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\*CORRESPONDENCE Long Huang, I long.huang@xjtlu.edu.cn Joseph Camm, I joseph.camm@liverpool.ac.uk

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# Recent advances in the applications of machine learning methods for heat exchanger modeling—a review

Junjia Zou<sup>1,2</sup>, Tomoki Hirokawa<sup>3</sup>, Jiabao An<sup>1</sup>, Long Huang<sup>1\*</sup> and Joseph Camm<sup>2\*</sup>

<sup>1</sup>School of Intelligent Manufacturing Ecosystem, Xi'an Jiaotong-Liverpool University, Suzhou, China, <sup>2</sup>School of Engineering, University of Liverpool, Brownlow Hill, Liverpool, United Kingdom, <sup>3</sup>Department of Mechanical Engineering, University of Hyogo, Himeji, Hyogo, Japan

Heat exchanger modeling has been widely employed in recent years for performance calculation, design optimizations, real-time simulations for control analysis, as well as transient performance predictions. Among these applications, the model's computational speed and robustness are of great interest, particularly for the purpose of optimization studies. Machine learning models built upon experimental or numerical data can contribute to improving the state-of-the-art simulation approaches, provided careful consideration is given to algorithm selection and implementation, to the quality of the database, and to the input parameters and variables. This comprehensive review covers machine learning methods applied to heat exchanger applications in the last 8 years. The reviews are generally categorized based on the types of heat exchangers and also consider common factors of concern, such as fouling, thermodynamic properties, and flow regimes. In addition, the limitations of machine learning methods for heat exchanger modeling and potential solutions are discussed, along with an analysis of emerging trends. As a regression classification tool, machine learning is an attractive data-driven method to estimate heat exchanger parameters, showing a promising prediction capability. Based on this review article, researchers can choose appropriate models for analyzing and improving heat exchanger modeling.

#### KEYWORDS

machine learning, heat exchanger, modeling, design optimization, performance prediction

## **1** Introduction

A heat exchanger is a device that facilitates heat transfer between fluids at different temperatures. It is widely employed in applications such as air-conditioning, refrigeration, power plants, oil refineries, petrochemical plants, natural-gas processing, chemical plants, sewage treatment, and many others (Hall, 2012; Singh et al., 2022). Theoretical analysis, analytical models, experimental methods, and numerical methods were conventionally applied to study the heat transfer and fluid flow processes within the heat exchangers (Du et al., 2023). The analytical models generally involve several assumptions in the derivation of relevant equations and formulae. The process of heat transfer can be evaluated through classical methods, such as the logarithmic mean enthalpy difference (LMHD), the logarithmic mean temperature difference (LMTD), ε–NTU, etc. (Hassan et al.,

2016). However, these techniques are generally based on certain assumptions and conditions, such as constant physical properties, steady-state operation, negligible wall heat conduction, uniform distribution of flow properties, and a consistent air fluid temperature along the fin height.

For numerical modeling of heat exchangers, discretization of the refrigerant flow field and of the governing equations is required (Prithiviraj and Andrews, 1998). To achieve detailed analysis in computational solutions, one might consider employing advanced numerical techniques such as the Finite Volume Method (FVM) or the Finite Element Method (FEM). It is essential to achieve a balance of heat and mass in each cell (Moukalled et al., 2016). Computational Fluid Dynamics (CFD) can be a useful tool in designing, troubleshooting, and optimizing heat exchanger systems (Bhutta et al., 2012). It transforms the integral and differential terms in the governing fluid mechanics equations into discrete algebraic forms, thereby generating a system of algebraic equations. These discrete equations are then solved via a computer to obtain numerical solutions at specific time/space points. Nonetheless, numerical methods like CFD often require significant computational resources (Thibault and Grandjean, 1991; Yang, 2008).

In bridging the gap between computational efficiency and accuracy, several studies on machine learning methods for heat exchanger analysis have been developed to predict the performance of heat exchangers. Some representative machine learning methods recently used to analyze heat exchangers include Artificial Neural Networks (ANN), Support Vector Machine (SVM), Tree models, etc., which were shown to generate satisfactory results (Patil et al., 2017; Zhang et al., 2019; Ahmadi et al., 2021; Wang and Wang, 2021; Ewim et al., 2021; Fawaz et al., 2022). An analysis of the number of papers in this field clearly shows a significantly growing trend in recent years, as illustrated in Figure 1.

In this review, we mainly focus on the review of machine learning models for air-cooled heat exchangers (finned tube heat exchangers, microchannel heat exchangers, etc.) in the field of refrigeration and air-conditioning. The three main objectives of this paper are: 1) to summarize the studies on machine learning methods related to heat exchanger thermal analysis over the last 8 years; 2) to compare different machine learning methods employed in heat exchanger thermal analysis 3) to point out the limitations and emerging applications of machine learning in heat exchanger thermal analysis. The organization of this paper consists of the following five sections: Section 2 summarizes and classifies the machine learning methods. Section 3 summarizes applications of machine learning methods for modeling heat exchangers in recent years. Sections 4, 5 discuss the limitations of ANN modeling for heat exchanger analysis and future trends in this area, respectively.

# 2 Introduction to machine learning models

As illustrated in Figure 2, the machine learning approaches to modeling heat exchangers reviewed in this paper include Random Vector Functional Link Network (RVFL), Support Vector Machine (SVM), K-Nearest Neighbor (KNN), Gaussian Process Regression (GPR), Sequential Minimal Optimization (SMO), Radial Basis Function (RBF), Hybrid Radial Basis Function (HRBF), Least Square Fitting Method (LSFM), Artificial Neural Networks (ANN), Random Forest, AdaBoost, Extreme Gradient Boosting (XGBoost), LightGBM, Gradient Boosting Tree (GBT) and Correlated-Informed Neural Networks (CoINN). The following section of the paper focuses on the classifications of the various methods.

# 2.1 Classification of machine learning methods

Machine learning methods were introduced to predict or regress the performance indicators of heat exchangers, such as the Nusselt number (*Nu*), the Heat Transfer Coefficient (*HTC*), the pressure drop ( $\Delta P$ ), etc. Based on the learning approaches, machine learning





categories generally include supervised learning, unsupervised learning, and reinforcement learning. Semi-supervised learning and active learning were also employed in studies as a machine learning category, as shown in Figure 2.

In heat exchanger applications, machine learning techniques primarily use supervised learning, which involves developing predictive models using labeled data. Labeled data establishes a connection between input and output, enabling the prediction model to generate corresponding outputs for specific inputs. The essence of supervised learning lies in understanding the statistical principles that govern the mapping of inputs to outputs (Cunningham et al., 2008). Unsupervised learning is a machine learning approach in which predictive models are developed without relying on labeled data or a clear purpose (Celebi and Aydin, 2016).

Reinforcement learning refers to learning optimal behavior strategies by an intelligent system in continuous interaction with the environment (Wiering and Van Otterlo, 2012). For instance, Keramati, Hamdullahpur, and Barzegari introduced deep reinforcement learning for heat exchanger shape optimization (Keramati, Hamdullahpur, and Barzegari 2022).

Semi-supervised learning refers to the learning prediction considering both labeled data sets and unlabeled data (Zhu and Goldberg, 2009). There is typically a small amount of labeled data and a large amount of unlabeled data because constructing labeled data often requires labor and high cost, and the collection of unlabeled data does not require much cost. This approach aims to use the information in unlabeled data to assist in labeling data for supervised learning and achieve enhanced learning results at a lower cost (Zhu, 2005). Active learning refers to a specialized training approach where the model actively selects the data it wants to learn from. Unlike traditional machine learning methods where all training data is provided upfront, active learning allows the model to selectively acquire new labeled data during its learning process. As a result, semi-supervised learning and active learning are closer to supervised learning. The differences between active learning and semi-supervised learning are: In active learning, the algorithm selectively picks the most informative instances for manual annotation, aiming to enhance model accuracy while minimizing labeling workload. In contrast, in semi-supervised learning, the emphasis is not on actively selecting instances. Instead, it leverages a combination of labeled and unlabeled data to enhance model generalization and performance through the integration of these data sources. Chen et al. (Chen et al., 2021) introduced a hybrid modeling method combining the mechanism with semi-supervised learning for temperature prediction in a roller hearth kiln, which implies the possibility of being employed in heat transfer.

# 2.2 Introduction of the various machine learning methods

As shown in Table 1, the classification of the machine learning methods considered here is the following:

- Neural networks refer to a series of methods that simulate the human brain in the hierarchical structure of neurons to recognize the relationships among specified data (Mahesh, 2018). Supervised neural network refers to a network consisting of many neurons connected by weighted links, which was first introduced by Hopfield in 1982 in biological research (Hopfield, 1982; Mahesh, 2018). In the literature, the methods presented for heat exchangers, such as ANN or RVFL, are distinctive due to the structure of their network.
- A tree model in machine learning is a type of predictive modeling tool, transitioning from observed attributes of an entity, symbolized by the branches, to deductions about the entity's target value, encapsulated in the leaves (Clark and Pregibon, 2017). This model employs a hierarchical structure to parse the data, whereby each internal node corresponds to a specific attribute, each branch signifies a decision rule, and each leaf node represents an outcome or a prediction. The process

Machine learning categories	Output type	Learning strategy	Methods
Supervised Neural network	Classification, Regression	Minimize the loss function	Artificial Neural Networks (ANN), Random Vector Functional Link Network (RVFL), Correlated-Informed Neural Networks (CoINN), Hybrid Radial Basis Function (HRBF), Radial Basis Function (RBF)
Tree model	Classification, Regression	Maximum likelihood estimation for regularization	Random Forest (RF), AdaBoost, Extreme Gradient Boosting (XGBoost), LightGBM, Gradient Boosting Tree (GBT)
Support vector machine	Binary Classification	Soft margin maximization	Sequential Minimal Optimization (SMO)
Bayesian	Classification	Maximum likelihood estimation, maximum <i>a posteriori</i> estimation	Gaussian Process Regression (GPR)
K-nearest neighbor	Classification, Regression	Minimization of distance	K-Nearest Neighbor (KNN)

#### TABLE 1 The primary classification of machine learning.

initiates from the root node and progressively branches out based on defined decision rules, effectively segmenting the data space into non-overlapping regions (Rattan et al., 2022). The tree model defines how to get a prediction score. It can be employed for classification and regression, such as Random Forest, AdaBoost, XGBoost, LightGBM, GBT, etc.

