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# Theory and numerical simulation study on the plastic slip failure mechanism of multi-layered coal seam Floors-A case analysis

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Coal seam mining induces disturbances in underground floors, leading to plastic failure, which presents significant safety risks, particularly in areas with underlying pressurized water. Accurately assessing the maximum depth of such floor failure is crucial for ensuring safe mining operations. This study investigates the evolution of apparent resistivity in the floor of the 4,301 working face using the network parallel electrical method. The observed maximum failure depth was found to be 19.3 m. Based on these measurements, the plastic slip theory for a homogeneous rock layer was applied, incorporating mining parameters such as burial depth and mining height. Five mechanical models for plastic slip failure in multi-layer composite floors were developed, with the maximum failure depth calculated to be 18.26 m. The study also explores the impact of factors such as mining height, burial depth, and the internal friction angle of the rock layers on floor failure depth. The results demonstrate that multilayer composite floors exhibit a 23.1% reduction in failure depth on average compared to homogeneous floors. Numerical simulations confirmed that the maximum failure depth under mining disturbance is 19.2 m, with shear failure identified as the predominant failure mode. The findings from the theoretical analysis, numerical simulations, and field measurements align closely, validating the applicability of the plastic slip theory for multi-layer composite floors. This research provides critical theoretical support for safe mining operations in coal seams above confined aquifers and effective water control strategies.

#### KEYWORDS

multi-layered floor, apparent resistivity, plastic slip theory, failure depth, failure characteristics

## **1** Introduction

Longwall coal mining induces support pressure on the floor, leading to damage in the underlying strata within a certain depth range (Xu et al., 2019; Zhang et al., 2018; Wu et al., 2022; Wu et al., 2024), which poses significant safety risks to the mining of coal seams under confined water. Thus, determining the depth of floor damage is a critical issue in mining coal seams under confined water. Experts have extensively studied this topic, yielding valuable results (Zhang et al., 2024; Xuyang et al., 2022; Li et al., 2020; Yang et al., 2025; Wu et al., 2025a).

Numerous theoretical studies on floor damage mechanisms have been conducted, revealing the effects under various conditions (Liu et al., 2022b; Jia et al., 2019; Guo et al., 2021; Wu et al., 2025b). Zhang proposed the classic plastic slip line field theory, which clarified the process of floor compression damage and provided a method for calculating the maximum depth of floor damage (Zhang and Liu, 1990). Li developed a mechanical model of floor water inrush induced by confined water, based on the plastic slip line theory. He derived expressions for confined water pressure and waterproof coal pillar width under limit equilibrium, and analyzed the deformation and damage characteristics of the floor under various coal pillar widths (Li et al., 2021). Sun developed a mechanical model for floors in inclined working faces, deriving the stress at any point on the inclined floor and providing a method to calculate the maximum depth of floor damage in inclined coal seams (Sun et al., 2019). He incorporated multiple stress superimpositions and developed a mechanical model of floor damage based on elastic foundation theory and the superposition principle. He also proposed a criterion for floor damage depth, comprehensively determining the range of damage (He et al., 2022).

Research on the plastic damage characteristics of the floor using numerical simulation has matured, supporting the understanding of stress field, deformation field, and plastic zone evolution during working face advancement (Meng et al., 2019; Zhu et al., 2016; Liu et al., 2022a; Zhu et al., 2017). Liang developed a FLAC3D numerical model for mining under confined water, finding that floor damage depth increases with working face advancement. At 160 m, the maximum depth of floor damage reaches 16.71 m (Liang et al., 2020). Zhu developed a numerical model for mining coal seams under confined water, finding that floor stress decreases with depth and eventually returns to the original rock stress state (Zhu et al., 2014). In field measurements, researchers often combine multiple detection techniques to determine the depth and characteristics of floor disturbance and damage (Chang et al., 2020). Commonly used field detection techniques include direct current resistivity (Zhou et al., 2019), three-dimensional CT (Tao and Zheng, 2018), mine geological radar (Xu et al., 2018), distributed optical fiber sensing (Bernini et al., 2011), borehole imaging (Liu et al., 2023), acoustic wave detection (Shan et al., 2022), and microseismic technology (Gai et al., 2024). Zeng combined in-situ strain testing and borehole imaging to measure the depth of floor damage in five coal mines in the Yanzhou mining area, finding that damage depth ranged from 8.4 to 20 m (Zeng et al., 2020). Yu proposed a global optimization algorithm for acoustic wave tomography, achieving an accuracy of 0.56 m after 7 iterations. This method was used to determine that the floor damage depth after mining No. 3 coal seam in Bao'an coal mine was 17 m (Yu et al., 2020).

The theoretical research above is based on the plastic slip theory, extended in various dimensions, yet still simplifies the floor as a single homogeneous rock layer. In reality, the floor of coal seams is typically a composite rock layer consisting of multiple rock types, and calculations based on a single rock layer may introduce errors. Based on field measurements, this paper integrates mining conditions, such as mining height and burial depth, into the classic plastic slip theory. It constructs a multi-layer composite floor damage model, derives analytical solutions for maximum floor damage depth under different states, and verifies the theory's scientific validity and practicality through numerical simulation. The research provides theoretical support for mining coal seams under confined water and water control operations.

# 2 Field measurement of the damage depth of floor

### 2.1 Overview of the study area

Longquan Coal Mine is located in Loufan County, Taiyuan City, Shanxi Province (Figure 1a). The mine contains three coal seams suitable for mining: 4#, 7#, and 9#. The main mining seam, 4#, is nearly horizontal, with an average thickness of 6.47 m. The coal seam structure is complex, consisting of several layers of mudstone and carbonaceous mudstone intercalated with gangue. The 4,301 working face, located in the third mining area, is the first to be mined. It has a strike length of 720 m, a dip width of 180 m, an average burial depth of approximately 600 m, an average mining height of 6.25 m, and a roof treatment method involving full collapse (Figure 1b). Drilling records near the 4,301 working face show that the immediate roof of the 4# coal seam consists of 3.53 m of siltstone, while the old roof is 7.24 m thick sandy mudstone. The immediate floor is 6.75 m of fine sandstone, and the old floor is 11.63 m of sandy mudstone, forming a typical hard-soft-hard composite structure. The geological columnar diagram is shown in Figure 1c.

