



Can The Pore Scale Geometry Explain Soil Sample Scale Hydrodynamic Properties?

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For decades, the development of new visualization techniques has brought incredible insights into our understanding of how soil structure affects soil function. X-ray microtomography is a technique often used by soil scientists but challenges remain with the implementation of the procedure, including how well the samples represent the uniqueness of the pore network and structure and the systemic compromise between sample size and resolution. We, therefore, chose to study soil samples from two perspectives: a macroscopic scale with hydrodynamic characterization and a microscopic scale with structural characterization through the use of X-ray microtomography (X-ray μ CT) at a voxel size of 21.5³ μ m³ (resampled at 43³ μ m³). The objective of this paper is to unravel the relationships between macroscopic soil properties and microscopic soil structure. The 24 samples came from an agricultural field (Cutanic Luvisol) and the macroscopic hydrodynamic properties were determined using laboratory measurements of the saturated hydraulic conductivity (Ks), air permeability (ka), and retention curves (SWRC). The X-ray µCT images were segmented using a global method and multiple microscopic measurements were calculated. We used Bayesian statistics to report the credible correlation coefficients and linear regressions models between macro- and microscopic measurements. Due to the small voxel size, we observed unprecedented relationships, such as positive correlations between log(Ks) and a μ CT global connectivity indicator, the fractal dimension of the μ CT images or the μ CT degree of anisotropy. The air permeability measured at a water matric potential of -70 kPa was correlated to the average coordination number and the X-ray µCT porosity, but was best explained by the average pore volume of the smallest pores. Continuous SWRC were better predicted near saturation when the pore-size distributions calculated on the X-ray µCT images were used as model input. We also showed a link between pores of different sizes. Identifying the key geometrical indicators that induce soil hydrodynamic behavior is of major interest for the generation of phenomenological pore network models. These models are useful to test physical equations of fluid transport that ultimately depend on a multitude of processes, and induce numerous biological processes.

Keywords: soil, X-ray micro-computed tomography, saturated hydraulic conductivity, soil water retention curve, air permeability, Bayesian statistics

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INTRODUCTION

The development of visualization techniques has played a major role in fully describing soil functions. Serial sectioning, a wellestablished method (Cousin et al., 1996), has been replaced by replaced by 3D non-destructive visualization techniques are becoming more easily available, with added benefit of less timeconsuming procedures that provide higher resolution images (Grevers et al., 1989). However, Roose et al. (2016) have wisely said, "Technological advances alone are not sufficient. Real advances in our understanding will only be achieved if these data can be integrated, correlated, and used to parameterize and validate image based and mechanistic models." X-ray microcomputed tomography (X-ray µCT) has been widely used in soil science making comparisons between studies possible. (Taina et al., 2008) and Wildenschild and Sheppard (2013) discuss the use of X-ray µCT to study the vadose zone. We also will mention the visual analysis of the air and water distributions within pore spaces, which are both important physical variables for activity of soil biota (e.g., Young et al., 1998; Or et al., 2007; Falconer et al., 2012; Monga et al., 2014; Vogel et al., 2015). One approach is to visualize the soil at high resolution to identify hot-spots of microbial activity (e.g., Gutiérrez Castorena et al., 2016), simulate air-water interfaces within the pore network (e.g., Pot et al., 2015) or quantify the impact of the pore network architecture on the microorganism's activity (e.g., Kravchenko and Guber, 2017). Another approach is to provide a more specific description of the fluid transport capacities (Vogel et al., 2015) which could ultimately improve field-scale models of microbial activity and biochemical processes (Blagodatsky and Smith, 2012). De facto, when dealing with agricultural and environmental properties of the soil, an accurate description and prediction of its transport capacities in the unsaturated state is the overarching goal.

It is well-known that, due to natural or anthropogenic actions, there is quite a range in the variability in fluid transport parameters [e.g., saturated hydraulic conductivity (Ks) or air permeability (ka)] between samples with homogenous textures (Baveye and Laba, 2015; Naveed et al., 2016), due to the uniqueness of the porosity distribution and the connectivity within a sample. Studies have, therefore, focused on the link between the inner pore space structure of a sample and its specific fluid transport properties. On one hand, experimentally visualized infiltration studies shed light on the effective conducting pore network which represents only a small portion of the total network (Luo et al., 2008; Koestel and Larsbo, 2014; Sammartino et al., 2015). The procedures developed in these studies are promising, but restricted to the analysis of large macropores because of the trade-off between resolution and acquisition time. On the other hand, numerical simulations based on pore space are used to predict conductivity. Many studies focused on idealized porous structures (e.g., Vogel et al., 2005; Schaap et al., 2007) and a few deal with actual soil (Elliot et al., 2010; Dal Ferro et al., 2015; Tracy et al., 2015). The latter show encouraging results, but are restricted to a defined resolution and/or sample size (Baveye et al., 2017). Indeed, the direct approach of linking one structure to one function is limited by the difficulty in analyzing the structure in a representative way, so that the soil is adequately characterized (Vogel et al., 2010). The description of soil microscopic structure via global characteristics could encompass that challenge and comparisons of one soil microscopic structure to its own macroscopic properties have indeed gained attention.

Luo et al. (2010) were among the first to measure Ks and the break through curve characteristics on soil samples that were also scanned with X-ray µCT and analyzed in 3D (16 soil cores of 5 \times 6 cm and 10.2 \times 35 cm and voxel sizes ranging from $250^2 \times 1,000 \ \mu\text{m}^3$ to $1^2 \times 10 \ \text{mm}^3$). They found that µCT macroporosity, the number of independent macropore, macropore hydraulic radius and angle were identified as the most important microscopic characteristics to explain fluid transport. From 18 soils cores (10×9 cm) scanned at a voxel size of 186^3 μ m³ and 17 soil cores (19 × 20 cm) scanned at 430² × 600 μm³, respectively, Naveed et al. (2012) and Katuwal et al. (2015b) found that the lowest μ CT macroporosity value for any quarter length of sample height adequately explained air permeability (ka) measured at a water matric potential (h) of -3 or -2 kPa, respectively. Paradelo et al. (2016) showed that the minimum value of macroporosity along a sample depth was most correlated to Ks and ka (45 soil cores of 20 \times 20 cm and voxel size of 430 $^2 \times$ 600 μm³). Mossadeghi-Björklund et al. (2016) also demonstrated that Ks was significantly correlated to µCT macroporosity within a compaction experiment (32 soils cores of 20 \times 20 cm and voxels size of $430^2 \times 600 \,\mu\text{m}$). Eventually, Naveed et al. (2016) suggested that biopore-dominated and matrix-dominated flow soil cores should be distinguished before analyzing relationships between microscopic and macroscopic soil properties. They indeed found distinct significant power regressions between Ks or ka (measured at h = -3 and -0 kPa) and μ CT macroporosity for the two categories of the 65 soil cores (6 \times 3.5 cm and voxel size of $129^3 \ \mu m^3$). These observed relationships between flow parameters and µCT porosity are actually intuitive, but they depend on image resolution, water matric potential and soil type. For example, Lamandé et al. (2013) did not find the expected relationship between μ CT porosity and ka measured at h =-10 kPa, but rather a linear positive relationship between the number of pores and ka (32 soil cores of 19×20 cm and voxel size of $600^3 \,\mu\text{m}^3$). Finally, Anderson (2014) found that Ks could reasonably be estimated from the µCT number of pores and the μCT macroporosity fractal dimension (336 soil cores of 7.62 \times 7.62 cm and voxel size of $0.19^2 \times 0.5 \,\mu\text{m}^3$).