- A Support Vector Machine (SVM) is a widely used supervised learning model in machine learning. It is used for both classification and regression tasks (Mahesh, 2018). However, it is primarily used in classification problems. The basic idea behind SVM is to find a hyperplane in N-dimensional space (where N is the number of features) that distinctly classifies the data points. The chosen hyperplane is systematically optimized to maximize the "margin," which is defined as the distance to the nearest data points across different classes. This maximization strategy is intended to minimize the model's generalization error, thus enhancing its predictive accuracy for classifying new instances. In the domain of SVM, Sequential Minimal Optimization (SMO) serves as an efficient algorithm for training. SMO can be optimized as a heuristic algorithm whose basic idea is to optimize only two variables at one iteration while fixing the remaining variables (Sun et al., 2008).
- Bayesian regression is a statistical method that uses the principles of Bayesian statistics to estimate the parameters of a regression model. It is an alternative to traditional regression models like linear regression, and it takes a fundamentally different approach to model the relationship between the dependent and independent variables (Sun et al., 2008). In Bayesian statistics, probabilities are treated as a measure of belief or uncertainty, which can be updated based on new data. This is especially useful for modeling systems where uncertainty is inherent, providing a flexible framework that allows for iterative refinement as new data is incorporated. Thus, Bayesian regression offers an alternative but robust way of tackling regression problems
- K-nearest neighbor can solve the classification and regression issues related to heat exchangers. A similarity metric is established within the data space, enabling the prediction of data labels by utilizing the nearest neighbors in the data space for reference (Kramer, 2013). In the K-nearest neighbor (KNN) algorithm,

when one seeks to predict the label of an unobserved data point, the algorithm specifically identifies 'K' instances from the training set that are in closest proximity to the given point. The determination of "proximity" is generally quantified using a distance metric, with the Euclidean distance being the most commonly employed metric in numerous applications. For illustrative purposes, if we set K to 3, the KNN procedure will focus on the three most proximate training data instances relative to the unobserved point to facilitate the prediction. In the realm of classification, the predominant label amongst these three neighbors is then allocated to the unobserved data point. In the context of regression analysis, the algorithm might predict the label by computing the mean value from the labels of the three nearest neighbors.

# 3 Machine learning models applied for heat exchanger modeling

Traditional physics-based models may encounter difficulties when dealing with complex and non-linear problems, requiring extensive specialist knowledge and experience. In this context, machine learning methods have been introduced to the field of heat exchangers. Machine learning models built upon experimental or numerical data can improve state-of-the-art simulation methodologies. Machine learning can reduce calculation time, increase prediction accuracy, and handle complex and non-linear issues. In recent years, there have been notable advances in the application of machine learning methods in the field of heat exchangers, such as using machine learning to predict heat transfer coefficients (Section 3.2.1), pressure drop (Section 3.2.2), and heat exchanger performance (Section 3.2.3) performing real-time analysis of complex experimental data, and optimizing large-scale thermal systems.

This section reviews the recent advances in applications of machine learning methods for heat exchanger modeling in the following categories: (Section 3.2.1) Modeling of Heat Transfer Coefficient (HTC), (Section 3.2.2) Modeling of pressure drops, (Section 3.2.3) Modeling of heat exchanger performance (Section 3.3) Fouling factors, (Section 3.4) Refrigerant thermodynamic properties, and (Section 3.5) Flow pattern recognition based on machine learning methods.



### 3.1 Heat exchangers

For the heat exchanger reviewed in this section, as shown in Figure 3A, microchannel heat exchangers consist of small-scale finned channels etched in silicon wafers and a manifold system that forces a liquid flow between fins (Harpole and Eninger, 1991). As shown in Figure 3B, the shell and tube heat exchangers are devices consisting of a vessel containing either a bundle of multiple tubes or a single tube bent several times, with the wall of the tube bundle enclosed in the shell being the heat transfer surface. This design has the advantages of simple structure, low cost, and wide flow cross-section (Mirzaei et al., 2017). As shown in Figure 3C, a plate heat exchanger is more compact than the shell and tube heat exchanger design because of its smaller volume and larger surface area and because its modular design can increase or reduce the number of required plates to satisfy different requirements, retaining excellent heat transfer characteristics (Abu-Khader, 2012). As shown in Figure 3D, Tube-Fin Heat Exchangers (TFHXs) are important components in heat pump and air conditioning systems, which consists of a bundle of finned tubes (Li et al., 2019).

## 3.2 Parameters modeling of heat exchangers

This subsection summarizes the use of machine learning in modeling heat exchangers, with each subsubsection describing different parameters predicted in the research, providing a comprehensive summary of the classifications. The different types of heat exchangers are shown in Tables 2–6. Tables 2–6 delineate specific literature references pertaining to each unique type of heat exchanger. Each table incorporates specific references correlating to a distinct type of heat exchanger. This systematic organization of information aims to streamline the process to effectively locate and review pertinent literature based on the unique type of heat exchanger they are researching.

To conduct a robust, quantitative assessment of the models introduced in this research, we have incorporated a range of error metrics, as cataloged in Tables 2–9. These metrics not only facilitate an empirical evaluation of model performance but also provide prospective users with a criteria-based framework for model selection relative to specific applications. We delineate the mathematical equations that form the basis for each type of error metric employed as shown in the following equations.

Mean Relative Error (MRE) is a metric that quantifies the relative size of the prediction errors with respect to the actual observed values. The formula for MRE is:

$$MRE = \frac{1}{n} \sum_{i=1}^{n} \frac{|X_{predict} - X_{real}|}{X_{real}}$$
(1)

Mean Absolute Error (MAE) is a popular metric for regression. It measures the average absolute difference between observed and predicted values. The formula is:

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |X_{predict} - X_{real}|$$
(2)

Authors	Type of machine learning	Input	Output	Error analysis
Moradkhania et al. (Moradkhani	GPR	$Pr_{tp}, Re_{tp}$ , x, $P_{red}, R, We_{go}, Fr_l, Bo$	Nusselt number	MRE 4.50%
et al., 2022a)	RBF	-		MRE 19.41%
	HRBF	-		MRE 24.53%
Ma et al. (Y. Ma et al., 2022)	GBT	$\alpha$ , N, Re and A	Nusselt number	RMSE 219.74% R <sup>2</sup> 99.90%
			Pumping power	RMSE 5.4% R <sup>2</sup> 99.95%
Hughes et al. (Hughes et al., 2022)	SVR	$Re_g, Re_f, Bo, We, ScV, Scl, Pr_f, Ja, T^*$	Nusselt number	MAE 4.95% for SVR
	RFR	-		MAE 8.6% for RFR
	GB	-		MAE 6.2% for GB
	ANN			MAE 5.3% for ANN
		Reg, Ref, Bd, We, ScV, ScL	Friction factor	MAE 5.0% for SVR
				MAE 8.9% for RFR
				MAE 7.0% for GB
				MAE 5.0% for ANN
Zhou et al. (Zhou et al., 2020a)	ANN	$\begin{aligned} & Bd, Co, Fr_f, Fr_{fo}, Fr_g, Fr_{go}, Ga, Ka, Pr_f, Pr_g, Re_f, Re_{fo}, Re_g, \\ & Re_{go}, Su_f, Su_g, Su_{fo}, Su_{go}, We_f, We_{fo}, We_g, We_{go} \end{aligned}$	Heat transfer coefficient	MAE 6.80% R <sup>2</sup> 98%
	Random Forest			MAE 18.56% <i>R</i> <sup>2</sup> 87%
	AdaBoost			MAE 34.60% R <sup>2</sup> 75%
	XGBoost	-		MAE 9.06% R <sup>2</sup> 97%
Montanez-Barrera et al. (Montañez-Barrera et al., 2022)	CoINN	Mixture vapor quality, Micro-channel inner diameter, Available pressure drop correlation	Pressure drop	MRE 6%
Qiu et al. (Qiu et al., 2021)	ANN	$ \begin{array}{c} Bd, \ Bo, \ Fr_f, \ Fr_{fo}, \ Fr_g, \ Fr_{go}, \ Fr_{tp}, \ Pr_f, \ Pr_g, \ Pe_g, \ Pe_f, \ Re_f, \\ Re_{fo}, \ Re_{go}, \ Re_{go}, \ Re_{eq}, \ Su_f, \ Su_g, \ We_f, \ We_{fo}, \ We_g, \ We_{go}, \ We_{tp} \end{array} $	Flow boiling pressure drop	MAE 9.58% for ANN
	KNN	-		MAE 10.38% for KNN
	XGBoost			MAE 13.52% for XGBoost
	Light GBM	-		MAE 14.49% for Light GBM
Zhu et al. (Zhu et al., 2021a)	ANN	The channel geometry size, Fluid thermal properties, The working fluid conditions and Heat flux or other derived	HTC (boiling and condensation)	MRE 11.41% for boiling
		dimensionless parameters		MRE 6.06% for condensation

#### TABLE 2 Machine learning applications for modeling microchannel heat exchangers.

Root Mean Squared Error (RMSE) is another commonly used regression metric. It first calculates the square of the difference between each observed value and its predicted value, averages these, and then takes the square root. Its formula is:

$$RMSE = \frac{1}{n} \sqrt{\sum_{i=1}^{n} \left( X_{predict} - X_{real} \right)^2}$$
(3)

Median Absolute Error (MedAE) is similar to MAE, but instead of using the mean of the absolute errors, it uses the median. The formula is:

$$MedAE = \frac{1}{n} \sum_{i=1}^{n} |X_{predict} - X_{median}|$$
(4)

R-squared, also known as the coefficient of determination, is used to measure how well the model explains the variability

Authors	Type of machine learning	Input	Output	Error analysis
Amalfi et al. (Amalfi and	RF	Mass flow rate, Saturation temperature, Heat flux, and	Nusselt number	MAE 10.0%
Kim, 2021)		Geometrical parameters	Local frictional pressure gradient	MAE 10.3%
Longo et al. (Longo et al., 2020c)	GBM	$\Phi$ , $\beta/\beta max$ , $Prf$ , Specific kinetic energy number, $P/Pc$ , and Boiling or condensation	Frictional pressure gradient	MAE of 6.6%
Longo et al. (Longo et al., 2020b)	ANN	$\Phi$ , $\beta / \beta max$ , $Pr_f$ , $Re_{eq}$ , and Reduced pressure	Heat transfer factor (boiling)	MAE 4.8%
Longo et al. (Longo et al., 2020a)	ANN	$\Delta T, \Delta T_{sup}, \Phi, Re_{eq}, Pr_f$	Heat transfer factor (condensation)	MAE 3.6%
Gupta et al. (Gupta et al., 2017)	ANN	Q, P1, P2, Pcd, Phd, T1, T3	Outlet cold fluid temperature	Average error of 0.25% for ANN
	ANFIS			Average error of 0.896% for ASNFIS
			Outlet hot fluid temperature	Average error of 0.19% for ANN
				Average error of 0.192% for ASNFIS

