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Evaluation methods and engineering applications of *in-situ* stress in deep, strong heterogeneity terrestrial shale oil and gas reservoirs: a case study of jurassic shales in the Yingshan-Pingchang area, northeast Sichuan

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Introduction: The Jurassic terrestrial shale in the Yingshan–Pingchang area of the northeastern Sichuan Basin holds substantial exploration and development potential. However, the area exhibits significant vertical heterogeneity and anisotropy in *in-situ* stress. Thus, precise vertical evaluation of *in-situ* stress is urgently required to provide a scientific basis for selecting hydraulic fracturing layers in future operations.

Methods: This study conducted a detailed *in-situstress* analysis utilizing paleomagnetic data, velocity anisotropy measurements, differential strain experiments, hydraulic fracturing results, and both conventional and specialized logging data. A transversely isotropic *in-situstress* prediction model was developed to evaluate the stress distribution, aiming to identify target layers favorable for hydraulic fracturing.

Result: Comprehensive analysis indicates that the *in-situstress* orientation of Jurassic shale in the Yingshan-Pingchang area generally aligns with the regional stress orientation (NE90° \pm 10°). Due to the influence of local NW-trending structures, the *in-situstress* orientation exhibits a clockwise deflection. In the Jurassic formation, the maximum horizontal principal stress ranges from 42.33 MPa to 102.56 MPa, averaging 74.89 MPa; the minimum horizontal principal stress ranges from 39.20 MPa to 84.04 MPa, averaging 67.20 MPa; and the vertical principal stress varies between 31.91 MPa and 91.39 MPa, averaging 60.23 MPa. These findings were corroborated by *in-situstress* magnitudes determined via differential strain analysis are highly accurate. The analysis of the three-dimensional stress relationships indicates that the study area predominantly exhibits a strike-slip faulting regime. Comparative analysis reveals

that the minimum principal stress gradient in shale is higher than that in limestone and sandstone. Furthermore, the transverse isotropic *in-situs*tress prediction model demonstrates high accuracy. When comparing its predictions for minimum and maximum horizontal principal stresses to measured *in-situs*tress data, the model exhibits average relative errors of only 3.39% and 3.23%, respectively.

Discussion: In the study area, vertical high-low-high (HLH) stress difference profiles exhibit the highest oil-bearing potential and a reduced likelihood of fracturing-induced artificial fractures crossing through layers. This makes HLH profiles the optimal structural type for selecting fracturing stages in *in-situ*stress difference fracturing operations.

KEYWORDS

terrestrial shale oil and gas, strong heterogeneity, *in-situ* stress orientation and magnitude, VTI formation, transversely isotropic

1 Introduction

Following the significant breakthroughs of the 'Shale Revolution' in North America, a global surge in the exploration and development of marine shale oil and gas resources has been ignited (Jarvie et al., 2007; Wang et al., 2014). Concurrently, the successful exploitation of terrestrial shale oil in the Uteland Butte member of the Green River Formation in the Uinta Basin, United States, has sparked widespread interest in terrestrial shale resources (Vanden Berg et al., 2014). According to the 2015 EIA report on shale oil resources across 45 countries (excluding the United States), among the 101 shale oil basins and 152 shale oil formations worldwide, 24 formations are classified as lacustrine, accounting for approximately 19% of the total shale oil resources. In recent years, successful cases of lacustrine shale oil and gas development have been documented in Argentina and China (Legarreta and Villar, 2011; Wang et al., 2014), while numerous promising lacustrine shale basins are also present in Africa, Asia, and Europe, offering substantial economic potential. Notably, China, Chad, and Indonesia possess significant lacustrine shale oil and gas resources, with technically recoverable reserves estimated at 41.3 billion tonnes, 19.2 billion tonnes, and 10.8 billion tonnes, respectively, representing approximately 46.4%, 21.7%, and 12.2% of the global total (excluding the United States) (US ElA, 2015).

The large-scale development of marine shale gas has led to innovations in shale oil and gas enrichment theories (He and Bai, 2022; Hu et al., 2023). With the rapid advancement of exploration theories and development technologies (Guo et al., 2023; Chen and Liu, 2024), China, as a major country rich in lacustrine shale oil resources, is gradually expanding exploration into more extensive lacustrine shale formations. Significant breakthroughs have been achieved in the Cretaceous formations of the Songliao Basin, the Permian formations of the Junggar Basin, the Paleogene formations of the Bohai Bay Basin, and the Triassic formations of the Ordos Basin (Feng et al., 2015; Guo et al., 2023; Bao et al., 2023; Chen and Liu, 2024; Du et al., 2024). In the Sichuan Basin, the exploration and development of terrestrial shale oil and gas are concentrated in the Middle and Lower Jurassic strata. Five oil-bearing segments have been developed sequentially from the bottom up, including the Zhenzhuchong, Dongyuemiao, Da'anzhai, Lianggaoshan, and Shaximiao formations, all of which have yielded industrial-scale oil and gas (Feng et al., 2015; Li et al., 2016; Zhang et al., 2023; Xiong et al., 2024). Compared to the marine shales in the Sichuan Basin, Jurassic shale, claystone, siltstone, sandstone, carbonate rock, tuff, and other interbedded formations exhibit more frequent longitudinal interactions (Fang et al., 2023; Yang et al., 2023). Under the background of complex tectonics and high stress, the Jurassic shale exhibits characteristics such as great burial depth, high formation pressure, and strong vertical heterogeneity and anisotropy (Zhang et al., 2023; Shu et al., 2024). These factors pose a series of challenges in evaluating of shale oil and gas resources, reservoir characterization, and the selection of sweet spots. Therefore, accurate assessment of the vertical distribution characteristics of *in-situ* stress is critical.

In-situ stress, also known as original rock stress, refers to the natural forces present within the Earth's crust that remain undisturbed by engineering activities (Wang et al., 2010). It primarily arises from the interplay of gravitational stress, tectonic stress, pore pressure, thermal stress, and residual stress (Ganguli et al., 2018; Baouche et al., 2021; Ganguli et al., 2021; Yong et al., 2022). Regarding the identification of in-situ stress in terrestrial shale oil and gas reservoirs (Lv et al., 2017), we determined the orientation of in-situ stress for the Xinchang Xujiahe V section in western Sichuan using paleomagnetic and anisotropy experiments. Additionally, Cai (2023) obtained measured values of in-situ stress for the Shahejie Formation in the Bohai Bay Basin through core acoustic emission Kaiser effect experiments and limited LOT data. He et al. (2024) identified the timing of the ancient tectonic stress in northeastern Sichuan's Jurassic by determining the Kaiser effect points from acoustic emission tests. Li (2016) conducted differential strain measurements on cores from the Shahejie Formation in the Bohai Bay Basin, quantifying strain variations in multiple directions and calculating the magnitude and orientation of in-situ stress using elastic mechanics theory.

Regarding the prediction of *in-situ* stress in terrestrial shale oil and gas reservoirs, Yu et al. (2020) and Xiong et al. (2023) determined the magnitude of *in-situ* stress for the fracturing intervals of the Yanchang Formation in the Ordos Basin and the Fengcheng Formation in the Zhungeer Basin using fracture pressure calculation methods. They employed a spring-combination model to calculate the tectonic strain coefficients for the orientations of the maximum and minimum principal stresses. Wang (2021) established an *in-situ* stress model for the Yanchang Formation in the Ordos Basin, considering both isotropic and transverse isotropic properties. Wang (2022) further identified key parameters in the model through core mechanical experiments and compared the predicted *in-situ* stress results with actual measurements, confirming that the transversely isotropic model yielded the smallest errors. Lin et al. (2022a) compared the accuracy of the combined spring *in-situ* stress calculation model with that of the transversely isotropic *in-situ* stress calculation model, concluding that the transversely isotropic model provided higher accuracy for terrestrial shale in the Fengcheng Formation of the Zhungeer Basin.

Exploration experiences from various regions worldwide indicate that lacustrine shale formations exhibit complex geological characteristics and strong reservoir heterogeneity, with in-situ stress playing a crucial role in controlling reservoir stimulation effectiveness. Compared to marine shales, terrestrial shale reservoirs are generally more compact, exhibit greater variability in brittle mineral content, and develop more complex interbedded layers. These factors collectively determine the critical influence of insitu stress on reservoir stimulation outcomes. However, research on *in-situ* stress in terrestrial shales remains insufficient, with limited findings and a relatively nascent stage of development. The applicability of conventional *in-situ* stress identification and prediction methods established for marine shales to lacustrine shale formations requires further verification and optimization. Therefore, establishing a comprehensive *in-situ* stress identification and evaluation framework based on multi-source data integration and multi-method analysis has become a critical focus in terrestrial shale research (Cao et al., 2020; Gao et al., 2023; Peng, 2023; Sun et al., 2023).