The μ CT porosity, number of pores, average pore radius, surface area, and pore network connectivity and tortuosity all depend on the minimal visible pore size, in other words, on the resolution of the binary X-ray μ CT images used to obtain the pore network (Houston et al., 2013; Peng et al., 2014; Shah et al., 2016), additionnaly, useful information about conducting pores is lost with increased voxel size. One strategy to minimize this limitation is to use grayscale information. Crestana et al. (1985) demonstrated a linear dependence between the gray value of the

Abbreviations: h, water matric potential; θ , water content; SWRC, soil water retention curve; Ks, saturated hydraulic conductivity; ka, air permeability; LabPO, laboratory measured air-filled porosity at a water matrix potential of 1 kPa; BF, Bayes factor. The rest of the uncommon abbreviations are defined in **Table 1**.

soil matrix in Hounsfield unit (HU) and the soil water content. More recently, Katuwal et al. (2015a) found the CT number of the soil matrix (average grayscale value in HU) as a useful descriptor for determining the magnitude of preferential flow, and Paradelo et al. (2016) showed that global macroporosity values combined with the CT-matrix number best explained the variation in air and water transport parameters. Another strategy would be to scan soil samples at higher resolutions. For example, Sandin et al. (2017) worked at a voxel size of $120^3 \ \mu m^3$ and observed significant correlations between Ks and a global measure of the pore network connectivity (from the percolation theory) which had, to our knowledge, never been observed (20 soil samples of 6.8 \times 10 cm). Pore network connectivity and tortuosity are important indicators of flow capacities (Perret et al., 1999; Vogel, 2000). There is still a lack of information on the links between global pore network complexity indicators and flow parameters. It is indeed challenging to identify and describe the part of the conducting pore network that dominates flow. We, however, hypothesize that it might come from the resolution at which previous studies were performed.

Within that context, the objectives of this study are to: (i) characterize the microscopic structure of twenty-four soil samples at a resolution of $21.5 \,\mu$ m resampled to $43 \,\mu$ m; and (ii) explore the relationships between soil microscopic characteristics and its saturated hydraulic conductivity, air permeability and retention capacities using Bayesian statistics.

MATERIALS AND METHODS

Soil Sampling

Twenty-four vertical undisturbed soil samples (3 cm in diameter and 5 cm in height) were taken at the surface of an agricultural soil in Gembloux, Belgium ($50^{\circ}33'$ N, $4^{\circ}42'$ E). According to the WRB soil system (2006), this soil is classified as a *Cutanic Luvisol* with an average of 14.3% of clay, 78.3% of silt and 7.4% of sand. This type of soil is representative of the intensive central agricultural area in Belgium. Sampling was performed 24 to 48 h after a rain. In order to minimize sampling disturbance, the plastic cylinders were manually driven into the soil until the top of the cylinder was at the surface level and then manually excavated.

Macroscopic Measurements

Soil samples were first upward saturated with distilled water. Their characteristic soil water retention curve (SRWC) was then measured using pressure plates (Richards, 1948; DIN ISO 11274, 2012). After being weighed at a water matric potential of -7, -10, -30 and -70 kPa, the air permeability of the samples was measured by applying an air flow across the sample and measuring the resulting inner-pressure with an Eijkelkamp air permeameter 08.65 (Eijkelkamp Agrisearch Equipment, Giesbeek, The Netherlands). As recommended by the constructor, each measure was repeated five times and kept as short as possible. Corey's law was then applied to calculate the air permeability [L²] (Corey, 1986 in Olson et al., 2001). At -70 kPa, the soil samples were scanned using an X-ray microtomograph (see next section) before the end of their SWRC

was measured (water matric potential of -100, -500, and -1500 kPa). After reaching -1,500 kPa, the soil samples were saturated once again and the saturated hydraulic conductivity (Ks [LT⁻¹]) was measured using a constant head device (Rowell, 1994) and applying Darcy's law. Finally, the soil samples were oven-dried at 105° for 7 days to obtain their dry weight. Porosity [L³L⁻³] was calculated as the ratio between the volume of water within the saturated soil sample and its total volume (McKenzie et al., 2002). From McKenzie et al. (2002), the bulk density (BD) [ML⁻³] was deduced from the porosity value (PO) assuming a particle density of 2.65 g/cm³.

Microscopic Measurements Image Acquisition

After reaching a water matric potential of -70 kPa, the soil samples were scanned using a Skyscan-1172 desktop micro-CT system (Bruker microCT, Kontich, Belgium). The choice of scanning parameters (filters, number of projections, 180 or 360°, projection averaging) was made by evaluating reconstruction quality over acquisition time. The X-ray source was set at 100 kV and 100 µA and an aluminum-copper filter was used to reduce the beam hardening artifacts in the reconstruction. The rotation step was set at 0.3° over 180° and, to improve the signal-to-noise ratio, the average of 2 projections was recorded at each rotation step. The exposure time was 600 ms. The field of view was 21 \times 14 mm and, to cover the entire sample, a 2 \times 4 grid of subregions were scanned (in the Skyscan software this corresponds to using both the "wide image" mode and "oversize scan" mode). Given these parameters, the total acquisition time was \sim 4 h. We adjusted the detector configuration (16-bit X-ray camera with 4×4 binning, creating 1000 \times 666 pixel radiograms) and the distance between the camera and the soil sample in order to obtain radiographs with a pixel size of $21.5 \,\mu$ m.

Image Processing

Tomographic reconstruction was performed with the NRecon^(R) software, freely provided by Brüker. Automatic misalignment compensation was used along with a level 7 (out of 20) ring artifact correction. No beam hardening post-corrections were applied. The lower limit for the histogram grayscale range was set at zero, as recommended by Tarplee and Corps (2008). The upper limit, the same for all samples, was the maximum value between the automatically generated upper limit for each sample. After reconstructions, the 3D images were cropped to only select the volume within the sampling cylinders (radius of 700 pixels) and the image's contrast was improved in Matlab (MathWorks, UK).