### TABLE 3 Machine learning applications for modeling plate heat exchangers.

### TABLE 4 Machine learning applications for modeling tube-fin heat exchanger.

Authors	Type of machine learning	Input	Output	Error analysis
Najafi et al. (Najafi et al., 2021)	RF	$xv, Re, (1-x)/x, Re_f, Re_{go},$	Frictional pressure drop	MARD 6.72%
Ardam et al. (Ardam et al., 2021)	RF	$X, F_{go}, n, Bo, e/D_{int}$	Pressure drop	MARD 6.41%
Xie et al. (Xie et al.,	ANN	<i>L</i> , α, β	Nusselt number	R <sup>2</sup> 99%
2022a)			Friction factor	R <sup>2</sup> 99.8%
Du et al. (Du et al., 2020)	ANN	$\theta$ , Re, DC, Re <sub>w</sub> , $T_{ia}$ , $T_{iw}$ , Ntr, Ntp the outer length of the	Nusselt number	MSE 78.97%
		major axis, the outer length of the minor axis, Dc	Friction factor	MSE 1.08%
Skrypnik et al.			Nusselt number	MAE 16.3%
(Skrypnik et al., 2022)			Friction factor	MAE 11.8%
Subbappa et al.	ANN	Refrigerant, Tubes per bank, Tubes per bank per circuit	Heat transfer and Refrigerant pressure	ANN and SVR ± 20% for 90%
(Subbappa et al., 2022)	RR	(i.e., circuitry), Tube banks, Tube length, Fins per inch, Air velocity, Refrigerant temperature, Refrigerant G	drop	
	SVR			
Li (Li et al., 2016) RSM based NN $T_{s,in}, x_{in}, m_r, V_a, T_{db,in}$ , and $T_{wb,in}$		$T_{s,in}$ , $x_{in}$ , $m_r$ , $V_a$ , $T_{db,in}$ , and $T_{wb,in}$	Total cooling capacity, Sensible heat ratio, and Pressure drops on both refrigerant and air sides	Dry condition <i>R</i> <sup>2</sup> >99.8%
				Wet condition $R^2 > 97.4\%$
Krishnayatra	KNN	Fin spacing, Fin thickness, Material, and Convective heat transfer coefficient	Overall efficiency	$R^2$ 90.14% k = 2
(Krishnayatra et al., 2020)		transier coenficient	Total effectiveness	$R^2$ 85.37% k = 8

Authors	Type of machine learning	Input	Output	Error analysis
El-Said et al. (El-Said et al., 2021)	RVFL	Cold fluid, and injected air volume flow rates	Outlet temperature of cold fluids	RMSE 52.78% for RVFL
	SMO	-		RMSE 149.6% for SMO
	SVM			RMSE 53.56% for SVM
	KNN			RMSE 140.0% for KNN
			Outlet temperature of hot fluids	RMSE 71.91% for RVFL
				RMSE 247.7% for SMO
				RMSE 174.1% for SVM
				RMSE 185.5% for KNN
			Pressure drop	RMSE 0.9093% for RVFL
				RMSE 2.3525% for SMO
				RMSE 1.5391% for SVM
				RMSE 0.8944% for KNN
Kunjuraman and Velusamy (Kunjuraman and Velusamy, 2021)	ANN	CF, FIT, SF	Condensate temperature	MRE 0.971% for ANN
	ANFIS	-		RMSE1.175% for ANN
				<i>R</i> <sup>2</sup> 94.56% for ANN
				MRE 0.381% for ANFIS
				RMSE 0.532% for ANFIS
				<i>R</i> <sup>2</sup> 99.98% for ANFIS
Roy and Majumder (Roy and Majumder, 2019)	FFBN	Tube configurations (30, 40, 60, and 90), Different fluids, surface, Temperature	Exergetic Plant Efficiency	Accuracy 98.11%
			Energetic Cycle	Accuracy 97.40%
			Efficiency	Accuracy 96.35%
			Electrical Power Cost	Accuracy 97.23%
			Fouling factor	Accuracy 98.32%
Muthukrishnan et al. (Muthukrishnan et al., 2020)	SVM	Nt, Sb, Nb, Dc	Heat transfer rate	Accuracy >90%

#### TABLE 5 Machine learning applications for modeling shell and tube heat exchanger.

among the observed values. It ranges between 0 and 1, with values closer to 1 indicating a better fit. Its formula is:

$$R^{2} = 1 - \frac{\sum_{i=1}^{n} (X_{predict} - X_{real})^{2}}{\sum_{i=1}^{n} (X_{predict} - X_{average})^{2}}$$
(5)

## 3.2.1 Modeling of Heat Transfer Coefficient

The Heat Transfer Coefficient (HTC) plays a pivotal role in the design and optimization of heat exchangers. It is a key parameter that describes the rate of heat transfer per unit area, per unit of temperature difference. In fluid dynamics and heat transfer studies,

### TABLE 6 Machine learning applications for modeling other heat exchangers.

Authors	Type of heat exchangers	Type of machine learning	Input	Output	Error analysis
Azizi and Ahmadloo (Azizi	Inclined tube	ANN	$IA, G, T_s, xv$	Heat transfer coefficient	MAE 1.94%
and Ahmadloo, 2016)					R <sup>2</sup> 99.5%
Zheng et al. (Zheng et al., 2022)	Heat exchange channels with bulges	GRNN RF	Order of the bulge heights at different locations (6 nodes)	Heat transfer coefficient	Both <i>R</i> <sup>2</sup> >97% for GRNN and RF
Moradkhani et al.	Inside smooth helically	GPR	$Re_{tp}, Pr_{tp}, X, P_{red}, Bo, Dt/Dc$	Boiling heat transfer	MRE 5.93% for GPR
(Moradkhani et al., 2022b)	coiled tubes	RBF	and Frf	coefficient	MRE 6.67% for RBF
		MLP	-		MRE 9.27% for MLF
<b>Kwon et al. (</b> Kwon et al., 2020)	Rough cooling channel	RF	Height of channel geometries e1, e2, e3, e4, e5 (5 nodes)	Convection heat transfer coefficients	$R^2 > 96.6\%$
Dalkilic et al. (Dalkilic et al., 2019)	Smooth pipe	ANN	Re, $Gr\Delta T^{*}10^{-6}6$ , Pr, Bd, f, f0, $\mu w/\mu b$ , $f v p$	Tube length averaged the Nusselt number and Nusselt number in forced convection	Accuracy ±5%
Chokphoemphun et al. (Chokphoemphun et al.,	Grooved channel air heater	NN	Turbulator, Depth ratio, <i>IA</i> ,	Nusselt number	<i>R</i> <sup>2</sup> 99.8864%
2020)			and Re	Friction factor	<i>R</i> <sup>2</sup> 99.9772%
				Thermal enhancement factor	R <sup>2</sup> 99.8858%
Alireza Zendehboudi*, Xianting Li (Zendehboudi	Inclined smooth tubes	PSO-ANN	$IA, G, xv$ , and $T_s$	Pressure drop	<i>R</i> <sup>2</sup> 96.092% for PSO-ANN
and Li, 2017)		GA-LSSVM	_		<i>R</i> <sup>2</sup> 99.931% for GA- LSSVM
		Hybrid-ANFIS			<i>R</i> <sup>2</sup> 99.932% for Hybrid-ANFIS
		GA-PLCIS	_		<i>R</i> <sup>2</sup> 99.937% for GA- PLCIS
					MSE RRMSE et al
				Frictional pressure drop	<i>R</i> <sup>2</sup> 97.753% for PSO-ANN
					<i>R</i> <sup>2</sup> 99.932% for GA- LSSVM
					<i>R</i> <sup>2</sup> 99.940% for Hybrid-ANFIS
					<i>R</i> <sup>2</sup> 99.944% for GA- PLCIS
					MSE RRMSE et al
Garcia et al. (Garcia et al.,	R407C in horizontal tubes	ANN	$Dt, G, P_s, and xv$	Pressure drop	MAE 6.11%
2018)					<i>R</i> <sup>2</sup> 99.9%
Shojaeefard et al. (Shojaeefard et al., 2017)	Compact heat exchanger (evaporator)	Numerical	$T_{a,in,db}, T_{a,in,wb}, P_{ref,in}, T_{ref,in}, \dot{m}_{ref}, and Va$	$Q_{evap}, P_{ref,out}, T_{ref,out}, T_{a,out,db}$ , and $T_{a,out,wb}$	RMSE (avg) 228.6% for Numerical
		FFNN	_		RMSE (avg) 501.7% for FFNN
		GA-trained			RMSE (avg) 479.1% for GA-trained
		RNN			RMSE (avg) 116.9% for RNN
					MSE, R <sup>2</sup>

(Continued on following page)

Authors	Type of heat exchangers	Type of machine learning	Input	Output	Error analysis
Uguz and Iperk (Uguz and	Compact heat exchanger	ANN	$T_{hw}, T_{hwi}, T_{cw}$ , $T_{cwi}$ , and $\dot{m_{cw}}$	T <sub>cw,out</sub>	<i>R</i> <sup>2</sup> 96.0% for ANN
Ipek, 2022)		MLR			<i>R</i> <sup>2</sup> 96.1% for MLR
		SVR	_		<i>R</i> <sup>2</sup> 94.2% for SVR
				T <sub>hw,out</sub>	MSE, MAE and MedAE
Peng and Ling et al. (Peng and	Compact heat exchangers	SVR	Fin height, Fin pitch, Fin,	Friction factor	MSE 2.645 *10-4
Ling, 2015)			Thickness, Fin length, and Reynolds number at the air side	Colburn factor	MSE 1.231 * 10-3
Azizi et al. (Azizi et al., 2016)	Gas-liquid flow in	ANN	$IA$ , $Re_{sg}$ , and $Re_{sl}$	Void fraction	MAE 1.52%
	horizontal, upward and downward inclined pipes				R <sup>2</sup> 99.48%
Bhattacharya et al. (Bhattacharya et al., 2022)	Heat exchanger	CNN-GRU SSM	$\dot{m}_{a\_in}, P_{atm}, T_{in}, RH_{in}, \dot{m}_{ref\_in},$ $h_{in}, P_{out}, h_{out}$	$p_{inlet}, p_{outlet}, h_{inlet}, h_{outlet}, Q_{total}, \dot{m}_{total}$	Maximum percentage error is capped at 0.2%
Li et al. (Li et al., 2023)	Printed circuit heat	ANN	$\dot{m}$ , D, $T_{in}$ , $P_{in}$ , Wall heat flux,	HTC	<i>R</i> <sup>2</sup> 99.94% for ANN
	exchangers	XGBoost	$V_{in}, \rho_{in},$ Length, Re and Pr		
		LightGBM		ΔΡ	<i>R</i> <sup>2</sup> 99.96% for ANN
		Random forest			
Chen et al. (Chen et al., 2023)	Energy pile heat pump system	ANN	T <sub>amb</sub> , RH <sub>amb</sub> , T <sub>room</sub> , RH <sub>room</sub> , P <sub>sys</sub>	Coefficient of performance	MAE 31.4%

