



# Dynamics of Water Absorption in Callovo-Oxfordian Claystone Revealed With Multimodal X-Ray and Neutron Tomography

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The Callovo-Oxfordian claystone is a material with notoriously complex hydro-mechanical behaviour. Combined neutron and x-ray tomography modalities are used for the first time to characterise the dynamics of water absorption in this material by comparing material deformation as well as water arrival. Exploiting recent work on multimodal registration, neutron, and x-ray datasets are registered pairwise into a common coordinate system, meaning that a vector-valued field (i.e., neutron and x-ray reconstructed values) is available for each timestep, essentially making this a 5D dataset. The ability to cross-plot each field into a *joint histogram* (an inherent input into the registration) allows an improved identification of mineral phases in this complex material. Material deformation obtained from the application of Digital Volume Correlation on the x-ray timeseries data is *locally* compared to changes in water content available from the neutrons, opening the way toward a quantitative description of the hydro-mechanics of this process.

Keywords: multimodal tomography, timeseries analysis, digital volume correlation, hydro-mechanics, callovo-oxfordian claystone

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### 1. INTRODUCTION

The beginning of the study of clay-rich formations as a potential geological barrier for the storage of nuclear waste dates back to a couple of decades (Bonin, 1998; Andra, 2005; Delay et al., 2010). In France, the Callovo Oxfordian claystone (COx) is being studied by Andra (The French radioactive Waste Management Agency) through an impressive volume of in-field and lab-scale work. This claystone's properties (low permeability, self-sealing properties) make it a favourable host rock, however, the complex couplings that govern its hydromechanical behaviour are still under investigation.

The mechanical response of the COx claystone is strongly related to its water content (Armand et al., 2017), the variation of which (drying-wetting process) has been related to the modification of its microstructure (Montes et al., 2004; Robinet et al., 2012). The non-linear response observed at high relative humidity has not only been related to damage (Chiarelli et al., 2000; Escoffier, 2002), but also to the non-linear swelling of the clay mineral (Wang et al., 2014) under these conditions. The swelling properties of the Callovo Oxfordian are linked to the presence of smectite in the clay matrix, which is very sensitive to water content changes and triggers swelling at high degrees of relative humidity (Homand et al., 2006).

A number of authors have studied the kinematics of clay-rich rocks due to wetting using different imaging tools, such as environmental scanning electron microscopy (ESEM) (Montes et al., 2004; Wang et al., 2015), scanning electron microscopy (SEM) (Desbois et al., 2017), optical

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microscopy (Bornert et al., 2010), or x-ray tomography (Lenoir et al., 2007). All these methods allow structural modification due to water content changes to be captured and consequently the computation of strains, however, they do not provide direct information related to water presence.

Moisture change in geomaterials has been investigated through neutron tomography, since neutrons are sensitive to hydrogen (due to their high attenuation of cold neutrons itself due to elastic scattering of neutrons). DiStefano et al. (2017) measured imbibition into a shale using in-situ neutron imaging. Combined x-ray and neutron tomographies on shales Chiang et al. (2018) indicate that the combination of techniques allows a better identification of the composition of these complex materials. Stavropoulou et al. (2019) combined x-ray tomography and neutron radiography to study wate imbibition in COx (albeit on twin samples) linking the cracking and propagation to the water penetration. Even though interesting trends have been revealed, this study is limited by the use of similar but different samples, meaning that the characterisation of a mechanism linking crack opening and water penetration is difficult to quantify locally.

This paper presents a significant technical evolution of Stavropoulou et al. (2019) with the analysis of a wetting test on Callovo Oxfordian claystone using a simultaneous x-ray and neutron tomography on the same sample.

#### 2. EXPERIMENTAL SETUP

# 2.1. Sample Preparation

For sample preparation, a fresh claystone core was used (EST57917, h = 300 mm, d = 120 mm) extracted from a depth of 490 m. The samples have been cut to a cylindrical shape (h = d = 20 mm) using a wire saw in neighbouring locations within the core. The average water content ( $\frac{m_{\text{water}}}{m_{\text{dry}}}$ ) has been measured after drying at 105°C for at least 24 h equal to 6.54%, a value a bit lower than what has been reported by Conil et al. (2018). This paper presents the analysis of the first sample of a series, the vertical axis of which is parallel to the bedding plane of the claystone.

Even though the experimental equipment that was designed and used for this study allows a confining pressure to be applied within a pressure vessel, this particular test is performed without confining pressure (other than that offered by the latex membrane). The experimental setup is shown in **Figure 1**. The sample is positioned on top of an aluminium base through which the water is supplied to the bottom of the sample. In order to ensure water arrival, a double hole and spiral passage is manufactured and placed on top of the aluminium base (see later **Figure 3** bottom), while the uniform distribution of the water supply to the sample is achieved using a filter paper at its bottom.

An initial tomography (numbered 001) with both modalities (details in next section) is acquired of the sample before starting water imbibition. Thereafter the air is vacuumed out of the water supply lines, and the imaging systems are readied. Water is supplied to the sample and back-to-back scans are immediately started. Tomographies are recorded back-to-back starting from

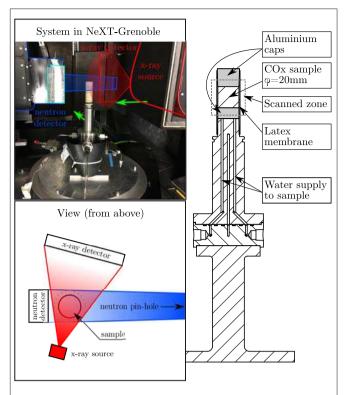


FIGURE 1 | Design of experimental used in this work. Left: photo of setup set up on NeXT-Grenoble scanner, with the sample set up on pedestal. Right: illustrative top view (scales and angles not exact) showing the dual-modality scanning setup on NeXT-Grenoble.

number 002, which is used as the reference state for the following analysis.

# 2.2. Neutron and x-Ray Tomography Acquisition

X-ray and neutron tomographies were acquired simultaneously on NeXT-Grenoble (Tengattini et al., 2017, 2019), which is equipped with an almost-parallel cold neutron beam and now a micro-focus x-ray setup with a flat panel detector. The addition of the x-ray setup is a significant improvement from our preliminary study Stavropoulou et al. (2019) where twin samples were required for separate scanning with the two different modalities (neutrons and x-rays).

