

Interval Prediction Method for Wind Speed Based on ARQEA Optimized by Beta Distribution and SWLSTM

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The interval prediction of wind speed is crucial for the economic and safe operation of wind farms. To overcome the probability density function parameter optimization and long-term correlation of time series problems in an interval prediction method, a hybrid model based on the beta distribution of an allele real-coded quantum evolutionary algorithm (ARQEA) and a shared weight long short-term memory (SWLSTM) neural network is proposed for predicting the interval of short-term wind speed, which is beta–ARQEA–SWLSTM. Input variables are determined *via* autocorrelation functions, and the shape and position parameters in the beta distribution function are optimized by the ARQEA algorithm. An interval-divided multi-distribution function aggregation is proposed to deal with the fluctuation of wind speed series. Lastly, case studies are provided to demonstrate the effectiveness of the proposed method.

OPEN ACCESS

Edited by: Jun Liu.

Jun Liu, Xi'an Jiaotong University, China

Reviewed by:

Xing Lu, Texas A&M University, United States Giuseppe Ciaburro, Università della Campania, Italy

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Specialty section:

This article was submitted to Smart Grids, a section of the journal Frontiers in Energy Research

Received: 24 April 2022 Accepted: 27 May 2022 Published: 05 July 2022

Citation:

Sun Z, Shen Y, Chen Z, Teng Y and Qian X (2022) Interval Prediction Method for Wind Speed Based on ARQEA Optimized by Beta Distribution and SWLSTM. Front. Energy Res. 10:927260. doi: 10.3389/fenrg.2022.927260 Keywords: wind speed, interval prediction, SWLSTM, beta distribution, ARQEA optimization

1 INTRODUCTION

Wind power generation differs from traditional fossil power generation methods. The integration of wind power into a power grid is restricted by the uncertainty and intermittency of wind speed. Therefore, to maximize the use rate of wind power, more accurate wind speed prediction is crucial for the control strategy of wind farms (Li et al., 2019; Naik et al., 2019; Li et al., 2020; Gan et al., 2021). This process can simultaneously deal with the indetermination of wind farms and decrease the schedule deflection of power systems (Zhang YX. et al., 2016; Liang et al., 2017; Khosravi et al., 2018; Wang and Li, 2018). A precise wind speed prediction interval (PI) can assist policymakers to control deviations in transmission network planning and dispatching, risk evaluation, and reliability estimation. It is also a key factor to be considered in reducing peak loads, guaranteeing backup capacity, and increasing the safe performance of large-scale wind power generation systems (Wang et al., 2016).

In general, wind speed prediction methods can be divided into two types: point wind speed prediction (PWS) and PI of wind speed (PIWS). Compared with PWS, PIWS can obtain additional upper and lower bounds for the predicted wind speed, which can provide more predictive information. Traditional PWS methods include physical, statistical, and artificial intelligence models. A PWS prediction method is simple in construction and facile to implement in wind farms. However, it is usually difficult to obtain accurate prediction results with this method because of the randomness and intermittent nature of wind resources. Although a lot of studies focus on improving the preciseness of the PWS method and have made some progress, the impact of wind power uncertainty still cannot be solved. For instance, the inhomogeneous distribution of wind farms is affected by local terrain, the nonlinear vibration of wind generators, and machine halts outside the plan (Kiplangat et al., 2016; Li and Jin, 2018; Wang et al., 2018). Therefore, errors occur in wind power prediction, posing risks to grid dispatch. By contrast, PIWS can provide additional forecast information and reduce risks in grid dispatch (Yuan et al., 2017a; Peng et al.,

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2017); thus, it will improve the understanding of decision-makers on the indeterminacy of wind power fluctuations to avoid potential risks.

In recent years, many studies were conducted on the uncertainties of wind power generation, and PIWS has already been used for many actual items. There are two sorts divisions of the PIWS methods. The first one uses neural networks to directly obtain the upper and lower bounds of PIs. As an instance, the lower bound/upper bound estimation (LUBE) for forecasting wind speed time series is a significant breakthrough in PIWS (Zhang et al., 2016b). The method solves the problem of probability prediction by constructing PIs, wherein an interval is represented by upper and lower estimates. However, the LUBE cannot deal with the fluctuation as an indetermination in wind speed time series. Another interval prediction method involves estimating PIs on the basis of the probability density of a point prediction result. To determine the uncertainty of wind speed, it is necessary to construct the probability density curve of prediction results, which requires the probability density prediction method. This can provide accurate prediction information on power system operation through this curve.