The 4# coal seam is mined under pressure from Taihui and Ordovician limestone aquifers. The aquifer groups impacting the 4# coal seam mining include the K3 sandstone, L3 limestone aquifer, L2 limestone aquifer group, and the Ordovician limestone aquifer, which poses the greatest threat to mining safety. The Ordovician limestone aquifer is, on average, 153.5 m from the floor of the 4,301 working face, with a water pressure of approximately 6 MPa. The water inrush coefficient of the Ordovician limestone aquifer in the 4# coal seam ranges from 0.036 to 0.097 MPa/m, with some areas of the third mining area exceeding the critical value of 0.06 MPa/m. Additionally, a floor water inrush of 140 m<sup>3</sup>/h occurred during the mining of the 4,301 working face. The interaction between the floor mining damage zone and the aquifer pressure elevation zone is considered a key factor in the floor water inrush at the working face. Therefore, clarifying the floor damage depth is crucial for the safe and efficient mining of the working face and for early water disaster warning.

## 2.2 Monitoring program design

To clarify the floor damage depth at the 4,301 working face, this study employs the network parallel electrical method to continuously monitor the evolution of the floor's apparent resistivity during mining advancement, analyzing the damage characteristics and maximum depth of floor damage.

In the return air roadway, four measuring lines are arranged in a hole-road combination to detect the apparent resistivity of the waterproof layer. Two floor boreholes are drilled, with one measuring line placed in each borehole (measuring lines 1 and 2), and two measuring lines (measuring lines 3 and 4) are installed on the coal wall of the return air roadway. As a result, the two measuring lines in the roadway and the two in the boreholes form



Overview of the study area: (a) Study area location; (b) Layout plan of roadway for 4301 working face; (c) Comprehensive columnar diagram of 4301 working face.



a hole-road three-dimensional electrical observation system. Each measuring line is equipped with 16 electrodes, spaced 4 m apart. Each electrode is connected to a measuring point, resulting in a total of 64 measuring points. The layout of the electrical detection system's measuring lines is shown in Figure 2.

# 2.3 Monitoring results of floor damage depth

The first monitoring was conducted after the installation of the hole-lane three-dimensional electrical observation system was completed. At this point, the working face was 103 m from the opening of the 1# borehole. The floor rock layer within the effective detection range of the network parallel electrical system was largely unaffected by the mining-induced stress of the working face. Thus, the apparent resistivity of the impermeable layer at this point was used as the background value, as shown in Figure 3. In the figure, the ordinate at 0 m represents the junction of the coal seam and the floor, while the abscissa represents the distance from the stopmining line. To ensure the accuracy and continuity of the detection results, floor apparent resistivity measurements were taken every 4 h after the initial detection.

As illustrated in Figure 3, the apparent resistivity of the aquiclude unaffected by mining predominantly ranges from 200 to 500  $\Omega$  m, with localized values between 600 and 800  $\Omega$  m. It is widely accepted that the resistivity in the fracture development zone increases by a factor of 1.5–2.5. Consequently, when the apparent resistivity exceeds 1,200  $\Omega$  m, it indicates that the floor



has experienced plastic failure induced by mining. The evolution of apparent resistivity in the floor aquiclude during the mining process of the working face is depicted in Figure 4.

As illustrated in Figure 4:

- (1) When the working face advanced 22.84 m, the apparent resistivity of the floor increased due to the influence of advance stress (Figure 4a), but no significant damage was observed. As the working face progressed, areas of the floor where resistivity exceeded 1,200  $\Omega$  m began to appear (Figures 4b, c), indicating the initiation and gradual development of floor cracks. Subsequently, regions with resistivity exceeding 1,200  $\Omega$  m expanded (Figure 4d), with the maximum damage depth reaching 11.2 m. When the working face advanced to 141.72 m, areas with resistivity greater than 1,200  $\Omega$  m merged, and the maximum damage depth extended to 19.3 m (Figure 4e).
- (2) Under the influence of advance stress, damage initially occurs in the floor of the working face, extending from the coal wall to the peak of the advance support pressure. As mining progresses, cracks develop in the floor of the goaf, extending horizontally and increasing in depth. Beyond a certain distance, the destruction depth of the floor ceases to increase.
- (3) The morphology of high-value apparent resistivity regions indicates that the floor damage range is arc-shaped, exhibiting slip characteristics. As the working face advances, the damage area expands while maintaining its overall shape. The resistivity values gradually increase, signifying plastic failure of the floor.

# 3 Multilayer composite floor plastic slip theory

# 3.1 Plastic slip theory and classification of multilayer floors

The measured results indicate that the failure of the working face floor aligns with the classical plastic slip theory (Zhang and Liu,



Working face advances 22.84 m; (b) Working face advances 52.28 m; (c) Working face advances 84.28 m; (d) Working face advances 109.48 m; (e) Working face advances 141.72 m.



1990). Based on the characteristics of coal seam support pressure, ignoring pore water pressure, and based on the theory of elastic-plastic mechanics, the calculation method of ultimate bearing capacity and failure depth of floor rock mass is proposed, as shown in Figure 5. The floor rock mass conforms to isotropic and static boundary conditions and other relevant assumptions. In Figure 5,  $L_0$  represents the distance from the coal face to the peak of the advanced support pressure, m;  $L_1$  and  $L_2$  are the horizontal distances from the coal face to the plastic slip line, m;  $H_0$  is the maximum depth of the active limit failure zone, m;  $H_m$  represents the maximum failure depth of the floor, m;  $l_0$  and  $l_m$  denote the initial and endpoint radii of the logarithmic spiral line, m; l is the radius of the logarithmic spiral line at point E, representing the maximum floor failure depth, m;  $\alpha$  is the angle between  $l_0$  and  $l_s$  °;  $\theta$  is the angle between l and  $H_m$ .

Under the influence of the advancing support pressure, the floor, extending from the coal wall of the working face to the peak of the support pressure, experiences normal extrusion stress, leading to tensile failure and the formation of an active limit failure zone (zone I in Figure 5). Once the rock mass in the active limit failure zone deforms, additional extrusion stress is applied to the transition zone (zone II in Figure 5), leading to plastic failure. The rock mass in the transition zone (zone II in Figure 5), resulting in plastic flow until complete failure. The maximum failure depth of the floor is expressed as follows:

$$H_{\rm m} = \frac{L_0}{2\cos(\frac{\pi}{4} + \frac{\varphi_1}{2})} e^{(\frac{\pi}{4} + \frac{\varphi_1}{2})\tan\varphi_1}\cos\varphi_1 \tag{1}$$

Based on the above, assuming the coal body is a homogeneous isotropic material and applying elastic-plastic theory along with the principle of stress equilibrium, the expression for the distance  $L_0$  from the peak point to the coal wall is as follows:

$$L_0 = \frac{M}{2\xi \tan \varphi_f} \ln \frac{k\gamma H + C \cot \varphi}{\xi (P_i + C \cot \varphi)}$$
(2)

In this equation, *M* and *H* represent the mining thickness and burial depth of the coal seam, m;k is the stress concentration factor;  $\gamma$  denotes the average unit weight of the overlying rock strata, kN/m<sup>3</sup>; $\varphi_f$  is the internal friction angle of the overlying strata, °; *C* is the cohesion of the coal body, MPa;  $\varphi$  is the internal friction angle of the coal body, °;  $\xi$  is the stress coefficient,  $\xi = \frac{1+\sin\varphi}{1-\sin\varphi}$ ;  $P_i$  is the resistance provided by the support to the coal face, MPa.

