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Analysis of low-frequency oscillation characteristics and damping enhancement strategy for grid-forming PV with DC-voltage controller

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Introduction: Grid-forming (GFM) converters with DC-voltage controller can emulate inertia and support frequency stability while maintaining a stable DC voltage, making this method well-suited for PV systems. However, the introduction of the DC voltage control loop exacerbates the issue of low-frequency oscillations in GFM converters. Although existing studies have identified negative resistance behavior through impedance analysis, t the overall impedance characteristics of the unit make it difficult to pinpoint the key sources of internal negative damping, posing challenges for the design of oscillation suppression strategies.

Methods: Building on this, by applying the damping torque method, this paper analyzes the components of damping torque and synchronizing torque in DC-voltage controller based GFM (DC-GFM) converter and the stability conditions of multi-converter systems. This provides a clear explanation of the underlying mechanism behind negative damping and the influence of control parameters.

Result: The analysis reveals that the negative damping originates from the integral parameters in the DC-voltage controller. Based on this insight, a damping enhancement strategy for multi-DC-GFM system is proposed. The simulation results validate the effectiveness of both the parameter analysis and the proposed strategy.

Discussion: Finally, the limitations of this paper and the future research directions are discussed.

KEYWORDS

grid-forming converter, DC-voltage controller, low-frequency oscillation, damping torque method, lead-lag compensator

1 Introduction

With the accelerating transition of power systems, renewable energy sources like photovoltaics (PVs) are making up a larger portion of the generation mix. However, because they are generally grid-connected via phase-locked loop-based grid-following control, the inertia of the system is progressively reduced. Major blackout events in countries such as Australia and the UK have been confirmed to be closely related to

the decline in system inertia caused by the large-scale integration of renewable energy sources (Commission, 2019; ESO, 2019). In contrast, grid-forming (GFM) converters, which autonomously establish voltage and frequency, are capable of providing inertia support and actively regulating the grid, and have received widespread attention from both academia and industry in recent years (Liu et al., 2016; Li M. et al., 2022; Wang et al., 2025; Rahman et al., 2024; Ji et al., 2024).

Currently, the main control strategies for GFM converters include droop control (Guerrero et al., 2011; Tayab et al., 2017), virtual synchronous generator (VSG) control (Zhong and Weiss, 2011; Driesen and Visscher, 2008; Su et al., 2025), virtual oscillator control (Johnson et al., 2014; Dhople et al., 2013), and DC-voltage controller based GFM (DC-GFM) control—also known as matching control (Guo et al., 2021; Zhao et al., 2023a; Jouini et al., 2016; Hu et al., 2023). Both droop control and VSG control emulate the external characteristics of synchronous machines, and existing studies have shown that they are approximately equivalent in dynamic behavior (Arco and Suul, 2014). When these two control strategies are used to provide frequency support to the grid, a constant DC voltage and additional power reserve is typically required on the DC side. Therefore, when PV systems adopt either of these grid-forming control methods, they must operate below the maximum power point or incorporate energy storage, leading to resource underutilization or increased investment (Hui Liu et al., 2024). The virtual oscillator is implemented based on the principle of limit cycles in nonlinear systems (Li J. et al., 2022). Due to its complex implementation and lack of intuitive interpretability, its application in large power grids remains limited. In contrast, DC-GFM control provides inertia and frequency support to the system through the DC-side capacitance. It has low power reserve requirements for the grid-side source, and its synchronization mechanism is similar to that of synchronous machines, offering strong interpretability. This makes it particularly promising for renewable energy sources with power limitations, such as PV and wind power.

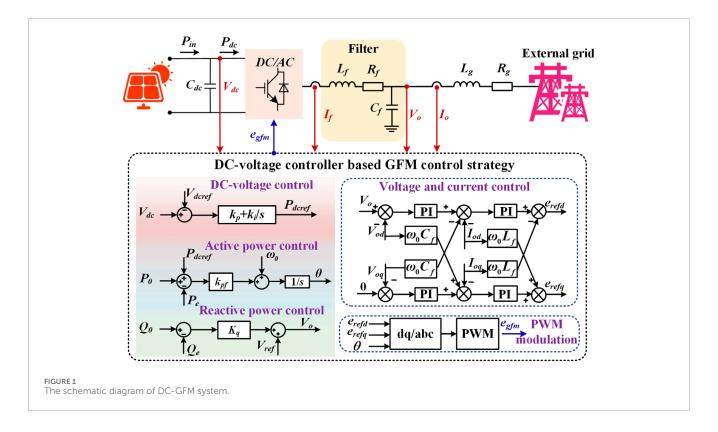
However, the establishment of the synchronization mechanism between the DC voltage and AC frequency also provides an additional channel for disturbances to transfer between the AC and DC sides, potentially leading to severe low-frequency oscillations (LFOs) in the system. In reference (Zhao et al., 2023a), the root locus of DC-GFM control without AC power feedback was analyzed, and the results showed that a pair of poles consistently appears in the low-frequency range of the right half-plane. In reference (Guo et al., 2021), the impedance characteristics of DC-GFM control under two different power feedback controls were analyzed, revealing that both controls exhibited a portion of negative resistance in the 2-9 Hz range. In reference (Liu et al., 2025), it compared the stability of VSG control and DC-GFM control under different grid strengths, and the results indicated that the system using DC-GFM control may experience oscillatory instability under strong grid conditions. The above studies indicate that the LFO modes in DC-GFM control pose a risk of system instability. However, the related stability analyses are primarily based on the eigenvalue distribution or impedance characteristics of the overall system, making it difficult to clearly identify the mechanisms behind negative damping and to provide targeted guidance for the design of low-frequency oscillation suppression strategies.