The preciseness of the wind speed probability distribution function (PDF) is determined by the selected approaches and the prediction error level, because the key factor of PIWS estimation is the PDF of forecasting error (Allen et al., 2017; Naik et al., 2018; Zhao et al., 2018). A shared weight long short-term memory (SWLSTM) neural network can decrease the variable number that should be optimized (Zhang et al., 2019). It also exhibits the advantages of nonlinear prediction, fast convergence, and the capability to capture the long-term correlations of the time series. At present, the SWLSTM model has been applied for wind speed prediction. Previous studies have shown that wind speed time series demonstrate long-term memory characteristics. The present study adopts the SWLSTM model as the basis for wind speed prediction. In addition, normal or Laplace distribution functions and beta distribution functions are also widely used as PDFs in the field of PIWS. Among them, the beta distribution is more effective in estimating the PIWS than the normal distribution and Laplace distribution (Ren et al., 2016). The beta distribution is selected as the basis of the PIWS in the present study consequently.

In this study, to improve the accuracy of wind speed, a new hybrid method based on the SWLSTM model and beta-ARQEA algorithm is proposed, which combines methods of artificial intelligence and statistics. The main contributions are listed as follows in four parts:

- The SWLSTM model is applied to wind speed prediction. The partial autocorrelation function is adopted to determine the input variables of the SWLSTM model to reduce the prediction error.
- 2) The real-coded quantum evolutionary algorithm (ARQEA) of alleles (Zhang et al., 2016c) is adopted to optimize the shape and position parameters in the beta distribution function for selecting the appropriate distribution function to fit the wind speed prediction error obtained by the SWLSTM model.
- The entire wind speed time series are divided into plenty of intervals per error distribution to improve the prediction accuracy of PIWS methods.



4) The optimized parameters of different distribution functions are utilized to fit the prediction error of each wind speed interval, then confirm the confidence interval of the wind speed series, and superimpose them to get the PI of the entire wind speed. The PIWS based on beta-ARQEA-SWLSTM achieves higher reliability and narrower interval bandwidth.

Eventually, the PI of the entire wind speed series is acquired by superimposing the confidence interval of each wind speed level. Therefore, the PIWS based on beta–ARQEA–SWLSTM achieves higher reliability and narrower interval bandwidth.

The rest part of this study is as follows: a review of the principle of an SWLSTM neural network is shown in **Section 2**. **Section 3** presents the key theory of ARQEA optimization parameters based on beta distribution and discusses how to use it to calculate confidence intervals. The PIWS process with the beta-ARQEA-SWLSTM model is introduced in **section 4**. **Section 5** contains a case study and result analysis. **Section 6** provides the conclusion drawn from the study.

2 SWLSTM NEURAL NETWORK

The SWLSTM model is a special artificial intelligence model. It keeps the characteristics of the recurrent neural network model, which can make use of a series of memory cells to deal with the

TABLE 1 | Hyperparameters of the SWLSTM model.

Model	Symbol	Meaning		
SWLSTM	t	Present cycle		
_	Xt	Input of the input layer		
_	nett	Intermediate variable		
_	St	Shared gates		
_	a_t	Information state		
_	C_t	Cell state		
_	h_t	Output of the hidden layer		
_	Уt	Output of the output layer		
_	1	One minus		
_	tanh	Activation function of tanh		
_	$\sigma(x)$	Activation function of sigmoid		
_	w,b	Weight variables		

arbitrary input data and enhance the learning process of the time series. In addition, the SWLSTM model can capture the longterm dependence of the input data to prevent the gradient disappearing from information transmission, which enhances its capacity to capture the dynamic changes of the time series.

In SWLSTM, a new type of shared gate is proposed, which is composed of input, output, and forget gate. The network structure is shown in **Figure 1**. SWLSTM does not change the gate structure of the standard long short-term memory (LSTM), but shares the weight and bias of the gate structure. The advantages of SWLSTM are reducing the number of variables that must be optimized and shortening the training time (Zhang et al., 2019).

As shown in **Figure 1**, the shared gate in the SWLSTM model has an inherent relationship with the time series, of which the purpose is to ensure that the training results often tend to be the new input information. Hence, training the time series model by the SWLSTM model has some advantages.