For the x-ray tomographies, the geometric pixel size is  $42.70\,\mu\text{m/px}$ . The Hamamatsu L-12161-07 x-ray source is operated at  $140\,\text{kV}$  and  $130\,\mu\text{A}$ . The source focuses its electron stream into a small point, creating a divergent conical beam. The Varex 2530HE Flat-panel detector records the beam with an exposure time of 1/9 s behind a B<sub>4</sub>C filter. Each radiograph is the result of averaging 5 exposures.

Regarding neutron tomographies, NeXT-Grenoble is on a cold source, and the beam reaches the sample after going through a 30 mm diameter pinhole (with no filter). A very large collimation distance is used (around 10 m), meaning that at the sample the beam is practically parallel. A camera-mirror-scintillator system

is used to detect neutrons, with a 25 x 25 mm field of view. The Hamamastu Orca Flash V2 is equipped with Canon 180 mm F3.5 optics. The camera is used in binning 4 yielding a pixel size of approximately  $50\,\mu$ m/px. The camera is set to 0.6 s exposure. The scintillator used is a  $50\,\mu$ m thick LiF.

The x-ray and neutron acquisitions are controlled together by a proprietary RX-Solutions system. For both modalities 896 radiographs are acquired meaning scans last around 8 min. The two beams are oriented roughly perpendicular to each other (but not exactly at  $90^{\circ}$  to optimise the use of the x-ray cone beam).

During the test an interruption was necessary, meaning that seven scans are missing around the middle of the test. Due to probable neutron capture effects some greyscale corrections (detailed below) were necessary particularly after this pause.

## 3. DATA ANALYSIS

Both series of simultaneously acquired x-ray and neutron tomographies are reconstructed individually using the usual Filtered Back-Projection technique: the Feldkamp algorithm for the divergent x-rays and a parallel algorithm for the neutrons. The software used is RX-Solutions' UniCT, and a software correction for both beam-hardening and ring correction is applied. The resulting 3D fields of reconstructed values lumped attenuation coefficients for both modalities (henceforth referred to as  $\mu_x$  for x-rays and  $\mu_n$  for neutrons) are then saved on a 16-bit data range (scaling factors are kept constant for each modality).

In order to be able to simply compare noise levels between the two modalities, both tomographies of state 002 are linearly rescaled such that the mean value of the air (background) is 0.0 and the mean value of the clay matrix (foreground) is 1.0. After rescaling, the standard deviation of the background for  $\mu_n$  is 0.069 and 0.011 for  $\mu_x$ . The Signal to Noise Ratio can coarsely be taken as the reciprocal of these quantities since the claystone is scaled to 1.0, giving SNR<sub>n</sub> = 14.5 and SNR<sub>x</sub> = 90.

In order to denoise the  $\mu_n$  field, each field is smoothed using the bilateral filter (Tomasi and Manduchi, 1998) offered in the Insight Toolkit (ITK) (Yoo et al., 2002) with a  $\sigma_{\rm domain}$  = 1 and  $\sigma_{\rm range}$  = 3,000. According to the definition above, the SNR<sub>n-bilateral</sub> significantly increases to 36, at the cost of a small loss of sharpness. In what follows, these filtered images will be used for  $\mu_n$ .

Since this study is mostly concerned with the entry of water into the claystone, the SNR is also computed taking the pure clay matrix as background (see later for the computation of its greylevel) and the water as the phase of interest. For safety the standard deviation of greyvalues is computed on the aluminium top cap (since the claystone has natural variations). This yields an  $\text{SNR}_{n\text{-bilateral}}^{\text{clay/water}} = 125$  and  $\text{SNR}_{x}^{\text{clay/water}} = 37$ , which confirms the significant interest in the use of neutron tomography for following water.

#### 3.1. Multimodal Registration

With a long time-series of both neutron and x-ray tomography it is very useful to be able to have a common coordinate system. If an exact match between  $\mu_x$  and  $\mu_n$  measurements can be

achieved, the 3D data collected can be thought of as a *vector-valued* 3D field, where every voxel contains a value of  $\mu_x$  and  $\mu_n$ . Within the same modality the image registration problem can be written as the minimisation of the difference between the greyvalues, however since different modalities offer different contrast mechanisms, this subtraction no longer makes sense.

To this end a "multimodal registration" tool is used as first presented in Tudisco et al. (2017) and subsequently developed in Roubin et al. (2019). The inherent linearisation of the problem requires a good initial guess of the solution for registration to converge. The  $\mu_x$  and  $\mu_n$  volumes collected during this campaign are not easy to correlate, and the final result was found to be sensitive to the initial guess. A graphical user interface was implemented to allow an initial alignment by eye to be done, as illustrated in **Figure 2**.

The transformation to be applied to the neutron image by trilinear interpolation is described as a "linear deformation function"  $\Phi$  (represented as a 4  $\times$  4 matrix), meaning that rotations, shear and zoom changes of shapes can be described as well as sub-pixel translations.

For a few key states in the test (i.e., 002, 010, 020, 028, 040, 050) the entire multimodal registration procedure is performed (on 2-binned  $\mu_x$  fields and  $\mu_n$  fields), yielding the transformations presented in **Table 1**. It is important to stress that the  $\Phi$  discussed here is the transformation between the  $\mu_x$  and  $\mu_n$  fields and not the deformation of the sample itself. Given the relatively coarse effective pixel-size used (2-binning implies 85.4 µm/px), practically no relative movement of the two imaging systems is expected. Table 1 shows that the transformation is relatively stable, and allows a very coarse approximation of the registration error (assuming no relative movement between imaging systems) to be guessed, which is in the order of 0.1 px translation 0.2° for rotations and a factor 0.002 on "zoom." The fact that the "zoom" vector is not equal in the z direction to that found in the x and y directions may be explained by a 1% misalignment of the mirror of the neutron camera, stretching the pixels slightly in the z direction. The obtained transformations are averaged and this final transformation is then applied to all  $\mu_n$  fields. Please note that the these registered data sets are made available, see "Data Availability Statement."