Prior to segmentation, a 3D median filter with a radius of 2 pixels was applied to the images to decrease noise (Smet et al., 2017). Because of computational cost, sub-sampling was performed and the final voxel size was 43 μ m in all directions. This process follows recommendation from Houston et al. (2013) and Shah et al. (2016), which is to scan a sample at the highest possible resolution even if a post-scan coarsening is necessary. We then applied the global porosity-based segmentation method developed by Beckers et al. (2014b). To that purpose, we firstly calculated the potential maximal visible pore size from capillary

law and voxel size information $(43^3 \mu m^3)$. Then, from the laboratory SWRC data, the potential visible porosity for each soil samples was obtained; it was the air-filled porosity at h= -1 kPa (equivalent radius of 150 μ m). The porosity-based segmentation method selects an initial global threshold with Otsu's method (Otsu, 1979), and then compares the porosity of the resulting binary image (ratio of pore voxels over the total amount of voxels) to the estimated soil sample visible porosity. Through an iterative loop, the threshold is then adjusted to minimize the difference between this calculated porosity and the estimated soil sample visible-porosity. This method has been proven satisfactory (Beckers et al., 2014b; Smet et al., 2017) and the Matlab R2015a (MathWorks, UK) code was provided by the authors. Finally, a visual inspection was performed to evaluate the segmentation quality and, in case the porosity-based segmentation method failed, Otsu's segmentation was used. A post-segmentation cleanup was applied to remove any pores smaller than five voxels.

Quantification of Soil Microscopic Features

After segmentation, the images were imported into Avizo where codes developed by Plougonven (2009) were used. Those codes provide a 3D morphological quantification of the pores based on the skeleton where a pore is defined as "part of the pore space, homotopic to a ball, bounded by the solid, and connected to other pores by throats of minimal surface area" (Plougonven, 2009), the pore boundaries are demarcated by the local geometry. The resulting 3D quantification information regarding pores chambers connected by pores throats included pore localization, volumes, specific surface, connected surfaces, number of connections, deformation and inertia tensor. From those data, we calculated several microscopic parameters (Table 1) as well as the pore-size distribution with radius calculated from the assumption that pores were elliptic cylinders (Beckers et al., 2014a). After morphological processing in Avizo, we imported the binary images in ImageJ (Schneider et al., 2012) where the BoneJ plugin (Doube et al., 2010) functionalities were used; all the measurements into ImageJ were performed in 3D. The skeletonisation tool was used to find the pore's centerline and extract a skeleton made of branches that are connected by junctions. It was achieved by external erosion with a 3D medial axis thinning algorithm. All the calculated microscopic parameters presented in Table 1 are commonly used in studies regarding the use of X-ray in soil science. We calculated the large porosity (Large_PO) in order to be comparable to the results discussed in the introduction of this paper where the voxel size was ~ 10 times larger.

3D Visualization

In order to obtain clear 3D representations, all 24 soil X-ray μ CT images were subjected to the following process: any pore that was not part of the largest connected component was removed using the MorphoLib plugin (Legland et al., 2016) in ImageJ (Schneider et al., 2012), a cylindrical region of interest of 295 pixels in radius was then used to remove the edge effects caused by sampling with the initial height going unchanged. Visualization was performed

using the 3DViewer plugin (Schmid et al., 2010) in ImageJ (Schneider et al., 2012).

Results Analysis

Basic descriptive statistics were performed on the macroscopic and microscopic data. The correlation coefficients (ρ) between the different microscopic parameters were then calculated using Bayesian statistics (see next section) to account for data uncertainty. Then, Bayesian correlation coefficients were calculated between relevant microscopic and macroscopic measurements as well as Bayesian linear regression models. Before implementation, the data were randomly split into calibration (18 soil samples) and validation (6 soil samples) sets. To that purpose, a number was assigned to each of the 24 soil samples and six numbers were randomly picked. Therefore, the soil samples have a sequential numbering. The calibration set includes samples from #1 to #18 and the validation set from #19 to #24.

Bayesian Statistics for Correlation and Linear Regression

When a linear relationship was visually assumed between two variables, the correlation coefficient between those two variables was calculated using Bayesian statistics. In Bayesian statistics a probability is assigned to a model [P(observations|model)] rather than to an observation, as in frequentist statistics. From the observations, the models (the prior) are updated to posterior distributions [P(model|observations)] and the uncertainty of the statistic description is expressed in a probabilistic way through the posterior distributions parameters. We refer to Marin and Robert (2007) for more information about Bayesian statistics. In this study, we used the package "BayesMed" (Nuijten et al., 2015) in R (R Core Team, 2015), which computes a Bayesian correlation test, the null hypothesis (H_0) being that the correlation coefficient is null. The correlation test is based on a linear regression between two variables with a Jeffreys-Zellner-Siow (JZS) prior as a mixture of g-priors (Liang et al., 2008; Wetzels and Wagenmakers, 2012). The correlation coefficient is extracted from the posterior variance matrix. We computed the test without expectation about the direction of the correlation effect (Wagenmakers et al., 2016). The credibility of the test is assumed by comparing the marginal likelihoods of the regression model to the same regression model without the explaining variable (Bayes Factor, BF), which quantify the evidence for one or the other hypothesis. Another advantage of using the Bayesian approach is the possibility of quantifying the evidence for the null hypothesis (Wetzels and Wagenmakers, 2012). Non-significant tests in frequentist statistics are interpreted in favor of the null hypothesis although the result could be induced by a noisy data set. Therefore, because the posterior distributions are updated from the observations, the conclusion of the test will not depend on the number of observations and it is possible to recalculate BF as the observations are logged-in and stop the collect when the evidence is compelling. Adapted from Jeffreys (1961) in Wetzels and Wagenmakers (2012), BF's larger than 100 were interpreted as decisive evidence for H1: BF's between 30 and 100 as a very strong evidence for H₁, BF's between 10 and 30 as a strong TABLE 1 | Calculated microscopic parameters on the X-ray µCT images and their definition.