To enhance the small-signal stability of DC-GFM control, some researchers have proposed several effective suppression strategies. In references (Jouini et al., 2016; Arghir and Dörfler, 2020), parallel resistors are added at the DC capacitor to simulate converter switching losses, thereby improving the damping capability of the system. However, the presence of resistors results in unnecessary power loss, reducing the energy transmission efficiency. In reference (Zhao et al., 2023b), it proposes an oscillation damping strategy based on a notch filter, which enhances low-frequency damping by reshaping the gain of the power feedback loop. However, the damping ratio of the notch filter affects both synchronization and LFO mitigation, leading to a trade-off in parameter design. In reference (Ai et al., 2024), an equivalent damping strategy based on power feedback is introduced. The damping effect is achieved by leveraging the mismatch between the renewable generation and the output power of converter. Thus, the damping capability it provides is limited and may lead to reduced converter efficiency. A parameter alternating controller applicable to DC-GFM system was introduced in reference (Wang et al., 2020). Although it enhances the overall damping of system, it may fall short of delivering optimal damping for individual oscillation modes. In reference (Zhao et al., 2023a), a method based on feeding the q-axis voltage back into the frequency control loop was proposed. However, this control approach may introduce coupling between voltage and frequency dynamics.

Overall, existing research have made some progress in analyzing the stability of DC-GFM converters and in developing damping enhancement strategies; however, they primarily focus on single-converter systems. As a result, they fall short in revealing the stability mechanisms in multi-converter systems, and the applicability of proposed damping strategies in such systems remains uncertain. Based on this, this paper analyzes the LFOs in DC-GFM systems using the damping torque method. The main contributions are as follows.

- a. The torque components in DC-GFM converters are analyzed, revealing the mechanism behind the generation of negative damping torque and how various control parameters influence it.
- b. The stability mechanism of multiple DC-GFM converters parallel system is revealed: as long as the damping torque coefficient of each DC-GFM converter is positive, the entire system remains stable.
- c. A damping enhancement strategy applicable to multi-DC-GFM systems is proposed. By introducing power feedback, additional damping torque is provided to compensate for the negative damping introduced by the DC voltage control, thereby improving the overall system stability.

The remainder of this paper is organized as follows: first, Section 2 presents a complete small-signal model of the system, and analyzes the influence of different control parameters on LFOs. Section 3 then analyzes the torque composition of the DC-GFM and derives the stability conditions for a multi-converter DC-GFM system. Based on this analysis, a damping enhancement strategy is proposed. In Section 4, simulations are conducted to verify both the accuracy of the parameter analysis and the performance of the proposed approach. Section 5 outlines the applicability of this paper and highlights future research opportunities. Section 6 finally concludes the paper.



2 System modeling and analysis of parameter influence

2.1 Small-signal model of DC-GFM system

Figure 1 shows the topology and control block diagram of a gridforming PV system based on DC-voltage controller (hereinafter referred to as the DC-GFM system). Here, P_{in} is the output power of the PV array, and P_{dc} is the power injected into the converter. C_{dc} denotes the DC-side capacitor. L_f and R_f represent the filter inductor and equivalent resistance, respectively; C_f is the filter capacitor; L_g and R_g correspond to the grid-side inductance and equivalent resistance. I_f denotes the current at the converter port, while I_o and V_o represent the output current and voltage of the converter, respectively. The converter employs a DC-GFM control strategy, which mainly includes a DC voltage control loop, active power control loop, reactive power control loop, and a dual-loop control for voltage and current. $V_{\it dcref}$ denotes the reference voltage on the DC side; P_0 and Q_0 are the reference active and reactive power outputs of the converter; $V_{\it ref}$ and ω_0 represent the rated output voltage and frequency, respectively. P_e and Q_e represent the active and reactive power outputs of the converter, respectively, while ω and θ denote the angular frequency and voltage phase angle at the converter output.