### TABLE 6 (Continued) Machine learning applications for modeling other heat exchangers.

### TABLE 7 Prediction of the fouling factor for heat exchangers based on machine learning methods.

Authors	Type of heat exchangers	Type of machine learning	Inputs	Outputs	Error analysis
Hosseini et al. (Hosseini et al., 2022)	Preheat exchanger networks of petroleum refineries	GPR	Operation time, Surface temperature, Fluid velocity, Fluid density, Fluid temperature, and	Fouling factor (m²K/kW)	<i>R</i> <sup>2</sup> 13.89% for GPR
		DT	Equivalent diameter		<i>R</i> <sup>2</sup> 16.64% for DT
		Bagged Trees	-		<i>R</i> <sup>2</sup> 8.86% for Bagged Trees
		SVR	-		<i>R</i> <sup>2</sup> 35.39% for SVR
Mohanty (Mohanty, 2017)	Shell and tube heat exchanger		The Inlet temperature, Re, and Mass flow rate on both tube and shell sides	Tube-side temperature difference,	3.1 (predicted value)
				Shell side temperature difference	2.2 (predicted value)
				Efficiency	7.26% (predicted value)
Kuzucanlı et al. (Kuzucanlı et al.,	zucanlı et al.,	Varied flow rate, Inlet temperatures	Heat transfer coefficient and fouling	100% for Naïve Bayes	
2022)		DT	-	factor	99.3% for decision tree
		KNN			96.3% for KNN (Predict accuracy)
Sundar <i>et al.</i> (Sundar et al., 2020)	Cross-flow heat exchanger	Deep learning	$T_{fin}$ , $T_{win}$ , $\dot{m}_w$ , $f/\dot{m}_w$ , $\dot{m}_{flue}$ , $f/\dot{m}_{flue}$ , $T_{fo}$ , $T_{wo}$ ,	Overall fouling factor	<i>R</i> <sup>2</sup> 99.86%

Authors	The refrigerants	Type of machine learning	Inputs	Outputs	Error analysis
Zhi et al. (Zhi et al., 2018)	R1234ze(E), R1234yf, R32, R152a, R161 R245fa	ANFIS	Τ, Ρ, ρ	Viscosity	MAE 414.96% for ANFIS
		RBFNN	_		MAE 500.57% for RBFNN
		BPNN	_		MAE 515.61% for BPNN
					R <sup>2</sup> , RMSE
Gao et al. (Gao et al., 2019)	HFC-23, HFC-32, HFC-125, HFC-134a, HFC-143a, HFC-152a, HFC-161, HFC-227ea, HFC-236fa, HFC-245fa, HFO-1234yf, HFO-1234ze(E)	ANN	$P_{red}$ , 1 – Tr, $\omega$ , Pc/Pcr	Reduced residual heat capacity	MAE 0.779%
					RMSE 11.05%
					R <sup>2</sup> 99.52%
					MAD 13.6%
Wang et al. (X. Wang	R125, R134a, R143a, R152a, R161, R227ea, R236fa,	ANN	$P_{red}, Tr, M, \omega$	Viscosity	MSE 1.019e-5
et al., 2020)	R32, R1234yf, R1234yf, R1234ze(E), R1336mzz(Z)			Thermal conductivity	MSE 1.46774e-6
Zolfaghari and Yousefi	HFC-134a, Decane, Octane, Heptane, Diethyl	ANN	T, P, Mole fraction,	Density	MAE 0.34%
(Zolfaghari and Yousefi, 2017)	carbonate, Dimethyl carbonate, n-Nonane, n-Dodecane, CO2		Total molecular weight, Normal boiling temperature	-	
Nabipour (Nabipour,	R143a-R227ea, R32-R125, R290-152a, R32-R227ea,	ANN	T, Pc, Tc, Critical	Surface tension	MRE 0.7582%
2018)	R143a-R125, R125-R152a, R32-R134a, R125-R134a, R134a-R152a, R290-R600a, R290-R32, R134a- R143a, R290-RE170, R22-R115, R134a-R1234yf, R134a-R1234ze(E), R32-R1234yf, R32-R1234ze(E)		volume, ω		<i>R</i> <sup>2</sup> 99.97%

#### TABLE 8 Prediction of the thermodynamic properties for refrigerants based on machine learning methods.

the Nusselt number is often introduced as a dimensionless parameter delineating the relative significance of convective heat transfer to conductive heat transfer across a defined boundary. It essentially offers a normalized representation of the Heat Transfer Coefficient (HTC). Accurate prediction of HTC can lead to more efficient design and optimization of heat exchangers, resulting in improved performance and reduced energy consumption (Zhu et al., 2021). This subsection summarizes and categorizes studies related to the prediction of the Heat Transfer Coefficient (HTC) presented in recent literature. The classification is primarily based on the types of input parameters used, with a particular focus on distinguishing between dimensionless parameters and structural parameters. Additionally, a separate classification is conducted based on the different sources of data used, including historical literature, experimental data, and Computational Fluid Dynamics (CFD) simulations.

A plethora of research efforts has been methodically invested in the predictive modeling of the Heat Transfer Coefficient (HTC), focusing primarily on the influence of structural parameters to construct effective machine learning training datasets. For instance, Zheng *et al.* (Zheng et al., 2022) introduced General Regression Neural Network (GRNN) and RF algorithms to predict HTC in heat exchange channels with bulges with the inputs of each bulge height at different locations. Other works by Moradkhani et al. (Moradkhani et al., 2022a) and Kwon et al. (Kwon et al., 2020) have delved into the specifics of boiling and convection heat transfer coefficients, respectively. In these works, the effect of surface roughness on HTC has not been sufficiently explored, and the amount of measurement data on the topic is insufficient to include the impact of surface roughness in predictive models. Therefore, the empirical model that incorporates the effects of surface roughness into the HTC prediction model needs further research.

For a predictive model, the exclusive reliance on structural parameters may prove insufficient. Some studies in the literature have indeed embraced models where the database inputs consist of dimensionless numbers or physical properties, which can standardize data, enhance the stability and performance of the model, and make the model's output easier to understand and interpret. For instance, Longo et al. (Longo et al., 2020b) developed ANN to estimate the boiling heat transfer coefficients of refrigerants in Brazed Plate Heat Exchangers (BPHEs), where the inputs are the corrugation enlargement ratio ( $\Phi$ ), the reduced inclination angle ( $\beta/\beta max$ ), the liquid Prandtl number ( $Pr_f$ ,), the equivalent Reynolds number ( $Re_{eq}$ ), the boiling number (Bo), and the reduced pressure ( $P/P_{cr}$ ).

In understanding the various methodologies applied in machine learning modeling, a clear distinction arises from the source of databases utilized in various research. A portion of these investigations derives data from pre-existing literature, while

#### TABLE 9 Prediction of flow regime based on machine learning methods.

Authors	Type of experimental subjects	Type of machine learning	Input	Flow regime	Error analysis
Shen et al. (Shen et al., 2020)	Microchannels heat exchanger (Liquid- liquid biphasic flow patterns in the perfluoroalkoxy capillary with the inner diameter of 1 mm)	CNN	32,383 flow pattern images with labeled classification	(Camera) Annular/parallel flow, Slug flow, Droplet flow, Wavy annular flow, and Dispersed flow	Prediction accuracy > 98%
Ahmad et al. (Ahmad et al., 2022)	Millimetric closed-loop pulsating heat pipe (PHP)	DL	648 images flow pattern images with labeled classification	(Camera) Bubbly flow, Slug- plug flow, Elongated flow, and Annular flow	Prediction accuracy 96%
Giri Nandagopal et al.	Microchannel heat exchangers	ANN-PR	Confluence angle,	(Camera) Slug Flow, Bubble	<i>R</i> <sup>2</sup> 83.83% for ANN-PR
(Giri Nandagopal and Selvaraju, 2016)		ANN-FF	Superficial velocity of water, Superficial velocity	flow, Annular flow, Elongated slug flow, Deformed flow,	<i>R</i> <sup>2</sup> 88.64% for ANN-FF
		CFN	of dodecane	Stratified flow	<i>R</i> <sup>2</sup> 95.34% for CFN
		PNN			<i>R</i> <sup>2</sup> 97.66% foe PNN
		GRNN	-		<i>R</i> <sup>2</sup> 98.8% for GRNN
		ANFIS			$R^2$ 77.64% for ANFIS
Giri Nandagopal et al.	Microchannel heat exchangers	ANN-PR	Confluence angle,	(Camera) Slug Flow, Bubble	<i>R</i> <sup>2</sup> 93.95% for ANN-PR
(Giri Nandagopal et al., 2017)		ANN-FF	<ul> <li>Superficial velocity of water, Superficial velocity</li> <li>of dodecane</li> </ul>	flow, Annular flow, Elongated slug flow, Deformed flow, Stratified flow	<i>R</i> <sup>2</sup> 91.98% for ANN-FF
		CFN			$R^2$ 96.6% for CFN
		PNN			<i>R</i> <sup>2</sup> 95.58% for PNN
		GRNN			<i>R</i> <sup>2</sup> 98.8% for GRNN
		ANFIS	-		$R^2$ 90.22% for ANFIS
Roshani et al.	A Pyrex-glass pipe with outside	RBF NN	With two full energy	(Gamma ray) Annular,	MAE 0.6026%
(Roshani, Nazemi, and Roshani, 2017)	diameter 100 mm, thickness 2.5 mm and length 50 cm		peaks in both transmission detectors	Stratified, Bubbly	MRE 0.0496%
Hanus et al. (Hanus	Horizontal pipeline (inner diameter of	PNN	9 feature values of signal analysis	(Gamma ray) Slug, Plug, Plug-	Accuracy = 1 for the
et al., 2018)	30 mm)	MLP		Bubble, and Bubble	four classifications unless Single DT
		RBF			(0.992)
		SVM			PNN chosen as the best
		Single DT	-		
		K-means			
Giannetti et al.	Microchannel heat exchangers	ANN	Re, Fr, Ca, β	(Prigogine's Theorem	RMSE 4.3%
(Giannetti et al., 2020)				(Onsager, 1931; Prigogine and Van Rysselberghe, 1963)) Take-off ratio	<i>R</i> <sup>2</sup> 98.02%
Godfrey Nnabuife et al. (Godfrey et al., 2021)	S-shaped pipeline	Deep NN	Vectors that contain all the information	(CWDU) Annular, Churn, Slug, and Bubbly	Predict accuracy 99.01%
Khan et al. (Khan	Horizontal pipe with 5 cm inner	CNN (ResNet	Scalograms convered	(Pressure signals) Stratified	ResNet50 85.7%
et al., 2022)	diameter	and ShuffleNet)	from pressure detectors	flow, Slug flow, Annular flow	ShuffleNet 82.9%

some data are procured from Computational Fluid Dynamics (CFD). Amalfi and Kim (Amalfi and Kim, 2021) introduced the randomized decision trees to predict the Nu. The consolidated experimental database was collected from Amalfi *et al.* (Amalfi et al., 2016a). The results showed that it could significantly improve the prediction of the thermal performance of two-phase cooling systems compared to the study of Amalfi et al. (Amalfi et al.,

2016b), which used physics-based modeling methods. Differently, Ma *et al.* (Ma et al., 2022) constructed a GBT tree model based on the output of CFD simulations of microchannel refrigerant flow to predict the Nusselt number and the pumping power (*WPP*). This study demonstrates that the most influential parameters are *A*, *N*, and  $\alpha$ , while Nu shows an insensitivity to the Reynolds number of the inlet flow.