	Microscopic parameter (abbreviation, metric)	Definition				
Avizo	Porosity (µCT_PO, %)	Ratio of pore voxels over the total amount of voxels				
	Large porosity (Macro_PO,%)	Part of the porosity composed by pores of at least 1,000 voxels				
	Number of pores (NP, -)	Total number of pores				
	Averaged pore volume (Avg_vol, mm ³)	Ratio of the total volume of pores over the number of pores				
	Averaged pore volume of the biggest pores (Avg_Bvol, mm ³)	The biggest pores are the ones that account for 90% of the pores volumes by only representing 10% of the number of pores				
	Averaged pore volume of the smallest pores (Avg_Svol, mm ³)	The smallest pores are the ones that account for 10% of the pores volumes by representing 90% of the number of pores				
	Proportion of isolated pores (IP, %)	Ratio of the number of pores that have no connection over the total number of pores				
	Proportion of isolated porosity (IPO, %)	Ratio of the isolated porosity over the total porosity				
	Averaged coordination number(Avg_Z, -)	The average of Z, which is the number of connections at one point (Perret et al., 1999), of the connected pores				
	Averaged surface connectivity (SC, L^{-1})	The average of sc which is sc = Nc * Ac / Vp, where Nc is the number of connections, Ac the mean surface area of the connections (L ²) and Vp the pore volume (L ³)				
	Total surface connected (Con_surf, mm ²)	The sum of each pore's connected surface				
	Specific surface (SS, m^{-1})	Sum of the specific surface of each pore which is the ratio of the pore surface area over its volume				
Av. + IJ	Global connectivity (Γ, -)	The sum of each pore's volume squared divided by the total volume of pores. It measures the probabilit that two pores voxel are part of the same pore (Renard and Allard, 2013).				
Image J	Total length of the pore network (L, m)	After skeletonization, it is the sum of all the branches length				
	Total nomber of branches (B, –)	After skeletonization				
	Total number of junctions (J, –)	After skeletonization				
	Degree of connectivity (B/J, -)	Ratio of the number of branches over the number of junctions. As negative is the ratio, as connected should be the medium				
	Global tortuosity (r , m ⁻¹)	The geometric tortuosity between two points is the ratio between the effective pore path and the shortest distance between the two extreme points (Perret et al., 1999). We calculated the global tortuosity (τ) of the pore network as the average of the tortuosity of each branch				
	Fractal dimension (FD, –)	FD was calculated with a box-counting algorithm (Perret et al., 2003)				
	Degree of anisotropy (DA, –)	The value of DA is between 0 and 1, 0 for an isotropic medium. DA was calculated with the mean intercept length method (Harrigan and Mann, 1984)				
	Euler number (ɛ, –)	The Euler number is a quantification of the connectivity. Originally calculated as ϵ =N-L+O, where N is the number of isolated objects; L is the number of redundant connections and O the number of cavities or holes (Vogel et al., 2010). As negative is the Euler number, as connected is the medium				
	Lowest Euler number (Min_ɛ, –)	The Euler number of the largest connected component of the pore network				

evidence for H_1 , BF's between 3 and 10 as a substantial evidence for H_1 and BF's below 3 as an anecdotal evidence for H_1 . The values of BF's that were inferior to one (1/100; 1/30; 1/10; 1/3) were interpreted in the same way as the BF values superior to one, the evidence going for H_0 .

We also established a Bayesian linear regression design to extract relationships between micro- and macroscopic measurements. All combinations between Y and $X_1 + X_2$ were tested and regression models were compared against the same models without the explaining variable (BF). The variables priors were JZS prior as a mixture of g-priors (Liang et al., 2008). We used the "BayesFactor" package (Morey and Rouder, 2015) in R (R Core Team, 2015), the autocorrelation and the convergence were verified. In Bayesian statistics, the starting point is not to identify the best regression equation but rather evaluate the unknown values of the equation explaining variables and intercept. We did it through the quantification of the 2.5 and 97.5% quantiles. The regression equations are reported in the Supplementary Materials section. Afterwards, we aimed at predicting the validation data points through the use of the slopes and intercepts posterior mean. The relative root mean square errors (RRMSE) were calculated as follows:

$$RRMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} \left(\frac{d_i - D_i}{D_i}\right)^2}$$
(1)

Where *n* is the number of data points, d_i is the predicted data point and D_i the observed data point.

RESULTS AND DISCUSSIONS

Macroscopic Measurements

The agricultural soil we studied showed large variations between samples with porosity values ranging from 43.09 to 57.70% and density from 1.12 to 1.51 g/cm^3 . **Table 2** presents the maximum, minimum, and average values as well as the associated standard deviations of the logarithmic saturated hydraulic conductivities

TABLE 2 | Logarithmic saturated hydraulic conductivities (Ks, cm/day) and air permeability (ka, μ m²) measured after applying a draining pressure of -4, -7, -10, -30, and -70 kPa for the calibration and validation data sets [minimum values (Min), maximum values (Max), mean values (Mean), and standard deviation (St dev)].

	[cm/d]			log [µm²]		
	log(Ks)	ka(–4 kPa)	ka(–7 kPa)	ka(–10 kPa)	ka(- 30 kPa)	ka(–70 kPa)
CALIB	RATION	DATA SET				
Max	1.591	2.920	3.076	2.992	3.235	3.231
Min	0.443	0.059	0.017	0.095	0.418	0.936
Mean	1.015	1.681	1.735	1.916	2.164	2.318
St error	0.149	0.505	0.478	0.478	0.603	0.400
VALID	ATION D	ATA SET				
Max	1.709	1.773	2.532	2.718	2.837	3.217
Min	0.352	0.395	-0.051	0.581	1.077	0.402
Mean	1.149	1.132	1.018	1.601	1.852	1.885
St error	0.400	0.801	1.028	1.013	0.893	0.891
ALL D	ATA					
Max	1.709	2.920	3.076	2.992	3.235	3.231
Min	0.352	0.059	-0.051	0.095	0.418	0.402
Mean	1.049	1.584	1.572	1.853	2.086	2.220
St error	0.147	0.443	0.445	0.424	0.496	0.376

[Ks (cm/day)] and air permeabilitys [ka (μ m²)]. As expected, the range of Ks and ka values is large due to the singular nature of pore network organization and the resulting transfer properties. For all studied soil samples, we observed a power-law type relationship between ka and the associated air-filled porosity measured from the SWRC (e.g., Ball and Schjønning, 2002). There was, however, no linear relationship between log(Ks) and log(ka) as opposed to what has been shown in other studies (e.g., Loll et al., 1999; Mossadeghi-Björklund et al., 2016). Those transport properties, as well as the water content at various matric potentials, were compared to the microscopic measurements made on the X-ray images.

X-ray µCT Images Analysis

The segmentation step, within the image processing scheme, has a great impact on the visible porosity calculated on the X-ray µCT image and on the extracted microscopic measurements (Lamandé et al., 2013; Smet et al., 2017). We, therefore, visually verified the accuracy of the global segmentation on each of the 24 X-ray µCT images by superimposing the grayscale images on the binary images. It appears that the porosity-based global segmentation method did not provide satisfactory results for two soil X-ray µCT images (#6 from the calibration set and #20 from the validation set). Those samples had a large air-filled porosity at h = -1 kPa (Lab_PO); the porosity-based segmentation method increased the threshold (increased µCT PO) in order to obtain a µCT_PO as close as possible to Lab_PO [resulting threshold of 94 (0-255)]. In addition, the algorithm did not converge for one soil sample (#2), which had a large Lab_PO. Otsu's method was, therefore, applied to those three samples and the global threshold values for samples #2, #6, and #20 were 67, 69, and 69 (0-255), respectively. The threshold values comparisons obtained with the porosity-based method for the other samples supported this processing choice; the averaged threshold value was $63 (\pm 0.75)$. Finally, the samples #10, #13, #16 and #17 were segmented using the Otsu's method because their soil water retention curves (SWRC) were not measured. **Figure 1** presents a 3D visualization of each soil sample (calibration and validation sets) followed by a 2D vertical slice from the middle of the soil sample. We will refer to this figure within the Results section.