The result of this application is now a vector-valued timeseries which is valuable and complex to plot. **Figure 3** shows some selected horizontal slices from the registered volumes in state 002. The quality of the registration is apparent, as well as the complementarity of the fields measured with both modalities. Notably in the first slice, the denser aluminium attenuates the x-ray beam significantly whereas the membrane is hard to distinguish. The reverse is true for the neutron beam where the hydrogen-rich membrane attenuates enough to cause artefacts and where the aluminium is close to the background value for air.

These complementary measurements are also useful for identifying different types of inclusions in the sample studied. Furthermore, the neutron tomographies allow the identification of dry and water-filled cracks. **Table 2** shows a number of phases whose corresponding grey values have been identified by hand averaging over small homogeneous zones in the image. The table

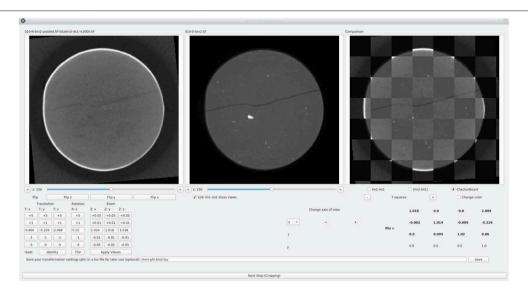


FIGURE 2 | Example of graphical tool (available in spam) developed in Qt allowing an accurate initial Φ to be manually applied to the neutrons to initialise the multimodal registration as close as possible to the correct solution. **Top row:** Horizontal slices through tomographies: (left) neutron (middle) x-rays (right) "checkerboard" allowing comparison. **Bottom row:** (left) Buttons to apply displacements, rotations and zooms to left image (middle) slice view settings (right) current Φ matrix. This software is free software and is included in the "spam" python package.

**TABLE 1** | Results of multiplicative polar decomposition of different  $\Phi$  into translation, rotation, and "zoom" components to register  $\mu_n$  fields onto  $\mu_X$  fields for different imaged states.

State	z y x Translation vector (px)	$\begin{bmatrix} z \\ y \\ x \end{bmatrix}$ Rotation vector (degree)	$\begin{bmatrix} z \\ y \\ x \end{bmatrix}$ Zoom vector
002	2.147 –5.167 0.028	5.279 0.027 -0.077	1.018 1.018 1.028
010	2.132 -5.328 0.022	5.263 -0.003 -0.090	1.017 1.021 1.031
020	2.089 -5.226 0.060	5.152 -0.028 -0.053	1.018 1.018 1.024
028	2.190 -5.128 0.237	5.113 0.062 -0.102	1.018 1.019 1.026
040	2.291 -5.405 -0.096	5.457 -0.003 -0.157	1.020 1.020 1.035
050	2.293 -5.384 -0.095	5.462 -0.002 -0.179	1.020 1.020 1.033
Mean	2.190 –5.273 0.026	5.288 0.009 -0.110	1.019 1.019 1.030

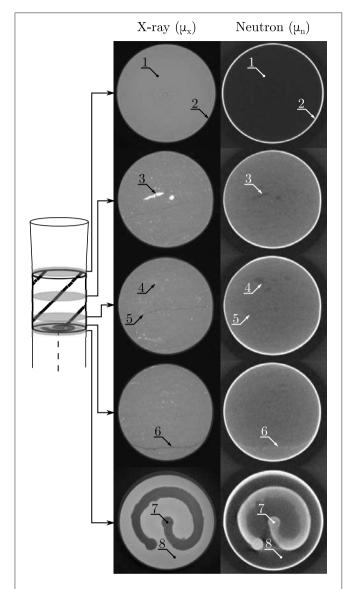
Z is the vertical direction. Pixels of the translation vector are 2-binned (i.e., have a pixel size of 85.4  $\mu$ m/px).

offers a numerical confirmation of the particular sensitivity of neutrons to water, which will be essential for the identification of the movements of water in this specimen. It is important to note that a small variation in the values of  $\mu_x$  is observed throughout the timeseries, thus, a linear rescale of the values is applied to all images after 002, based on the grey values of air and water which should not vary in time. Considering air as the zero-intercept a linear correction is applied to all images such that the values of the air and the aluminium are always the same throughout the timeseries.

A powerful tool to look at the correspondence of greyvalues in these registered images is the *joint histogram* of  $\mu_x$  and  $\mu_n$  values. For two aligned voxelised volumes, the joint histogram is simply computed by discretising the greyvalues of  $\mu_x$  and  $\mu_n$  into bins, and for each voxel position in *both* volumes, adding

1 into the corresponding bin in  $\mu_x$  and  $\mu_n$  that two greylevels falls into. The result is a 2D space of discretised  $\mu_x$  and  $\mu_n$  values inside which counts are recorded. Large number of voxel pairs are expected to be found at the intersections of greylevels in **Table 2**. **Figure 4** shows the joint histogram for state 002, with the full 16-bit image range discretised into 128 bins. In fact, this joint histogram (and the fitting of each relevant peak with a bivariate Gaussian distribution) is a fundamental part of the multimodal registration presented above.

The images acquired during the wetting process in this material are numerous, so a subselection has been selected in **Figure 5**, which shows the evolution of a slice normal to the crack initially present in the sample, which is labelled as "Dry" crack in **Figure 3**. **Figure 5** also presents—in the black and white right column—the corresponding joint histograms for the entire



**FIGURE 3** | Selected horizontal slices through registered  $\mu_{\rm X}$  and  $\mu_{\rm R}$  fields in state 002, highlighting the different phases in the material. The greylevels shown are [0–42,000] for  $\mu_{\rm X}$  and [0–52,000] for  $\mu_{\rm R}$ . As per convention, dark values in the slices represent lower values. 1. Aluminium top cap, 2. Latex membrane, 3. "Dense" inclusions, 4. "Less dense" inclusions, 5. "Dry" crack, 6. Water-filled crack, 7. Pure water, 8. Aluminium bottom cap.

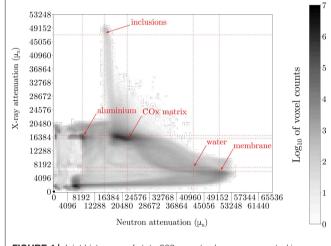
volume of each pair. The changes in the joint histogram are rather subtle, however if attention is paid to the zone around the clay matrix, some changes can be observed.