By substituting Equation 2 into Equation 1, we obtain the expression for the maximum failure depth  $H_{\rm m}$  of the floor, which incorporates the characteristics of the coal seam occurrence and the impact of mining techniques:

$$H_{\rm m} = \frac{\frac{M}{2\xi \tan \varphi_f} \ln \frac{kyH+C \cot \varphi}{\xi(P_f+C \cot \varphi)}}{2 \cos\left(\frac{\pi}{4} + \frac{\varphi_1}{2}\right)} e^{\left(\frac{\pi}{4} + \frac{\varphi_1}{2}\right) \tan \varphi_1} \cos \varphi_1 \tag{3}$$

Equation 3 provides a method for calculating floor failure depth by simplifying the floor rock strata as a single homogeneous layer. However, this simplification does not accurately reflect actual conditions, resulting in some discrepancy between the calculated floor failure depth and field observations. Therefore, the following section integrates factors such as mining pressure in the working face, coal seam characteristics, and the lithology of the coal seam floor. By considering variations in the floor failure depth  $(H_0)$ caused by the advanced concentrated stress at different stratigraphic positions, the plastic slip failure states of multilayer composite floors are categorized into five types, as illustrated in Figure 6. Here,  $H_1$ represents the thickness of the first (upper) rock layer beneath the coal seam floor, and  $H_2$  represents the thickness of the second (middle) rock layer. Each layer has different properties and interfaces between composite layers are perfectly bonded, with no slippage or delamination.

### 3.2 Failure depth of the floor under operating conditions

#### 3.2.1 Failure depth of the floor under $H_0 < H_1$

When  $H_0 < H_1$ , as shown in Figure 6a, the thickness of the upper rock layer  $H_1$  of the floor is expressed by the endpoint radius  $l_1$  of the logarithmic spiral line BB<sub>1</sub>:

$$H_{1} = \frac{\frac{M}{2\xi \tan \varphi_{f}} \ln \frac{k\gamma H + C \cot \varphi}{\xi(P_{f} + C \cot \varphi)}}{2 \cos\left(\frac{\pi}{4} + \frac{\varphi_{1}}{2}\right)} e^{\alpha_{1} \tan \varphi_{1}} \sin\left(\frac{\varphi_{1}}{2} + \alpha_{1} + \frac{\pi}{4}\right)$$
(4)

By performing a Taylor expansion on the unknown coefficient  $\alpha_1$  in Equation 4 and substituting the first two terms into Equation 4, the expression for the thickness  $H_1$  of the upper rock layer of the floor is obtained as follows:

$$H_{1} = \frac{\frac{M}{2\xi \tan \varphi_{f}} \ln \frac{kyH+C \cot \varphi}{\xi(P_{i}+C \cot \varphi)}}{2 \cos\left(\frac{\pi}{4} + \frac{\varphi_{1}}{2}\right)} \left(1 + \alpha_{1} \tan \varphi_{1}\right) \\ \times \left[\left(\frac{\varphi_{1}}{2} + \alpha_{1} + \frac{\pi}{4}\right) - \frac{1}{6}\left(\frac{\varphi_{1}}{2} + \alpha_{1} + \frac{\pi}{4}\right)^{3}\right]$$
(5)

By performing a Taylor expansion on Equation 5, its expression can be written as follows:

$$\begin{pmatrix} -\frac{1}{6}\tan\varphi_{1} \end{pmatrix} \alpha_{1}^{4} + \begin{bmatrix} -\frac{1}{6} - \frac{1}{2} \left(\frac{\varphi_{1}}{2} + \frac{\pi}{4}\right) \tan\varphi_{1} \end{bmatrix} \alpha_{1}^{3} \\ + \begin{bmatrix} \tan\varphi_{1} - \frac{1}{2} \left(\frac{\varphi_{1}}{2} + \frac{\pi}{4}\right) - \frac{1}{2} \left(\frac{\varphi_{1}}{2} + \frac{\pi}{4}\right)^{2} \tan\varphi_{1} \end{bmatrix} \alpha_{1}^{2} \\ + \begin{bmatrix} 1 - \frac{1}{2} \left(\frac{\varphi_{1}}{2} + \frac{\pi}{4}\right)^{2} + \left(\frac{\varphi_{1}}{2} + \frac{\pi}{4}\right) \tan\varphi_{1} - \frac{1}{6} \left(\frac{\varphi_{1}}{2} + \frac{\pi}{4}\right)^{3} \tan\varphi_{1} \end{bmatrix} \alpha_{1} \\ + \begin{bmatrix} \frac{\varphi_{1}}{2} + \frac{\pi}{4} - \frac{2H_{1}\cos\left(\frac{\pi}{4} + \frac{\varphi_{1}}{2}\right)}{\frac{M}{2\xi\tan\varphi_{j}}\ln\frac{kyH+C\cot\varphi}{\xi(P_{i}+C\cot\varphi)}} - \frac{1}{6} \left(\frac{\varphi_{1}}{2} + \frac{\pi}{4}\right)^{3} \end{bmatrix} = 0$$

$$(6)$$

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 $L_2$ L.  $L_0$ Advanced support ompaction stress Gob  $\varphi$ H Π Upper rock layer Middle rock layer H. Lower rock layer  $B_2$ E (a)  $L_2$ L  $L_0$ Advanced support stress Compaction stress Gob  $\frac{\pi}{\varphi}$ 12  $H_{c}$ н Upper rock lave  $(H_1)$ GB Middle rock layer Π  $H_{\gamma}$ θ Lower rock layer B E (b) L, L  $L_{i}$ Advanced support stress Compaction stre Gob Upper rock layer  $C_1$ Middle rock layer 7 H.  $[\Pi l_1]$ B Lower rock layer  $E_1$ (c)  $L_2$ Advanced support stres Compaction stress Gob πφ Ē Upper rock layer Middle rock θ E. Lower rock laver E (d) Advanced support stress Gob πφ ia. Upper rock layer Middle rock layer 4  $p \Pi$ Lower rock layer Ε (e) FIGURE 6

Calculation model of plastic slip failure zone depth of multi-layer floor: (a) The floor failure state:  $H_0 < H_1$ ; (b) The floor failure state:  $H_0$ =  $H_1$ ; (c) The floor failure state:  $H_1 < H_0 < H_1 + H_2$ ; (d) The floor failure state:  $H_0 = H_1 + H_2$ ; (e) The floor failure state:  $H_0 > H_1 + H_2$ .