Microscopic Measurements

Table 3 presents the data ranges, averages and associated standard deviations for all the previously introduced microscopic measurements made on the X-ray μ CT soil images (Table 1). The calculated µCT porosities, taking into account pores of at least five voxels, were only slightly higher than those calculated taking into account pores of at least 1,000 voxels. The differences represented \pm 90% of the number of pores (the pores having a volume between five and 1,000 voxels happened to be the "small pores" as defined in Table 1). There was no surprise that we observed longer pore networks (L), higher numbers of pore branches (B) and junctions (J) than Katuwal et al. (2015b) or Garbout et al. (2013) who both worked with larger voxel sizes. Consequently to the high number of pores (NP), the observed Euler numbers (ε) were frequently highly positive and the differences between the percentage of isolated pore (IP) and isolated porosity (IPO) was large. Comparisons to others studies are however tricky because the pore network skeleton is highly sensitive to the scanning equipment and procedure, the image processing, the skeletonisation process and the pore identification.

Table 4 provides the credible (BF > 3) Bayesian correlation coefficients between each of the microscopic measurements. The coefficients were initially calculated for the calibration data and then the validation data were included. In Bayesian statistics, the number of observations does not count for the credibility of a hypothesis, so when a BF was improved with the addition of the validation data, it meant that the correlation was more credible thanks to the observation *values*. The BF were highlighted with colors according to the classes described in the Materials and Methods section. We did not compute the Bayesian regression equations between microscopic measurements since it was not in the scope of this paper. We did not observe any substantial evidence for the null hypothesis between any of the microscopic measurements.

As Perret et al. (1999) observed, μ CT_PO and NP were not correlated; NP cannot be a measure of porosity, but rather expresses a notion of pore density and distribution through the soil sample. The positive correlation between μ CT_PO and the fractal dimension (FD) has often been observed in the literature (Rachman et al., 2005; Larsbo et al., 2014) and its dependence on μ CT_PO is actually the main drawback of being used as an indicator of pore network heterogeneity and complexity. FD was also correlated to the specific surface area (SS), L, B, J, and NP, which is consistent with studies from Kravchenko et al. (2011)



and Anderson (2014). Those five parameters were all highly correlated to each other but selecting one to represent the other could distort the analysis.

The correlation between μ CT_PO and average pore volumes (Avg_vol, Avg_Bvol, and Avg_Svol) also made sense since the average pore volumes were not negatively correlated to NP. The average pore volumes were all slightly correlated to Avg_Z; we observed that larger pores tended to be more connected; Avg_Z and Large_PO were also correlated. This is consistent with the results from Luo et al. (2010); Larsbo et al. (2014); Katuwal et al. (2015a,b). Regarding the other connectivity indicators [degree of connectivity (B/J), the Euler number $[\varepsilon]$, and the average surface connectivity (SC)], we observed that AvgZ was correlated to B/J but not to ε or to SC while B/I was correlated to ε and not to SC, and SC was correlated to ε . Those connectivity indicators did not carry the exact same information and should, therefore, be used for their potential explanatory power, as pointed out by Renard and Allard (2013) and Katuwal et al. (2015a), Jarvis et al. (2017), and Sandin et al. (2017) have focused on connectivity indicators based on the percolation theory, and they found that four indicators of connectivity were interchangeable and dependent on soil porosity. We calculated the global connectivity (Γ) indicator from the pore size distribution extracted from Avizo and, from the cluster distribution extracted from BoneJ to be comparable to Jarvis et al. (2017) and Sandin et al. (2017). We observed drastically different Γ values from the two methods of computation. As Houston et al. (2017) assessed it, the software, and the decomposition method that goes with it, influence the final pore size distribution. The very low values of Γ from Avizo came from the decomposition of the pore space into a large amount of connected (or not) pores and the resulting smaller (by two orders of magnitude) largest component than the one identified in BoneJ, where cluster of connected pores are quantified. In the following, to be comparable to Sandin et al. (2017), we used the Γ value computed from the BoneJ's cluster size distribution.

Relationships Between the Microscopic and Macroscopic Measurements Measured, Calculated, and Predicted Soil Water Retention Curves

In the following section, samples #10, #13, #16, and #17 were not included because SWRC were not measured; the calibration data set included 14 samples instead of 18.

Air-filled porosity at h = -1 kPa

In the calibration data set, the relationship between μ CT_PO and Lab_PO was neither linear nor credible because of three outliers (#1, #2, #7, **Figure 2**). As discussed above, samples #2 and #7 were segmented with Otsu's method. In the case of sample #7, Lab_PO was too large for the porosity-based method, introducing unrealistic porosity that would explain the deviations. Lab_PO was calculated by weighing the soil samples after draining. If the pore surfaces were rough or loose, water films could have covered up the pores surface by adsorption and pores could appear smaller than they are. Difference between adsorption and desorption curves, also known as the hysteresis effect, can indeed be substantial close to saturation (McKenzie et al., 2002). A physical explanation for sample #1 could be that it had large pores which drained just before being weighed at TABLE 3 | Microscopic measurements on μ CT X-ray images for the calibration and validation data set [minimum values (Min), maximum values (Max), mean values (Mean), and standard deviation (St dev)].