Based on the power balance on the DC side, the dynamic of the DC voltage can be derived as:

$$V_{dc}C_{dc}\frac{dV_{dc}}{dt} = P_{in} - P_{dc} \tag{1}$$

Assuming the PV operates under maximum power point tracking and irradiance and temperature remain constant, the

output power of the PV array P_{in} is steady. By expressing the variables in Equation 1 as the sum of their steady-state and perturbation components, the following expression can be obtained:

$$C_{dc}(V_{dc0} + \Delta V_{dc})\frac{d\Delta V_{dc}}{dt} = P_{in} - (P_{dc0} + \Delta P_{dc})$$
 (2)

By eliminating the steady-state and higher-order perturbation components, the resulting relationship between the DC voltage and the DC output power is:

$$\Delta V_{dc} = \frac{-\Delta P_{dc}}{sC_{dc}V_{dc0}} \tag{3}$$

By neglecting the power losses in the converter, P_{dc} in Equation 3 can be substituted with the output power of the converter P_e . The voltage and current dynamics across the LCL filter are given by:

$$\frac{dI_{fdq}}{dt} = \frac{1}{L_f} \left(V_{cdq} - V_{odq} - R_f I_{fdq} \right) \pm \omega_0 I_{fqd} \tag{4}$$

$$\frac{dV_{odq}}{dt} = \frac{1}{C_f} \left(I_{fdq} - I_{odq} \right) \pm \omega_0 V_{oqd} \tag{5}$$

$$\frac{dI_{odq}}{dt} = \frac{1}{L_g} \left(V_{odq} - V_{gdq} - R_g I_{odq} \right) \pm \omega_0 I_{oqd} \tag{6}$$

Therefore, based on Equations 4–6, the output power of the converter can be derived using the instantaneous power theory as:

$$\begin{cases} P_e = 1.5 * (I_{od}V_{od} + I_{oq}V_{oq}) \\ Q_e = 1.5 * (I_{od}V_{oq} - V_{od}I_{oq}) \end{cases}$$
(7)

In DC-GFM, the DC voltage control loop maintains a constant DC voltage via a PI controller. Its control equation is given by:

$$\Delta P_{dcref} = \left(k_p + \frac{k_i}{s}\right) \left(\Delta V_{dc} - \Delta V_{dcref}\right) \tag{8}$$

Here, $P_{\it dcref}$ is the output of the DC voltage control loop and serves as the reference input for the active power control loop. The active power control loop employs a proportional controller to regulate the output active power of converter and establish its frequency. The control equation is given by:

$$\omega = k_{pf} \left(\Delta P_{dcref} + \Delta P_0 - \Delta P_e \right) + \omega_0 \tag{9}$$

Here, k_{pf} is the proportional gain of the active power control loop. The reactive power control loop adjusts the output reactive power of the converter and establishes the AC voltage. Its control equation is:

$$V_o = K_a (Q_0 - Q_e) + V_{ref}$$
 (10)

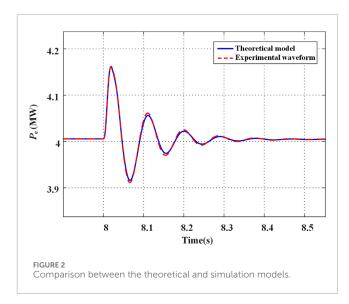
Subsequently, the output of the reactive power control loop is used as the input to the voltage and current control loop for rapid tracking of the grid-side voltage and current variations. Since the time scale of the voltage and current control loop is typically much faster than that of the power control loop, the dynamics of the voltage and current control loop can be neglected when studying the power-frequency dominated LFO issue (Qu et al., 2021). Therefore, the state space formed by Equations 1–10 can provide a detailed description of the system dynamics when low-frequency disturbances occur in the grid, namely,:

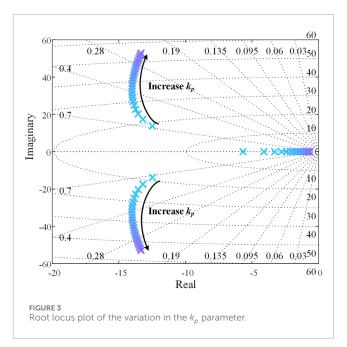
$$\begin{cases} \dot{X}_{sys} = AX_{sys} + BU \\ Y_{sys} = CX_{sys} + DU \end{cases}$$
 (11)

Where X_{sys} is the state variable matrix of the state space, U and Y_{sys} represent the input and output matrices, respectively. A, B, C and D are the corresponding state-space matrices. Figure 2 presents the waveforms obtained from the theoretical model based on Equation 11 and the hardware-in-the-loop experiment, under a 0.4 MW load disturbance on the grid side occurring at 8 s. The close agreement between the two curves confirms the reliability of the developed state-space model.