Let:

$$\begin{split} \delta_1 &= -\frac{1}{6} \tan \varphi_1, \delta_2 = -\frac{1}{6} - \frac{1}{2} \left( \frac{\varphi_1}{2} + \frac{\pi}{4} \right) \tan \varphi_1, \\ \delta_3 &= \tan \varphi_1 - \frac{1}{2} \left( \frac{\varphi_1}{2} + \frac{\pi}{4} \right) - \frac{1}{2} \left( \frac{\varphi_1}{2} + \frac{\pi}{4} \right)^2 \tan \varphi_1, \\ \delta_4 &= 1 - \frac{1}{2} \left( \frac{\varphi_1}{2} + \frac{\pi}{4} \right)^2 + \left( \frac{\varphi_1}{2} + \frac{\pi}{4} \right) \tan \varphi_1 - \frac{1}{6} \left( \frac{\varphi_1}{2} + \frac{\pi}{4} \right)^3 \tan \varphi_1, \\ \delta_5 &= \frac{\varphi_1}{2} + \frac{\pi}{4} - \frac{2H_1 \cos \left( \frac{\pi}{4} + \frac{\varphi_1}{2} \right)}{\frac{M}{2\xi \tan \varphi_f} \ln \frac{k\gamma H + C \cot \varphi}{\xi(P_f + C \cot \varphi)}} - \frac{1}{6} \left( \frac{\varphi_1}{2} + \frac{\pi}{4} \right)^3 \end{split}$$

Then Equation 6 can be transformed into a univariate quartic equation containing only the unknown coefficient  $\alpha_1$ , and its expression is as follows:

$$\delta_1 \alpha_1^{\ 4} + \delta_2 \alpha_1^{\ 3} + \delta_3 \alpha_1^{\ 2} + \delta_4 \alpha_1 + \delta_5 = 0 \tag{7}$$

By applying Ferrari's solution to the quartic equation, the expression for the unknown coefficient  $\alpha_1$  is derived as follows:

$$x_{1} = -\frac{\delta_{2}}{4\delta_{1}} + \frac{1}{2}\sqrt{\frac{\delta_{2}^{2}}{4\delta_{1}^{2}} - \frac{2\delta_{3}}{3\delta_{1}} + \Delta} - \frac{1}{2}\sqrt{\frac{\delta_{2}^{2}}{2\delta_{1}^{2}} - \frac{4\delta_{3}}{3\delta_{1}} - \Delta - \frac{-\frac{\delta_{2}^{3}}{\delta_{1}^{3}} + \frac{4\delta_{2}\delta_{3}}{\delta_{1}^{2}} - \frac{8\delta_{4}}{\delta_{1}}}{4\sqrt{\frac{\delta_{2}^{2}}{4\delta_{1}^{2}} - \frac{2\delta_{3}}{3\delta_{1}} + \Delta}}$$
(8)

In the equation,

0

$$\Delta = \frac{3\sqrt{2}\Delta_1}{3\delta_1 3\sqrt{\Delta_2 + \sqrt{-4\Delta_1^3 + \Delta_2^2}}} + \frac{\sqrt{3}\Delta_2 + \sqrt{-4\Delta_1^3 + \Delta_2^2}}{33\sqrt{2}\delta_1}$$
$$\Delta_1 = \delta_3^2 - 3\delta_2\delta_4 + 12\delta_1\delta_5$$
$$\Delta_2 = 2\delta_3^3 - 9\delta_2\delta_3\delta_4 + 27(\delta_1\delta_4^2 + \delta_2^2\delta_5) - 72\delta_1\delta_3\delta_5$$

The endpoint radius of the first logarithmic spiral  $l_1$  can be expressed as:

$$l_1 = l_0 e^{\alpha_1 \tan \varphi_1} \tag{9}$$

By substituting Equation 8 into Equation 9, the expression for  $l_1$  can be obtained as follows:

The endpoint radius of the second logarithmic spiral  $l_2$  can be determined by solving the following system of equations:

$$\begin{cases} l_2 = l_1 e^{\alpha_2 \tan \varphi_2} = \frac{H_1}{\sin\left(\frac{\varphi_1}{2} + \alpha_1 + \frac{\pi}{4}\right)} e^{\alpha_2 \tan \varphi_2} \\ l_2 = \frac{H_1 + H_2}{\sin\left(\frac{\varphi_1}{2} + \frac{\pi}{4} + \alpha_1 + \alpha_2\right)} \end{cases}$$
(10)

In the equation:  $\alpha_2$  represents the angle between the radii of the endpoints of the logarithmic spiral for the median rock layer, °;  $H_2$  is the thickness of the median rock layer, m.

Solving Equation 10 yields:

$$\begin{aligned} H_1 + H_2 &= l_1 e^{\alpha_2 \tan \varphi_2} \sin \left( \frac{\varphi_1}{2} + \frac{\pi}{4} + \alpha_1 + \alpha_2 \right) \\ &\approx l_1 (1 + \alpha_2 \tan \varphi_2) \left[ \left( \frac{\varphi_1}{2} + \alpha_1 + \frac{\pi}{4} + \alpha_2 \right) - \frac{1}{6} \left( \frac{\varphi_1}{2} + \alpha_1 + \frac{\pi}{4} + \alpha_2 \right)^3 \right] \end{aligned}$$
(11)

By performing a Taylor expansion on Equation 11, with the calculation process following the same procedure as in Equations 6–8, the expression for the maximum failure depth  $H_{\rm m}$  of the multilayer composite floor under the first failure condition is given by:

$$H_{\rm m} = l\cos\theta = l_2 e^{\alpha_3 \tan\varphi_3} \cos\left(\frac{\varphi_1}{2} + \alpha_1 + \alpha_2 + \alpha_3 - \frac{\pi}{4}\right) \tag{12}$$