Microscopic measurements		Calibratio	n data set	Validation data set				
	Min	Max	Mean	St dev	Min	Max	Mean	St dev
μCT_PO [%]	3.71	14.23	7.66	2.69	2.76	12.77	8.55	4.06
Macro_PO [%]	2.87	13.22	6.69	2.68	1.97	11.86	7.54	3.93
NP [-]	31,770	79,749	46,649	12,957	32,197	66,192	44,478	12,346
Avg_vol [mm ³]	0.0260	0.1110	0.0567	0.0223	0.0260	0.1010	0.0620	0.0294
Avg_Bvol [mm ³]	0.1350	1.3450	0.5958	0.3656	0.1210	2.0190	0.7795	0.7191
Avg_Svol [mm ³]	3.000E-03	1.200E-02	6.278E-03	2.372E-03	3.000E-03	1.100E-02	7.000E-03	3.162E-03
IP [%]	66.29	87.32	76.58	5.97	64.28	83.76	75.51	7.31
IPO [%]	3.10	12.76	8.44	2.62	4.16	12.88	7.93	3.02
Avg_Z [–]	3.07	5.40	4.29	0.83	3.58	5.24	4.36	0.59
SC [voxel-1]	0.206	0.304	0.250	0.029	0.209	0.315	0.258	0.036
Con_surf [mm ²]	2553	7921	4722	1321	2696	5984	4703	1282
SS [m ⁻¹]	2.040E-03	5.078E-03	2.991E-03	8.484E-04	2.027E-03	4.008E-03	2.843E-03	7.034E-04
Г [–] / Avizo	9.200E-04	4.817E-02	5.152E-03	1.080E-02	1.400E-03	4.100E-02	1.307E-02	1.601E-02
Г [–] / BoneJ	0.8613	0.5356	0.7386	0.0820	0.8286	0.6724	0.7365	0.0649
L [m]	28.22	71.58	43.83	10.95	30.97	57.57	43.63	12.17
B[-]	77,776	22,3143	126,510	36,757	81,850	158,219	124,115	30,407
J [–]	28,480	94,542	51,812	16,524	32,605	65,150	51,595	13,053
B/J [-]	2.230	2.930	2.529	0.183	2.280	2.740	2.443	0.166
Tortuosity [mm ⁻¹]	1.240	1.280	1.257	0.014	1.240	1.276	1.258	0.013
FD [-]	2.405	2.642	2.527	0.072	2.313	2.653	2.507	0.118
DA [-]	0.112	0.384	0.206	0.080	0.104	0.352	0.252	0.092
ε [-]	-14,125	27,434	8,761	10,969	-9,897	30,112	6,534	13,836
Min_ε [-]	-39,624	-7,196	-20,034	9,141	-2,7461	-9,747	-19,667	6410

The abbreviations of the microscopic measurements are listed in Table 1.

saturation. Therefore, the volume of water used to calculate the total laboratory porosity could have been under-evaluated. This is most likely since one gram of water can change the Lab_PO from 8.02 to 14.21%. The 3D visualization of sample #1 shows that a large part of its porosity was connected from top to bottom (**Figure 1**). The validation data were in agreement with the calibration data except for sample #20, which was segmented with Otsu for the same reasons as sample #7, and sample #22, which showed a behavior similar to sample #1.

Eventually, the samples that were segmented with the porosity-based method displayed similar Lab_PO and µCT_PO values. Lab_PO was used as a target during the segmentation process. Elliot et al. (2010) also found congruent air-filled porosity values measured by X-ray μ CT (voxel size of $45^3 \mu$ m³) and by weight determination. The slope of the relationship between Lab_PO and µCT_PO was higher than one and Lab_PO was indeed positively correlated to the difference between Lab_PO and µCT_PO. The applied capillary theory to calculate Lab_PO and μ CT_PO simplifies the pore network to capillaries. We, therefore, suggest that the difference between Lab_PO and µCT_PO reflected the systematic error produced by considering pores as capillaries, and increasing the volume of data to which the theory was applied (PO) had increased the error (the difference). The difference between Lab_PO and μ CT_PO, whether in absolute value or not, could, however, not be correlated to any microscopic measurements. We presumed that the pore network real connectivity would explain the imperfect applicability of the capillary law. For example, Parvin et al. (2017) reported that the percentage of isolated pores explained the difference in volumetric water content (between laboratory evaporation measurements and X-ray μ CT calculation) at a water matric potential ranging from -0.35 to -0.4 kPa by only considering pores larger than 350 μ m (pores that should drain at a matric potential of -0.42 kPa from capillary law). The isolated pores were actually connected to others by throats smaller than the voxel size and may not have drained at the required potential calculated from capillary law.

From discrete to continuous data

Beckers et al. (2014a) and Parvin et al. (2017) applied nearly the same methodology to compare predicted SWRC with the bimodal version (Durner, 1994) of the van Genuchten (1980) model. On one hand, they only used macroscopic input data [from pressure plates weighting procedure for Beckers et al. (2014a) and from the evaporation method for Parvin et al. (2017)], and on the other hand, they used those macroscopic data in combination with microscopic data (pore-size distribution extracted from X-ray μ CT images) as input. They both found that using the X-ray μ CT data allows a better prediction of SWRC close to saturation in terms of RRMSE. We noted, however,



₃_niM		-0.70 -0.74	-0.83	-0.84 -0.86	0.63	0.60 —.49			
3					0.64	84			
AQ									
ED		0.72 0.75	0.57 <mark>0.58</mark>	0.53					
1					-0.52				
1					0				
B\1			-0.51	-0.60 -0.49					
r		0.95 0.93	0.95 0.99						< 10.
8		0.95 (0.94 (13 < BF
		0.							ind greer
L/BoneJ									F < 30 a
osivA\ T									v 10 < B
SS									00, yellov
juns_no⊃									 BF < 10
SC									nge 30 <
Z_gvA									100, ora
Ю									ed BF >
Ы									ble 1 . P
lov2_pvA									sted in Ta
lov8_pvA									nts are lis
Ιον_βνΑ									asuremer
Nb Farge_PO									opic me
	a a	a a	a a	g r	m g	g "	p r	g "	a microsc
	Cal. data All data	Cal. data All data	Cal. data All data	Cal. data All data	Cal. data All data	Cal. data All data	Cal. data All data	Cal. data All data	Cal. data All data tions of the n
	Γ/BoneJ		m	- -	B/J	£	FD	DA	 Cal. data All data The abbreviations of the microscopic measurements are listed in Table 1. Red BF > 100, orange 30 < BF < 100, yellow 10 < BF < 30 and green 3 < BF < 10.

TABLE 4 | Continued



FIGURE 2 | Air-filled porosity measured in the laboratory at a water matric potential of -1 kPa (Lab_PO) vs. the visible porosity measured on X-ray images (μ CT_PO) for the calibration data set (black circles) and the validation data set (white circles).

that those studies used macroscopic data from one set of soil samples and microscopic data from another set of soil samples. We aimed at validating the results by using the same samples for both types of measurements. To that purpose, capillary theory was applied to the pore-size distribution extracted from the Xray µCT images and the calculated SWRC were adjusted to the total laboratory porosity. Figure 3 illustrates the SWRC for three samples and shows that for all samples, except #1, the volumetric water content (θ) close to saturation was higher when predicted with the combination of X-ray µCT data and pressure plates data (µCT+PP) than with only the pressure plates data (PP), confirming previous results from Beckers et al. (2014a) to Parvin et al. (2017). We also observed that according to the RRMSE values, prediction with μ CT+PP data were better than with only the PP data (Table 5), except for sample #1. Lamandé et al. (2013) also found that X-ray μ CT measurements (voxel size of $600^3 \ \mu m^3$) allowed a more complete description of the pore space than classical laboratory measurements, and Rab et al. (2014) have concluded that X-ray µCT was likely a better method than laboratory SWRC measurements for determining air-filled macroporosity (pores larger than 300 µm in diameter). The poor performance from sample #1 came from the fact that Lab_PO was lower than μ CT_PO, as discussed in Figure 2. Apart from sample #1, the use of microscopic information undeniably improved the prediction of continuous SWRC with the bimodal version (Durner, 1994) of the van Genuchten model (1980).