2.2 Analysis of parameter impact and associated stability risks

To investigate how control parameters affect LFOs in the DC-GFM system, root locus diagrams corresponding to parameter variations are plotted based on Equation 11. Figures 3–5 respectively show how the root locus of the LFO mode evolves with increasing proportional gain k_p and integral gain k_i of the DC voltage control loop, and the proportional gain k_p of the active power control loop. As shown in Figure 3, as k_p increases, the imaginary part of the eigenvalue corresponding to the LFO mode increases steadily, while the real part first increases and then decreases. The magnitude of change in the imaginary part is significantly greater than that of the real part, indicating that increasing k_p has limited impact on the

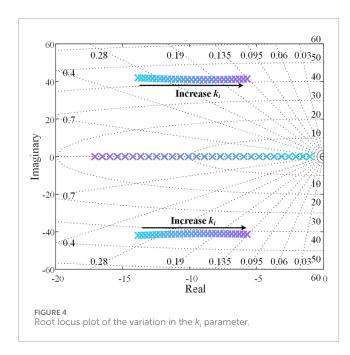


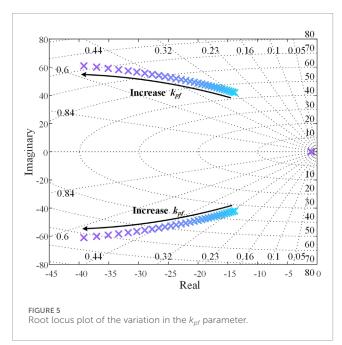


duration of LFOs under the same disturbance, but it does result in a higher oscillation frequency.

As shown in Figure 4, when k_i is gradually increased, the imaginary part of the eigenvalue corresponding to the LFO mode remains nearly unchanged, while the real part decreases significantly. This indicates that for a given disturbance, increasing k_i has little effect on the oscillation frequency but noticeably extends the duration of oscillations. Moreover, if k_i becomes too large, the eigenvalue may cross the imaginary axis into the right-half plane, potentially causing system instability.

In contrast, as shown in Figure 5, with the gradual increase of k_{pf} , both the real and imaginary parts of the eigenvalue corresponding to the LFO mode increase, leading to an enhanced damping ratio. This indicates that under a disturbance, increasing k_{pf} raises the oscillation frequency while significantly reducing the oscillation duration.

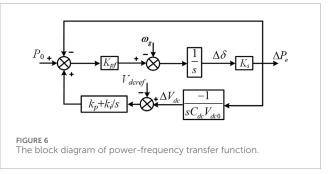




3 Identification of negative damping components and strategies for enhancing damping torque

3.1 Torque components in DC-GFM systems

As shown in the analysis of Section 2, an excessively large k_i or a too-small k_{pf} can compromise system stability under DC-GFM control. Although tuning these parameters can improve the damping of LFO mode, they often affect other aspects of system performance—for example, a small k_i may result in slow DC voltage regulation. An effective approach is to introduce an additional



control loop to the existing control structure, providing the system with extra degrees of freedom. However, although the root locus-based parameters analysis can comprehensively reveal the evolution of system poles, it heavily relies on model parameters and falls short of uncovering the underlying mechanism of negative damping, thus making the design of supplementary control loops more challenging.

The damping torque method, based on classical control theory and the decomposition of the torque acting on the motion of generator rotor, quantifies the damping capability of synchronous generators. It is widely used in LFO risk assessment in traditional power systems. It provides clear physical insight into the occurrence of weak or negative damping modes, thereby guiding control design for oscillation suppression. Based on this, the damping torque method is employed in this paper to analyze the sources of negative damping in DC-GFM systems. In high-voltage grids, the grid impedance is primarily inductive, resulting in a decoupling of active and reactive power. Under this condition, the active power can be expressed by the power flow equation as follows:

$$P_e = \frac{V_o V_g}{X_g} \sin \delta \tag{12}$$

Here, δ represents the phase angle difference between the converter output voltage and the grid voltage. By linearizing Equation 12, we can obtain:

$$\Delta P_e = \frac{V_o V_g}{X_o} \Delta \delta = K_s \Delta \delta \tag{13}$$

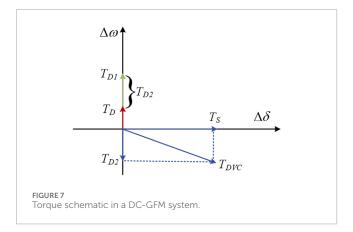
Here, K_s denotes the power synchronization coefficient of the converter, which reflects the power transfer limit of the DC-GFM system. Accordingly, by combining Equations 3, 8, 9 and 13, the power–frequency transfer function block diagram of the system is shown in Figure 6.

When the reference values remain unchanged, the power angle dynamics of the DC-GFM system can be derived from Figure 6 as follows:

$$s\Delta\delta + \left(\frac{k_{pf}k_{p}K_{s}}{sC_{dc}V_{dc0}} + \frac{k_{pf}k_{i}K_{s}}{s^{2}C_{dc}V_{dc0}}\right)\Delta\delta + k_{pf}K_{s}\Delta\delta = 0$$
 (14)

Multiplying Equation 14 on both sides by the Laplace operator s leads to:

$$s^{2}\Delta\delta + \underbrace{\left(k_{pf}K_{s} + \frac{k_{pf}k_{i}K_{s}}{s^{2}C_{dc}V_{dc0}}\right)}_{T_{c}}s\Delta\delta + \underbrace{\frac{k_{pf}k_{p}K_{s}}{C_{dc}V_{dc0}}}_{T_{s}}\Delta\delta = 0$$
 (15)