This study focuses on the Jurassic terrestrial shale in the Yingshan-Pingchang region of the northeastern Sichuan Basin. Using methods such as core testing, well logging identification, and field measurements, the in-situ stress orientation and magnitude of the target formation were identified, calculated, and validated. A transverse isotropic in-situ stress calculation model was developed, completed the interpretation of in-situ stress profiles for wells. Additionally, the structural characteristics of stress difference were optimized. Meanwhile, to enhance the development efficiency of terrestrial shale oil and gas resources, it is crucial to focus on the controlling effect of in-situ stress on fracture initiation and propagation within the reservoir. This research provides essential technical support for the efficient calculation of in-situ stress in terrestrial shale reservoirs, facilitating the development of a refined identification framework applicable to different basins. Furthermore, it offers scientific guidance for safe well drilling, optimized reservoir stimulation, and long-term stable production.

2 Geological background

The Sichuan Basin, located in the southwestern part of China, is a typical superimposed oil and gas basin (Liu et al., 2021). It is situated in the western part of the Yangtze Plate and is an east-west extending basin overall (Zhang et al., 2011). The basin began to take shape during the Indosinian period and underwent folding and deformation during the Himalayan orogeny, forming its presentday structure (Liu et al., 1994). The basin can be divided into six structural units (Figure 1A) (Zhang et al., 2011): the northern Sichuan low gentle zone, the western Sichuan low steep zone, the central Sichuan gently sloping zone, the southwestern Sichuan fold zone, the southern Sichuan low-steep dome-shaped zone, and the eastern Sichuan high-steep fault-fold zone.

During the Mesozoic-Cenozoic era, the northeastern Sichuan area experienced reverse thrusting along the Micangshan and Dabashan basins. This was followed by multiple superimposed and reworked tectonic stresses from various orientations, resulting in the area's complex tectonic deformation characteristics (Figure 1B) (He et al., 2024). The main tectonic orientations in the northeastern Sichuan area are predominantly northeast, northwest, and nearly east-west (He and Bai, 2022). The junction area between the Micangshan and Dabashan basins experienced three major tectonic events during the Indosinian, Yanshan, and Himalayan periods. Tectonic movements during the Yanshan and Himalayan periods had the most significant impact on the formation of tectonic deformation in the region (Zhu, 2020). The Jurassic system in northeastern Sichuan develops extruding and compression-torsion reverse faults, resulting in a tectonic pattern characterized by two uplifts, one concave structure, and one gentle slope across the area (Jiang et al., 2016). Simultaneously, compressive forces originating from the Dabashan region resulted in the formation of numerous east-west-trending syn-sedimentary faults within the area (Figure 1C) (Wang et al., 2024). These faults, characterized by minor displacements and predominantly terminating in the upper strata of the Lianggaoshan Formation, are highly conducive to enhancing reservoir quality and preserving hydrocarbons.

The Jurassic formation in northeastern Sichuan is primarily composed of delta-lacustrine terrestrial clastic rock deposits, with thicknesses ranging from 1,500 to 4,000 m. It exhibits a characteristic pattern of greater thickness in the north and west, and reduced thickness in the south and east (Xu, 2023). From bottom to top, several oil and gas-bearing layers have developed, including the Ziliujing Formation (comprising the Zhenzhuchong, Dongyuemiao, Ma'anshan, and Da'anzhai Sections), the Lianggaoshan Formation, and the Shaximiao Formation (Figure 1C) (Ni et al., 2015; Li et al., 2016). The Jurassic system underwent three major phases of lake transgression. The first phase of lake transgression occurred in the Dongyuemiao member of the Ziliujing Formation, with lithology primarily characterized by mud shale intercalated with limestone and small amounts of fine sandstone. The second phase of lake transgression took place in the Da'anzhai member, where the early to middle period was characterized by a transgressive process, with the maximum transgression occurring during the middle of the deposition (Chen et al., 2019). The overall lithology of the Da'anzhai member is characterized by mud shale intercalated with limestone. The third phase of lake transgression was marked by deeper water and a calm lake surface, with lithology composed of mud shale intercalated with fine sandstone. The Lianggaoshan Formation is divided into two sub-members: the Upper Lianggaoshan and Lower Lianggaoshan. The Lower Lianggaoshan member consists of mudstone intercalated with fine sandstone, while the Upper Lianggaoshan member differs, featuring organic-rich shale intercalated with fine sandstone (Chen and Liu, 2024).



FIGURE 1

(A) Structural zoning map of the Sichuan Basin; (B) Structural map of northeastern Sichuan Basin; (C) Comprehensive stratigraphic column of Lower Jurassic Formation; (D) Demonstrate the materials covered in this study.

3 Sample source and methods

3.1 Workflow and samples

3.1.1 Workflow

In the research process of this study, we utilized a variety of sources for our research (Figure 1D). We first used core paleomagnetism and velocity anisotropy experiments, combined with imaging logging and dipole shear wave interpretation, to evaluate the direction of *in-situ* stress. Using core differential strain experiments and hydraulic fracturing test data, completed the interpretation of *in-situ* stress magnitude. Secondly, we constructed a transverse isotropic *in-situ* stress calculation model and assigned values to all parameters within the model. Finally, we performed a detailed evaluation of *in-situ* stress for wells. The following sections provide a detailed explanation of the core experimental methods.

3.1.2 Samples

The samples used in this experiment were primarily obtained from core samples taken from ten wells in the Yingshan-Pingchang area of northeastern Sichuan. These samples underwent paleomagnetic testing, velocity anisotropy testing, differential strain testing, and rock mechanics testing.

3.2 Paleomagnetic experiment

Paleomagnetic experiments can be used to restore the original orientation of core samples in the subsurface. In this regard, a viscous remanence measuring instrument was employed, implemented in accordance with the DD 2006-04" Paleomagnetic Test Technical Requirements" standard.

First, a reference line parallel to the core axis is drawn on the core surface, which serves as a common reference for both the paleomagnetic and ultrasonic anisotropy experiments. Cylindrical samples of $25 \times 25 \text{ mm}$ are drilled along the axial direction, and parallel reference lines are drawn on the cylindrical surface, passing through the center of the core's end surface (Figure 2A). The remanent magnetization strength and orientation are measured at 20°C. The sample is then subjected to thermal demagnetization treatment, which typically involves heating the sample from room temperature to a set temperature, cooling it to room temperature in a zero-magnetic environment, and measuring the remanent magnetization strength. The temperature is subsequently raised, and measurements are repeated. The thermal demagnetization steps are conducted at intervals of 40°C, with remanent magnetization strength and direction measured at temperatures ranging from 60°C to 300°C. Finally, the standard Fisher statistical method is employed to calculate the average orientation of the viscous remanent magnetization in the geomagnetic coordinate system, thereby restoring the original orientation of the core in the subsurface (Figure 3A).

3.3 Wave velocity anisotropy experiment

Stress orientation can be determined through the analysis of core ultrasonic wave velocity anisotropy. The experiment was

conducted in accordance with the DZ/T0276.31-2015" Rock Mass Acoustic Velocity Test" standard. The experiment utilized the wave velocity anisotropy module of the multi-function rock mechanics instrument (GCTS-RTR-2000, GCTS, United States), which primarily consists of a core holder, an ultrasonic probe, and an automatic expansion device for the probe. This testing system can measure the wave velocity of longitudinal (P-wave) and transverse (S-wave) waves, with P-waves selected for wave velocity anisotropy testing.

The sample is processed into a cylindrical specimen with dimensions of $25 \text{ mm} \times 50 \text{ mm}$ (Figure 2B). A reference line is marked on the full-diameter core, parallel to the wellbore orientation, with an arrow pointing toward the top surface. This reference line is maintained consistently with the paleomagnetic reference line. The time taken for longitudinal wave propagation along the diameter at the reference line is measured using an ultrasonic device. Propagation time is measured at 10° intervals in a clockwise direction along the diameter, and velocity deviation is calculated. A curve of velocity deviation is plotted, and the angle corresponding to the minimum velocity represents the angle between the maximum horizontal principal stress and the reference line (Figure 3B). The orientation of the maximum principal stress at the reference line, combined with the paleomagnetic orientation results, allows for the determination of the orientation of the maximum horizontal principal stress. The calculation Formula 1 is as follows:

$$\alpha = \beta + \theta \tag{1}$$

In this formula: α is the orientation of the maximum horizontal principal stress, in °, β is the orientation of the core as determined by paleomagnetic data, in °; θ is the angle between the maximum principal stress and the reference line, in °.

3.4 Differential strain experiment

The differential strain experiment determines the overburden pressure, maximum horizontal principal stress, and minimum horizontal principal stress exerted on a cubic rock core under subsurface conditions by measuring strain changes in three orthogonal directions during hydrostatic pressure loading. The experiment was conducted in accordance with the DZ/T0276.20-2015"Testing Procedures for Physical and Mechanical Properties of Rocks" standard. The loading apparatus employed the WTB3824 static strain measurement system, which can automatically, accurately, reliably, and quickly measure static strain values at multiple points during stress testing of large structures, models, and materials.