### 3.2.2 Modeling of pressure drops

Pressure drop or pressure differential refers to the decrease in pressure that a fluid experiences as it flows through a conduit, valve, bend, heat exchanger, or other equipment. This decrease in pressure is due to factors such as frictional resistance, local resistance, or thermal effects (Ardhapurkar and Atrey, 2015). It is imperative to minimize the pressure drop across a heat exchanger (HX) because a reduced pressure drop directly translates to decreased pumping power and a subsequent reduction in the energy input required for the system in which the HX operates. This section summarizes and categorizes historical literature related to the prediction of pressure drop. The categorization is primarily based on the type of machine learning method used, including predictions based on neural networks, random forest algorithms, predictions support vector regression, and other methods. Additionally, some studies specifically focus on predicting frictional pressure drop.

In literature, ANN can be considered one of the most common machine learning models used for pressure drop prediction. Montanez-Barrera et al. (Montañez-Barrera et al., 2022) and Qiu et al. (Qiu et al., 2021) employed ANN or Correlated-informed neural networks to predict pressure drops. In addition, Qiu et al. (Qiu et al., 2021) also explored other techniques, including XGBoost and GBM. Subbappa et al. (Subbappa et al., 2022) employed three different methods, Ridge Regression (RR), Support Vector Regression (SVR), and ANN. In this work, it is reported that the radiator, condenser, and evaporator baseline models are developed with a different database. The inputs involve the refrigerant properties, the number of tubes per bank, the number of tubes per bank per circuit (i.e., circuitry), the tube banks, the tube length, the number of fins per inch, the air velocity, the refrigerant temperature, and the refrigerant mass flux. It is concluded that ANN and SVR can avoid the expensive simulations with a reasonable error of  $\pm 20\%$  for the testing data used in the study. However, the validation of this study needs to be verified using highfidelity models, which refer to models that are highly accurate and detailed. It closely represents or mirrors the real-world system or situation that is being modeled. High-fidelity models aim to capture the intricacies and complexity of the actual system to the maximum extent possible (Jagielski et al., 2020). The machine learning models that have been trained substantially expedite the investigation of the design space, leading to a considerable reduction in engineering time required to reach designs that are nearly optimal.

Despite the highlighted prominence of ANN in the realm of machine learning models, various other computational approaches are also employed as evidenced in the literature. Ardam et al. (Ardam et al., 2021) developed the prediction of pressure drop based on the Random Forest algorithm in microfinned tubes with evaporating R134a flow. It employed five features (X, f qo, n, Bo, e/Dint) selected among 19 features, which showed the highest prediction accuracy through parametric optimization. The results showed that the proposed methodology is better than the physical model used to respresent the same data (Shannak, 2008). In addition, Zendehboudi and Li (Zendehboudi and Li, 2017) predicted  $\Delta P$  and the frictional pressure drop in inclined smooth tubes based on different models, such as PSO-ANN, GA-LSSVM, Hybrid-ANFIS, and GA-PLCIS. The two databases are collected from the experimental study of Adelaja et al. (Adelaja et al., 2017).

In the context of pressure drop predictions discussed thus far, it is of considerable importance to recognize the frictional pressure drop as a major component contributing to the overall pressure losses. Some studies have focused on investigating the frictional pressure drop in heat exchangers, such as Najafi et al., (Najafi et al., 2021), Xie et al. (Xie et al., 2022), Skrypnik et al. (Skrypnik et al., 2022), Peng and Ling et al. (Peng and Xiang, 2015) and Du et al. (X. Du et al., 2020), introduced the estimation model of the friction factor using different machine learning methods. Najafi et al. (Najafi et al., 2021) demonstrated that data-driven estimation of frictional pressure drop provides greater prediction accuracy compared to theoretical physical models (Chisholm, 1967) for two-phase adiabatic air-water flow in micro-finned tubes using the Random Forest model. Their research focused on five dimensionless features  $(xv, Re, (1 - x)/x, Re_f, Re_{go})$  selected from 23 features which are slightly different features compared to selection of Ardam et al. (Ardam et al., 2021). Their research estimates the two-phase gas multiplier in two-phase adiabatic air-water flow in micro-finned tubes based on Random Forest model.

#### 3.2.3 Modeling of heat exchanger performance

The overall performance of a heat exchanger is typically measured by the overall heating or cooling heat transfer rate capacity, which will be dependent on the dimensions of the heat exchanger, or heat exchanger effectiveness or efficiency, which are dimension-independent. Various research studies have applied different machine learning methods to distinct aspects of heat exchanger performance prediction. Both the work of Li et al. (Li et al., 2016) and Shojaeefard et al. (Shojaeefard et al., 2017) focused on the prediction of cooling capacity in heat exchangers. While Li et al. employed a Response Surface Methodology (RSM)-based Neural Network (NN) model, Shojaeefard et al. evaluated different Artificial Neural Network (ANN) structures in their model. On the other hand, Krishnayatra et al. (Krishnayatra et al., 2020) and Roy and Majumder (Roy and Majumder, 2019) investigate the prediction of performance parameters in shell and tube heat exchangers, including exergetic plant efficiency, energetic cycle efficiency, electric power, fouling factor, and cost, utilizing the FFBN algorithm with tube configurations, fluid type, surface area, temperatures as input parameters. Furthermore, and Muthukrishnan et al. (Muthukrishnan et al., 2020) developed a Support Vector Machine (SVM) in shell and tube heat exchangers to predict the heat transfer rate, with results showing the superior prediction accuracy of SVM over mathematical models. The consolidated database is from the experiments conducted by Wang et al. (Wang et al., 2006). The main differences between these studies lie in the focus of the research (such as cooling capacity, efficiency, heat transfer rate, etc.), the prediction model used (such as RSM-based NN, ANN, FFBN, SVM, etc.), and the type of heat exchanger studied.

Turning our attention to predicting coefficient of performance of heat exchanger systems, it is also clear that this segment has been at the forefront of integrating innovative machine learning approaches in research. Bhattacharya et al. (Bhattacharya et al., 2022) developed and validated a model that combines Convolutional Neural Networks (CNN) with Gated Recurrent Units in a State Space Model framework. Their work aimed to predict the intricate dynamics of heat exchangers observed in vapor

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compression cycles in heat exchanger. The model processed inputs like  $\dot{m}_{a_{in}}$ ,  $P_{atm}$ ,  $T_{in}$ ,  $RH_{in}$ ,  $\dot{m}_{ref_{in}}$ ,  $h_{in}$ ,  $P_{out}$ ,  $h_{out}$  and produced predictions for  $p_{inlet}$ ,  $p_{outlet}$ ,  $h_{inlet}$ ,  $h_{outlet}$ ,  $Q_{total}$ ,  $\dot{m}_{total}$ . Their research demonstrated remarkable accuracy, with the maximum percentage error being limited to 0.2%. In addition, Chen et al., (Chen et al., 2023) constructed two-year field tests based on an energy pile heat pump system, where in situ results were used as sample points, and the measured ambient temperature and humidity, room temperature and humidity, and hourly power consumption were used as input parameters to predicted coefficient of performance. The results showed that the accuracy was higher than that of the empirical regression models. Moreover, Zhu et al. (Zhu et al., 2021a) investigated the boiling and condensation heat transfer of R134a refrigerant within microchannels under various conditions. Data collected from these experiments were utilized to train machine learning-based artificial neural network models for predicting heat transfer performance. The models effectively forecasted the heat transfer coefficients for both boiling and condensation processes. Further, Li et al. (Li et al., 2023) employed four machine learning methods to anticipate the thermal performance of supercritical methane flow in a Printed Circuit Heat Exchanger. The ANN proved to be highly precise in forecasting the local heat transfer coefficient and unit pressure drop following hyperparameter optimization.

#### 3.2.4 Conclusion of heat exchangers modeling

Upon the review of the recent studies using machine learning to predict various performance indicators for different types of heat exchangers, several key themes and opportunities for enhancement emerge. Regarding the interaction of various factors within the models, it is critical to understand that the reliability and precision of machine learning predictions depend on a comprehensive understanding of the interactions between model parameters. In many of the reviewed studies, parameters such as the Reynolds number, Weber number, and the Froude number were utilized, yet the dynamic interactions between these parameters were not explicitly elucidated. For example, the interplay between Reynolds number and Froude number could potentially influence the prediction of pumping power significantly. A deeper investigation into these correlations could lead to more refined and precise predictions and ultimately, more effective heat exchanger designs. Employing methods such as feature importance analysis or sensitivity analysis could provide more tangible insights into these interactions.

When scrutinizing the model's training and validation procedures, it becomes imperative to thoroughly outline each stage of the process. Regrettably, the comprehensive explanation of this process, encompassing critical aspects such as the selection of training and validation datasets, hyperparameter tuning, and overfitting prevention, is commonly absent in the studies reviewed. This lack of essential information hampers both reproducibility and potential model enhancement. Therefore, advancing in this field is reliant on a more transparent and detailed presentation of these steps.

On this basis, the role of data transparency and reproducibility cannot be overstated in ensuring the credibility and utility of these models. Some studies, however, fall short by failing to explicitly state their data sources or by not providing clear definitions of model parameters. These omissions could obstruct other researchers' understanding and reproduction of the models. Hence, by improving data openness and providing a more transparent presentation of model parameters, the field could experience significant advancements, facilitating replication and model improvement.

Lastly, when we turn our attention to the exploration of emerging techniques, it is clear that traditional machine learning methods such as Artificial Neural Networks (ANN), Gradient Boosting Machines (GBM), and Ridge Regression have been well documented. However, a noticeable gap exists in the exploration and application of more recent machine learning methodologies. Techniques like deep learning and reinforcement learning, which have shown promise in various other disciplines, could potentially enhance predictive capabilities and robustness in heat exchanger performance prediction. This untapped potential area is, thus, deserving of further, in-depth investigation.