For a better understanding of the evolution of the joint histograms, the difference between each time-step (005, 020, 039, 050) to the initial (002) has been calculated, indicating the increase of number of voxels in red and a decrease in blue (**Figure 5**). In addition, this difference of the joint histograms has been calculated on a cropped subvolume wholly within the sample, resulting in a range of values that cover a smaller area in the space of the joint greylevels. Similarly to **Figure 4**,

**TABLE 2** | Manually-measured average grey values of different phases visually present in  $\mu_x$  and  $\mu_n$  in state 002.

Grey value		
$\mu_{x}$	$\mu_n$	
2,100	6,700	
5,900	49,400	
16,000	22,500	
47,000	15,300	
17,000	8,800	
7,800	41,600	
	μ <sub>x</sub> 2,100 5,900 16,000 47,000 17,000	

The high degree of complementarity between the two measurement is clear, with very different contrasts obtained for both water and inclusions, key elements in the process being studied.

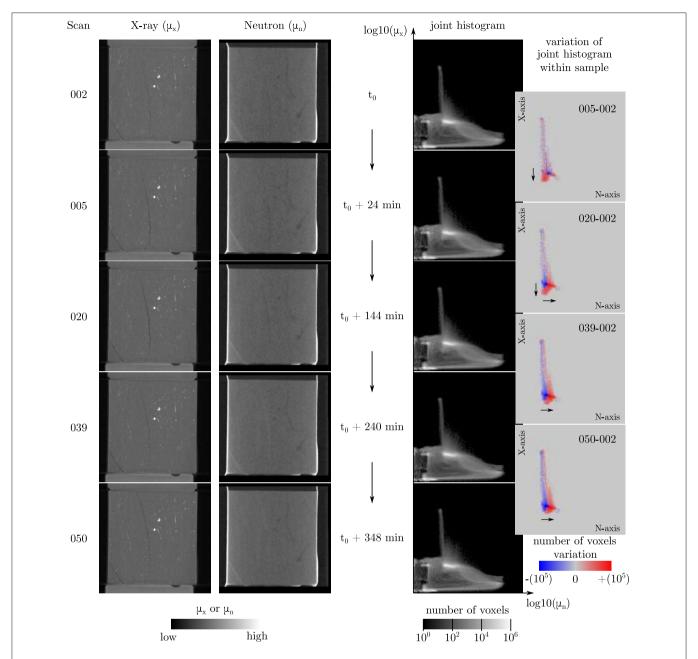


 $\label{eq:FIGURE 4 | Joint histogram of state 002, count values are presented in a $\log_{10}$ scale. Intersecting values from Table 2 are highlighted.}$ 

the horizontal axis of these joint histograms corresponds the grey level values of the neutron images, while the vertical axis represents the grey level from x-rays, plotted in  $\log_{10}$  scale.

As deduced from the incremental joint histograms, at the beginning (005–002), an increase of the number of voxels at the bottom of the vertical axis (x-ray axis) occurs in a location corresponding to the grey values of the "Dry" crack. This implies that between Scan 002 and Scan 005 an increase of the "quantity of Dry crack" is measured based on the amount of the corresponding grey level voxels from the x-ray images. Indeed, looking at the vertical slices, crack opening is well observed in the x-ray images—unlike the neutron ones.

In the following increment of joint histograms (020–002) crack opening is still observed—always along the vertical axis—however, an evolution along the horizontal axis (neutron axis) starts to appear around the same location. Increase of the grey values in the neutron images can be related to water appearance, an increase that becomes even more apparent in the following increments (039–002 and 050–002). When relating the observed evolution to the actual vertical slices, it can be confirmed that a clear water increase is depicted in the neutron image, with a



**FIGURE 5** | Vertical slices through registered  $\mu_x$  and  $\mu_n$  fields throughout the wetting experiment. Slice has been chosen to be normal to the main crack present since the beginning of the experiment in the specimen. As per **Figure 3**, the greylevels shown are [0-42,000] for  $\mu_x$  and [0-52,000] for  $\mu_n$ . As per convention, dark values in the slices represent lower values. Columns 3 and 4 represent the joint histograms of the pairs of images: column 3 is the entire joint histogram of the two images, with the counts being presented in  $\log_{10}$ . Column 4 represents a difference in counts (also in  $\log_{10}$ ) from 002 on a cropped zone within the specimen.

filled-up crack (high attenuation). From then on, a continued increase in water penetrating the clay matrix is revealed from the last increment of joint histograms (050–002).

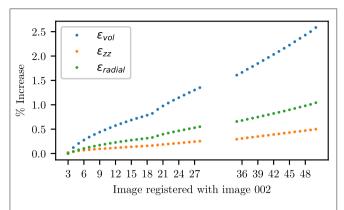
# 3.2. Displacement and Strain Field Measurements

In order to measure the deformation of the material with time, a local-DVC code is first used (the spam-ldic script available in spam, Andò et al., 2017). With this technique, a regularly-spaced

grid of points is spread through the "reference" 3D image (in this case the x-ray scan of state 002). A cubic subvolume, centred on each grid point is extracted from the 3D image and a transformation  $\Phi$  is sought for each point to minimise:

$$\eta = \sum (\operatorname{ref}(\vec{X}) - \operatorname{def}(\Phi \cdot \vec{X})^2) \tag{1}$$

Here the Lucas and Kanade technique is used (Lucas and Kanade, 1981) with a deformation function (Grédiac and Hild, 2013; Tudisco et al., 2017). In this work, the x-ray volumes are used



**FIGURE 6** | Vertical and volumetric deformations obtained from registrations (i.e., a correlation yielding a single  $\Phi$  for the entire 3D volume) with  $\mu_X$  fields with state 002. Each tomography takes 8 min.

to measure the displacement, although in the future, the *vector-valued* ( $\mu_x$  and  $\mu_n$ ) field could be used for the minimisation.