The hyperparameters of the SWLSTM model are shown in **Table 1**.

In **Figure 1**, x_t is the input of the input layer in the *t*-th cycle, *net*_t is the intermediate variable in the *t*-th cycle, S_t is the shared gates in the *t*-th cycle, a_t is the information state in the *t*-th cycle, C_t is the cell state in the *t*-th cycle, h_t is the output of the hidden layer in the *t*-th cycle, y_t is the output of the output layer in the *t*-th cycle, I is one minus, and *tanh*, σ is the activation function.

SWLSTM has two stages: forward propagation and backpropagation. The process of forward propagation of SWLSTM in the *t*th cycle is discussed as follows.

1) Calculate the shared gate state and calculate the information gate state:

$$net_t = w_h \cdot h_{t-1} + w_x \cdot x_t + b, \tag{1}$$

$$S_t = \sigma(net_t) = \sigma(w_h \cdot h_{t-1} + w_x \cdot x_t + b), \qquad (2)$$

$$a_t = \tanh(net_t) = \tanh(w_h \cdot h_{t-1} + w_x \cdot x_t + b).$$
(3)

2) Update the cell state:

$$C_t = s_t * C_{t-1} + (1 - s_t) * a_t.$$
(4)

3) Calculate the output of the hidden layer:

$$h_t = s_t * \tanh(C_t). \tag{5}$$

4) Output predicted value of the output layer:

$$y_t = s(z_t) = \sigma(w_y \cdot h_t + b_y).$$
(6)

In the preceding formula and figure, *t* represents the current cycle, x_t is the input of the input layer, S_t is the shared gates, and a_t is the information state. C_{t-1} and C_t represent the cell state in the previous and current cycles, respectively. h_{t-1} and h_t denote the output of the hidden layer in the previous and current cycles, respectively. y_t is the forecasted value of the current cycle. Intermediate variables are represented by net_t and z_t . $[w_h, w_x, b]$ and $[w_y, b_y]$ are two sets of weight variables that must be optimized. Symbol \cdot and * indicate matrix multiplication and multiplication between matrix elements, respectively. $\sigma(x)$ is the activation function of sigmoid and tanh(x) is the activation function of tanh.

The process of error back-propagation in the *t*th cycle of the SWLSTM is discussed as follows.

1) Use the squared error function as the optimization objective:

$$Et = \frac{1}{2} (y_t - Y_t)^2.$$
 (7)

2) Calculate the error of variables in the output layer:

$$\delta y_t = \frac{\partial E_t}{\partial y_t} = y_t - Y_t, \tag{8}$$

$$\delta z_t = \frac{\partial E_t}{\partial z_t} = \frac{\partial E_t}{\partial y_t} \frac{\partial y_t}{\partial z_t} = \delta y_t * [y_t * (1 - y_t)], \tag{9}$$

$$\delta w_{y} = \frac{\partial E_{t}}{\partial w_{y}} = \frac{\partial E_{t}}{\partial z_{t}} \frac{\partial z_{t}}{\partial w_{y}} = \delta z_{t} \cdot h_{t}, \qquad (10)$$

$$\delta b_{y} = \frac{\partial E_{t}}{\partial b_{y}} = \frac{\partial E_{t}}{\partial z_{t}} \frac{\partial z_{t}}{\partial b_{y}} = \delta z_{t} \cdot 1 = \delta z_{t}.$$
 (11)

3) Calculate the error of variables in the hidden layer:

$$\delta h_{t} = \frac{\partial E_{t}}{\partial h_{t}} = \begin{cases} \frac{\partial E_{t}}{\partial z_{t}} \frac{\partial z_{t}}{\partial h_{t}} = \delta z_{t} \cdot w_{y}, & t = T, \\ \frac{\partial E_{t}}{\partial z_{t}} \frac{\partial z_{t}}{\partial h_{t}} + \frac{\partial E_{t}}{\partial net_{t+1}} \frac{\partial net_{t+1}}{\partial h_{t}} = \delta z_{t} \cdot w_{y} + \delta net_{t+1} \cdot w_{h}, & t \neq T, \end{cases}$$
(12)

$$\delta C_t = \frac{\partial E_t}{\partial C_t}$$

$$= \begin{cases} \frac{\partial E_t}{\partial h_t} \frac{\partial h_t}{\partial C_t} = \delta h_t * s_t * \left[1 - \tanh^2(C_t)\right], & t = T, \\ \frac{\partial E_t}{\partial h_t} \frac{\partial h_t}{\partial C_t} + \frac{\partial E_t}{\partial C_{t+1}} \frac{\partial C_{t+1}}{\partial C_t} = \delta h_t * s_t * \left[1 - \tanh^2(C_t)\right] + \delta C_{t+1} \cdot s_t, & t \neq T. \end{cases}$$
(13)