The differential strain measurement experiment requires processing the core into cubic samples with dimensions of 50 mm \times 50 mm (Figure 2C), with a strain gauge array attached to each of the three mutually perpendicular surfaces. After sealing the sample with silicone rubber, it is placed in a pressure vessel where hydrostatic pressure is applied until it exceeds the expected *in-situ* stress, causing microcracks to fully close. Strain variations in each orientation before and after the closure of the microcracks are measured



FIGURE 2

(A) Photograph of samples before paleomagnetic and wave velocity anisotropy experiment; (B) Photograph of samples after paleomagnetic and wave velocity anisotropy experiment; (C) Photograph of the sample before the differential strain experiment; (D) Photograph of the sample after the differential strain experiment.



(A) Palaeomagnetic experiment core positioning diagram; (B) wave velocity deviation with the change of circumferential angle curve, well YY1H, 2017.46 m.

using nine strain gauges on the surface of sample (Figure 2D). The six strain components based on the core coordinate system are then calculated, and the ratios of the three principal stresses are determined using elasticity theory. The pressure at the microcrack closure point is used as the maximum principal stress, or vertical stress is estimated based on the core sample's depth. Finally, the three-dimensional stress magnitude at the location is calculated by combining the principal stress ratios.

3.5 Rock mechanics test experiment

In this experiment, a triaxial rock mechanics test system (RTR-1000, GCTS, America) was used to apply the stress to the specimen until the rock reaches the yield strength. The test process is in accordance with the GB/T50266-99"Standard for test methods of engineering rock mass."

3.6 VTI *in-situ* stress magnitude logging calculation model

The calculation process for the anisotropic *in-situ* stress magnitude using VTI media-based logging parameters consists of the following five steps: (1) calculate vertical stress; (2) calculate pore pressure; (3) calculate rock mechanical parameters; (4) invert tectonic stress coefficients; and (5) calculate the *in-situ* stress magnitudes.

4 Results

4.1 In-situ stress orientation evaluation

4.1.1 Paleomagnetic and velocity anisotropy experiment results

Combining paleomagnetic and velocity anisotropy experimenting, the results show that the current *in-situ* stress orientation of the Jurassic formation in the Pingchang area ranges from N82.7° to N116.65°E, with the main direction concentrated at N95° \pm 10°E. In the Yingshan area, the stress orientation range is from N76° to N111.6°E. The maximum principal stress orientation at well YY1H ranges from 71.77° to 106.45°, while at well PY1, it ranges from 59.1° to 85.6° (Table 1). Due to the influence of local NW-trending structures, the *in-situ* stress orientation is deflected clockwise, and the three-dimensional stress regime exhibits a strikeslip stress regime. The stress orientation at well YY1H shows a slight clockwise deflection due to its proximity to the fault.

4.1.2 Imaging logging for determining the *in-situ* stress orientation

The resistivity differences in wellbore imaging logging can explain rock fractures caused by stress. By utilizing these characteristics, the orientation of the maximum horizontal stress can be further determined (Andrew et al., 2016; Ju et al., 2018). During the drilling process, due to the coupling of wellbore stress concentration and mud pressure, induced fractures or wellbore breakouts can form under specific conditions. The former is manifested in wellbore imaging logging as approximately vertical or feather-like dark bands or a single feather-like dark band (Figures 4A, B), with their orientation indicating the orientation of the maximum horizontal principal stress (Zoback et al., 2003; Colleen et al., 2009; Schmitt et al., 2012). The latter appears in wellbore imaging logging as an approximately symmetric distribution of dark bands or patches, which are discontinuous along the longitudinal orientation with blurred boundaries (Figures 4C, D). The long axis of the breakout is generally parallel to the orientation of the minimum horizontal principal stress

(Zoback et al., 2003; Ju et al., 2018). The wellbore imaging logging at depths of 1044-1046 m in well YS8 characteristics is represented by feather-like dark bands arranged in a fan-shaped pattern, while at depths of 1581-1583 m in well YS5, a single feather-like dark band is observed. Based on the identified orientation of the induced fractures, the orientation of the maximum horizontal principal stress for the corresponding intervals in the two wells is 185° and 176°, respectively. The wellbore imaging logging at depths of 3,424-3,426 m in well DY1 and 1581-1583 m in well YS8 show significant wellbore breakouts, with breakout orientations of 6° and 80°, respectively. The interpreted orientations of the maximum horizontal principal stress are 96° and 170°, respectively. In intervals with more developed fractures, false breakout phenomena can easily be observed in borehole imaging imaging. Caution should be exercised during the identification process to avoid misinterpretation.

Electrical imaging logging interpretation software was utilized to identify induced fractures and wellbore breakouts in the DY1 well. The interpretation results indicate that the current stress orientation is primarily EW (Figure 4E).

4.1.3 Dipole shear wave for determining *in-situ* stress orientation

For anisotropic formations, by considering the variation in shear wave velocities under different array configurations, can reveal the anisotropic characteristics of the subsurface rock layers (Heng et al., 2015). In anisotropic strata, *in-situ* stress primarily acts along different directions of the layers. Since the shear wave velocity is closely related to the anisotropy, particularly when the direction of shear wave propagation aligns with the stress direction, changes in velocity can reflect the direction of the *in-situ* stress. The polarization orientation of the fast shear wave indicates the maximum horizontal stress orientation. The time difference between the fast and slow waves is commonly used to measure the anisotropy of the formation. The stronger the anisotropy, the higher the reliability of the extracted data. The Formula 2 for calculating the anisotropy coefficient is as follows:

$$IDT = \frac{\Delta t_{ss} - \Delta t_{sf}}{\left(\Delta t_{ss} + \Delta t_{sf}\right)/2} \times 100\%$$
(2)

In this formula: Δt_{ss} is the time difference for the fast shear wave, in µs/ft; Δt_{sf} is the time difference for the slow shear wave, in µs/ft.

The interpretation of dipole shear wave logging indicates that the current *in-situ* stress orientation is primarily EW (Figure 5). The anisotropy analysis results show that as the difference coefficient between the two principal stresses increases, shear wave anisotropy becomes stronger, reducing the number of interpreted maximum principal stress orientations and increasing the reliability of the interpretation.

4.1.4 Changes in *in-situ* stress orientation

The current stress orientation in the Yingshan-Pingchang area of the Jurassic Formation, determined by comprehensive analysis of differential strain, electrical imaging logging, and dipole shear wave logging, is primarily in the EW orientation (Figure 6A). The orientation ranges from N $87^{\circ}-120^{\circ}$ E, with the main direction maintaining a consistent range of NE $95^{\circ} \pm 10^{\circ}$.

Number	Well name	Stratigraphy	Depth (m)	Lithology	Core orientation (°)	The angle between maximum principal stress and reference line (°)	The orientation of maximum principal stress (°)
1	PY1-5H	Upper Liang	3,554.30	Clayey shale	N99.80°E	0	N99.80°E
2	PY 1-5H	Upper Liang	3,562.82	Mixed shale	N111.65°E	175°	N116.65°E
3	PY 1-5H	Upper Liang	3,563.82	Clayey Shale	N105.95°E	5°	N100.95°E
4	PY 1-2H	Upper Liang	3,459.12	Fine sandstone	N105.70°E	170°	N95.70°E
5	PY 1-2H	Upper Liang	3,550.41	Feldspathic shale	N127.40°E	20°	N107.40°E
6	PY 1-2H	Upper Liang	3,462.41	Feldspathic shale	N104.20°E	0°	N104.20°E
7	YS5	Dongyuemiao	1893.90	Clayey shale	N135.75°E	145°	N100.75°E
8	YS 5	Dongyuemiao	1895.50	Clayey shale	N137.60°E	35°	N102.60°E
9	YS 8	Da'anzhai	1699.78	Calcareous shale	N111.50°E	5°	N106.50°E
10	YS 8	Dongyuemiao	1823.75	Mixed shale	N85.00°E	180°	N85.00°E
11	DY1	Upper Liang	3,180.44	Feldspathic shale	N112.15°E	10°	N102.15°E
12	DY 1	Da'anzhai	3,365.46	Feldspathic shale	N87.70°E	5°	N82.70°E
13	DY 1	Dongyuemiao	3,490.93	Mixed shale	N55.50°E	125°	N110.50°E
14	PA101	Upper Liang	3,160.00	Feldspathic shale	N86.60°E	155°	N111.60°E
15	PA 101	Upper Liang	3,340.58	Feldspathic shale	N158.05°E	75°	N83.05°E
16	PA 101	Upper Liang	3,359.62	Clayey shale	N176.80°E	100°	N76.80°E

TABLE 1 Test results of maximum horizontal principal stress orientation determined by paleomagnetic and seismic velocity anisotropy experiments in Yingshan-Pingchang area, northeastern Sichuan Basin.