An initial time-saving step is the measurement of an overall  $\Phi$  between the field of  $\mu_x$  in state 002 and later states, which serves as an initial guess for the displacement of all points on the grid which will then be correlated. **Figure 6** shows the progression of  $\varepsilon_{\rm zz}$ ,  $\varepsilon_{\rm radial}$ , and  $\varepsilon_{\rm vol}$  with progressive registration with state 002. These scalars are obtained by extracting the displacement gradient tensor from the measured  $\Phi$ : the component  $\varepsilon_{\rm zz}$  is directly read out, the volume change is computed as the determinant of the displacement gradient tensor, and  $\varepsilon_{\rm radial} = \frac{1}{2}(\varepsilon_{\rm vol} - \varepsilon_{\rm zz})$  is computed as per Wood (1990).

Analysis of **Figure 6** immediately reveals that there is indeed swelling occurring *on average*. The extent of swelling is significantly less than what was expected from the previous study (Stavropoulou et al., 2019)—which is likely explained by a higher initial water content in the sample studied here, together with its different shape, size, and a potential confinement applied by the membrane

In order to look at swelling locally, a displacement field must be measured and strains computed. Of particular interest is to be able to compare local strains to changes in  $\mu_n$ , which should indicate—all other things being the same—water arrival. In this work, displacement fields are measured with two different image correlation techniques, non-rigid local correlation and global correlation, both available in the spam toolkit.

The local displacement field is measured by defining a regular grid of measurement points with an equal spacing of 40 pixels (in non-binned images, which means 1.7 mm) in all directions. Each point is represented by a cuboid subvolume of greylevels centred on the point. The overall registration is then used as an initial guess for the displacement of each measurement point. The volumetric strain can either be extracted from the determinant of a locally-measured  $\Phi$  as above, or by deriving the displacement gradient from the translation part of  $\Phi$  from neighbouring measurement points. The first approach is extremely noisy, and cannot be used meaningfully given the relatively subtle volumetric strains that are trying be to captured. The second

technique works well, however since measurement points are represented by subwindows and are used multiple times to measure strains, the physical space represented by a strain point is not direct. However, the displacement fields measured are of excellent quality, and are added to the data uploaded to Zenodo for a variety of subvolume sizes (see Data Availability Statement).

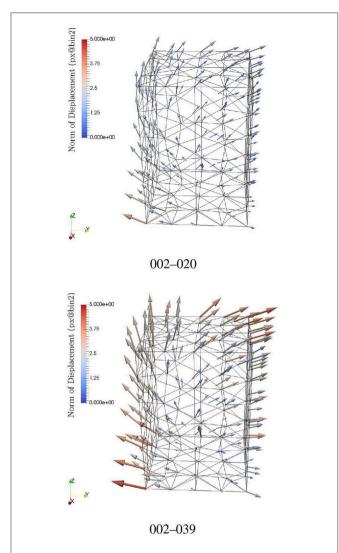
The lack of a direct interpretation of the physical subvolume represented by a strain measurement point in local DVC motivates the use of global DVC (Leclerc et al., 2011), where a continuous mesh is deformed to best match two images (to minimise  $\eta$  as above). In this case a cubic tetrahedral mesh of 360  $\times$  160  $\times$  160 pixels or 15.4  $\times$  6.8  $\times$  6.8 mm within the specimen is used. The edges are avoided since the current implementation of the technique has no mechanical regularisation and therefore problematic behaviour can occur on the edges. A characteristic size of tetrahedron of 80 pixels or 3.4 mm is found to give sufficiently low-noise in the strain computation<sup>1</sup>. The global convergence criterion is the norm of the displacement vector and for the correlations performed here, the criterion is slowly relaxed from 0.01 px for the early steps to 0.15 px for the later ones. The mesh generated contains 448 tetrahedra, on which strains are computed from the obtained nodal displacements. Figure 7 illustrates the quality of the measured global displacement field in the two penultimate increments of the images presented in Figure 5 (the correlations of the last two images 002-049 and 002-050 present two diverging points on the boundary). Furthermore, **Figure 9** shows a part of the field measured.

# 3.3. Measurement of Local Greyscale Variations

Given the ability to follow material points through time with the displacement fields described above, the variation of the measured fields ( $\mu_x$  and  $\mu_n$ ) will now be discussed. Considering as an example the case of thermal expansion with no mass transfer, the expectation would be for the density of the material to reduce, and for both  $\mu_x$  and  $\mu_n$  to decrease proportionally to the change in density. In this experimental configuration however, it is likely that the swelling is caused by water interaction with the material. This hypothesis will be evaluated for the process being studied by looking at change of  $\mu_x$  and  $\mu_n$  inside each tetrahedron, compared to the expected change due to the measured volume change. The particular sensitivity of neutrons to water should reveal water entry into the clay matrix.

During fluid entry, two major phenomena will cause a variation in the absorption levels of x-rays and neutrons. On one hand, if the material swells, assuming (for now) mass conservation of the solid part, this implies that the mass density of the solid part will decrease, leading to a decrease in the level of attenuation. On the other hand, if the swelling is associated with an increase in the water content, then the presence of the additional fluid will modify the material's attenuation level (and

 $<sup>^1\</sup>text{This}$  validation is performed by "zooming"  $\mu_x$  002 by 1.01 in all directions and correlating the original image with the zoomed version of itself. The application of this 3% volumetric strain to the greylevels of  $\mu_x$  is done through interpolation which reduces noise. Variance is additive, so the variance is measured in the original image, and the missing noise is added to the zoomed image.



**FIGURE 7** | Displacement field as measured with Global DVC. The displacement at the nodes of the mesh is shown with vectors scaled up by  $25\times$ , and whose colour represents the norm of the vector. The mesh is shown in its reference state (i.e., in 002).

may increase it if the attenuation coefficient of water is higher than the solid).

Considering that the infinitesimal volume can be decomposed into a solid part "s," a free water part " $w_f$ ," an adsorbed water part " $w_a$ " and air "a," the decomposition in the initial configuration (time 0) and the deformed configuration (time t) is (in the style of Coussy, 2007):

$$\Omega_0 = \Omega_0^{s} + \Omega_0^{w_f} + \Omega_0^{w_a} + \Omega_0^{a}$$
 (2)

and

$$\Omega_{t} = \Omega_{t}^{s} + \Omega_{t}^{w_{f}} + \Omega_{t}^{w_{a}} + \Omega_{t}^{a}$$
(3)

with

$$\Omega_{\rm t} = J\Omega_0 \tag{4}$$

where *J* is the Jacobian of the transformation i.e.,  $J \approx 1 + \varepsilon_v$ . A number of hypotheses are made:

First it is assumed (common assumption in soil mechanics), that the volume of the solid skeleton does not change in time, leading to  $\Omega_0^s = \Omega_t^s$ .