The shared gates in SWLSTM reserve the functions of the three gates in the LSTM and still have the ability to discard useless historical information and keep current useful information. Coupling the input and forget gates simplified the LSTM without significantly decreasing the performance. Activation functions Sigmoid and tanh are retained in the SWLSTM. These two points indicate that the SWLSTM does not significantly reduce the prediction accuracy.

3 ESTIMATION OF RANDOM SAMPLES BASED ON THE BETA-ARQEA MODEL

Considering the optimization problem of probability density function parameters in interval prediction methods, to find the appropriate distribution function for fitting prediction errors of wind speed obtained by the SWLSTM model, the present study uses random sample estimation based on the beta-ARQEA model. The position parameters in the beta distribution function are optimized by using ARQEA. The beta distribution is expressed for a random sample R ={ $r_1, r_2, ..., r_n$ } as follows:

$$\beta(\gamma,\eta) = \int_0^1 z^{\gamma-1} (1-z)^{\eta-1} dz, \qquad (14)$$

where $\gamma > 0$, $\eta > 0$. z = (r - a)/(b - a), where a and b are the position parameters of the beta distribution (Yuan et al., 2019). The PDF based on beta distribution can be expressed as $Y = f(R, \gamma, \eta, a, b), n = 1, 2, \dots$

Using ARQEA to find the optimal parameters of the beta distribution function can further improve the precision of the beta distribution model.

Allele real-coding for beta position parameters is as follows (Zhang YX. et al., 2016):

where *position parameter*_i and *position parameter*_i' are encoded in the form of probability stacking. This process can effectively increase population diversity, prevent the occurrence of premature phenomena, and provide preconditions for improving optimization. The relative superiority of *position parameter*_i and *position parameter*_i' is determined in accordance with the distance relationship between each iteration process and the present optimal solution. The one that is closer to the present optimal solution is called the "better gene" x_i , and the other is called the "poor gene" x'_i . The hybrid evolution strategy is adopted to balance the global search and local search for different advantages.

1) The "better gene" x_i fully uses existing information to approach the present optimal solution under the guidance of the present optimal solution while searching for a better solution, which is

$$x_{inew} = x_i + sign(x_i^* - x_i) \cdot (K|x_i^* - x_i|), \quad (16)$$

where $sign(x_i^* - x_i)$ controls the evolution direction, *K* is the set constant that controls the step length of the directional evolution, and $|x_i^* - x_i|$ is the maximum range of evolution.

For the "poor gene" x_i, a local search with a scale shrink is used, that is,

$$x_{inew} = x_i + U(-1, 1) \cdot \left(1 - \arctan\left(\frac{r}{g}\right)\right) \cdot \Delta d,$$
 (17)

where U(-1, 1) is a random distribution between -1 and 1; r is the present algebra; g is the maximum iteration algebra; $(1 - \arctan(\frac{r}{g}))$ is the contraction function that decreases from 1 to 0 as algebra r increases, causing the scale of variation to decrease gradually with evolution; and Δd is the allowable range of variation.

The "better gene" and the "poor gene" perform local search and global search, respectively. A hybrid evolution strategy is developed when the two genes are transformed into each other, enhancing the balance between the local search and global search of the algorithm.

To evaluate the performance of the beta distribution model, the approximate index I is selected, which is defined as follows:

$$I = \frac{\sum_{n=1}^{M} (y_n - \bar{N}_n)^2}{M}, y_n = f(\bar{C}_n), n = 1, 2, ..., M,$$
(18)

where M is the number of frequency distribution histograms; in the *n*th histogram, \bar{N}_n and \bar{C}_n are the height and center position, respectively; the approximation PDF is represented as $f(\bar{C}_n)$; and y_n is the approximate PDF value of \bar{C}_n center position. When the fitting index I is small, approximation accuracy is high.