The overall in-situ stress orientation of the Jurassic formation in the study area is consistent with that of the neighboring Yuanba and Langzhong areas (Figure 6B). In the Yingshan area, the local tectonic influence causes a clockwise deviation of the in-situ stress orientation, primarily ranging from N60° to 80°E. Taking YS6 Well as an example (Figure 6C), the in-situ stress orientation at the target layer between 1,650 and 1,900 m is mainly influenced by the NWW-trending fault, resulting in a deviation of the stress orientation. Figure 6D presents a simulation showing the area's maximum principal stress deviating due to its 25° angle with a local NW-trending fault. The direction of the maximum horizontal principal stress clearly deviates along the fault strike and propagates in a localized manner along it. Fault activity leads to the displacement of rock layers. When a fault forms a specific angle with the orientation of the maximum horizontal principal stress, the distribution of the original stress field undergoes significant alteration. In such cases, the fault exerts a strong guiding effect on the in-situ stress orientation. In areas distant from the fault (depths less than 1,650 m and greater than 1,900 m), the in-situ stress orientation at Yingshan Well six remains generally stable, exhibiting a characteristic EW orientation without noticeable deviation. This stability is because, away from the fault zone, the rock layers experience relatively uniform compression or tension and are not significantly affected by fault activity. Regional tectonic stress plays a dominant role during this period.

4.2 In-situ stress magnitude evaluation

4.2.1 Differential strain experiment for *in-situ* stress magnitude

During the differential strain experiment, strain data were directly collected from nine directions on three orthogonal surfaces of the rock sample. The ratio of the three-dimensional stress was then calculated using elasticity theory. The pressure at the microfracture closure point was used to estimate the maximum principal stress, or alternatively, the vertical stress was inferred from the depth of the core sample. Finally, the three-dimensional stress was estimated by combining the principal stress ratios (Figure 7).



FIGURE 4

Examples of drilling-induced fractures and wellbore breakouts in image logging of Yingshan-Pingchang area, northeastern Sichuan Basin. (A) Well YS8, drilling-induced fractures; (B) Well YS5, drilling-induced fractures; (C) Well DY, wellbore breakouts; (D) Well YS8, wellbore breakouts; (E) Induced fracture identification and maximum principal stress orientation determination from electrical imaging logging, well DY1.

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The results of the three-dimensional stress from the differential strain experiment indicate that the maximum horizontal principal stress ranges from 42.33 MPa to 102.56 MPa, averaging 74.89 MPa; the minimum horizontal principal stress ranges from 39.20 MPa to 84.04 MPa, averaging 67.20 MPa; the vertical principal stress ranges from 31.91 MPa to 91.39 MPa, averaging 60.23 MPa (Table 2).

Based on the stress-strain relationship along the three principal orientations, the ratio of the magnitudes of the three-dimensional stress can be obtained. The stress ratio of the tested samples indicates that the maximum horizontal principal stress value > vertical principal stress value > minimum horizontal principal stress value, suggesting a strike-slip stress regime. Statistical analysis

of the minimum principal stress gradient for different lithologies shows that, the minimum principal stress gradient of shale is higher than that of limestone and sandstone (Figure 8A). Due to the high clay mineral content in shale, the minimum horizontal principal stress gradient tends to be relatively high. According to the formula for calculating the minimum horizontal principal stress, a higher content of plastic minerals results in a larger tectonic strain coefficient, which in turn leads to an increase in the minimum horizontal stress gradient. Overall, the Jurassic stress values are higher in the Pingchang area than in the Longgang area and higher than in the Yingshan area due to the burial depth (Figure 8B).



FIGURE 6

In-situ stress orientation characteristics in Jurassic of Yingshan-Pingchang area, northeastern Sichuan Basin. (A) Multi-data rosette for determining *In-situ* stress orientation; n (B) *In-situ* stress orientation interpretation map of key wells; (C) Interpretation diagram of *in-situ* stress orientation for well Yingshan6; (D) Simulation diagram of the disturbance to *in-situ* stress orientation by nearby faults around well YS6.



4.2.2 Hydraulic fracturing analysis for *in-situ* stress magnitude

The hydraulic fracturing method for *in-situ* stress measurement relies primarily on the pressure-time curve recorded during the fracturing process. By integrating relevant rock mechanics parameters and fracturing theory, the magnitudes of *in-situ* stresses can be calculated. Compared to other measurement methods, this approach does not require prior knowledge of the rock's mechanical parameters, yet it enables the determination of multiple stress parameters within the formation. Additionally, it offers several advantages, including simple equipment, convenient operation, significant measurement depth, the ability for continuous or repeated testing at any depth, rapid measurement speed, intuitive measurement values, and comprehensive representation of the stress field (Schmitt et al., 2012; Wang et al., 2020). The use of fracturing data to determine *in-situ* stress is one of the most direct and reliable methods currently available.

Through the analysis and calculation of fracturing data (Table 3), it is concluded that the shut-in pressures for wells PA101, PY1-1H, PY1-2H, and PY1-3H mainly range from 35 to 42 MPa, averaging 37.01 MPa. Using the fracturing data, the *in-situ* stress magnitudes calculated by the hydraulic fracturing method are obtained (Table 3). Taking well PA101H as an example, the calculated maximum horizontal principal stress is 75.52 MPa, and the minimum horizontal principal stress is 66.187 MPa. A comparison of the results from the differential strain experiment with the hydraulic fracturing stress calculation results at the same depth (Table 3) shows that the *in-situ* stress values measured in the differential strain experiment are close to those calculated by hydraulic fracturing, demonstrating considerable accuracy.

Based on the calculated magnitudes of *in-situ* stresses derived from construction parameter data, it was determined that the relationship among the stresses follows the pattern of maximum principal stress > vertical principal stress > minimum principal stress. Comprehensive analysis suggests that the stress regime in the Jurassic formation in this area is characterized by a strike-slip faulting stress type, which is consistent with the results obtained from the differential strain experiment.

4.3 VTI *in-situ* stress magnitude logging calculation model

In the Jurassic formations of the Yingshan-Pingchang area in northeastern Sichuan, bedding develops between layers, with the rock layers generally being isotropic in the horizontal direction (Zhang et al., 2021). Such layers can be modeled using the Vertical Transverse Isotropy (VTI) medium theory. For VTI formations, the axis of symmetry is in the vertical direction, while the plane of symmetry is horizontal. The rock properties are identical in the horizontal direction but differ in the vertical direction (Gary et al., 1995; Romain et al., 2004).

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Number	Well name	Stratigraphy	Lithology	Depth (m)	Three-	Three-dimensional stress (MPa)	tress (MPa)	Three-	Three-dimensional stress gradient (MPa/100 m)	ess gradient 1)	Ratio of three - dimensional stress
					Vertical	Maximum horizontal	Minimum horizontal	Vertical	Maximum horizontal	Minimum horizontal	Vertical: maximum : minimum
1	PY1-5H	Upper Liang	Clayey shale	3553.00	77.92	82.64	67.98	2.48	2.63	2.16	1:1.06:0.87
2	PY 1-5H	Upper Liang	Clayey shale	3554.30	77.78	85.44	68.92	2.47	2.71	2.19	1:1.09:0.88
ŝ	PY 1-5H	Upper Liang	Mixed shale	3560.86	77.68	82.74	71.12	2.47	2.63	2.26	1:1.06:0.91
4	PY 1-2H	Upper Liang	Fine sandstone	3449.15	76.68	84.65	66.74	2.44	2.69	2.13	1:1.10:0.87
Ω	PY 1-2H	Upper Liang	Fine sandstone	3449.15	76.66	85.07	67.37	2.44	2.70	2.15	1:1.10:0.87
9	PY 1-2H	Upper Liang	Fine sandstone	3449.20	76.37	85.23	67.90	2.43	2.71	2.16	1:1.11:0.88
7	PA101	Upper Liang	Feldspathic shale	3333.55	80.67	89.67	73.34	2.42	2.69	2.2	1:1.11:0.90
8	PA 101	Upper Liang	Feldspathic shale	3335.58	80.72	85.39	69.72	2.42	2.56	2.09	1:1.05:0.86
6	PA 101	Upper Liang	Feldspathic shale	3340.58	80.84	88.86	72.49	2.42	2.66	2.17	1:1.09:0.89
10	DY1	Upper Liang	Feldspathic shale	3179.50	77.21	85.69	71.54	2.45	2.72	2.25	1:1.10:0.92
11	DY 1	Da'anzhai	Mixed shale	3365.37	82.12	92.55	70.00	2.44	2.75	2.08	1:1.12:0.85
12	DY 1	Dongyuemiao	Clayey shale	3490.80	86.23	102.63	74.01	2.47	2.94	2.12	1:1.19:0.85
13	YS5	Upper Liang	Clayey shale	1613.09	39.52	42.75	34.85	2.45	2.65	2.16	1:1.08:0.88
14	YS5	Dongyuemiao	Calcareous Shale	1893.90	45.83	51.89	40.15	2.42	2.74	2.12	1:1.13:0.87
15	YS5	Dongyuemiao	Mixed shale	1893.90	46.59	50.38	42.61	2.46	2.66	2.25	1:1.08:0.91
16	YS8	Da'anzhai	Calcareous Shale	1694.66	41.69	41.35	36.95	2.46	2.44	2.18	1:0.99:0.88
17	YS8	Dongyuemiao	Clayey shale	1814.15	44.27	46.44	38.82	2.44	2.56	2.14	1:1.04:0.87
18	YS8	Dongyuemiao	Clayey shale	1823.75	44.32	50.16	39.21	2.43	2.75	2.15	1:1.13:0.88