### 3.3 Fouling factor

The fouling factor is an index that measures the unit thermal resistance of solid sediments deposited on heat exchange surfaces and reduces the overall heat transfer coefficient of the heat exchanger (Müller-Steinhagen, 1999). Fouling deposits that clog the channels of compact heat exchangers will increase pressure drops and reduce flow rates, resulting into poor heat transfer and fluid flow performance (Asadi et al., 2013). Table 7 lists the details of the literature dealing with fouling factors of heat exchangers. A summary of these investigations is discussed in this subsection. For predicting the fouling factor, Hosseini et al. (Hosseini et al., 2022) estimated the fouling factor through four machine learning methods: Gaussian Process Regression (GPR), Decision Trees (DT), Bagged Trees, and Support Vector Regression (SVR). The database was collected from experiments, and the model inputs were the operation time, the surface temperature, the fluid velocity, the fluid density, the fluid temperature, and the equivalent diameter, selected based on Pearson's correlation analysis. Mohanty (Mohanty, 2017) estimated the temperature difference on the tube and shell sides of a shell-and-tube heat exchanger, as well as the heat exchanger efficiency as the outputs of a fouling factor-based ANN with network structure 6-5-4-2.

For estimating the fouling factor, Kuzucanlı et al. (Kuzucanlı et al., 2022) predicted the behavior of the overall heat transfer coefficient and of the in plate heat exchangers. It is noteworthy that this work introduced the classification solution. The dataset was collected from the experiment with variable flow rates and inlet temperatures as input parameters. In a similar work, Sundar *et al.* (Sundar et al., 2020) predicted the fouling factor based on deep learning. A total of 15,600 samples were collected in a database, using the inlet fluid temperatures, the ratio of fouled fluid flow rates to flow rates under clean circumstances, and the outlet temperatures (gas and fluid) as inputs.

Machine learning methods have proven effective in modeling and predicting the fouling factor in heat exchangers, a measure that significantly impacts thermal performance. Techniques such as Gaussian Process Regression, Decision Trees, Bagged Trees, and Support Vector Regression have been used, leveraging operational parameters like operation time, surface temperature, fluid velocity, and more. These methods have shown acceptable prediction accuracy, demonstrating machine learning's effectiveness in this field. Additionally, machine learning has been effective in predicting fouling's impact on other parameters, like temperature difference and heat exchanger efficiency. While existing algorithms have been primarily used, there's potential for new machine learning algorithms to further improve fouling factor prediction.

### 3.4 Refrigerant thermodynamic properties

The conventional prediction of the refrigerant thermodynamic properties is usually carried out by means of empirical, theoretical, and numerical models. Although these methods have been successfully applied in many cases, their numerical modeling still suffers from computational issues in dealing with the complex molecular structure of refrigerants (Meghdadi Isfahani et al., 2017; Alizadeh et al., 2021a). Table 8 lists several machine learning prediction models of the thermodynamic properties of refrigerants available in the literature, which are briefly described in this subsection.

In literature, neural network models have been widely employed by many researchers for the prediction of refrigerant properties. For example, Gao et al. (Gao et al., 2019), Wang et al. (Wang et al., 2020), Zolfaghari and Yousefi (Zolfaghari and Yousefi, 2017), Nabipour (Nabipour, 2018) employed ANN to predict the thermodynamic properties, such as,  $P_{red}$ ,  $1 - T_r$ ,  $\omega$ , Pc/Pcr, etc. They employed different parameters to investigate the prediction performance, for instance, Wang et al. (Wang et al., 2020) introduced ANNs to estimate the viscosity and the thermal conductivity, using the reduced pressure  $(P_{red})$ , the reduced temperature  $(T_r)$ , the molar mass (M), and the acentric factor ( $\omega$ ) as inputs. Similarly, Zolfaghari and Yousefi (Zolfaghari and Yousefi, 2017) developed an ANN to predict the density of sixteen lubricant/refrigerant mixtures, considering a total of 3,961 data points from the literature. In this study, the temperature (T), the pressure (P), the molar fraction (x), the total molecular weight  $(M_w)$ , and the average boiling temperature  $(T_b)$  of pure refrigerants were considered as input parameters.

Shifting away from the singular prediction model approach, numerous studies have adopted a more extensive analysis by examining multiple prediction models. Several studies have embraced a more comprehensive analysis by investigating more than one prediction model; for example, Zhi *et al.* (Zhi *et al.*, 2018) developed three prediction models of viscosity based on ANFIS, RBFNN, and BPNN for six pure refrigerants, specifically R1234ze(E), R1234yf, R32, R152a, R161, and R245fa in the saturated liquid state. It is reported that a total of 1,089 data points were collected from the literature, of which 80% were allocated to training and 20% to testing, while the algorithm inputs were temperature, pressure, and liquid density. Results demonstrate that the ANFIS algorithm shows the highest prediction accuracy.

Upon reviewing the impressive statistics presented in Table 8, it is evident that machine learning has proven to be an invaluable tool for predicting the thermodynamic properties of refrigerants. A common thread across the studies indicates that factors such as temperature, pressure, and density often serve as inputs for these predictive models. However, we observe variations in the algorithms used and the specific properties predicted. This could be attributed to the unique characteristics of the refrigerants studied and the specific objectives of each study. While these models demonstrate impressive prediction accuracy, it is crucial to acknowledge that model performance varies depending on the refrigerant and property in question. A broader observation reveals a notable trend toward using machine learning in refrigerant property prediction, which presents opportunities for further exploration. Future work could include comprehensive comparative studies of these different machine learning algorithms, considering their strengths and weaknesses in various scenarios. There is also potential for integrating these machine learning models with other computational tools for more robust and accurate predictions. Furthermore, as the field continues to evolve, there may be scope to explore new machine-learning techniques and develop novel approaches for predicting the thermodynamic properties of refrigerants.

## 3.5 Flow patterns

Two-phase flow is critical in many chemical processes, heat transfer, and energy conversion technologies. The flow pattern in two-phase flow has a critical role in heat transfer coefficient and pressure drop, because the physics governing the pressure drop and the heat transfer is intrinsically linked to the local distribution of the liquid and vapor phases (Cheng et al., 2008). Recently, the prediction of flow patterns based on machine learning has received growing attention. Table 9 summarizes the studies about flow pattern recognition based on machine learning reported in the present work. Identifying flow patterns is crucial in fluid mechanics, employing various methods. High-speed cameras offer direct visual insight but are limited to transparent media. Gamma rays can analyze opaque fluids but raise safety concerns. Pressure sensors can infer flow patterns from pressure changes, albeit with interpretational challenges. The Continuous Wave Doppler technique measures particle velocities using frequency shifts but requires particles or bubbles for measurement. The appropriate method hinges on factors like flow type, fluid transparency, piping material, safety, and the depth of analysis required.

Some studies identified the flow regimes using the high-speed cameras, Shen et al. (Shen et al., 2020) Ahmad *et al.* (Ahmad et al., 2022), Giri Nandagopal et al. (Giri Nandagopal and Selvaraju, 2016) and Giri Nandagopal et al. (Nandagopal et al., 2017) investigate the flow pattern recognition through high-speed cameras. For instance, Giri Nandagopal et al. (Nandagopal et al., 2017) investigated the same liquid-liquid system in a circular microchannels of 600  $\mu$ m diameter as the confluence angle of the two fluids was varied in the range 10–170 degrees, in order to predict the flow pattern maps using the confluence angle and the superficial velocities of the two liquids as input. The algorithms considered could identify slug flow, bubble flow, deformed flow, elongated slug flow, deformed flow, and stratified flow. The results showed that GRNN gives the best prediction accuracy again.

Instead of using a high-speed camera to record the flow regimes included in the datasets, some studies used gamma rays to construct the database. For example, Roshani *et al.* (Roshani *et al.*, 2017) identified the flow regimes by means of the multi-beam gamma ray attenuation technique. In this study, the outputs of two detectors are introduced as input parameters into the RBF models in order to predict the flow regimes. Similarly, Hanus *et al.* (Hanus *et al.*, 2018) used the gamma-ray attenuation technology to identify flow regimes and generate input data for the algorithm. In particular, nine features obtained from the signal analysis were selected as inputs and applied to six different machine-learning methods. The results showed a promising accuracy for all the methods considered.

In contrast to those described above, some studies employed other methods, such as pressure sensors, ultrasound, and a new concept (take-off ratio). For example, Godfrey Nnabuife et al. (Godfrey et al., 2021) used Deep Neural Networks (DNNs) operating on features extracted from Continuous Wave Doppler Ultrasound (CWDU) to recognize the flow regimes of an unknown gas-liquid flow in an S-shaped riser. A Twinwindow Feature Extraction algorithm generates the vectors that contain all the information used as input of the Deep NN, reducing the amount of input data and eliminating the noise. The identified flow regimes are annular, churn, slug, and bubbly flow. The results show the highest prediction accuracy, which is better in comparison with that of four conventional machine learning methods: AdaBoost, Bagging, Extra Trees, and DT. Khan et al. (Khan et al., 2022) developed CNN to identify the flow regimes in air-water flow in a horizontal pipe with a 5 cm inner diameter, using the scalograms obtained from pressure detectors as input database. Differently from the described above, Giannetti et al. (Giannetti et al., 2020) introduced the concept of take-off ratio to develop an ANN to predict the two-phase flow distribution in microchannel heat exchangers based on a limited amount of input information. The concept of take-off ratio is based on Prigogine's theorem of minimum entropy generation (Onsager, 1931; Prigogine and Van Rysselberghe, 1963). As a result, the 4-3-3-3-1 architecture achieves the highest prediction accuracy reported.

Machine learning has increasingly been applied to predict and understand flow patterns in two-phase flow systems, a topic of substantial significance across various fields, from chemical processes to energy conversion technologies. The range and diversity of research in this domain underline the complex interplay between the physical parameters governing the pressure drop and heat transfer, which are intricately related to the local distribution of liquid and vapor phases. Key to this research is the use of machine learning to identify and distinguish different flow patterns accurately. This has been addressed using diverse techniques, such as CNNs, DL, and various types of ANNs, including the PNN, GRNN, and ANFIS. These methods have demonstrated high degrees of prediction accuracy in their respective applications, offering promising advancements in the field. The generation of input data for these machine learning models has employed an array of innovative methodologies, such as high-speed camera image capturing and the use of the multi-beam gamma ray attenuation technique. Some studies have further expanded upon this by introducing novel concepts, such as the take-off ratio, which applies Prigogine's theorem of minimum entropy generation to predict two-phase flow distribution. Other research has veered towards the use of Deep Neural Networks (DNNs) to identify flow regimes based on Continuous Wave Doppler Ultrasound (CWDU) information, exhibiting high prediction accuracy rates. This move toward the use of DNNs and similar methods demonstrates the field's continuous evolution and the trend toward more sophisticated, precise prediction models.