According to Eq. 18, the fitness function of the beta distribution optimization model and its constraints can be obtained as follows:

$$\min fitness = \min(I), \tag{19}$$

s.t.
$$\begin{cases} y, \eta \in (0, 1), \\ a, b \in (x_{\min}, x_{\max}), \end{cases}$$
 (20)

where x_{min} and x_{max} are the minimum and maximum values, respectively, of the sample.

To obtain the PDF of beta-ARQEA, we calculate the histogram of the frequency distribution of the sample $X = \{x_1, x_2, \ldots, x_n\}$ to obtain the desired fitting objective, then randomly initialize the parameters (a, b, γ, η) of the beta distribution function according to the constraint (20). After that, calculate the distance of each position parameter, determine the better gene and poor gene, then calculate the fitness of the genes, and retain the genes with better fitness. When the maximum number of iterations is reached, stop the loop. Finally, obtain the optimal parameters (a, b, γ, η) of the beta distribution function. According to **Eq. 14**, we can get the PDF based on optimized beta distribution.

After obtaining the PDF, the distribution function F(x) can be calculated by integration, the definition of which is as follows:

$$F(x) = \int_0^1 (\text{PDF}(p)) dx.$$
 (21)

Presume the confidence level is $100(1-\alpha)\%$, and the unknown parameter for sample *X* is θ . If $P\{\theta 1 < \theta < \theta 2\} = 1-\alpha$ and the interval $[\theta 1, \theta 2]$ is minimum, these two conditions are satisfied at the same time, and the interval $[\theta 1, \theta 2]$ occurs at a certain level of confidence, then



$$\begin{cases} \theta_1 = F\left(\frac{\alpha}{2}\right), \\ \theta_2 = F\left(1 - \frac{\alpha}{2}\right). \end{cases}$$
(22)

Then, we can obtain the confidence interval ($\theta 1$, $\theta 2$) of θ with the confidence level $100 \times (1 - \alpha)\%$.

4 PIWS ESTIMATION BASED ON THE BETA-ARQEA-SWLSTM MODEL

Since the SWLSTM's point prediction accuracy is high and beta–ARQEA's probability prediction results are reliable, SWLSTM and beta–ARQEA are combined to obtain high-precision point prediction, high-reliability interval prediction, and probability prediction. The wind speed PI implementation process based on the beta–ARQEA–SWLSTM model can be shown as follows:

Step 1: Divide the wind speed historical data into training dataset *Data*1 and test dataset *Data*2, *Data*1 = { $x_1, x_2, ..., x_n$ }, *Data*2 = { $x_1, x_2, ..., x_n$ }.

Step 2: *Data*1 and *Data*2 are normalized, and new training data X_1 and new test data X_2 are obtained.

Step 3: The PACF of X_1 is calculated, and the lag coefficient with a value of k is obtained. Then, the input data of the SWLSTM



model are determined as follows: *input* = { x_{t-1} , x_{t-2} , ..., x_{t-k} }, where $t = (k, k+1, k+2, ..., m), t \ge k$, and k > 0.

Step 4: X_1 is used to train the SWLSTM model, and the trained SWLSTM model is obtained.

Step 5: X_2 is used to test the trained SWLSTM model, and wind speed prediction $Y_2 = \{y_1, y_2, ..., y_n\}$ is determined.

Step 6: The errors between X_2 and Y_2 are calculated, and the error can be written as $D = \{d_1, d_2, ..., d_n\}$, where $d_i = y_i - x_i$ and i = 1, 2, ..., n.

Step 7: The predicted data Y_2 are divided into K levels in accordance with the rated speed of a wind farm.

Step 8: Wind speed prediction values and their forecasting errors under each wind speed level are statistics. The values and errors are denoted as $Y_{2k} = \{y_1^k, y_2^k, ..., y_{nk}^k\}$ and $D_k = \{d_1^k, d_2^k, ..., d_{nk}^k\}$, where the prediction error number of the *k*th wind speed level is represented as *nk*.

Step 9: Input D_k to the beta-ARQEA, and the upper-lower limits of every wind speed level are calculated according to **Eq. 22**. Then obtain the PI of the *k*th wind speed level $[\Delta_k^1, \Delta_k^u]$.

Step 10: The wind speed series PI of every level, which can be represented as $[Y_{2k} + \Delta_k^1, Y_{2k} + \Delta_k^u]$, is acquired.

Step 11: The entire wind speed series PI consists of each wind speed level.