When  $\frac{\partial H_{\rm m}}{\partial \alpha_3} = 0$ , The corresponding value of  $H_{\rm m}$  obtained for  $\alpha_3$  represents the maximum failure depth of the floor, as follows:

$$\frac{\partial H_{\rm m}}{\partial \alpha_3} = l_2 e^{\alpha_3 \tan \varphi_3} \left[ \tan \varphi_3 \cos \left( \frac{\varphi_1}{2} + \alpha_1 + \alpha_2 + \alpha_3 - \frac{\pi}{4} \right) - \sin \left( \frac{\varphi_1}{2} + \alpha_1 + \alpha_2 + \alpha_3 - \frac{\pi}{4} \right) \right] = 0$$
(13)

By setting the value inside the brackets of Equation 13 to 0, the value of  $\alpha_3$  is obtained as follows:

$$\alpha_3 = \varphi_3 - \frac{\varphi_1}{2} + \frac{\pi}{4} - \alpha_1 - \alpha_2 \tag{14}$$

By substituting Equation 14 into Equation 12, the expression for  $H_{\rm m}$ , representing the maximum failure depth of the multilayer composite floor under the first failure condition, is obtained as follows:

$$H_{\rm m} = l_2 e^{\left(\varphi_3 - \frac{\varphi_1}{2} + \frac{\pi}{4} - \alpha_1 - \alpha_2\right) \tan \varphi_3} \cos \varphi_3$$
  
=  $\frac{H_1 + H_2}{\sin\left(\frac{\varphi_1}{2} + \frac{\pi}{4} + \alpha_1 + \alpha_2\right)} e^{\left(\varphi_3 - \frac{\varphi_1}{2} + \frac{\pi}{4} - \alpha_1 - \alpha_2\right) \tan \varphi_3} \cos \varphi_3$  (15)

#### 3.2.2 Failure depth of the floor under $H_0 = H_1$

According When  $H_0 = H_1$ , as shown in Figure 6b, the logarithmic spiral line is located between the middle and lower rock layers, with the initial radius of the first segment of the spiral line positioned at the interface between the upper and middle rock layers. Based on the solution process for the first failure condition, the endpoint radius of the logarithmic spiral in the middle rock layer  $l_1$  can be obtained by solving the following system of equations (Equation 16):

$$\begin{cases} l_1 = l_0 e^{\alpha_1 \tan \varphi_2} = \frac{H_1}{\sin\left(\frac{\varphi_1}{2} + \frac{\pi}{4}\right)} e^{\alpha_1 \tan \varphi_2} \\ l_2 = \frac{H_1 + H_2}{\sin\left(\frac{\varphi_1}{2} + \frac{\pi}{4} + \alpha_1\right)} \end{cases}$$
(16)

From Equations 8, 9 for  $\alpha_1$  and  $l_1$ , and based on Figure 2b, the expression for the maximum failure depth  $H_m$  of the multilayer composite floor under the second failure condition is obtained as follows:

$$H_{\rm m} = l\cos\theta = l_1 e^{\alpha_2 \tan\varphi_3} \cos\left(\frac{\varphi_1}{2} + \alpha_1 + \alpha_2 - \frac{\pi}{4}\right) \tag{17}$$

When  $\frac{\partial H_{\rm m}}{\partial \alpha_2} = 0$ , The value of  $H_{\rm m}$  corresponding to the obtained  $\alpha_2$  represents the maximum failure depth of the floor, as follows:

$$\frac{\partial H_{\rm m}}{\partial \alpha_2} = l_1 e^{\alpha_2 \tan \varphi_3} \left[ \tan \varphi_3 \cos \left( \frac{\varphi_1}{2} + \alpha_1 + \alpha_2 - \frac{\pi}{4} \right) - \sin \left( \frac{\varphi_1}{2} + \alpha_1 + \alpha_2 - \frac{\pi}{4} \right) \right] = 0$$
(18)

By setting the value inside the brackets of Equation 18 to 0, the value of  $\alpha_2$  is obtained as follows:

$$\alpha_2 = \varphi_3 - \frac{\varphi_1}{2} + \frac{\pi}{4} - \alpha_1 \tag{19}$$

Substituting Equation 19 into Equation 17, the expression for the maximum failure depth of the multi-layer composite floor under the second failure condition  $H_{\rm m}$  (Equation 20) is obtained as follows:

$$H_{\rm m} = l_1 e^{(\varphi_3 - \frac{\varphi_1}{2} + \frac{\pi}{4} - \alpha_1)\tan\varphi_3} \cos\varphi_3$$
  
=  $\frac{H_1 + H_2}{\sin\left(\frac{\varphi_1}{2} + \frac{\pi}{4} + \alpha_1 + \alpha_2\right)} e^{(\varphi_3 - \frac{\varphi_1}{2} + \frac{\pi}{4} - \alpha_1)\tan\varphi_3} \cos\varphi_3$  (20)

## 3.2.3 Failure depth of the floor under $H_1 < H_0 < H_1 + H_2$

When  $H_1 < H_0 < H_1 + H_2$ , as shown in Figure 6c, the logarithmic spiral is located within the middle and lower rock layers. However, the starting radius of the first segment of the spiral lies within the middle rock layer, and the center of rotation for the spiral is at the intersection point  $O_1$  of the extended line connecting the starting and ending radii of the spiral. The starting radius of the first segment of the spiral  $l_0$  can be expressed as follows:

$$l_{0} = \overline{NB} + \overline{O_{1}N} = \frac{\frac{M}{2\xi \tan \varphi_{f}} \ln \frac{kyH + C \cot \varphi}{\xi(P_{i} + C \cot \varphi)} - 2H_{1} \tan\left(\frac{\pi}{4} - \frac{\varphi_{1}}{2}\right)}{2 \cos\left(\frac{\pi}{4} + \frac{\varphi_{2}}{2}\right)} + H_{1}\left[\tan\left(\frac{\pi}{4} + \frac{\varphi_{1}}{2}\right) + \tan\left(\frac{\pi}{4} - \frac{\varphi_{1}}{2}\right)\right] \cos\left(\frac{\pi}{4} + \frac{\varphi_{2}}{2}\right)$$
(21)

The value of the endpoint radius  $l_1$  of the logarithmic spiral within the middle rock layer is:

$$\begin{cases} l_1 = l_0 e^{\alpha_1 \tan \varphi_2} \\ l_1 = \frac{\overline{O_1 P} + H_2}{\sin\left(\frac{\varphi_2}{2} + \frac{\pi}{4} + \alpha_1\right)} \end{cases}$$
(22)