# 3.6 Structured approach to model selection in machine learning: A guide

The selection and evaluation of machine learning algorithms necessitates a comprehensive and multi-faceted approach, involving numerous interdependent steps and considerations. This section delineates a systematic methodology devised to aid practitioners in judiciously selecting the pertinent machine learning algorithm tailored for a specific problem domain.

- 1. Problem Definition: The preliminary step involves a comprehensive understanding of the problem landscape. This encompasses identifying the nature of the problem—be it a classification, regression, clustering, or another variant.
- 2. Exploratory Data Analysis: Exploratory Data Analysis is the initial phase of understanding data, aiming to summarize its main characteristics, often visually. This phase includes assessing feature distributions through histograms or boxplots to spot understanding data sparsity skewness, with matrix visualizations, detecting outliers via scatter plots or Interquartile Range methods, and discerning missing value patterns with heatmaps or bar charts. Correlation matrices and pair plots can reveal relationships between variables. Dimensionality reduction techniques, such as Principal Component Analysis or t-distributed Stochastic Neighbor Embedding, provide a compressed visual perspective on multidimensional data.
- 3. Data Pre-processing: Based on Exploratory Data Analysis findings, data pre-processing refines the dataset for modeling. Feature engineering may involve creating polynomial features, encoding categorical variables, or extracting time-based metrics. Outliers could be capped, transformed, or removed entirely. Standard practices also include scaling features using methods like Minimum-Maximum or z-score normalization. Categorical data often require encoding techniques such as one-hot or ordinal. Finally, data may be split into training, validation, and test sets to evaluate the model's performance effectively.
- 4. Evaluation Metric Selection: The choice of an evaluation metric should align closely with both the problem definition and organizational objectives. For instance, in classification problems, metrics like accuracy, MAE, MRE, etc. may be considered.
- 5. Comparative Model Assessment: Employing techniques like cross-validation, the performance of multiple candidate algorithms should be rigorously compared to ascertain the most effective model based on the validation dataset.

- 6. Hyperparameter Optimization: Subsequent to model selection, hyperparameter tuning is conducted to further refine the performance of the selected models.
- 7. Validation and Testing: Final performance evaluation is conducted using an independent test set to ascertain the generalizability of the model and to mitigate the risk of overfitting.

## 4 Limitations and potential solutions

Despite the remarkable potential and superior performance of machine learning techniques compared to traditional computational methods, their unique features, such as a tendency towards overfitting and interpretability can present hurdles in their application within heat exchanger systems. The ensuing discussion will delve into the primary issues in deploying machine learning strategies in the process of modeling heat exchangers, alongside exploring possible solutions.

## 4.1 Overfitting

Like most probabilistic models, the issues of overfitting and under-fitting are unavoidable in machine learning models (Dobbelaere et al., 2021). Overfitting refers to the prediction accuracy being extremely high in the training dataset, while the performance on the testing dataset is unsatisfactory (Dietterich, 1995). There are multiple potential explanations of the phenomenon, such as noise over-learning on the training set (Paris et al., 2003), hypothesis complexity (Paris et al., 2003), and multiple comparison procedures (Jensen and Cohen, 2000).

In order to mitigate overfitting problems, it is recommended to introduce the following strategies: a) Early stopping (Jabbar and Khan, 2015), which requires defining the criteria of stopping functions, for instance, monitoring the performance of the model on a validation set during the training process. The training is stopped when the error on the validation set starts to increase, which is a sign of overfitting. The validation set is a small portion of the training data set aside to check the model's performance during training. b) Network structure optimization (Dietterich, 1995), which involves tuning the architecture of the neural network to find the most efficient structure. For example, one could experiment with different numbers of layers or different numbers of neurons per layer. Additionally, pruning methods can be used to reduce the complexity of decision trees or neural networks by eliminating unnecessary nodes. c) Regularization (Jabbar and Khan, 2015), similar to penalty methods, is used to reduce the influence of noise. This term discourages the model from assigning too much importance to any one feature, reducing the risk of overfitting. In conclusion, while several studies in Tables 1-8 have incorporated the early stopping and network structure optimization techniques, it is unclear if they significantly reduced overfitting. Further evaluation of these methods' effectiveness in the studies mentioned might offer more insights. Regularization, however, seems to be less frequently employed, based on our review.

## 4.2 Interpretability

Machine learning methods are essentially black box models, where data analysis can be understood as a pattern recognition process (Dobbelaere et al., 2021). According to Vellido (Vellido et al., 2012), interpretability refers to the ability to assess and explain the reasoning behind machine learning model decisions, which is one of the most significant qualities machine learning methods should achieve in practice. Model hyperparameters, such as node optimization in artificial neural networks, are key elements in constructing an effective model. The selection and tuning of these hyperparameters typically have a significant impact on the performance of the model. However, for these types of models, the analysis usually focuses on prediction accuracy rather than the interpretability of the model (Feurer and Hutter, 2019). To implement interpretability, dimensionality reduction can be introduced for supervised and unsupervised (Azencott, 2018) problems through feature selection and feature extraction (Dy et al., 2000; Guyon and Elisseeff, 2003; Guyon et al., 2008). In addition, Vellido (Alcacena et al., 2011) stated that information visualization is a feasible solution to interpret the machine learning models such as Partial Dependency Plots (PDP) (Greenwell, 2017) and Shapley Additive explanation (SHAP) (Mangalathu et al., 2020). It is important to build models that can self-learn to recognize patterns and self-evaluate.

In the latest study, Xie et al. (Xie et al., 2022) introduced a mechanistic data-driven approach called dimensionless learning. It identifies key dimensionless figures and governing principles from limited data sets. This physics-based method simplifies highdimensional spaces into forms with a few interpretable parameters, streamlining complex system design and optimization. It also states that the processes could find very useful application in heat exchanger modeling and heat exchanger experimental data characterization. This method unveils scientific knowledge from data through two processes. The first process embeds the principle of dimensionless invariance (i.e., physical laws being independent of the fundamental units of measurement) into a two-tier machine learning framework. It discovers the dominating dimensionless numbers and scaling laws from noisy experimental data of complex physical systems. The subjects of investigation include Rayleigh-Bénard convection, vapor-compression dynamics in the process of laser melting metals, and pore formation in 3D printing. The second process combines dimensionless learning with a sparsity-promoting technique to identify dimensionless homogeneous differential equations and dimensionless numbers from data. This method can enhance the physical interpretability of machine learning models.

## 4.3 Data quality and quantity

The prediction of parameters based on machine learning can provide a reference for scientific research and practical applications to both researchers and engineers However, it is worth mentioning that dealing with a database containing too many outsider data points can generate system errors. Compared with an extensive database, machine learning is more sensitive to a small database, which can influence machine learning models (Pourkiaei et al., 2016).

It is possible to increase the number of data points (Dietterich, 1995), delete the outsider data points, and use algorithms for anomaly detection, such as the principal component analysis (PCA) algorithm (Thombre et al., 2020) and LSTM (Zhang et al., 2019). In addition, it is also possible to carefully examine the data for stable, reliable, and repeatable data (Zhou et al., 2020). Although decades of modeling, simulations, and experiments have produced several datasets about heat exchangers, they are often archived in research laboratories or companies and are not open access.

Lindqvist et al. (Lindqvist et al., 2018) introduced the employment of structured and adaptive sampling methodologies. Structured sampling techniques, such as Latin Hypercube Sampling, systematically distribute sample points throughout the design space, thereby providing a robust approach to experimental design. Conversely, adaptive sampling dynamically modifies the location of sample points contingent on the predictive outcomes of the model, thereby optimizing model performance.

### 4.4 Model generalization

Model generalization refers to the ability of a machine learning model to adapt properly to new, unseen data drawn from the same distribution as the one used to train the model (Bishop and Nasrabadi, 2006). It is a critical aspect of machine learning models, particularly in complex fields such as fluid dynamics and heat transfer, where phenomena can be influenced by a multitude of factors. A model's generalization capability determines its utility and applicability in real-world scenarios beyond the confines of the training data. However, achieving good generalization is a significant challenge and often requires careful model design and validation strategies. When applying machine learning methods outside the scope of the database, outputs will be unreasonable. A limited training dataset determines the scope of the application.

When assessing unknown data points via a predictive model, users must ensure that these data points lie within the model's operational domain. "Unknown data points" typically represent data not previously encountered during the model's training process. As they are excluded from the training dataset, the model extrapolates its learned patterns to generate predictions for these data points. These unknown data points are instrumental in evaluating the model's generalization capabilities. However, should these data points fall outside the model's operational domain, the reliability of the resultant predictions could be undermined. To maintain the trustworthiness of computations under such circumstances, it is recommended to either augment the training database to encompass a broader data spectrum or cross-validate the predicted values employing alternative credible methodologies (Azencott, 2018).

## 5 Emerging applications

Here, the emerging heat exchanger applications involving machine learning will be discussed, including the novel nanofluid mixture modeling, heat exchanger design, and topology optimization.

## 5.1 Nanofluid

Nanofluids are widely used in solar collectors, heat exchangers, heat pipes, and other energy systems (Ramezanizadeh et al., 2019). The presence of nanoparticles within the fluid can enhance the thermophysical properties of the fluid to benefit the heat transfer behavior within the system. Currently, several machine learning models have been introduced to predict the thermodynamic properties of hybrid nanofluids (Maleki et al., 2021). According to the Web of Science database, about 3% of nanofluid research papers published in 2019 involved machine learning, with an increasing trend (T. Ma et al., 2021).

In the literature, several machine-learning models have been applied to heat exchangers containing nanofluids (Naphon et al., 2019; Ahmadi et al., 2020; Gholizadeh et al., 2020; Hojjat, 2020; Kumar and Rajappa, 2020; Alimoradi et al., 2022). Nanofluids involve complex physical, chemical, and fluid dynamic phenomena, and traditional modeling and analysis methods may face challenges. However, machine learning, as a data-driven approach, can help address the complex problems in nanofluid research by learning and discovering patterns and correlations in the data (Ma et al., 2021). For instance, Cao et al. (Cao et al., 2022) employed machine learning to simulate the electrical performance of photovoltaic/thermal (PV/T) systems cooled by water-based nanofluids. Alizadeh et al. (Alizadeh et al., 2021a) proposed a novel machine learning approach for predicting transport behaviors in multiphysics systems, including heat transfer in a hybrid nanofluid flow in porous media. Another study by Alizadeh et al. (Alizadeh et al., 2021b) used an artificial neural network for predictive analysis of heat convection and entropy generation in a hybrid nanofluid flowing around a cylinder embedded in porous media. Machine learning also can assist in analyzing large amounts of experimental data to extract useful information and trends, accelerating research progress. For example, machine learning algorithms can be used to predict and optimize the surface properties, dispersibility, and flow behavior of nanoparticles (El-Amin et al., 2023). Moreover, machine learning can be used for simulating and optimizing the design and performance of the system containing nanofluid providing more efficient solutions (T. Ma et al., 2021).