Wind speed PI implementation based on the beta-ARQEA-SWLSTM is shown in **Figure 2**.

5 CASE STUDY

5.1 Wind Speed Series Data

In the current study, the wind speed series data of a wind farm in Jilin, China, are used. The wind speed series data in April 2018 were selected, which were measured and recorded by the wind tower. The step of wind speed series data is 15 min. The model of the wind turbine used in the wind farm is S82–1.5, the rated wind speed is 13 m/s, and the cut-in wind speed and the cut-out wind speed are 4 m/s and 20 m/s, respectively. To verify the performance of the



model, four datasets are selected for testing, one of which is shown in **Figure 3**. Each dataset uses a data length of 7 days consisting of 672 wind speed time series. Take approximately 80% of the data from every set as a training set and take the remaining portion as a validation set. The training set is used to calibrate the parameters of the beta–ARQEA–SWLSTM model and the validation set is used to verify the performance of the beta–ARQEA–SWLSTM model for the prediction interval of wind speed.

5.2 Evaluation Criteria

5.2.1 Evaluation Criteria of PIWS

To evaluate the performance of different models, these indicators are selected to verify the effectiveness of the PI model: PI coverage probability (*PICP*), average bandwidth ($\Delta \bar{P}$), index *F*, and sharpness (\bar{S}^{α}) (Yu et al., 2018).

To clarify the definition, the *i*th measured value is represented by x_i , and thus, I(i) = [lb(i), ub(i)] represents the $100(1 - \alpha)\%$ confidence PI of x_i , which is a random interval, where lb(i) is the upper limit and ub(i) is the lower limit. The *PICP* is shown as follows:

$$PICP = \frac{1}{n} \sum_{i=1}^{n} c_i, \tag{23}$$

where *n* is the number of samples and c_i is the indicator of *PICP*. If X = 1, then $c_i = 1$; otherwise $c_i = 0$.

The average bandwidth $\Delta \overline{P}$ is defined as:

$$\begin{cases} \Delta \bar{P} = \frac{1}{n} \sum_{i=1}^{n} \Delta P_{i}, \\ \Delta P_{i} = ub(i) - lb(i). \end{cases}$$
(24)

At the same confidence level, a smaller $\Delta \bar{P}$ results in better performance of the PI.

If the interval width $\Delta \bar{P}$ is narrower and *PICP* is larger, there will be better prediction results. Therefore, we use a comprehensive index *F*, which considers *PICP* and $\Delta \bar{P}$, to evaluate the performance of the PI (Tasnim et al., 2018):

$$F = \frac{2 \times PICP \times \frac{1}{\Delta P}}{PICP + \frac{1}{\Delta P}}, \quad if \ PICP \ge (1 - \alpha). \tag{25}$$

The F value takes into account two contradictory indicators, which can integrate the evaluation of the quality of the PI. The higher the F, the more effective the test method will be.

TABLE 2 | Fitting indicators in each wind speed grade of the four models.

	(0.3–0.4) S	(0.4–0.5) S	(0.5–0.6) S	(0.6–0.7) S	(0.7–0.8) S
Beta-ARQEA-SWLSTM	0.128	0.406	0.227	0.118	0.128
Beta-PSO-SWLSTM	0.198	1.698	0.494	0.121	0.198
Beta-SWLSTM	4.976	12.219	8.887	26.295	4.976
LSSVM	5.601	14.181	9.852	24.577	4.601



TABLE 3 Performance of the compared PIWS models.					
	PICP/%	∆Ē/(m/s)	\bar{S}^{α}	F	
Beta-ARQEA-SWLSTM	90	4.32	0.672	4.42	
Beta-PSO-SWLSTM	90	4.592	0.784	5.85	
Beta-SWLSTM	90	5.416	0.744	6.27	
LSSVM	90	5.824	0.93272	6.33	

In accordance with the concept of sharpness, the quality of the PI opposite to x_i can be computed, denoted by $S^{\alpha}(x_i)$, which is

$$S^{\alpha}(x_{i}) = \begin{cases} -2\alpha \cdot \Delta P_{i} - 4[lb(i) - x(i)], & if \ x(i) < lb(i), \\ -2\alpha \cdot \Delta P_{i}, & if \ x(i) < l(i), \\ -2\alpha \cdot \Delta P_{i} - 4[x(i) - ub(i)], & if \ ub(i) < x(i). \end{cases}$$
(26)

Here, sharpness \bar{S}^{α} is defined as

$$\bar{S}^{\alpha} = \frac{1}{n} \left| \sum_{i=1}^{n} S^{\alpha}(x_i) \right|.$$
(27)

Here, a smaller $S^{\alpha}(x_i)$ indicates higher PI quality.