The expressions for  $\alpha_1$  and  $l_1$  are given by Equations 8, 9. Based on Figure 6*c*, the expression for the maximum failure depth  $H_{\rm m}$  of the multi-layer composite floor under the third failure state is as follows:

$$H_{\rm m} = l\cos\theta = l_1 e^{\alpha_2 \tan\varphi_3} \cos\left(\frac{\varphi_2}{2} + \alpha_1 + \alpha_2 - \frac{\pi}{4}\right) \tag{23}$$

When  $\frac{\partial H_{\rm m}}{\partial \alpha_2} = 0$ , The corresponding value of  $H_{\rm m}$  obtained from  $\alpha_2$  gives the maximum failure depth of the floor, which is:

$$\frac{\partial H_{\rm m}}{\partial \alpha_2} = l_1 e^{\alpha_2 \tan \varphi_3} \left[ \tan \varphi_3 \cos\left(\frac{\varphi_2}{2} + \alpha_1 + \alpha_2 - \frac{\pi}{4}\right) - \sin\left(\frac{\varphi_2}{2} + \alpha_1 + \alpha_2 - \frac{\pi}{4}\right) \right] = 0$$
(24)

By setting the value inside the brackets of Equation 24 to 0, the value of  $\alpha_2$  is obtained as:

$$\alpha_2 = \varphi_3 - \frac{\varphi_2}{2} + \frac{\pi}{4} - \alpha_1 \tag{25}$$

By substituting Equations 22, 25 into Equation 23, the expression for the maximum failure depth  $H_{\rm m}$  of the multi-layer composite floor under condition three (Equation 26) is obtained as:

$$H_{\rm m} = l_1 e^{\left(\varphi_3 - \frac{\varphi_2}{2} + \frac{\pi}{4} - \alpha_1\right) \tan \varphi_3} \cos \varphi_3 = \frac{\overline{O_1 P} + H_2}{\sin\left(\frac{\varphi_2}{2} + \frac{\pi}{4} + \alpha_1\right)} e^{\left(\varphi_3 - \frac{\varphi_1}{2} + \frac{\pi}{4} - \alpha_1\right) \tan \varphi_3} \cos \varphi_3$$
$$= \frac{\frac{H_1}{2} \left[ \tan\left(\frac{\pi}{4} + \frac{\varphi_1}{2}\right) + \tan\left(\frac{\pi}{4} - \frac{\varphi_1}{2}\right) \right] \sin\left(\frac{\pi}{2} + \varphi_2\right) + H_2}{\sin\left(\frac{\varphi_2}{2} + \frac{\pi}{4} + \alpha_1\right)} e^{\left(\varphi_3 - \frac{\varphi_1}{2} + \frac{\pi}{4} - \alpha_1\right) \tan \varphi_3} \cos \varphi_3$$
(26)

3.2.4 Failure depth of the floor under  $H_0 = H_1 + H_2$ 

When  $H_0 = H_1 + H_2$ , as shown in Figure 6d, the starting radius  $l_0$  of the logarithmic spiral is located at the contact surface between the middle and lower layers, with the center of rotation at the intersection point  $O_1$  of the extended line connecting the starting and ending radii of the spiral. The starting radius of the spiral is given by Equation 21. Based on Figure 6d, the expression for the maximum failure depth  $H_m$  of the multi-layer composite floor under condition four is obtained as:

$$H_{\rm m} = H_1 - \overline{O_1 P} + l\cos\theta = H_1 - \overline{O_1 P} + l_0 e^{\alpha_1 \tan\varphi_3} \cos\left(\frac{\varphi_2}{2} + \alpha_1 - \frac{\pi}{4}\right)$$
(27)

When  $\frac{\partial H_{\rm m}}{\partial \alpha_1} = 0$ , The corresponding value of  $H_{\rm m}$  obtained for  $\alpha_1$  represents the maximum failure depth of the floor, as follows:

$$\frac{\partial H_{\rm m}}{\partial \alpha_1} = l_0 e^{\alpha_1 \tan \varphi_3} \left[ \tan \varphi_3 \cos\left(\frac{\varphi_2}{2} + \alpha_1 - \frac{\pi}{4}\right) - \sin\left(\frac{\varphi_2}{2} + \alpha_1 - \frac{\pi}{4}\right) \right] = 0$$
(28)

By setting the value inside the brackets in Equation 28 to 0, the value of  $\alpha_1$  is obtained as follows:

$$\alpha_1 = \varphi_3 - \frac{\varphi_2}{2} + \frac{\pi}{4}$$
(29)

Substituting Equation 29 into Equation 27, the expression for the maximum failure depth  $H_{\rm m}$  of the multi-layer composite floor under the fourth failure state is obtained as follows:

$$\begin{split} H_{\rm m} &= H_1 - \overline{O_1 P} + l\cos\theta = H_1 - \overline{O_1 P} + l_0 e^{\left(\varphi_3 - \frac{\varphi_2}{2} + \frac{\pi}{4}\right) \tan \varphi_3} \cos \varphi_3 \\ &= H_1 - \frac{H_1}{2} \left[ \tan\left(\frac{\pi}{4} + \frac{\varphi_1}{2}\right) + \tan\left(\frac{\pi}{4} - \frac{\varphi_1}{2}\right) \right] \sin\left(\frac{\pi}{2} + \varphi_2\right) \\ &+ \left[ \frac{\frac{M_1}{2\xi \tan \varphi_f} \ln \frac{k p H + C \cot \varphi}{\xi (P_f + C \cot \varphi)} - 2 H_1 \tan\left(\frac{\pi}{4} - \frac{\varphi_1}{2}\right) \right] }{2 \cos\left(\frac{\pi}{4} + \frac{\varphi_2}{2}\right)} \\ &+ H_1 \left[ \tan\left(\frac{\pi}{4} + \frac{\varphi_1}{2}\right) + \tan\left(\frac{\pi}{4} - \frac{\varphi_1}{2}\right) \right] \cos\left(\frac{\pi}{4} + \frac{\varphi_2}{2}\right) \right] e^{\left(\varphi_3 - \frac{\varphi_2}{2} + \frac{\pi}{4}\right) \tan \varphi_3} \cos \varphi_3 \end{split}$$
(30)

3.2.5 Failure depth of the floor under  $H_0 > H_1 + H_2$ 

When  $H_0 > H_1 + H_2$ , as shown in Figure 6e, the active limit failure zone penetrates through three layers of the floor rock. At this point, the entire logarithmic spiral is located within the lower layer of rock. The initial radius  $l_0$  of the spiral is given by Equation 21, and in  $\Delta O_1 EF$ 

$$\overline{EF} = l_0 e^{\alpha_1 \tan \varphi_3} \cos\left(\frac{\varphi_3}{2} + \alpha_1 - \frac{\pi}{4}\right)$$
(31)