At the nanoscale, the conventional principles of fluid mechanics and heat transfer may not hold true, thus necessitating innovative theories to decode the behavior of nanofluids. While machine learning could reveal unseen patterns and correlations within data, it does not guarantee the applicability of these trends under nanoscale constraints. Nanofluidic research, given its complex nature, requires experimental verification for the predictions formulated by machine learning models. However, this verification process often demands sophisticated instrumentation, advanced methodologies, and considerable financial resources, which may pose significant challenges and potentially exceed the capabilities of numerous research groups. Nanofluid systems are marked by a high degree of complexity due to the interaction among various components such as fluids, nanoparticles, and interfaces,



thereby rendering the prediction process through machine learning models extremely challenging. Moreover, nanofluid research is dataintensive, and procuring the requisite amount of data can often be problematic.

# 5.2 Heat exchangers design and optimization

Machine learning algorithms can analyze large amounts of data, identify patterns, and make predictions or decisions without being explicitly programmed to perform the task. This ability to learn from data makes machine learning particularly useful in optimization problems, where the goal is to find the best solution among a set of possible solutions. It indicates that it can be a powerful tool for dealing with various engineering issues. It is reported that machine learning can potentially optimize the topology structure of heat exchangers. According to Fawaz (Fawaz et al., 2022), machine learning algorithms can be combined with a density-based topology algorithm, which is mainly aimed at structural design at the present stage (Sosnovik and Oseledets, 2019; Abueidda et al., 2020; Chandrasekhar and Suresh, 2021; Chi et al., 2021). Moreover, few studies are coupled with ML and Topology (TO) for HXs, which may be related to the complexity of coupled heat transfer (particularly the fluid flow part) and the complexity of HXs structure (Fawaz et al., 2022). Michalski (Michalski and Kaufman, 2006) introduced the Learnable Evolution Model (LEM), containing the hypothesis generation and instantiation to create new designs based on machine learning methods, which can automatically search for the highest capacity heat exchangers under given technical and environmental constraints. LEM has a wide range of potential applications, especially in complex domains, optimization, or search problems (Michalski, 2000). The results of the methods have been highly promising, producing solutions exceeding the performance of the best human designs (Michalski and Kaufman, 2006).

Although machine learning holds significant promise for the design and optimization of heat exchangers, however, it is crucial to acknowledge that the application of these techniques in this field is still in its infancy. The intricate physical phenomena and interactions involved in heat exchanger systems present a significant challenge for machine learning models. Despite the potential, there are substantial hurdles to overcome. Future work in this field should concentrate on enhancing the interpretability of machine learning models, as previously mentioned. Additionally, efforts should be made to develop methods for generating novel design concepts and to create high-quality datasets for training these models. By addressing these challenges, we can better harness the power of machine learning in the design and optimization of heat exchangers.

## 6 Conclusion

This paper provides a comprehensive review of heat exchanger modeling based on machine learning methods, drawing on literature published over the past 8 years. The review evidences a clear expansion of this field, with a significant publication growth rate observed after 2018. As shown in Figure 4, neural networks have been widely implemented, accounting for about 56% of the literature. This is attributed to their high prediction accuracy and powerful parallel and distributed processing capabilities. The paper systematically explores the entire gamut of heat exchanger modeling based on machine learning methods, focusing on types of algorithms, input parameters, output parameters, and error analysis. These insights can guide researchers in selecting appropriate machine learning models for various heat exchangers, predicting fouling factors, and thermodynamic properties of refrigerants, tailored to their specific objectives.

Despite the promising performance of machine learning methods under the right database conditions, several limitations exist, including data overfitting, anomaly processing, limited scope, and low interpretability. Accordingly, feasible schemes have been introduced to mitigate these limitations. The paper also emphasizes the potential of Dimensionless Learning as discussed in Section 3. Specifically, incorporating the interplay between dimensionless numbers such as Re, We, and Fr numbers could provide a more generalizable and physically intuitive understanding of heat exchanger performance and fluid flow behavior. Furthermore, an area that is conspicuously underrepresented in the current literature is the modeling of surface roughness using machine learning methods, presenting a clear opportunity for future research.

Finally, two emerging areas, nanofluids in new energy applications and heat exchanger design optimization, are also discussed. The data-driven approach to machine learning offers new possibilities for thermal analysis of fluids, cycles, and heat exchangers with faster calculation and higher prediction accuracy. The information provided in this paper will greatly benefit researchers who aim to utilize machine learning methods in the field of heat exchangers and thermo-fluid systems in general.

## Author contributions

JZ: Writing-original draft, Writing-review and editing, Investigation, Project administration. TH: Writing-review and editing, Methodology. JA: Writing-review and editing, Visualization. LH: Writing-review and editing, Conceptualization, Funding acquisition, Methodology, Project administration, Supervision. JC: Writing-review and editing, Conceptualization, Methodology, Supervision.

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## Nomenclature

Nomenclature		f	Friction factor (by Haaland) (Hall, 2012)
ANFIS	Adaptive Neuro Fuzzy Interface System	fo	Isothermal friction factor in forced convection
ANN	Artificial Neural Network	FIT	Feed inlet temperature
ANN – FF	ANN-Function Fitting	Fr	Froude number
ANN – PR	ANN-Pattern Recognition	fvp	Friction factor, Parlatan et al.'s friction factor
CFN	Cascade Forward Network	g	Gravity acceleration
CoINN	Correlated-Informed Neural Networks	G	Mass flux
DT	Decision Tree	Ga	Galileo number, $Ga = \frac{\rho_f g(\rho_f - \rho_g)D^3h}{\mu_f^2}$
FEM	Finite Element Method	Gr	Grashof number
FFBN	Feed Forward Back Propagation Network	h	Enthalpy
FFNN	Feed-Forward Neural Network	Н	Heat of vaporization of the fluid
FVM	Finite Volume Method	HTC	Heat transfer coefficient
GA – PLCIS	Genetic Algorithm-power Law Committee with Intelligent Systems	IA	Inclination angle
GA – LSSVM	Genetic Algorithm-least Square Support Vector Machine	j	Colburn factor
GBM	Gradient Boosting Machine	Ja	Jakob number, $\frac{L(T_{sut}-T_{wall})Cp}{h_{lv}}$
GBT	Gradient Boosting Tree	Ka	Kapitza number, $Ka = \frac{\mu_j^k g}{\rho_j \sigma^3}$
GPR	Gaussian Process Regression	L	Length of fin
GRNN	General Regression Neural Network	m	Mass flow rate
HRBF	Hybrid Radial Basis Function	M	Mole molecule mass
KNN	K-Nearest Neighbor	n	Number of fins
PNN	Probabilistic Neural Network	Ν	Number of channels
PSO – ANN	Particle Swam Optimization-Artificial Neural Network	Ntr	Number of tube rows
RBF	Radial Basis Function	Ntp	Number of tube-passes
RF	Random Forest	Nu	Nusselt numbers
RR	Ridge Regression	Nuo	Nusselt number in forced convection
SVM	Support Vector Machine	Р	Pressure
SVR	Support Vector Regression	$\Delta P$	Pressure drop
A	Cross-sectional area	<b>P</b> 1	Pressure at cold inlet
atm	Atmosphere	<b>P</b> 2	Pressure at hot inlet
Bd	Bond number, $Bd = \frac{g(\rho_j - \rho_g)D^2h}{\sigma}$	Рс	Critical pressure
Во	Boiling number, $Bo = \frac{q''}{\Delta HG}$	Pcd	Cold fluid Pressure drop
BPHEs	Brazed Plate Heat Exchangers	Pcr	Critical pressure of the corresponding hydrocarbon to the refrigerant
Ca	Capillary number	Pe	Peclet number
CF	Condensate flow	Phd	Hot fluid Pressure drop
Со	Convection number, $Co = \left(\frac{1-x}{x}\right)^{0.8} \left(\frac{\rho_{\mu}}{\rho_{f}}\right)^{0.5}$	Pr	Prandtl number
CT	Condensate temperature	Prg	Saturated vapor Prandtl number, $Pr_g = \frac{\mu_g C p_g}{k_g}$
D	Diameter of flow channel	<i>q</i>	Data point vector
Dc	Coil diameter	<i>q</i> ″	Heat flux
Dh	Hydraulic diameter of flow channel	Q	Flow rate, liters/min
Dt	Tube diameter	q''H	Heat flux based on heated perimeter of channel
е	Mean fin height	Re	Reynolds number

Res	Superficial Reynolds numbers	evap	Evaporator
Rh	Relative humidity	f	Saturated liquid, fluid
ScL	Liquid-phase Schmidt number	flue	Flue gas
ScV	Vapor-phase Schmidt number	fo	Liquid only
SF	Steam flow	fric	Frictional
Suf	Saturated liquid Suratman number, $Su_f = \frac{\sigma \varphi_f \cdot Dh}{\mu_f^2}$	g	Saturated vapor
Sug	Saturated vapor Suratman number, $Su_f = \frac{\sigma \cdot \rho_a \cdot Dh}{\mu_f^2}$	go	Vapor only
Т	Temperature	hw	Hot water
$T^{\star}$	Dimensionless temperature glide	i	Inlet
T1	Temperature at inlet of cold fluid	in	Inlet
<b>T</b> 2	Temperature at outlet of cold fluid	int	Internal
T3	Temperature at inlet of hot fluid	1	Liquid
<b>T</b> 4	Temperature at outlet of hot fluid	max	Max value
Tr	Reduced temperature	mix	Non-azeotropic mixtures
V	Volume flow rate, m <sup>3</sup> /s	0	Outlet
WPP	Pumping power	r	Reduced
We	Weber number	red	Reduced
x	Average volume quality	ref	Refrigerant
X	Lockhart-Martinelli parameter $X = \frac{m_l}{m_g} \sqrt{\frac{\rho_g}{\rho_l}}$	\$	Saturation
xv	Average volume quality	sp	Single-phase flow
		sup	Vapor super-heating
Greek symbols		sys	System
α	Heat transfer coefficient/aspect ratio $\alpha$ /arc angle	tp	Two-phase flow
β	Inclination angle of the corrugation/attack angle	ν	Vapor
Δ	The differences	w	Water
Φ	Enlargement factor of the corrugation	wb	Wet bulb
Г	Take-off ratio	wo	Water only
μ	Dynamic viscosity	MAE	Mean Absolute Error
η	Thermal enhancement factor	MedAE	Median Absolute Error
θ	Angle	MRE	Mean Relative Error
ρ	Density	RMSE	Root-Mean-Square Error
ω	Acentric factor	$R^2$	Coefficient of Determination
σ	Surface tension		

### Subscripts

а	Air
amb	Ambient
avg	Average
b	Bed
с	Critical
сw	Cold water
db	Dry bulb
eq	Equivalent