Furthermore, we assume that the density of free water is close to the density of adsorbed water, and consequently that the attenuation coefficients are the same:  $\mu^{w_f} \approx \mu^{w_a} \approx \mu^{w}$ . This is supported by recent work at the nano-scale on the properties of adsorbed water, see Honorio et al. (2017) and Brochard (2019).

If we now consider a voxel ( $\Omega_{\text{voxel}} = \text{cst}$ ), each phase will contribute to the total attenuation through what we name here "partial attenuation"  $\beta$  and thus,

$$\mu = \beta^{s} + \beta^{w} + \beta^{a} \tag{5}$$

This assumes that the measured attenuation coefficient of the material is the result of a Gaussian mixture of the component attenuation coefficients. The partial attenuation of each phase is the attenuation of the phase weighted by the volume fraction of  $O^i$ 

the phase as follows:  $\beta^i = \mu^i \frac{\Omega^i}{\Omega}$  where i is {s, w, a}.

In the case of a fully saturated sample,  $\Omega_a = 0$  and thus,

$$\frac{\Omega_{\rm t}^{\rm w}}{\Omega_{\rm t}} = 1 - \frac{\Omega_{\rm t}^{\rm s}}{\Omega_{\rm t}} = 1 - \frac{1}{I} \frac{\Omega_{\rm 0}^{\rm s}}{\Omega_{\rm 0}} \tag{6}$$

In terms of solid partial attenuation, we have:

$$\beta_0^s = \mu^s \frac{\Omega_0^s}{\Omega_0}$$
 and  $\beta_t^s = \mu^s \frac{\Omega_t^s}{\Omega_t} = \frac{1}{J} \beta_0^s$  (7)

In terms of water partial attenuation, we have initially:

$$\beta_0^{\rm w} = \mu^{\rm w} \frac{\Omega_0^{\rm w}}{\Omega_0} = \mu^{\rm w} \left(1 - \frac{\Omega_0^{\rm s}}{\Omega_0}\right) \quad \text{which leads to} \quad \frac{\Omega_0^{\rm s}}{\Omega_0} = 1 - \frac{\beta_0^{\rm w}}{\mu^{\rm w}} \tag{8}$$

and at time *t*:

$$\begin{split} \beta_{\mathrm{t}}^{\mathrm{w}} &= \mu^{\mathrm{w}} \frac{\Omega_{\mathrm{t}}^{\mathrm{w}}}{\Omega_{\mathrm{t}}} = \mu^{\mathrm{w}} \Big( 1 - \frac{1}{J} \frac{\Omega_{0}^{s}}{\Omega_{0}} \Big) = \mu^{\mathrm{w}} \Big[ 1 - \frac{1}{J} \Big( 1 - \frac{\beta_{0}^{\mathrm{w}}}{\mu^{\mathrm{w}}} \Big) \Big] \\ &= \frac{1}{J} \beta_{0}^{\mathrm{w}} + \mu^{\mathrm{w}} \Big( 1 - \frac{1}{J} \Big) \end{split} \tag{9}$$

Injecting these expressions of  $\beta$  into Equation (5) at time t gives:

$$\mu_{t} = \beta_{t}^{s} + \beta_{t}^{w} = \frac{1}{J}\beta_{0}^{s} + \frac{1}{J}\beta_{0}^{w} + \mu^{w} \left(\frac{J-1}{J}\right)$$
 (10)

Finally, the change in attenuation will be:

$$\Delta \mu = \mu_{\rm t} - \mu_0 = \frac{1 - J}{J} (\beta_0^{\rm s} + \beta_0^{\rm w} - \mu^{\rm w}) \tag{11}$$

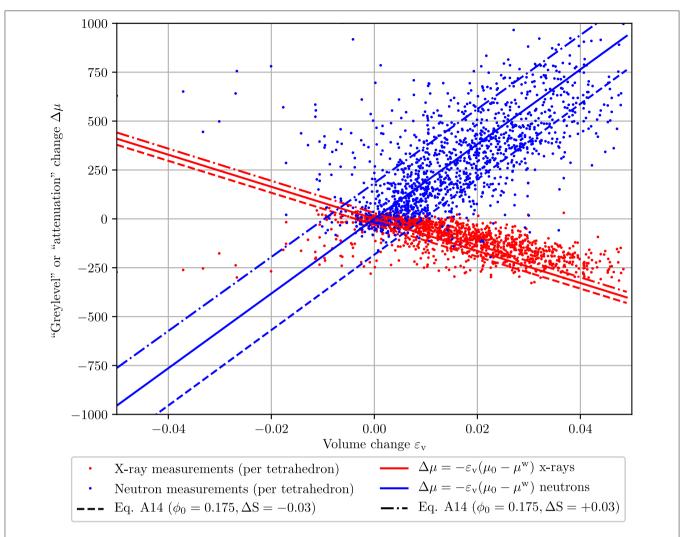


FIGURE 8 | Data from Global DVC on increments 002-020, 002-039, and 002-0045. Volumetric strain of each tetrahedron plotted against the measured greylevel change in each tetrahedron. Expected changes of greylevel due only to the solid are added as per Equation (12). These scattered values for x-rays and neutrons are fitted with a linear regression separately.

For small strains,  $J \approx 1 + \varepsilon_v$ , thus Equation (11) becomes,

$$\Delta \mu = -\varepsilon_{\mathbf{v}}(\beta_{\mathbf{0}}^{\mathbf{s}} + \beta_{\mathbf{0}}^{\mathbf{w}} - \mu^{\mathbf{w}}) = -\varepsilon_{\mathbf{v}}(\mu_{\mathbf{0}} - \mu^{\mathbf{w}}) \tag{12}$$

This model indicates, *in fine* that the change in attenuation coefficient (for both x-ray and neutron tomographies) is a simple function of the volumetric strain and two easily measurable greyscale quantities. For x-ray tomography,  $\mu_0$  is higher than the water absorption coefficient  $\mu^{\rm w}$  (as detailed in **Table 2**), meaning that swelling due to water uptake should induce a decrease of the global absorption coefficient. This is the reverse for neutron tomography, where  $\mu^{\rm w}$  coefficient is much higher than  $\mu_0$  absorption coefficient, and so the swelling due to water uptake induce an increase of the global absorption coefficient.