5.2.2 Probability Prediction Evaluation Indicator

To verify the certainty, ensemble, and probability prediction, the comprehensive evaluation indicator of prediction performance,

defined as

TABLE 4 | Probability prediction metrics in each dataset.

CRPS	Dataset 1	Dataset 2	Dataset 3	Dataset 4
Beta-ARQEA-SWLSTM	0.020	0.019	0.014	0.016
Beta-PSO-SWLSTM	0.025	0.023	0.019	0.021
Beta-SWLSTM	0.029	0.025	0.022	0.020
LSSVM	0.036	0.029	0.028	0.029

namely the continuous sorting probability score (*CRPS*) (Alessandrini et al., 2015), is adopted. Assuming that $p(y_i)$ is the PDF of the *i*th forecast value obtained by the beta-ARQEA-SWLSTM, $F(y_i)$ is the cumulative distribution function (CDF) of $p(y_i)$. The *CRPS* is defined as

$$CRPS = \frac{1}{Te} \sum_{i=1}^{Te} \int_{-\infty}^{+\infty} \left[F(y_i) - H(y_i - Y_i) \right]^2 dy_i, \quad (28)$$

$$F(y_i) = \int_{-\infty}^{y_i} p(x) dx,$$
 (29)

$$H(y_i - Y_i) = \begin{cases} 0, & y_i < Y_i, \\ 1, & others, \end{cases}$$
(30)

where $H(y_i - Y_i)$ is the Heaviside function. When the *CRPS* is smaller, the comprehensive performance is better.

5.2.3 Reliability Evaluation Indicator

Reliability is the statistical consistency between forecasting and observations. Probabilistic integral transformation (*PIT*) values are used to evaluate the reliability of forecasting by a unified probabilistic graph (Liu et al., 2018). *PIT* is computed by observation results and CDF, which is defined as:

$$PIT = F(Y_i) = \int_{-\infty}^{Y_i} p(x) dx.$$
(31)

To check whether the *PIT* values of the test samples follow uniform distribution, all test samples can be found from the uniform probabilistic graph. *PIT* values will be uniformly distributed between 0 and 1 if the forecast is reliable.

5.3 Results and Analysis

To verify the effectiveness of the method proposed in this research, beta-ARQEA-SWLSTM is compared with other wind speed prediction methods in terms of point prediction accuracy, PI suitability, and probability prediction comprehensive performance. Then, the reliability of beta-ARQEA-SWLSTM is verified.

1) Point prediction results of wind speed.

To test the point forecasting accuracy of the method, the beta-ARQEA-SWLSTM model is applied for wind speed forecasts. The results are shown in **Figure 4**.

It can be seen from **Figure 4** that the wind speed forecasted values of the SWLSTM model is near the observed values. The PDF is difficult to fit all the wind speed forecasting errors, so we partition the wind speed into 10 wind speed grades following the predicted value. The grade gap of wind speed is 0.1 *S*, in which *S* is



Wind Speed Interval Prediction



the cut-out wind speed. Compare the beta-particle swarm optimization (PSO)-SWLSTM model (beta-PSO-SWLSTM), standard beta distribution SWLSTM model (beta-SWLSTM), and least square support vector machine (LSSVM) model with the beta-ARQEA-SWLSTM model to verify the validity of the beta-ARQEA-SWLSTM model. In accordance with Eq. 19, the fitting indexes of these models are shown in Table 2.

When the results of each distribution model in **Table 2** are compared with that of the beta-ARQEA distribution model, the fitting indicator *I* output by the beta-ARQEA model is the smallest among the four distribution models for every wind speed grade, indicating that the beta-ARQEA-SWLSTM model has the highest accuracy. This finding proves that the beta-ARQEA-SWLSTM model is superior to other models in wind speed point prediction.

2) Interval estimation of wind speed.

The interval estimation of wind speed is to verify the suitability of beta-ARQEA-SWLSTM. The wind speed PI results obtained from beta-ARQEA-SWLSTM are shown in **Figure 5**.