(Continued on the following page)

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Pingchang area.	
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TABLE 2 (Continued	

Ratio of three - dimensional stress	Vertical: maximum : minimum	1:1.08:0.92	1:1.11:0.94	1:1.09:0.89	1:1.10:0.90	1:1.10:0.91	1:1.11:0.90	1:1.12:0.88	1:1.08:0.87	1:1.02:0.86
ess gradient ()	Minimum horizontal	2.26	2.29	2.18	2.19	2.23	2.19	2.14	2.11	2.09
Three-dimensional stress gradient (MPa/100 m)	Maximum horizontal	2.43	2.43	2.43	2.43	2.43	2.42	2.42	2.42	2.42
Three-(	Vertical	2.43	2.43	2.43	2.43	2.43	2.42	2.42	2.42	2.42
ress (MPa)	Minimum horizontal	45.22	68.87	67.85	68.2	70.76	69.14	67.47	63.23	62.72
Three-dimensional stress (MPa)	Maximum horizontal	52.76	81.57	82.80	83.27	85.69	85.23	85.80	78.48	74.45
Three	Vertical	48.68	73.26	75.70	75.67	77.21	76.37	76.35	72.53	72.75
Depth (m)		2000.76	3011.20	3111.68	3110.40	3173.50	3155.06	3151.55	2996.52	3005.40
Lithology		Clayey shale	Fine sandstone	Muddy Siltstone	Feldspathic shale	Fine sandstone	Clayey shale	Clayey shale	Shell Limestone	Fine sandstone
Well name Stratigraphy		Dongyuemiao	Upper Liang	Upper Liang	Upper Liang	Upper Liang	Upper Liang	Upper Liang	Upper Liang	Upper Liang
Well name		HIYY	PY1	ΡΥ 1	ΡΥ 1	ΡΥ 1	ΡΥ 1	ΡΥ 1	ЦЦН	ЦЦН
Number		20	21	22	23	24	25	26	27	28



### 4.3.1 Vertical stress calculation

The magnitude of horizontal *in-situ* stress is influenced by factors such as vertical *in-situ* stress, formation pressure, and tectonic stress. Therefore, accurate calculation of vertical *in-situ* stress and pore pressure is essential. Typically, vertical stress is determined by integrating the density log curve. However, not all well sections possess a density log curve. Consequently, vertical stress is initially calculated using the average density of sections lacking a density log curve and subsequently augmented by the vertical stress obtained from integrating the density log curves of sections with density logs. The Formula 3 for calculating the vertical stress at a given depth in the formation is as follows:

$$p_{\rm o} = 0.00981 \left[ \rho_{\rm av} H_1 + \int_{H_1}^{H_2} \rho(h) dh \right]$$
(3)

In this formula:  $P_o$  is the vertical stress, in MPa;  $\rho_{av}$  is the average overburden density of the intervals without density log curves, in g/cm²; p is the density of each individual rock layer, in g/cm²;  $H_1$  is the vertical depth of the deepest point of the interval without density log curves, in meters;  $H_2$  is the vertical depth of the overburden pressure calculation point (where density log curves are available), in meters; h is the formation thickness corresponding to the sampling interval depth of the log curve, in meters (commonly taken as 0.125 m).

The overburden pressure gradient in the Ying Shan area mainly ranges from 2.46 to 2.5 MPa/100 m, while in the Longgang area, it

ranges from 2.38 to 2.40 MPa/100 m, and in the Pingchang area, it ranges from 2.46 to 2.48 MPa/100 m.

### 4.3.2 Porosity pressure calculation

Pore pressure is a critical parameter in drilling processes, fracturing design, and various other applications, and it is essential for evaluating *in-situ* stresses. Based on an analysis of the target formation in the study area, the method adheres to Teraghi's effective stress theory. According to this theory, the overburden pressure within a given layer is partitioned into pore fluid pressure, supported by the pore fluids, and rock stress, supported by the solid grains of the bedrock. The relationship between overburden pressure, rock stress, and pore fluid pressure is calculated by Formula 4:

$$P_p = P_0 - \sigma \tag{4}$$

In this formula:  $P_0$  is the overburden pressure, in MPa;  $P_p$  is the pore fluid pressure, in MPa;  $\sigma$  is the effective stress, in Mpa.

Based on the measured formation pressure data, well logging interpretation results of lithology, physical properties, and electrical response analysis, and considering the relationships among clay content, porosity, P-wave velocity, and effective stress, a multiparameter regression algorithm was employed. To establish a formation pressure logging interpretation model that integrates data from different regions. The model is as follows in Formulas 5, 6:

Pingchang

$$\sigma = \frac{304.8}{AC} + 23.1 - 1.31\varphi + 0.9V_{sh} \tag{5}$$

		Gradient of minimum principal stress (MPa/100 m)		2.24				2.18			2.10		2.44	2.12	2.14	2.44
	ing	Minimum principal stress (MPa)		69.78				08.27			70.05		72.19	66.08	66.22	72.19
	Hydraulic fracturing	Gradient of maximum principal stress (MPa/100 m)		2.74			č	2.66			2.63		2.72	2.83	2.65	2.72
	Ŧ	Maximum principal stress (MPa)		85.41				61.68			87.56		89.06	88.08	82.22	89.06
		Depth(m)		3,340-3,350				3,3,9-5,572			3,327-3,342		2,894-3,702	3,110-3,119	3,100-3,114	2,894-3,702
		Gradient of minimum principal stress (MPa/100 m)	2.25	2.20	2.19	2.14	2.13	2.17	2.25	2.2	2.09	2.17	I	I	I	I
והדבר און אמומר וומרימו וווץ מווט מוווט בוונומו הקרבווונבות במרמנמוסת סו זוד אובש אובשה אוד אמו אמו אמו אמו	Ë	Minimum principal stress (MPa)	67.14	70.67	69.14	68.62	67.05	66.74	68.31	73.34	69.72	72.49	I	I	I	I
	Differential strain	Gradient of maximum principal stress (MPa/100 m)	2.70	2.71	2.58	2.63	2.67	2.53	2.70	2.69	2.56	2.66	I	I	I	I
		Maximum principal stress (MPa)	84.65	85.07	85.23	80.84	82.40	83.65	79.65	89.67	85.39	88.86	I	I	I	I
		Depth(m)	3,449.15	3,449.15	3,449.20	3,459.12	3,461.46	3,462.41	3,462.41	3,333.55	3,335.58	3,340.58	I	I	l	I
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Yingshan

$$\sigma = \frac{304.8}{AC} + 18.33 - 0.13\varphi - 21.45V_{sh} \tag{6}$$

In this formula: *AC* is the acoustic time delay from the sonic log, in  $\mu$ s/ft;  $\varphi$  is the porosity, in %; *V*_{sh} is the shale content, in %.

### 4.3.3 Rock mechanics parameters calculation

The relationship between stress and strain in a transversely isotropic medium (VTI medium) satisfies the generalized Hook's law 4, and can be expressed as follows in Formula 7:

$$\begin{bmatrix} C_{11} & C_{11} - 2C_{66} & C_{13} & 0 & 0 & 0 \\ C_{11} - 2C_{66} & C_{11} & C_{13} & 0 & 0 & 0 \\ C_{13} & C_{13} & C_{33} & 0 & 0 & 0 \\ 0 & 0 & 0 & C_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & C_{44} & 0 \\ 0 & 0 & 0 & 0 & 0 & C_{66} \end{bmatrix}$$
(7)

In this formula: *C* is the stiffness matrix, in GPa;  $\varepsilon$  is the strain; *C*₁₁ is the longitudinal modulus along the parallel to the bedding plane, in GPa; *C*₃₃ is the longitudinal modulus perpendicular to the bedding plane, in GPa; *C*₄₄ is the shear modulus perpendicular to the bedding plane, in GPa; *C*₆₆ is the shear modulus along the parallel to the bedding plane, in GPa; and *C*₁₃ is the stiffness modulus, in GPa.