When  $\frac{\partial \overline{EF}}{\partial \alpha_1} = 0$ , The corresponding value of  $\overline{EF}$  obtained for  $\alpha_1$  represents the maximum failure depth of the floor, as follows:

$$\alpha_1 = \frac{\pi}{4} + \frac{\varphi_3}{2} \tag{32}$$

By substituting Equations 30, 32 into Equation 31 and simplifying, the expression for the maximum failure depth  $H_{\rm m}$  of the multi-layer composite floor under the fifth failure state (Equation 33) is obtained as follows:

$$\begin{split} H_{\rm m} &= \overline{EF} + H_1 + H_2 - \overline{O_1P} = H_1 + H_2 + e^{\left(\frac{\pi}{2} + \frac{\pi}{4}\right) \tan \varphi_3} \cos \varphi_3 \\ & \left\{ \begin{array}{l} \left\{ H_1 \left[ \tan\left(\frac{\pi}{4} + \frac{\varphi_1}{2}\right) + \tan\left(\frac{\pi}{4} - \frac{\varphi_1}{2}\right) \right] + \frac{H_2}{\tan\left(\frac{\pi}{4} + \frac{\varphi_2}{2}\right)} + \frac{H_2}{\tan\left(\frac{\pi}{4} - \frac{\varphi_2}{2}\right)} \right\} \\ & \cos\left(\frac{\pi}{4} + \frac{\varphi_3}{2}\right) + \frac{\frac{M}{2\xi \tan \varphi_3} \ln \frac{k \chi H + C \cot \varphi}{\xi (F_1 + C \cot \varphi)} - 2H_1 \tan\left(\frac{\pi}{4} - \frac{\varphi_2}{2}\right) - 2H_2 \tan\left(\frac{\pi}{4} - \frac{\varphi_2}{2}\right)}{2 \cos\left(\frac{\pi}{4} + \frac{\varphi_2}{2}\right)} \\ & - \left\{ H_1 \left[ \tan\left(\frac{\pi}{4} + \frac{\varphi_1}{2}\right) + \tan\left(\frac{\pi}{4} - \frac{\varphi_1}{2}\right) \right] + \frac{H_2}{\tan\left(\frac{\pi}{4} + \frac{\varphi_2}{2}\right)} + \frac{H_2}{\tan\left(\frac{\pi}{4} - \frac{\varphi_2}{2}\right)} \right\} \\ & \cdot \frac{\sin\left(\frac{\pi}{2} + \varphi_3\right)}{2} \end{split}$$

$$\end{split}$$

### 3.3 Calculation of floor failure depth

For the 4,301 working face, the mining height M is 6.25 m, the burial depth H is 600 m, the average overlying rock unit weight  $\gamma$  is 25 kN/m<sup>3</sup>, and the average internal friction angle of the rock layers is 32°, The coal seam cohesion C and internal friction angle  $\varphi$  are 1.2 MPa and 28°, respectively. The average internal friction angle  $\varphi_0$  of the floor rock layer is 39°, and the stress concentration factor *k* is taken as 2.5. Substituting these parameters into Equation 3, the maximum failure depth of the single-layer homogeneous floor is calculated to be 23.94 m.

For the composite floor, the internal friction angles of the upper, middle, and lower layers of the floor are 39°, 37°, and 39°, respectively. The thicknesses of the upper and middle layers  $H_1$  and  $H_2$  are 6.75 m and 11.63 m, respectively. By substituting these parameters into the floor failure depth calculation formula, the maximum failure depth of the hard-soft-hard composite floor of the 4,301 working face is calculated to be 18.26 m. This result aligns more closely with field measurements compared to calculations based on the single-layer homogeneous floor.

### 4 Numerical simulation

#### 4.1 Establishment of numerical model

Using the geological comprehensive columnar diagram of the 4,301 working face (Figure 1c), a FLAC3D numerical model was developed to investigate the failure characteristics of the mining floor. The model dimensions are set to  $400 \text{ m} \times 400 \text{ m} \times 300 \text{ m}$  (length × width × height), with a mining length of 300 m. To account for boundary effects, protective coal pillars of 50 m are included on each side of the model, both laterally and longitudinally. In the floor, multiple survey lines were placed to monitor the evolution of stress during mining. The spacing between survey lines and measurement points on each line is 5 m. To improve computational efficiency, the model uses a lower grid density for the roof, while increasing the grid



TABLE 1 Physical and mechanical parameters of typical coal and rock masses.

Lithology	Density (kg/m <sup>3</sup> )	Bulk modulus /GPa	Shear modulus /GPa	Cohesion /MPa	Internal friction angle/(°)	Tensile strength/MPa
Sandy Mudstone	2,200	8.17	4.23	3.2	37	2.7
Mudstone	2,500	7.30	3.05	2.6	35	2.1
Middle Sandstone	2,550	12.00	6.54	6.3	41	4.2
Fine Sandstone	2,480	10.76	5.88	5.6	39	4.7
Siltstone	2,500	11.54	5.26	4.2	41	4.6
Coal	1,500	1.91	0.82	1.2	28	0.9
Coarse Sandstone	2,650	13.24	6.75	7.3	43	4.9
Limestone	2,800	14.68	7.21	6.1	40	5.2
Interface	Normal stiffness = 100 GPa/m, Shear stiffness = 50 GPa/m, Cohesion = 0.795 MPa, Internal friction angle = 31°					

density in the floor mesh. The four sides and bottom of the model are constrained to simulate displacement boundary conditions, while a vertical stress of 12.142 MPa is applied on the model's top surface to represent the overburden pressure. Additionally, a groundwater pressure of 6 MPa is applied to the Ordovician aquifer at the model base, with a lateral pressure coefficient set to 0.8. The numerical model configuration is shown in Figure 7, and the physical and mechanical parameters of each rock layer are provided in Table 1.

## 4.2 Characteristics of floor mining damage

The calculations are performed using the numerical model illustrated in Figure 7. Mining of the 4,301 working face progresses from left to right. The working face advances 10 m per mining cycle, with the goaf roof collapsing naturally. In the model, the opening eye is positioned at X = 50 m, and the stop line is at X = 350 m. Figure 8 presents the floor damage characteristics observed as the 4,301 working face advances 300 m. Figure 8 comprises







six sub-figures, each depicting the plastic zone and vertical stress distribution of the floor.