Altogether

The determination of SWRC through pressure plate measurements are likely more representative of the *in-situ* soil hydrodynamic, but those are not free of artifacts; for



FIGURE 3 | Measured and predicted soil-water retention curves for three samples. Unlike the samples, the SWRC for #1 predicted with the pressure plates data alone (plain line, Pred_PP_DP) performed better than with X-ray μ CT data (dotted line, Pred_PP+ μ CT_DP). Black circles represent the X-ray μ CT data and white circles the pressure plate measurements.

example, air entrapment might result in incomplete saturation leading to inaccurate estimation of the air-filled macroporosity. And, although the connectivity of the pore network was not taken into account with the X-ray μ CT SWRC calculation, we still observed that the combination of laboratory measurements and X-ray μ CT data improved the SRWC prediction close to saturation. The accurate characterization of the air-filled macroporosity is important for the study of microorganism development (e.g., soil fungal growth in Falconer et al., 2012).

Saturated Hydraulic Conductivity and Soil Porous Structure

The saturated hydraulic conductivity was positively correlated to the global connectivity indicator (Γ) computed from the

TABLE 5 | Relative root mean squared error (RRMSE, %) for the predicted soil water retention curves with the pressure plates data (PP) or the μ CT data plus the pressure plates data (μ CT + PP) for the calibration data set samples.

Sample	RR	MSE
	PP	μCT+PP
#1	3.445	0.0538
#2	1.816	0.0157
#3	2.867	0.0201
#4	3.617	0.0254
#5	3.711	0.0300
#6	2.311	0.0165
#7	1.727	0.0134
#8	2.906	0.0216
#9	6.526	0.0474
#11	2.427	0.0232
#12	6.135	0.0556
#14	2.734	0.0223
#15	3.840	0.0275
#18	4.781	0.0385

BoneJ cluster size distribution (**Figure 4A**, $\rho = 0.593$, BF = 9.5) as observed in Sandin et al. (2017), unlike that study, we did not observe a credible correlation, but a positive trend between μ CT_PO and Γ /BoneJ. It is worth noticing again that Sandin et al. (2017) worked with a resolution close to our but with a different textural soil. Pöhlitz et al. (2018) also reported similar trend of Ks and connectivity values (and µCT_PO) between cultural practices. They worked with a voxel size of $60^3 \mu m^3$ on different samples for the Ks and microscopic measurements, with although a large number of repetitions. Figure 4A shows the observations of the calibration data (black circles), the observations of the validation data (white circles), the predicted validation points with the 50% quantiles of the regression model (crosses) and the 25 and 75% quantiles of the regression models (dotted lines). The 50% quantiles of the regression models provided a RRMSE of 0.492 for the validation data and the predicted data points were, in most cases, underestimated. The reported regression models that included two explaining variables reported light credible evidence in the cases where Γ was one of the explaining variables. We did not observe relationships between µCT_PO and log(Ks), despite what the literature reported (Kim et al., 2010; Luo et al., 2010; Mossadeghi-Björklund et al., 2016; Naveed et al., 2016). The measured Ks from those studies were, however, higher by several orders of magnitude. We did observe a positive correlation between log(Ks) and FD when the calibration samples were visually separated in two groups according to their Ks value (Figure 4B, black circles). Samples #1, #2, #3, #4, #7, #11, #12, #14, #15, #16, #18 were part of group 1 and samples #5, #6, #8, #9, #10, #13, #17 were part of group 2. No microscopic measurements explained that separation and it was difficult to visually distinguish a pore distribution trend within the pore space (Figure 1). We noticed that some of the less conductive samples presented one or two large macropores (not necessarily vertically oriented



connectivity calculated from the pore size distribution extracted from BoneJ, (B) the fractal dimension measured on X-ray μ CT images, and (C) the soil degree of anisotropy measured on X-ray μ CT images. Black and white circles represent the observations from the calibration and validation data sets, respectively. Crosses represent predicted validation data points and dotted lines represent the 25 and 75% regression model quantiles.

nor connected from top to bottom) while some of the more conductive samples had more dispersed pore networks, and we observed a negative trend (not credible) between FD and the degree of anisotropy (DA) for group 2, but not for group 1. This suggested that the porosity arrangement led to the composition of two groups for the relationship between FD and log(Ks). By using the Ks value as a boundary, the validation data were assigned to a group (**Figure 4B**, white circles). FD measures the ability of the studied object to fill the Euclidian space within which it is integrated and, the larger the FD, the closer to a real fractal the object gets, meaning that its shape is similar at different scales. Although Pachepsky et al. (2000) reported that soils are far from being real fractal, Perret et al. (2003) and Kravchenko et al. (2011) pointed out that FD can be used as a global measure of the pore network complexity. For example, FD was found to vary with depth or soil treatment (Rachman et al., 2005; Udawatta and Anderson, 2008; Kim et al., 2010). Anderson (2014) also observed a positive correlation between log(Ks) and FD. By applying the regression equations, log(Ks) of group 1 equal to log(Ks) of group 2, when FD = 3.03, which was close to the upper limit of the possible FD values of a 3D object. At FD = 3, the object (the porosity) occupies each point of 3D Euclidian space, but that also meant that log(Ks) was limited to 128 cm/day. It is reasonable to ask if more groups would be created with increasing conductivity and if the slopes of the relationships would decrease, or if the solutions of the regression equations would be identical when the fractal dimension equals three, which is the fractal dimension upper limit for an Euclidian 3D object. The global RRMSE was 0.260, which is a rather good performance (Figure 4B, crosses). The 25 and 75% regression model quantiles were highly dispersed (Figure 4B, dotted lines) inducing uncertainty about the regression model.