The symmetry type of formation rocks can be determined by the number of independent elastic parameters. An isotropic formation has two independent elastic parameters, while a transversely isotropic formation has five independent elastic parameters. To describe the stress-strain relationship in a VTI formation, the stiffness coefficients  $C_{11}$ ,  $C_{33}$ ,  $C_{44}$ ,  $C_{66}$ , and  $C_{13}$  need to be determined. These coefficients are calculated in Formulas 8-12, respectively, as follows:

$$C_{11} = \rho V_{ph}^{2}$$
 (8)

$$C_{33} = \rho V_{\rho\nu}^{2}$$
 (9)

$$C_{44} = \rho V_{sv}^{2}$$
 (10)

$$C_{66} = \rho V_{sh}^{2}$$
 (11)

$$\left[\frac{\left(4\rho V_{p45}^{2}-C_{11}-C_{33}-2C_{44}\right)^{2}-\left(C_{11}-C_{33}\right)^{2}}{4}\right]^{\frac{1}{2}}-C_{44} \qquad (12)$$

In this formula:  $V_{ph}$  is the P-wave velocity parallel to the bedding plane, in km/s;  $V_{p\nu}$  is the P-wave velocity perpendicular to the bedding plane, in km/s;  $V_{sh}$  is the S-wave velocity parallel to the bedding plane, in km/s;  $V_{s\nu}$  is the S-wave velocity perpendicular to the bedding plane, in km/s;  $V_{p45}$  is the P-wave velocity at a 45° angle to the bedding plane, in km/s.

Using an ultrasonic transducer system, the velocity of sound is measured on core plug samples extracted from large natural shale samples with vertical stratification. The core plug samples are taken at 0°, 45°, and 90° orientations. The corresponding five independent elastic parameters at the specified depth points can be calculated (Table 4).  $C_{33}$  is calculated using the compressional wave velocity obtained from density and sonic data from well logging data.  $C_{44}$  is calculated from the shear wave velocity derived from density and sonic data.  $C_{66}$  can be determined by inversing the Stoneley wave velocity to compute the horizontal shear wave velocity and density. The parameters  $C_{13}$  and  $C_{11}$  need to be obtained from core experiments or empirical formulas. Based on core sample experimental data, Suarez-Rivera and Bratton proposed an improved ANNIE model called MANNE. By combining experimental data and using multiple linear regression to determine the coefficients of the MANNE model, resulting in the relationship Formulas 13-16 for  $C_{13}$  and  $C_{11}$ in vertical wells, sandstone, and shale as follows:

Vertical Well (Sandstone)

$$c_{13} = 0.795947c_{33} - 1.24059c_{44} \tag{13}$$

$$c_{11} = 1.008131c_{13} \tag{14}$$

Vertical Well (Shale)

$$c_{13} = 0.928115c_{33} - 1.66159c_{44} \tag{15}$$

$$c_{11} = 0.916093c_{13} \tag{16}$$

The Biot coefficient is a parameter used to describe the coupling relationship between the solid matrix and the pore pressure in a porous medium. It reflects the contributions of both the solid matrix and the pore space to the overall properties of the porous material. To obtain a more accurate estimate of the Biot coefficient, this study utilizes the effective stress theory. By employing experimentally measured parameters such as porosity, bulk modulus, and elastic modulus of the rock (Table 4), the Biot coefficient is estimated through theoretical derivation. The Biot coefficient is typically denoted by the symbol  $\alpha$  and is defined as Formula 17:

$$\alpha = 1 - \frac{K_{dry}}{K_{solid}} \tag{17}$$

In this formula:  $K_{dry}$  is the rock's bulk modulus;  $K_{solid}$  is the bulk modulus of the skeleton.

After obtaining all the stiffness coefficients, the anisotropic rock mechanical parameters, such as dynamic elastic modulus and Poisson's ratio, are calculated using the corresponding formulas. Based on the rock mechanical parameters derived from both mechanical experiments and acoustic logging data, a correction relationship model is established for the Pingchang and Yingshan areas, Formulas 18-25 are shown below:

Pingchang

$$\mu_{\nu} = 1.6588\mu_{d\nu} - 0.2339 \tag{18}$$

$$\mu_h = -0.9972\mu_{dh} + 0.4638 \tag{19}$$

$$E_v = 0.8981 E_{dv} - 14.502 \tag{20}$$

$$E_h = 0.9003 E_{dh} - 15.632 \tag{21}$$

Yingshan

$$\mu_{\nu} = 1.848\mu_{d\nu} - 0.3127 \tag{22}$$

TABLE 4 Stiffnes	TABLE 4 Stiffness coefficient expaerimental values.	imental values.												
Well Name	Lithology	Density g/cm ³	C ₁₁ /Gpa	C ₁₂ /Gpa	C ₁₃ /Gpa	C ₃₃ /Gpa	C ₄₄ /Gpa	C ₆₆ /Gpa	<i>E</i> _v /Gpa	E _h /Gpa	>>	<i>ч</i> ²	Biot_V	Biot_H
	Fine Sandstone	2.63	47.4	18.4	10.9	28.1	12.0	14.5	24.54	38.57	0.17	0.33	0.699	0.600
1224	Fine Sandstone	2.66	68.0	25.6	10.7	26.0	17.0	21.2	23.52	56.55	0.11	0.33	0.703	0.569
114	Fine Sandstone	2.67	72.6	24.3	17.9	62.4	22.8	24.1	55.86	62.02	0.18	0.29	0.655	0.612
	Fine Sandstone	2.60	77.9	27.6	24.5	69.0	23.7	25.2	57.64	64.04	0.23	0.27	0.644	0.646
	Fine Sandstone	2.66	68.3	34.2	23.4	54.1	16.1	17.0	43.42	48.13	0.23	0.41	0.812	0.643
, ,	Fine Sandstone	2.69	75.9	5.6	10.0	62.3	33.9	35.1	59.87	74.13	0.12	0.05	0.499	0.573
FA4	Fine Sandstone	2.64	71.3	5.4	2.6	62.2	32.3	32.9	62.05	70.75	0.03	0.07	0.510	0.525
	Clayey Shale	2.63	58.0	24.5	12.4	16.5	8.5	16.7	12.75	43.90	0.15	0.31	0.681	0.591
	Feldspathic Shale	2.66	75.1	5.0	11.4	67.6	29.7	35.0	I	I	I		I	I
H2-1 Y4	Feldspathic Shale	2.64	76.6	10.7	8.6	68.9	32.8	32.9	69.69	55.93	0.26	0.13	0.54	0.67
	Feldspathic Shale	2.52	68.7	29.1	15.2	22.6	14.0	19.8	56.68	19.42	0.13	0.30	0.67	0.58
DY1	Feldspathic Shale	2.54	60.5	8.3	12.2	11.5	8.2	26.1	48.90	9.85	0.10	0.32	0.69	0.56
	Mixed Shale	2.70	51.0	1.4	11.2	36.1	16.0	24.8	46.86	31.88	0.19	0.12	0.53	0.61
	Clayey Shale	2.58	60.7	6.7	2.0	12.3	9.3	27.0	59.75	12.22	0.03	0.11	0.53	0.52
CO I	Clayey Shale	2.53	57.3	7.5	18.2	10.9	7.4	24.9	41.61	6.57	0.17	0.10	0.53	0.60
0.021	Calcareous Shale	2.44	44.0	21.0	1.8	3.5	2.2	11.5	33.67	3.40	0.03	0.47	0.91	0.52
158	Mixed Shale	2.53	55.3	6.1	8.0	7.6	6.3	24.6	46.32	6.43	0.09	0.26	0.63	0.55
	Feldspathic Shale	2.65	67.2	11.5	64.3	61.5	29.4	27.8	60.61	64.79	0.08	0.16	0.55	0.53
PA 101	Feldspathic Shale	2.64	56.7	1.6	55.4	54.1	21.2	27.5	51.73	55.40	0.14	0.01	0.48	0.56
	Clayey Shale	2.66	57.9	11.3	52.1	46.7	11.5	23.3	27.49	41.52	0.35	0.09	0.63	0.74
In the table, $E_v$ and $E_l$ horizontal directions,	In the table, $E_v$ and $E_h$ is the static Young's modulus in the vertical and horizontal directions, in GPa, respectively; $\mu_v$ and $\mu_h$ is the Poisson's ratios in the vertical and horizontal directions, respectively; $Biot_v V$ and $Biot_v H$ is the Biot coefficients in the vertical and horizontal directions, respectively; $Biot_v V$ and $Biot_v H$ is the Biot coefficients in the vertical and horizontal directions, respectively, with no units.	dulus in the vertical and ts.	d horizontal directio	ons, in GPa, respec	ctively; $\mu_v$ and $\mu_h$ is	the Poisson's ratios	in the vertical and	horizontal direction	s, respectively; <i>l</i>	Biot_V and Biot_	H is the B	siot coeffici	ients in the ver	tical and

18

$$\mu_h = -1.9646\mu_{dh} + 0.6507 \tag{23}$$

$$E_v = 1.7827 E_{dv} - 26.312 \tag{24}$$

$$E_v = 1.7827 E_{dv} - 26.31 \tag{25}$$

In this formula:  $E_{dv}$  and  $E_{dh}$  is the dynamic Young's modulus in the vertical and horizontal directions, in GPa;  $\mu_{dv}$  and  $\mu_{dh}$  is the dynamic Poisson's ratio in the vertical and horizontal directions, with no units.