Figure 8 presents two quantities plotted together:

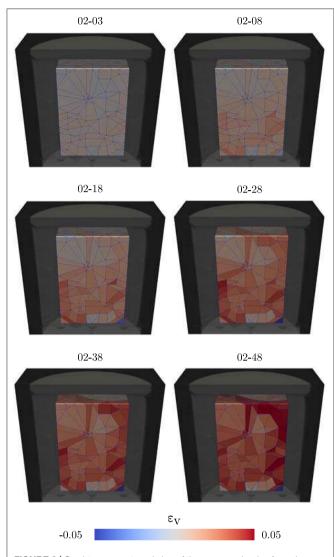
x axis The volumetric strain measured locally (i.e., on the tetrahedra in the mesh discussed above) always taking image 002 as a reference. This measurement comes directly from

the displacements of the mesh at the four nodes involving each tetrahedron.

y axis The change in greylevels  $\Delta\mu_x$  and  $\Delta\mu_n$  in each tetrahedron. This is computed as follows: All the voxels belonging to one tetrahedron are identified in the reference mesh, as well as in the deformed mesh. The mean value in the field corresponding to these voxels (which can be of different number in reference and deformed states) is recorded, and the difference is plotted here.

Each point in the space presented represents the evolution (of size and greyscale) of one tetrahedron.

Figure 8 also includes the prediction as per Equation (12) in solid lines, taking  $\mu_0$  as the mean measured value for the clay matrix from **Table 2**. The correspondence is quite satisfactory. The success of this simple model seems to indicate that the essential parts of the physics occurring have been captured adequately. Allowing a small change on the measured  $\mu_0$  for x-rays an even better correspondence can be obtained (not shown).



**FIGURE 9** | Semi-transparent rendering of the x-ray graylevels of specimen (state 002) with the mesh used for the total global correlation with tetrahedra colored by their volumetric strain. Using Equation (12) and its assumptions, the color bar for  $\varepsilon_{\rm V}$  corresponds to  $\frac{\delta\Omega^{\rm W}}{\delta\Omega}$ .

A more sophisticated mathematical model is developed in the **Appendix** releasing the hypothesis that  $\Omega^a=0$  (thus allowing states of partial water saturation) and with the hypotheses that the volume of macro-voids does not change, and that swelling occurs only due to water adsorbed onto the clay aggregates  $\Omega^{\text{Wa}}_t=\Omega^{\text{Wa}}_0+(J-1)\Omega_0$  (also valid above).

The upshot is that the change in greylevels can now be expressed as a function of volumetric strain (as before) and a new term linking the change of degree of saturation ( $\Delta S$ ) and the initial degree of open porosity ( $\phi_0$ ):

$$\Delta \mu = -\varepsilon_{\rm v}(\mu_0 - \mu^{\rm w}) + (1 - \varepsilon_{\rm v})\Delta S \,\phi_0(\mu^{\rm w} - \mu^{\rm a}) \tag{13}$$

This additional term allows the exploration of the influence of the change of degree of saturation during swelling. Taking  $\phi_0$  as

17.5 % from Conil et al. (2018),  $\Delta S$  can be evaluated, and lines for  $\pm 3$  % are shown in **Figure 8**.

Returning to the fully saturated model, the spatial distribution of volumetric strain can be directly related to the increase of water  $(\varepsilon_{\rm V} = \frac{\Omega^{\rm w}}{\Omega})$ . **Figure 9** presents a slice through half the sample colouring the tetrahedra in the analysed zone according to their volumetric strain for a few selected time intervals. In the first time increments an increase of strain at the bottom of the sample (which is in contact with the water supply) is visible, whereas toward the end of the experiment high values are recorded all over, with some indication of inhomogeneous levels of swelling.

### 4. CONCLUSION

This paper has presented a combined neutron and x-ray tomography analysis of water absorption behaviour in Callovo-Oxfordian claystone. These complementary imaging techniques are first of all registered into a common coordinate system using previous work, as well as a specially-developed graphical user interface to provide an initial guess. The resulting registered neutron and x-ray images of each state allow first of all a fine identification of the material phases present in the sample.

To characterise the gentle swelling process observed (around 2.5% overall volumetric increase after almost 6h) again the combination of x-rays and neutrons is exploited: local swelling is measured with Digital Volume Correlation thanks to the sharpness and low noise of the x-ray volumes (although it is mentioned that a correlation on the joint x-ray and neutron field could be developed in future). A mathematical model is developed for the expected local changes of greylevels in saturated conditions with all volume changes associated with water entry. The measurements are compared to this model with a good degree of correspondence, indicating that for this experiment on this sample, the model appears sufficient. This indicates that there are limited amounts of swelling due to chemical interactions for example.

This initial hydromechanical analysis (performed on a single sample) will obviously benefit from repetition, but a number of technical improvements to the analysis can also be envisioned.

- Anisotropic swelling–Instead of a scalar  $(\varepsilon_v)$  representing the change of volume of the material, the stretch tensor itself could be used to measure anisotropic parts of swelling related to the bedding known to affect this material.
- Taking into account microstructure-here the analysis has
  focused on the averaged local behaviour of the clay matrix.
  Further steps in the analysis could identify different types of
  inclusions known to be present (carbonates, quartz, pyrite)
  from the joint histograms, and relate a local degree of swelling
  to the presence of these aggregates.
- Taking into different initial states-further experiments are certainly necessarily, and of chief interest is to study different initial water contents as well as different stress states.
- Taking into account permeability/swelling times—The analysis
  as it stands implies a "time-free" relationship between water
  arrival and volumetric strain, whereas the characteristic times
  related to the very low permeability in the material may be

interesting to include in the model, and which would explain long distance interactions through fluid pressure/suction.