According to the Phillips model, the power angle dynamics of a synchronous generator can be described as follows (Du and Wang, 2015):

$$s^{2}\Delta\delta + \frac{D}{M}s\Delta\delta + \frac{\omega_{0}K_{1}}{M}\Delta\delta = 0$$
 (16)

Here, the term D/M, which is associated with frequency, represents the damping torque that affects the ability of system to dampen the LFO. Its physical meaning is clear: it is a force (torque) proportional to velocity (angular velocity), acting as a resistive force (torque) against motion (angular displacement), thereby providing damping. The term ω_{0K1}/M , which relates to the power angle, represents the synchronizing torque that determines the ability of units to maintain synchronism. It primarily influences the oscillation frequency of the output power [19]. Therefore, by comparing Equations 15, 16, it can be observed that $T_{\rm D}$ is the key factor determining the damping capability of LFOs in DC-GFM systems. When a LFO mode with frequency ω_r exists in the system, setting $s = j\omega_r$ yields $T_{\rm D}$ as:

$$T_{D} = K_{s} k_{pf} - \underbrace{\frac{K_{s} k_{pf} k_{i}}{\omega_{r}^{2} C_{dc} V_{dc0}}}_{T_{DC}} = K_{s} k_{pf} \left(1 - \frac{k_{i}}{\omega_{r}^{2} C_{dc} V_{dc0}} \right)$$
(17)

Figure 7 shows the torque diagram of the DC-GFM system, where T_{DVC} represents the equivalent torque generated by the DC voltage control loop. It can be seen that T_{D1} , formed by component $k_{pf}K_s$, provides positive damping torque to the system, while T_{D2} , involving the k_i parameter, introduces negative damping torque. When the system damping is positive, an increase in the k_i parameter and a decrease in k_{pf} will gradually reduce the damping of the LFO mode, making the oscillations more pronounced. Therefore, as discussed in Section 2, increasing the k_i parameter leads to a decrease in the real part of the LFO mode, while increasing k_{pf} results in an increase in the real part. Meanwhile, in Equation 15, T_s primarily influences the oscillation frequency of the DC-GFM system. As k_p and k_{pf} increase, T_s also increases, leading to a higher oscillation frequency. Therefore, in Section 2, as the k_p and k_{pf} parameters increase, the imaginary part of the LFO mode gradually increases.

3.2 Stability analysis of multi-unit system

As shown in Figure 8, n DC-GFM units operate in parallel, where the output power of GFM_i (i = 1, 2, ..., n) is denoted by P_i . The power-frequency transfer relationship at the point of common coupling (PCC) for each GFM_i is given by:

$$G_i(s) = \frac{-\Delta P_i}{\Delta \omega_{\sigma}} \tag{18}$$

For simplicity, the analysis begins with the case of n = 2. When a power disturbance P_L occurs on the grid side, the power balance at the PCC can be expressed as Equation 19:

$$\Delta P_L = \Delta P_1 + \Delta P_2 = -G_1(s)\Delta\omega_\sigma - G_2(s)\Delta\omega_\sigma \tag{19}$$

Therefore, the power–frequency relationship at the PCC can be derived as Equation 23:

$$\frac{\Delta \omega_g}{-\Delta P_L} = \frac{1}{G_1(s) + G_2(s)} = \frac{G_2(s)^{-1}}{1 + G_1(s)/G_2(s)}$$
(20)

Equation 20 can be interpreted as the closed-loop transfer function of a negative feedback system, as shown in Figure 9, where the feedforward gain is $G_2(s)^{-1}$ and the feedback gain is $G_1(s)$. Therefore, $G_1(s)/G_2(s)$ represents the open-loop transfer function of the system. According to the Nyquist stability criterion, the system shown in Figure 9 remains stable as long as the condition in Equation 21 is satisfied, ensuring a positive phase margin.

$$\forall \omega_r \in (0, +\infty), \arg\left(\frac{G_1(j\omega_r)}{G_2(j\omega_r)}\right) \in (-\pi, \pi)$$
 (21)

A sufficient condition for Equation 21 to hold is:

$$\forall \omega_r \in (0, +\infty), \operatorname{Re}(G_i(j\omega_r)) > 0$$
 (22)

Based on Figure 6 and Equation 18, the expression for G_i ($j\omega_r$) can be derived as follows:

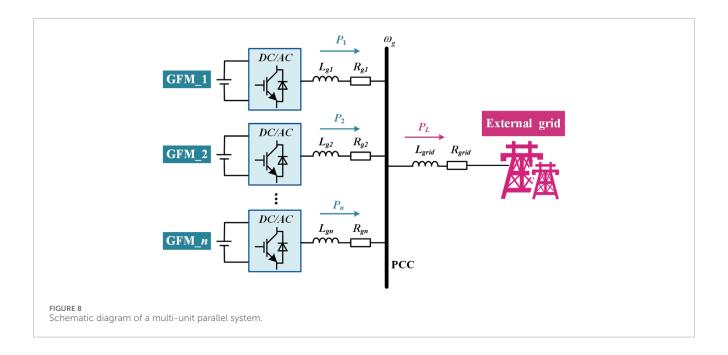
$$G_i(j\omega_r) = \frac{j\omega_r K_s}{\left(\frac{k_{pf}k_p K_s}{C_s V_{so}} - \omega_r^2\right) + \left(k_{pf}K_s - \frac{k_{pf}k_i K_s}{\omega_s^2 C_{ss} V_{so}}\right) j\omega_r}$$
(23)