Based on experimental measurements of the skeleton compression coefficient and the rock volume compression coefficient for the rock samples, a statistical analysis is conducted on the Biot coefficient in relation to parameters such as the acoustic travel time, rock bulk density, and other factors. A regression Formula 26 for the Biot coefficient with the GR and triple porosity logging curves is established as follows:

$$Biot = 2.791863 - 0.006GR + 0.002568AC - 0.00245CNL - 0.65217DEN$$
(26)

# 4.3.4 Maximum and minimum tectonic stress coefficient calculation

Using core experimental data combined with previously obtained parameters, including vertical stress, formation pore pressure, Young's modulus, Poisson's ratio, and Biot's coefficient, the maximum and minimum tectonic stress coefficients are subsequently inverted based on the transversely isotropic (*Sn*) model Equations 27, 28.

### 4.3.5 In-situ stress magnitude calculation

Higgins et al. analyzed the anisotropic characteristics of VTI formations and developed the Sn model for interpreting the horizontal principal stress in VTI formations. The formula for calculating the horizontal principal stress in a transversely isotropic medium is as follows:

$$\sigma_{h} = \frac{E_{horz}}{E_{vert}} \frac{v_{vert}}{1 - v_{horz}} (\sigma_{z} - a\sigma_{p}) + \frac{E_{horz}}{1 - v_{horz}^{2}} \varepsilon_{h} + \frac{E_{horz} v_{horz}}{1 - v_{horz}^{2}} \varepsilon_{H} + a\sigma_{p}$$
(27)

$$\sigma_{H} = \frac{E_{horz}}{E_{vert}} \frac{v_{vert}}{1 - v_{horz}} (\sigma_{z} - a\sigma_{p}) + \frac{E_{horz}}{1 - v_{horz}^{2}} \varepsilon_{H} + \frac{E_{horz} v_{horz}}{1 - v_{horz}^{2}} \varepsilon_{h} + a\sigma_{p}$$
(28)

In this formula:  $\sigma_h$  is the minimum horizontal principal stress, in MPa;  $\sigma_H$  is s the maximum horizontal principal stress, in MPa;  $\varepsilon_h$  is the minimum tectonic stress coefficient, with no units;  $\varepsilon_H$  is the maximum tectonic stress coefficient, with no units;  $\sigma_z$  is the overburden pressure, in MPa;  $\sigma_P$  is the pore pressure (MPa);  $V_{vert}$ is the vertical static Poisson's ratio under the transversely isotropic model, with no units;  $V_{horz}$  is the horizontal static Poisson's ratio under the transversely isotropic model, with no units;  $E_{horz}$  is the horizontal static Young's modulus under the transversely isotropic model in MPa;  $E_{vert}$  is the vertical static Young's modulus under the transversely isotropic model in MPa; *a* is the Biot coefficien, with no units.

# 5 Practical engineering application

### 5.1 Analysis of well stress profile

Taking well YS8 in the study area as an example. Using the parameters obtained above, the *in-situ* stress magnitude of the transversely isotropic terrestrial shale reservoir section was calculated using the VTI model. The calculated profile is shown in Figure 9.

The eighth and ninth channel show the vertical and horizontal Poisson's ratios and Young's moduli. It can be observed that in the terrestrial shale reservoir section,  $\mu_v > \mu_h$  and  $E_v > E_h$ , further confirming that the studied formation exhibits VTI characteristics. The 12th channel is the result of the calculated *in-situ* stress. The  $\sigma_H$  ranges from 27.37 to 63.90 MPa, averaging 39.66 MPa. The  $\sigma_h$  ranges from 15.87 to 58.26 MPa, averaging 28.10 MPa. The horizontal principal stress difference varies between 4.943 and 13.54 MPa. The difference in biaxial stress shows a strong correlation with the lithology. The stress difference decreases as the natural gamma logging curve increases (organic matter content and clay mineral content).

To further analyze the effectiveness of the model's *in-situ* stress calculations, the average relative error is used as the evaluation index. The calculation formula is given in Equation 29. The larger the average relative error indicates poorer model fitting and lower accuracy, while a smaller average relative error indicates higher model accuracy. The  $\sigma_H$  and  $\sigma_h$  calculated in the differential strain experiments are selected as accurate data references. The relative error data between the calculated and differential strain experiments for wells are shown in Table 5. The relative error for  $\sigma_H$  ranges from 1.83% to 5.43%, averaging 3.39%. The relative error for  $\sigma_h$  ranges from 1.99% to 6.08%, averaging 3.23%.

$$E = \frac{1}{N} \sum_{i=1}^{N} \frac{\left|\delta_{x,i-\delta_{y,i}}\right|}{\delta_{x,i}} \times 100\%$$
(29)

In this formula, *E* is the average relative error;  $\delta_{x,i}$  is the measured stress value at the *i*th depth differential strain experiments, in MPa;  $\delta_{y,i}$  is the model-calculated stress value at the same *i*th depth, in MPa; and *N* is the total number of measured stress values.

According to the *in-situ* stress profile of well YS81 (Figure 9), it can be observed that  $\sigma_H > P_o > \sigma_h$ . This corresponds to a Type III stress regime, and strike-slip faults are formed under this condition. The three-dimensional stress regime calculated by the above model is consistent with the stress regime results obtained from core stress testing in Sections 3.1.1, 3.1.2. Demonstrate that the model's calculation results are consistent with the actual geological conditions in the study area.

# 5.2 Classification and optimization of differential stress profile types

Stress differences between the reservoir and the adjacent upper and lower surrounding rocks arise from their varying degrees of compactness, resulting in distinct stress gradients. Interlayer stress influences the extension and propagation orientation of hydraulic fractures, making it a crucial aspect of *in-situ* stress research.

Formation	$\leq$	<b>E</b>	Dep	CP	CNI	01	0 <u>—</u> ●100 GPa	$\frac{\sigma}{MPa}^{100}$	Diat	$\frac{M\sigma_H}{0 - 100}$ MPa	Vsh	$\sigma_{H}$ - $\sigma_{h}$	$1 \frac{\text{LS}_1}{(\text{mg/g})} 10$	$1 \frac{\text{LS}_2}{(\text{mg/g})}$
<u>i</u>	Member	Lithology	Depth /m	0	42	01	CHE _h 0 GPa ¹⁰⁰	0 <u>1</u> 0 <u>1</u> MPa 100	⁰ Biot ₁	$ \begin{array}{c} \sigma_h \\ 0 \\ MPa \\ \hline M\sigma_h \\ 0 \\ 0 \\ 0 \\ \end{array} $ 100	0 <u>100</u> %	5 <u>WPa</u> 25	MS ₁ 20	02
-				0	$2\frac{\text{DEN}}{\text{g/cm}^3}3$	01 01	0 <u></u> 100 GPa	<i>Po</i> 0 100 MPa		0 100 MPa Po 0			0 (mg/g)	0 (mg/g)
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The horizontal stress differential is a key controlling factor for volumetric fracturing; a smaller differential facilitates the formation of a complex fracture network, whereas a larger differential tends to create fractures parallel to the maximum horizontal principal stress. Conversely, the height of fractures is primarily controlled by the distribution of the minimum principal stress within the fractured layer, while the length of fractures is mainly governed by the orientation of the maximum horizontal principal stress. Therefore, when selecting optimal fracturing intervals, it is necessary to further refine the classification of *in-situ* stress profiles from wells. Various stress profile types should be summarized, and fracturing should be targeted at the dominant type.