It can be seen from **Figure 5** that the PI adopting the beta-ARQEA-SWLSTM model basically contains all the actual wind speed data. The little green dots in **Figure 5** are the points at which the observation exceeds the prediction interval of beta-AEQEA-SWLSTM. The performance indicators of four models are computed and compared to verify the superiority of the beta-ARQEA-SWLSTM model. The results are shown in **Table 3**.

As indicated in Table 3, the coverage rate of each model reached 90%. When the coverage rate reaches the standard, the interval width represented by $\Delta \overline{P}$. In the four models. is the beta-ARQEA-SWLSTM model has the smallest $\Delta \overline{P}$, the smallest sharpness \overline{S}^{α} , and the highest *F* index, indicating that the bandwidth of the wind speed PI obtained by the beta-ARQEA-SWLSTM model is narrower and has the highest sharpness and quality. In addition, there is a higher preference for PI. Based on the aforementioned results, it can be seen that the beta-ARQEA-SWLSTM model has a better coverage rate and narrow bandwidth in the wind speed PI, and can realize high-quality wind speed PI.

3) Probability prediction results.

To verify the entire performance of the PDF of each model, probability prediction evaluation is applied. The *CRPS* is used to evaluate the whole PDF, and the results contain point forecast, PI, and the entire performance of the PDF (Tang et al., 2020; Zhang et al., 2020). The *CRPS* of each model on each dataset is shown in **Table 4**. In each dataset, the *CRPS* of beta–ARQEA–SWLSTM is optimal. This finding fits well with point prediction and PI.

4) Verification of beta-ARQEA-SWLSTM reliability.

guarantee that prediction of То the results the beta-ARQEA-SWLSTM are convincing, reliability evaluation is essential. If the prediction results are reliable, then the PIT of each predicted value in the validation set should satisfy uniform distribution (Liu et al., 2018). To see the distribution of PIT values intuitively, their uniform probability diagram is plotted, as shown in Figure 6.

As can be seen from **Figure 6**, the *PIT* range of the two datasets is uniformly covered (0,1), and uniformly distributed along the diagonal and at the Kolmogorov 5% visibility band, showing that the predicted PDF is in an appropriate range (Yuan et al., 2017b). In consequence, the prediction results of beta–ARQEA–SWLSTM are persuasive and reliable.

To summarize, compared with other models, the proposed hybrid model has higher accuracy, coverage rate and reliability in wind speed point prediction, interval estimation, probability prediction and reliability evaluation, and can provide higher quality wind speed prediction interval and more accurate results.

6 CONCLUSION

To achieve the goal of "carbon peaking, carbon neutralization," clean and renewable wind energy is very important. Accurate wind speed prediction is crucial for the smooth operation of wind turbines and improving their connection to grids. A new hybrid method based on the ARQEA algorithm and beta–SWLSTM model is proposed to improve the accuracy of wind speed prediction and the convergence speed. Compared with the traditional PIWS method, the hybrid model retains functionality while being able to capture the long-term correlations of the time series. The intervals of the wind speed time series are divided by the error distribution, which enables the hybrid model to obtain a PDF with higher reliability and narrower interval bandwidth.

The proposed method is applied on a wind farm in Jilin, China, to verify its effectiveness on wind speed forecasting. In order to accurately verify the applicability of point prediction, interval prediction, and the reliability of probability prediction, six reference indexes of *PICP*, $\Delta \overline{P}$, \overline{S}^{α} , *F*, *CRPS*, and *PIT* are adopted. Compared with the results of other models, it can be seen that the beta–ARQEA–SWLSTM model can obtain a wider coverage range and narrower interval bandwidth. Moreover, the prediction results can also show high performance in point prediction, interval prediction, and probability prediction. The proposed method can not only be used for wind speed prediction problems but also for other problems related to time series.

The beta distribution is considered in the proposed model. However, for the wind power prediction problem, other distributions such as the Gaussian distribution may have a better performance for different scenarios. In future, more wind farms in different geographical conditions and more probability distribution hypotheses will be testified.

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material; further inquiries can be directed to the corresponding author.

AUTHOR CONTRIBUTIONS

ZS was responsible for the specific work of this manuscript. XQ and YS carried out some of the calculation work. ZC and YT guided the work of this manuscript.

FUNDING

The authors acknowledge the funding of the National Key Research and Development Plan (2017YFB0902100).

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