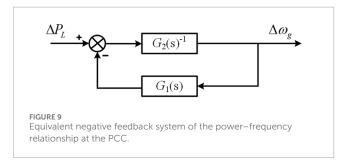
Therefore, when Equation 24 is satisfied, Equation 22 holds, indicating that the system shown in Figure 9 is stable.

$$k_{pf}K_s - \frac{k_{pf}k_iK_s}{\omega_r^2 C_{dc} V_{dc0}} > 0$$
 (24)

By comparing Equations 17, 24, it can be concluded that the parallel system remains stable when both GFM converters exhibit positive damping torque. This analysis is then extended to the case of multiple DC-GFM units operating in parallel. Consider the *j*th inverter as a separate subsystem, while treating the remaining inverters as another subsystem. Based on the power balance relationship at the PCC shown in Figure 8, we can derive Equation 25:

$$\Delta P_L = \sum_{i=1}^n \Delta P_i = -\left(G_j(s) + \sum_{i \neq j}^n G_i(s)\right) \Delta \omega_g \tag{25}$$





Similarly, the power–frequency relationship at the PCC can be expressed as:

$$\frac{\Delta \omega_g}{-\Delta P_L} = \frac{G_j(s)^{-1}}{1 + \sum_{i \neq j}^n G_i(s) / G_j(s)}$$
(26)

Equation 26 can also be viewed as the closed-loop transfer function of a negative feedback system. According to our earlier findings, Equation 22 is satisfied when each GFM converter contributes a positive damping torque. Hence, by applying the rules of complex addition, we obtain:

$$\forall \omega_r \in (0, +\infty), \operatorname{Re}\left(\sum_{i \neq j}^n G_i(j\omega_r)\right) > 0$$
 (27)

Since the real part of $G_i(j\omega_r)$ is also positive, it follows that:

$$\forall \omega_r \in (0, +\infty), \arg\left(\sum_{i \neq j}^n G_i(j\omega_r)/G_j(j\omega_r)\right) \in (-\pi, \pi)$$
 (28)

Equation 28 indicates that the equivalent negative feedback system described by Equation 26 maintains a positive phase margin at all times. Therefore, when n DC-GFM units operate in parallel, the system remains stable as long as each GFM converter provides positive damping torque. It is worth noting

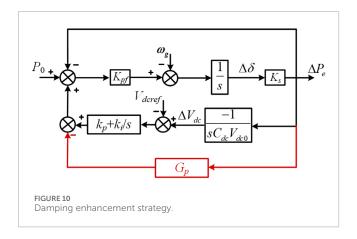
that Equations 27, 28 hold without imposing any constraints on the parameters of the DC-GFM converters. In other words, a multi-converter DC-GFM system with non-identical parameters remains stable as long as each DC-GFM provides positive damping torque.

3.3 Damping enhancement strategy

As demonstrated in Sections 3.1 and 3.2, whether considering a single DC-GFM system or a system composed of multiple DC-GFMs, system stability fundamentally depends on ensuring that the damping torque of each DC-GFM remains positive. However, the integral gain k_i of the DC voltage control loop introduces negative damping torque into the system, which may lead to instability. Therefore, an additional damping control strategy is required to enhance system stability. As shown in Figure 10, the introduction of negative damping torque by the k_i parameter arises from the -180° phase lag introduced by two successive integration stages in the power-to-frequency feedback path. Therefore, this paper proposes the use of a lead-lag compensator to inject additional damping torque through power feedback, thereby counteracting the negative damping caused by the DC voltage control loop, as illustrated in Figure 10. The transfer function of the lead-lag compensator, G_p , is given by Equation 29:

$$G_p = \frac{s + T_2}{s + T_2} \tag{29}$$

where, $T_1=10$, $T_2=1$, and T_1 and T_2 denote the lead and lag time constants of the lead-lag compensator, respectively. When $T_1>T_2$, the phase of G_p is positive. As a result, the power feedback introduces an additional torque into the system, which acts as a positive damping torque that compensates for the negative damping torque caused by the k_i parameter in the DC voltage control loop.