The typical profile types of horizontal principal stress difference in the Sichuan Basin are classified into the following five types: (1) High-Low-High type (Figure 10A-a1), the upper and lower peripheral rock stress difference magnitude are significantly higher than the reservoir stress difference; (2) High-Low-Low type (Figure 10A-a2), the upper enclosing ground stress difference is higher than the lower reservoir ground stress difference, while the difference between the lower enclosing ground stress difference and the reservoir ground stress difference is not significant; (3) Low-Low-High type (Figure 10A-a3), the lower enclosing ground stress difference, while the difference between the upper enclosing ground stress difference, while the difference between the upper enclosing ground stress difference, while

Well name	Depth /m	Measured ^{σ_H /Mpa}	Measured ^o h /Mpa	Calculated  /Mpa	Calculated  /Mpa	Relative error of σ _H (%)	Relative error of $\sigma_h$ (%)
	1694.74	41.35	33.56	38.76	34.54		
	1699.86	44.03	34.98	46	35.85		
	1711.91	45.19	34.92	44.2	34.98		
YS8	1814.15	46.44	36.46	43.54	37.08	3.87	2.08
	1823.65	50.24	39.02	50.16	40.23		
	1694.74	41.35	33.56	38.76	34.54		
	1613.09	42.75	34.85	41.56	33.69		
YS5	1893.90	51.89	40.15	53.5	40.56	3.11	2.70
	1893.90	50.38	42.61	52.12	44.21		
	3,111.68	81.57	68.87	84.3	70.35	-	
PY1	3,110.40	82.80	67.85	83.98	69.81		
	3,173.50	83.27	68.2	85.54	67.98	1.83	1.99
	3,155.06	85.69	70.76	86.21	68.85		
	3,151.55	85.23	69.14	84.32	67.84		
	3,333.55	89.67	73.34	92.32	75.76		
PA101	3,335.58	85.39	69.72	83.51	66.61	2.75	3.34
	3,340.58	88.86	72.49	86.12	74.12		
	3,180.44	81.29	68.06	85.29	70.06		
DY1	3,365.46	86.65	75.35	91.46	80.29	5.43	6.09
	3,491.13	92.45	76.22	97.84	82.90		

TABLE 5 Data of relative error in in-situ stress magnitude (part).

and the reservoir ground stress difference is not significant; (4) Interlayer type (Figure 10A-a4), the upper and lower peripheral rock and the reservoir section have comparable stress difference and mutual high and low; (5) Low type (Figure 10A-a5), the upper and lower peripheral rock and reservoir section are at relatively low stress difference levels with no significant difference between them.

A fine classification of the stress difference profile types was performed on the stress profile of the YS8 well (Figure 10B), and combined with the oil content and hydrocarbon generation potential curves  $S_1$  and  $S_2$  calculated from the well log data. The analysis showed that when the stress difference profile type is of the High-Low-High, the oil content calculated from the well log is the highest, making it the dominant stress difference profile types in the study area (Figure 10C). In this stress difference profile types, the relatively small value facilitates the formation of a complex fracture network, which enhances reservoir connectivity and improves oil and gas flow, thereby achieving better reservoir stimulation results. Moreover, when the stress difference is small, fractures typically do not extend excessively into other layers, thus reducing the risk of layer penetration.

# 6 Discussion

This study integrates three primary methods for obtaining *insitu* stress parameters in terrestrial shale reservoirs: core testing, field measurements, and well logging interpretation. Among these, core testing is the most direct and effective approach for acquiring stress parameters (Wang, 2014). However, this study does not employ acoustic emission testing for stress magnitude estimation, due to its low accuracy and significant uncertainty in identifying the Kaiser effect point of *in-situ* stress (Jayanthu, 2019; Fraser et al., 2021). Instead, the differential strain analysis method is used, which simulates formation conditions to measure the differential strain in



Characteristic profiles of different stress difference profile types (A) Typical stress difference profile types characteristics; (B) Example of YS8 stress difference profile types delineation; (C) Statistical plot of average S1 values for different stress difference profile types.

various directions of the core, thereby determining the stress state experienced by the rock in the formation (Shen et al., 2008).

In the absence of core samples, specialized logging techniques such as imaging logging and dipole shear wave logging can serve as effective alternatives (Han et al., 2020; Cao et al., 2022). However, in formations with well-developed high-angle fractures, borehole walls are prone to collapse due to fracturing, which affects stress direction interpretation based on borehole breakouts, thereby limiting its applicability. Additionally, in reservoirs with low differential stress coefficients, weak anisotropy and minimal borehole deformation further constrain the applicability of certain *in-situ* stress direction interpretation methods.

At the same time, due to the high cost of specialized logging, such techniques cannot be deployed in all wells in practical applications. In this context, conventional logging, with its lower cost and continuous distribution of test points, demonstrates significant application potential. Based on known rock mechanics parameters, this study establishes an *in-situ* stress interpretation model using the theory of transverse isotropic (VTI) media (Li, 2016; Yu et al., 2020; Lin et al., 2022b; Wang, 2022; Wang, 2023), enabling the indirect acquisition of continuous stress profiles. Finally, the accuracy of the transverse isotropy (VTI) model for stress calculation was validated using core-based stress measurement results. However, the model has certain limitations in calculating stress for different lithologies. These limitations primarily stem from the non-uniqueness of the well-log responses, the resolution limitations of the logging data, and the insufficient ability to characterize thin layers and subtle lithological variations. Therefore, the calculation of stress parameters should involve crossvalidation and confirmation through multiple systems and methods.

Previous studies on the calculation and application of *in-situ* stress in terrestrial shale reservoirs have primarily focused on

employing various methods and constructing multiple models for comparative analysis (Lin et al., 2022b; Wang, 2023) to enhance the accuracy of stress profile interpretation. Due to the poor physical properties of terrestrial shale reservoirs, achieving economic production often requires large-scale volumetric fracture network modifications along the entire wellbore (Mayerhofer et al., 2010). Building on this foundation, this study not only establishes continuous in-situ stress profiles for individual wells but also further explores the impact of the present-day stress state on reservoir stimulation effectiveness. Building on previous research findings, a greater horizontal principal stress difference is less conducive to forming a complex fracture network near the wellbore. In such cases, volumetric fractures tend to extend further in length while narrowing in width, leading to the formation of planar fractures during hydraulic fracturing. Conversely, a smaller stress difference promotes fracture propagation along natural fractures, resulting in a more intricate fracture network (Zhao and Li, 2014; Zhang et al., 2019; Ning et al., 2021). Therefore, when selecting fracturing intervals, it is essential to precisely characterize the interlayer stress distribution and accurately predict fracture propagation across layers. Failure to do so may lead to issues such as proppant blockage, premature termination of operations, or even complete engineering failure. Only by accurately evaluating the vertical and horizontal propagation of fractures can the optimal construction scale and well pattern be scientifically determined, thereby achieving the best reservoir stimulation results. Based on a systematic classification of five fundamental stress difference profile types in the study area, this study ultimately identifies the high-lowhigh (HLH) stress difference profile as the most promising in terms of production potential and reservoir stimulation effectiveness.

# 7 Conclusion

- (1) The current stress orientation in the Yingshan-Pingchang area of the Jurassic Formation, determined by comprehensive analysis of differential strain, electrical imaging logging, and dipole shear wave logging, is predominantly in the EW orientation. The orientation ranges from N 87°-120° E, with the main direction maintaining a consistent range of NE 95° ± 10°. In the Yingshan area, the local tectonic influence causes a clockwise deviation of the *in-situ* stress orientation, primarily ranging from N60° to 80°E.
- (2) Differential strain experiments in Jurassic shale reservoirs in the Yingshan-Pingchang area revealed the horizontal maximum principal stress ranges from 42.33 MPa to 102.56 MPa, averaging 74.89 MPa. The minimum horizontal principal stress ranges from 39.20 MPa to 84.04 MPa, averaging 67.20 MPa. The vertical principal stress ranges from 31.91 MPa to 91.39 MPa, averaging 60.23 MPa. The stress ratio of the tested samples indicates that the maximum horizontal principal stress value > vertical principal stress value > minimum horizontal principal stress value, suggesting a strike-slip stress regime. These results were validated using in-situ stress calculations from hydraulic fracturing, indicating that the accuracy of the stress magnitudes measured by the differential strain experiments is relatively high. Statistical analysis of the minimum principal stress gradient for different lithologies shows that the minimum principal stress gradient of shale is higher than that of limestone and sandstone.
- (3) The key parameters of the transverse isotropic *in-situ* stress model were derived by correcting well log data using laboratory experimental testing and analysis methods. Predicted results for the minimum and maximum horizontal principal stresses from the transverse isotropic *in-situ* stress prediction model showed average relative errors of only 3.39% and 3.23%, respectively, when compared to the measured *in-situ* stress values. Vertically, the high-low-high (HLH) stress difference profile type demonstrates the highest oil-bearing potential and a reduced likelihood of fracturing-induced artificial fractures penetrating through layers, making it the optimal structural type for selecting the fracturing stage in the study area's *in-situ* stress difference fracturing.

# Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

# Author contributions

SY: Funding acquisition, Project administration, Writing-original draft, Writing-review and editing. JZ: Formal Analysis, Software, Validation, Writing-review and editing. HD: Data curation, Funding acquisition, Methodology, Supervision, Project administration, Writing-original draft. HQ: Data curation, Visualization, Writing-review and editing. WX: Data curation, Visualization, Writing-review and editing. YD: Data curation, Investigation, Methodology, Visualization, Writing-review and editing, Writing-original draft. MG: Data curation, Investigation, Visualization, Writing-review and editing. TH: Data curation, Investigation, Visualization, Writing-review and editing. CL: Data curation, Investigation, Visualization, Writing-review and editing.

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# **Conflict of interest**

Authors SY, JZ, HQ, WX, and TH were employed by the Exploration and Development Research Institute of PetroChina Daqing Oilfield.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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# **Generative AI statement**

The author(s) declare that no Generative AI was used in the creation of this manuscript.

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### Supplementary material

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/feart.2025. 1530002/full#supplementary-material

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