermal conductivity (κ) of a hexagonal crystal is a second-order tensor with two independent components κ_a , κ_c ,

and is expressed as follows:

$$\kappa = \begin{pmatrix} \kappa_a & 0 & 0\\ 0 & \kappa_a & 0\\ 0 & 0 & \kappa_c \end{pmatrix}, \tag{A4}$$

which indicates that the thermal conductivity of the hexagonal crystal has anisotropy axially symmetric with respect to the *c* axis. It thus should be able to be expressed as a function of the angle θ with the effective thermal conductivity of an arbitrary direction with the *c* axis. Here, we set up the thermal conductivity tensor κ ' when the hexagonal crystal is rotated about the x_1 axis by the angle θ as follows:

$$\kappa' = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta \\ 0 & \sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} \kappa_a & 0 & 0 \\ 0 & \kappa_a & 0 \\ 0 & 0 & \kappa_c \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta & \sin\theta \\ 0 & -\sin\theta & \cos\theta \end{pmatrix}$$
(A5)
$$= \begin{pmatrix} \kappa_a & 0 & 0 \\ 0 & \kappa_a \cos^2\theta + \kappa_c \sin^2\theta & (\kappa_a - \kappa_c) \sin\theta \cos\theta \\ 0 & (\kappa_a - \kappa_c) \sin\theta \cos\theta & \kappa_a \sin^2\theta + \kappa_c \cos^2\theta \end{pmatrix}.$$

Considering the relationship of Equation (A3), the effective thermal conductivity $\kappa(\theta)$ is equal to the κ'_{33} component of the thermal conductivity tensor κ' after θ rotation. Therefore, $\kappa(\theta)$ can be written as

$$\kappa(\theta) = \kappa_a \sin^2\theta + \kappa_c \cos^2\theta. \tag{A6}$$