S _{base}	4 MW	$V_{\it base}$	311 V
C_{dc}	2.28 p.u.	V_{dc}	800 V
Z_f	0.03 + j0.1 p.u.	ω_0	$100\pi \text{ rad/s}$
C_f	0.05 p.u.	Z_g	0.03 + j0.1 p.u.
Z_g	0.06 + j0.2 p.u.	k _{pf}	0.02 p.u.
k_p	2 p.u.	k_i	2 p.u.
T_1	10	T_2	1

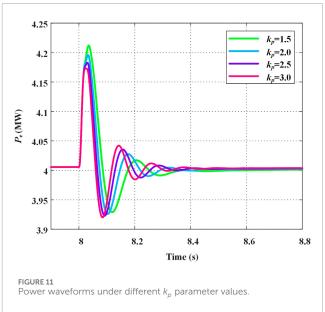
4 Experimental verification

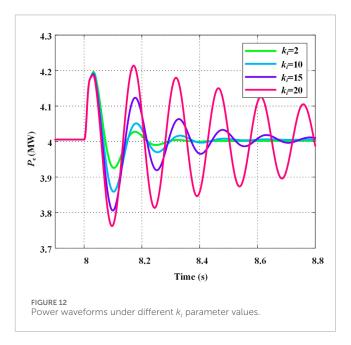
To validate the accuracy of the parameter analysis and the effectiveness of the proposed damping enhancement strategy, a DC-GFM system shown in Figure 1 was developed. The system parameters are listed in Table 1.

4.1 Validation of parameter influence

As shown in Figure 11, the power waveforms under different proportional gains k_p of the DC voltage control loop are presented for a 0.4 MW load disturbance occurring at 8 s. It can be observed that the oscillation frequency increases with larger k_p values. However, the DC-GFM system reaches steady state at approximately 8.4 s across all k_p settings, indicating that k_p has little impact on the oscillation duration. This phenomenon has been explained in Sections 2 and 3. It is primarily due to the fact that k_p affects the synchronizing torque of the DC-GFM system, which is reflected in the root locus as a change mainly in the imaginary part of the LFO mode.

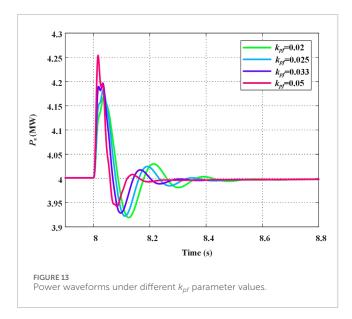
As shown in Figure 12, when a 0.4 MW load disturbance occurs at 8 s, the power waveforms under different integral gains k_i of the DC voltage control loop are presented. It can be observed that increasing k_i does not significantly affect the oscillation frequency of the DC-GFM system, but it does lead to a noticeable increase in oscillation amplitude, thereby requiring a longer time to reach steady

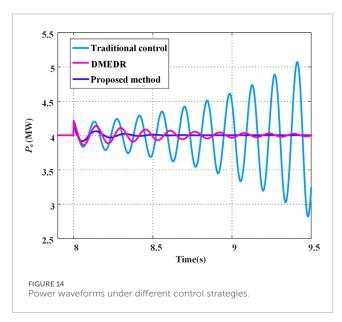




state. Similarly, the influence of the k_i parameter can be explained based on the analysis presented in Sections 2 and 3. As k_i increases, it introduces negative damping torque into the system, causing the real part of the LFO mode to gradually decrease. This leads to a reduction in system damping and results in more pronounced oscillations.

Figure 13 shows the power profiles under a 0.4 MW load disturbance occurring at 8 s, with different proportional gains k_{pf} in the power control loop. It can be observed that as k_{pf} increases, the oscillation frequency of the DC-GFM converter rises while the amplitude decreases, indicating that a higher k_{pf} helps the converter stabilize more quickly. As indicated by the analysis of Equation 15, this behavior arises because the k_{pf} parameter influences both the damping torque and the synchronizing torque of the system. When the total system damping is positive, increasing k_{pf} enhances both torque components. As a result, the real and imaginary parts of the



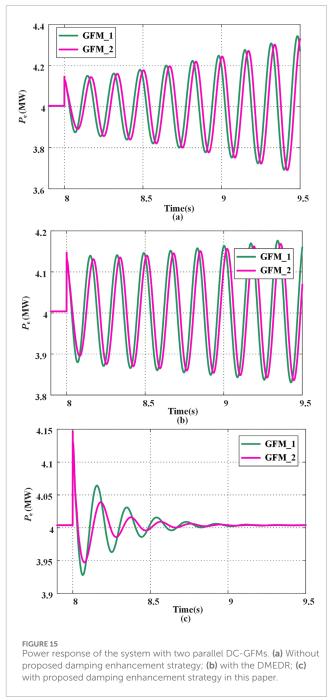


LFO mode increase, leading to a higher oscillation frequency and faster decay of oscillations.

4.2 Validation of the proposed damping enhancement strategy

To validate the effectiveness of the proposed damping enhancement strategy, compare the dynamic performance of the DC-GFM converter under identical disturbances using three approaches: conventional DC-GFM control, the damping method based on equivalent DC resistance (DMEDR) from reference (Ai et al., 2024), and the strategy proposed in this paper. Figures 14, 15 presents the power response waveforms with different control methods during a 0.4 MW load disturbance at 8 s. In this case, the parameter k_i is set to 30 p. u.