#### As depicted in Figure 8:

At a working face advance of 50 m (Figure 8a), the maximum floor failure depth reaches 5.6 m, while the load on the immediate floor remains minimal, peaking at 0.44 MPa. In terms of failure morphology, shear failure predominates in the floor, although some rock layers near the coal seam and immediate floor exhibit sheartension failure. At a working face advance of 100 m (Figure 8b), the primary disturbance depth of floor failure remains 5.6 m, but discontinuous shear failure extends to a maximum vertical depth of 19.2 m. Composed primarily of low-strength mudstone, this layer experiences shear failure as mining stress surpasses its bearing capacity. Elsewhere, shear failure remains the dominant failure mode.

At 150 m (Figure 8c), shear failure continues to dominate, while the junction between mudstone and sandy mudstone exhibits shear-tension failure. The plastic failure zone beneath the working face gradually penetrates, reaching a maximum depth of 19.2 m. At 200 m (Figure 8d), the maximum floor failure depth



remains at 19.2 m without further downward extension. As the working face progresses, the floor's bearing capacity increases to 8.5 MPa. Notably, despite adjustments in vertical stress, shear failure remains the predominant damage mode, showing no significant changes.

At 250 m (Figure 8e), the maximum floor failure depth remains 19.2 m, with shear failure continuing as the predominant mode without notable variation. At 300 m (Figure 8f), the floor failure depth stabilizes at 19.2 m, with shear failure remaining dominant. The rock formations at the coal-mudstone and mudstone-sandy mudstone junctions consistently exhibit shear-tension failure.

## **5** Discussion

### 5.1 Results comparison

The measured data indicate a maximum floor failure depth of 19.3 m for the 4,301 working face, while theoretical calculations estimate it at 18.26 m and numerical simulations at 19.2 m. A comparative analysis (Figure 9) reveals that the relative error between theoretical calculation and numerical simulation and measurement results is small, ranging from 0.5% to 5.4%. Compared with traditional statistical formulas (Lu et al., 2022), the calculation results of plastic slip theory are more reliable.

## 5.2 Influencing factor analysis

Existing studies have shown that mining height (Dong et al., 2024), burial depth (Li et al., 2022), and the characteristics of the underlying rock strata (Cicek, S., 2020) influence the depth of floor failure. To further analyze the impact of coal seam occurrence characteristics and mining operations on the floor failure depth, variation curves of the maximum floor failure depth under different

burial depths and mining heights are plotted, as shown in Figure 10. From the graph, it is evident that the maximum floor failure depth exhibits a linear correlation with burial depth and a logarithmic relationship with mining height, with the latter showing diminishing returns at greater heights.

Considering the hard-soft-hard composite floor of the 4,301 working face as an example, the immediate floor beneath the coal seam remains a 6.75 m thick fine sandstone layer, with constant rock parameters. The maximum floor failure depth variations were calculated under different burial depths and mining heights. Furthermore, while maintaining constant burial depth and mining height, the maximum floor failure depth was calculated under varying mechanical parameters of the second and third rock layers beneath the immediate floor. During the calculations, the floor failure state applicable to different mining conditions was determined. The calculation results are presented in Figure 11.

Figure 11 illustrates that:

- (1) The maximum failure depth of a multi-layer composite floor increases with burial depth and mining height. However, unlike the trend seen in single-layer floors, the rate of increase varies under different calculation methods for different failure states. Within the same failure state, changes in mining conditions yield similar failure depths to those of a single homogeneous floor. Additionally, the floor failure depth increases as the internal friction angle of the second and third layers below the immediate floor increases, though the overall rate of increase remains relatively low.
- (2) Notably, for the 4,301 working face, where the immediate floor is a 6.75 m-thick fine sandstone layer, calculations with a burial depth H = 200 m and mining height M = 2 m show that both  $H_0$  and  $H_m$  are less than  $H_1$ . Consequently, the floor failure depth calculated using Equation (3) is smaller than the result from Equation (15), indicating that layer characteristics significantly influence floor failure. Further comparison of the results from Figures 10, 11 shows that, compared to a

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single homogeneous floor, the maximum failure depth of a multi-layer composite floor is reduced by (-35.5%) to 63.1% under the same mining conditions, with an average reduction of 23.1%, quantifying the constraining effect of a multi-layer composite structure on floor failure depth. This finding is consistent with the research results of Zhu and Mo (Shuyun et al., 2013; Mo et al., 2019).

In addition, Cao and Liang pointed out that the water pressure of the bottom plate will also affect the bottom plate failure depth (Cao et al., 2021; Liang et al., 2020), but this study did not involve this. Further studies will introduce water pressure into the bottom plate failure depth calculation formula based on plastic slip theory to achieve more accurate prediction.

## 6 Conclusion

- (1) The apparent resistivity evolution during the working face advancement indicates that the floor damage depth increases progressively due to mining disturbance. The measured maximum damage depth of the floor is 19.3 m, characterized by plastic slip failure.
- (2) Mining factors, including burial depth and mining height, are incorporated into the plastic slip failure theory of a single homogeneous rock layer. This theory is extended to a plastic slip line model for multi-layer floors, deriving the theoretical solution for the maximum damage depth across five damage states. For the 4,301 working face, this depth is calculated as 18.26 m.
- (3) A numerical model for the 4,301 working face was established. The floor failure depth increased to 19.2 m during working face advancement and then stabilized. Shear failure was identified as the primary failure mode, while shear-tensile failure occurred at rock layer junctions. Stress adjustment in the floor restored its stress environment without altering its failure mode.
- (4) The theoretical and numerical results are consistent with the field results. The maximum relative error is only 5.4%, which verifies the multilayer plastic slip theory. By analyzing examples, the effects of mining height, burial depth, and rock internal friction angle on floor damage depth are elucidated. Compared to single homogeneous floors, multi-layer composite floors exhibit a 23.1% reduction in damage depth on average, quantifying the rock structure's restrictive influence. These findings offer theoretical support for coal seam mining and water prevention efforts above confined aquifers.

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## Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

## Author contributions

ZK: Methodology, Resources, Writing – original draft, Writing – review and editing. XC: Project administration, Validation, Writing – original draft, Writing – review and editing. XW: Writing – original draft, Formal Analysis, Investigation. DZ: Supervision, Writing – review and editing. LC: Conceptualization, Funding acquisition, Validation, Writing – original draft, Writing – review and editing. SG: Software, Visualization, Writing – original draft.

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## **Conflict of interest**

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

## **Generative AI statement**

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