Finally, a number of recommendations can be made for better estimations of the reconstructed attenuation coefficients:

- 1. Ensure that sufficient pure water is visible in a scan (on the neutron side in this case there are only 2 slices inside the spiral. Scanning a pure sample of water is also possible, but as far as neutron tomography is concerned, this must be a small cross-section to minimise the effects of scattering.
- 2. Given the importance that the mathematical model puts on the "physical" meaning of greyvalues, a long initial scan with lower noise provides a valuable reference for all  $\mu$  values.
- 3. Selection of a less neutron-attenuating membrane material such as Teflon, or fluorinated silicons.

## **DATA AVAILABILITY STATEMENT**

The raw datasets collected on NeXT-Grenoble are available at http://doi.ill.fr/10.5291/ILL-DATA.UGA-42 – the experiment analysed is 03-3N5. Furthermore, a number of key outputs from this paper are available on Zenodo https://zenodo.org/record/3628018 with doi: 10.5281/zenodo.3628018.

- **01-volumes** Registered  $\mu_x$  and  $\mu_n$  fields at a pixel size of 85.4  $\mu$ m/px which is 2-binning for the x-ray volumes.
- **02-JH** Dynamic Joint histograms for all pairs of registered  $\mu_x$  and  $\mu_n$  fields calculated over the mask available in folder 01.

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## **AUTHOR CONTRIBUTIONS**

All authors listed have made a substantial, direct and intellectual contribution to the work, and approved it for publication.

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**Conflict of Interest:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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# APPENDIX – THEORETICAL TREATMENT OF PARTIALLY SATURATED CASE

In order to relax the previous hypothesis of full saturation, a non-zero air volume must be allowed:  $\Omega^a \ge 0$ .

Introducing  $\phi_0$  as the macro-porosity or "open" voids volume-fraction at time 0:

$$\Omega_0^{\text{voids}} = \Omega_0^{\text{a}} + \Omega_0^{\text{w}_{\text{f}}} = \phi_0 \Omega_0 \tag{A1}$$

A hypothesis is however needed for the evolution of the voids volume with time during swelling; here we assume that the macro-porosity *volume* remains constant in time.

$$\Omega_t^a + \Omega_t^{W_f} = \Omega_0^a + \Omega_0^{W_f} = \phi_0 \Omega_0 \tag{A2}$$

With *S* as the degree of saturation:

$$\Omega_0^{w_f} = S_0 \Omega_0^{voids}$$
 and  $\Omega_t^{w_f} = S_t \Omega_t^{voids}$  (A3)

 $\Delta S$  is then defined as the change in degree of saturation between time 0 and time t:

$$\Delta S = S_t - S_0 \tag{A4}$$

Moving onto partial attenuations, for the solid part nothing changes:  $\beta^s_{\rm t}=\frac{1}{\tau}\beta^s_0$ 

For the water part:

$$\beta_0^{\text{w}} = \mu^{\text{w}} \frac{\Omega_0^{\text{w}}}{\Omega_0} = \mu^{\text{w}} \left( S_0 \phi_0 + \frac{\Omega_0^{\text{wa}}}{\Omega_0} \right)$$
 (A5)

$$\beta_{t}^{w} = \mu^{w} \frac{\Omega_{t}^{w}}{\Omega_{t}} = \mu^{w} \left( \frac{S_{t} \phi_{0}}{J} + \frac{\Omega_{t}^{w_{a}}}{J \Omega_{0}} \right)$$
 (A6)

With the hypothesis that only the adsorbed water changes in volume during swelling:

$$\Omega_{\rm t}^{\rm w_a} = \Omega_0^{\rm w_a} + (J-1)\Omega_0 \tag{A7}$$

and factoring by  $\frac{1}{I}$ :

$$\beta_{t}^{W} = \frac{\mu^{W}}{J} \left( S_{t} \phi_{0} + \frac{\Omega_{0}^{W_{a}}}{\Omega_{0}} + J - 1 \right)$$
 (A8)

Now splitting  $S_t$  into  $S_0 + \Delta S$ :

$$\beta_{\rm t}^{\rm W} = \frac{\mu^{\rm W}}{I} \left( S_0 \phi_0 + \Delta S \phi_0 + \frac{\Omega_0^{\rm W_a}}{\Omega_0} + J - 1 \right)$$
 (A9)

Combining with  $\beta_0^{\text{w}}$  finally yields:

$$\beta_{t}^{w} = \frac{1}{I}\beta_{0}^{w} + \mu^{w} \frac{\Delta S}{I}\phi_{0} + \mu^{w} \frac{J-1}{I}$$
 (A10)

Finally for the air:

$$\beta_0^a = \mu^a \frac{\Omega_0^a}{\Omega_0} = \mu^a (1 - S_0) \phi_0 \tag{A11}$$

$$\beta_{t}^{a} = \mu^{a} \frac{\Omega_{t}^{a}}{\Omega_{t}} = \mu^{a} \frac{(1 - S_{t})}{J} \phi_{0}$$

$$= \frac{1}{J} \mu^{a} (1 - S_{0} - \Delta S)$$

$$\phi_{0} = \frac{1}{I} \beta_{0}^{a} - \mu^{a} \frac{\Delta S}{I} \phi_{0}$$
(A12)

The attenuation at time t,  $\mu_t$ , can now be expressed as:

(A5) 
$$\mu_{t} = \frac{1}{J} (\beta_{0}^{s} + \beta_{0}^{w} + \beta_{0}^{a}) + \mu^{w} \left( \frac{\Delta S}{J} \phi_{0} \right) + \mu^{w} \left( \frac{J-1}{J} \right) - \mu^{a} \left( \frac{\Delta S}{J} \phi_{0} \right)$$
(A13)

Subtracting  $\mu_0$  in the same spirit as above:

$$\Delta \mu = \frac{1 - J}{J} \mu_0 + \mu^{w} \left( \frac{\Delta S}{J} \phi_0 \right) + \mu^{w} \left( \frac{J - 1}{J} \right) - \mu^{a} \left( \frac{\Delta S}{J} \phi_0 \right)$$
(A14)

In small strains:

$$\Delta \mu = -\varepsilon_{\rm v}(\mu_0 - \mu^{\rm w}) + (1 - \varepsilon_{\rm v})\Delta S\phi_0(\mu^{\rm w} - \mu^{\rm a}) \qquad (A15)$$