As shown in Figure 14, without any additional damping control, the DC-GFM converter diverges following the disturbance. In



contrast, when applying the DMEDR from reference (Ai et al., 2024) and the strategy proposed in this paper, the converter returns to steady state after a period of oscillation. When the DMEDR from reference (Ai et al., 2024) is applied, the DC-GFM converter requires a relatively long period of oscillation to reach steady state. In contrast, the strategy proposed in this paper enables the system to return to steady state within just two or three oscillation cycles. This demonstrates that the proposed method provides stronger low-frequency damping for single DC-GFM converter systems.

Figure 15 shows the power waveforms during parallel operation of two DC-GFM units. GFM_1 has a k_i value of 40 p. u., while GFM_2 has a k_i value of 10 p. u. As illustrated in the Figure 12, the system remains stable when only GFM_2 is connected to the

grid. However, as shown in Figure 15a, when the proposed damping enhancement strategy is not applied, the power outputs of both units begin to oscillate and gradually diverge after GFM_1 and GFM_2 are connected in parallel. The instability arises because the excessive negative damping torque generated by the high k_i value in GFM_1 drives the total system damping below zero. Therefore, even though GFM_2 itself provides positive damping torque, it still becomes unstable due to the gradual divergence of the electrical quantities of system. As shown in Figure 15b, after applying the DMEDR from reference (Ai et al., 2024), the equivalent resistance on the DC side provides some damping, which slows down the power divergence of GFM_1 and GFM_2. However, the system still gradually becomes unstable. In contrast, as shown in Figure 15c, when the proposed damping enhancement strategy is applied to both units, the output power of each unit reaches steady state around 9 s after experiencing a short oscillation. This demonstrates that the proposed strategy is also effective in suppressing oscillations in multi-unit systems.

5 Limitations and future research

This paper primarily discusses LFO in GFM systems following the introduction of the DC voltage control loop. Using the damping torque method, it analyzes the impact mechanisms of control parameters in both the DC voltage control loop and active power control loop of DC-GFM within high-voltage grids, examines the stability conditions of multiple DC-GFM parallel systems, and proposes a damping enhancement strategy. However, DC-GFM converters also include multiple cascaded control loops, such as reactive power control loops and voltage-current control loops (Yu et al., 2021). In high-voltage grids, due to the low R/X ratio, active and reactive power are approximately decoupled, and since the voltage-current control loop typically have bandwidths above several tens Hz, the reactive power and voltage-current control loops have minimal impact on the frequency dynamics of DC-GFM converters (Wen et al., 2021). However, in low-voltage grids with a low R/X ratio and in large-capacity stations, the active power control loop can become coupled with the reactive power and voltagecurrent control loops (Qu et al., 2021; Li C. et al., 2022), making the torque composition of DC-GFM converters highly complex. In this situation, the effects of parameters in the DC voltage control loop and active power control loop might alter. Therefore, further research is needed to analyze the parameter effects and stability of DC-GFM converters under different scenarios, considering the coupling among multiple control loops.

Moreover, the multi-unit stability analysis and damping enhancement strategies discussed in this paper primarily focus on scenarios where DC-GFM converters operate in parallel. With the increasing integration of renewable energy, power systems may include various types of grid-connected devices, such as grid-following converters (Rosso et al., 2020), synchronous generators, and power-synchronization-based GFM converters (Zhang et al., 2016). The dynamics of these devices differ significantly from those of DC-GFM converters. When they are located close to each other in the grid, interactions may occur that alter the LFO characteristics of the DC-GFM converters. Future research is needed to further investigate LFO issues arising from dynamic interactions among different devices.

6 Conclusion

To address the issue of LFOs in GFM converters based on DC capacitor synchronization, this paper establishes a state-space model of the converter and analyzes how the parameters of the DC voltage control loop and power control loop affect the LFO mode of system. The results show that increasing the proportional gain of the DC voltage control loop raises the oscillation frequency, while increasing the integral gain extends the duration of oscillations. In contrast, increasing the proportional gain of the power control loop leads to a higher oscillation frequency and a shorter oscillation duration. Subsequently, the damping torque method was employed to analyze the components contributing to damping torque and synchronizing torque in GFM converters, providing a clear explanation of the root causes of negative damping and the underlying mechanisms of parameter influence. The stability conditions of a multi-DC-GFM parallel system were analyzed, and the results indicate that the system remains stable as long as each DC-GFM converter pro-vides a positive damping torque. On this basis, a damping enhancement strategy was proposed using a lead-lag compensator. Finally, simulation results were used to validate both the parameter analysis and the effectiveness of the proposed control strategy.

Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

Author contributions

WK: Writing – original draft, Validation, Methodology. YZ: Writing – review and editing, Validation. JL: Investigation, Writing – review and editing, Conceptualization, Data curation. JW: Visualization, Writing – review and editing, Conceptualization. JX: Project administration, Writing – review and editing, Formal Analysis, Resources. LL: Software, Writing – review and editing, Supervision.

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Conflict of interest

Author YZ was employed by State Grid Lasa Power Supply Company.

Author JW was employed by State Grid Xizang Electric Power Company Limited.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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