Anisotropy has been shown to impact soil conductivity (Ursino et al., 2000; Raats et al., 2004; Zhang, 2014). Figure 4C plots log(Ks) as a function of DA (black circles for the observations of the calibration data) and by removing two outliers from the calibration data set (#9 and #10), we obtained a correlation coefficient of 0.74 (BF = 125.3), which presents a convincing link that has, to our knowledge, not been seen before. Such a positive correlation could be interpreted as a consequence of preferential flow through large macropores. For example, Dal Ferro et al. (2013) have found that anisotropy was scale-dependent by showing higher average DA in soil cores (DA of 0.32 and voxel size of $40\,\mu$ m) than in soil aggregates (DA of 0.14 and voxel size of 6.25 µm), they hypothesized that as a possible consequence of biological and mechanical macropores. This was later confirmed by a second study where they showed that only the macropores in the range of 250-500 µm were correlated to the global DA (Dal Ferro et al., 2014). From the DA calculation decomposition (in the Supplementary Materials section), it was possible, but not straightforwardly, to evaluate the main direction of the anisotropy which could be represented by a small amount of pores in that direction, or as the direction of the preferential orientation of one large pore. Ks was measured along the z-axis (vertically) but the main direction of anisotropy was not systematically in that direction. Therefore, the positive correlation between DA and log(Ks) was not necessarily a result of preferential pore networks paths. Moreover, the directions of the pore connections showed that a majority of the pores junction were horizontal (x- and y-axis). The repartition was practically the same between samples, 60% horizontal and 40% vertical connections. Applying the regression model to the validation data gave consistent results for four samples with a RRMSE for those of 0.414 (Figure 4C, crosses). Sample #21 gave poor results with a predicted log(Ks) of 1.03 cm/day instead of an observed log(Ks) of 0.35 cm/day and a resulting RSE of 3.742. As well, sample #22 gave a RSE of 0.433, its low DA and large log(Ks) made it similar to the two outliers of the calibration data (#9 and #10). The relationship between DA and log(Ks) may not be suitable for highly conductive soil sample presenting isotropic-like porosity distribution (Samples #9, #10, #22, **Figure 1**). Subjective comparisons between 3D representations and DA need to be made cautiously. We observed that, compared to samples #9, #10, #22, samples #15 and #18 had similar visually homogenous porosity (and equivalent low DA) but with a lower Ks. Samples from group 2 in **Figure 4** (#5, #6, #8, #13, #17 and #20, #23, #24) had higher log(Ks) with a more heterogeneous porosity (and higher DA). The narrower distribution of the 25 and 75% regression model quantiles came from the exclusion of two outliers in the model computation.

The prediction of the hydraulic conductivity curve is frequently extracted from the SWRC shape and absolute values of K(h) can be obtained by matching both curves with a specific point, which is often Ks (Vogel and Roth, 1998). Ks is however cumbersome and time-consuming to measure *insitu*. We reported here that the porosity arrangement described by the global connectivity, the fractal dimension, and degree of anisotropy had an impact on the soil conductivity, the combination of those indicators provided information that could be used across scales and to eventually better estimate Ks. No other relationships between log(Ks) or Ks and the other microscopic measurements were reported.

Air Permeability Variations Explained by Microscopic Structure

Macroscopic measurements showed, as expected, that the air permeability increased with air-filled porosity. We also observed positive credible Bayesian correlation coefficients between log(ka) measured at various h and microscopic indicators of the porosity (µCT_PO, Large_PO, Avg_vol, Avg_Bvol, and Avg_Svol), although only log(ka,-70 kPa) was positively correlated to μ CT_PO (**Table 6**). Given the X-ray μ CT image resolution, µCT_PO should be representative of the air-filled PO measured at h = -1 kPa although the soil samples were scanned at h = -70 kPa. The choice to scan soil samples at h = -70 kPa was a compromise between the fact that all the potential visible porosity should be air-filled and without cracks due to drying, and this particular correlation suggests that all the potential visible porosity was indeed air-filled. In their study, Katuwal et al. (2015b.) and Naveed et al. (2016) both observed a power-law function between, respectively, ka(-2 kPa) or ka(-3 kPa)kPa) and μ CT_PO. The μ CT_PO calculated on their images is equivalent to the Large_PO on our images as previously stated, and we also reported a correlation between Large_PO and log(ka) (Table 6). Therefore, the difference between μ CT_PO and Large_PO might be the part of the PO that should have drained at low negative potential (from the capillary law), but was actually drained at higher negative potential (due to unusable pathways). We refer to Hunt et al. (2013) to name that part of porosity, the inaccessible porosity. This assumption was confirmed by the credible correlations between the inaccessible PO and microscopic parameters which expresses a notion of pore network complexity (B, J, L, NP, SS, IPO, FD). We previously pointed out the drawback that, when calculating SWRC from the X-ray μ CT data (namely from the visual pore size distribution), the connectivity was not taken into account. We here confirmed that the pore network connectivity play a role in the desorption process.

Lamandé et al. (2013) found a positive correlation between log(ka,-10 kPa) and NP. We observed negatives correlations (as well as with B, J, and SS). Many pores of our samples were connected to others with connections smaller than the voxel size and were considered isolated (high IP and ε , Table 3). It would make sense, that an increasing volume of small (invisible) connections reduces the airflow through the pore network. The air permeability is also largely dependent on the tortuosity and connectivity of the pore network (Ball and Schjønning, 2002; Moldrup et al., 2003), but to our knowledge, no study has reported these links from μ CT measurements. From Table 6, it appears that the air permeability increased with a growing average number of connections (Avg_Z) as well with a growing global connectivity (Γ /BoneJ), but also with Min ε and B/J. The last two parameters indicate a decreasing connectivity with an increasing value. First, from Table 4, it was observed that B/J increased with decreasing B or decreasing J. That purely algebraic relationship might explain why the air permeability would decrease with decreasing B/J (increasing connectivity). Then, Min ε was calculated over the largest connected pore component, and, because there are no cavities in real soil pore space (Vogel and Roth, 1998), Min_ε decreased as the number of redundant connections increased. When calculating Avg_Z by class of pore according to their volumes, it appeared that the values of Avg_Z we observed came from a large number of small pores having few connections; the biggest pores had ten times

TABLE 6 | Credible Bayesian correlation coefficients between microscopic measurements and logarithmic air permeability (ka) measured at water matric potentials of -70, -30, -10, and -7 kPa for the calibration data set.

	log						
	ka (–7 kPa)	ka (–10 kPa)	ka (–30 kPa)	ka (–70 kPa)			
μCT_ΡΟ				0.53			
Large_PO	0.54	0.60		0.64			
Avg_Vol	0.72	0.76	0.72	0.79			
Avg_Svol	0.75	0.85	0.75	0.84			
Avg_Bvol	0.69	0.76	0.69	0.77			
NP		-0.70	-0.76				
Avg_Z	0.55	0.78	0.85	0.69			
SS	-0.64	-0.73	-0.80	-0.54			
IPO	-0.70	-0.76	-0.82	-0.62			
В	-0.56	-0.68	-0.72				
J	-0.52	-0.68	-0.71				
B/J		0.62	0.63				
Γ/BoneJ	0.54			0.54			
Min_ε		0.68	0.73				



more connections. Avg_Z was correlated to Avg_Z calculated on the pores having a radius between 250 and 375 μ m. Therefore, air permeability was correlated to the fact that "medium" size pores had more connections. Moreover, there was a negative trend between log(ka) and Avg_Z calculated on the largest pores which corroborated the positive correlation between ka and Min_ ϵ .

The best regression models calculated on the calibration data (Bayes factor) and applied on the validation data reported that the best explaining variable for all measures of log(ka) (RRMSE) was the average pore volume of the smallest pores (Avg_Svol). That parameter might be seen as a limiting factor, and this suggested that ka was more related to pore size distribution than porosity. **Figure 5A** displays log(ka, -70 kPa) as a function of Avg_Svol and the distribution of the 25 and 75% regression model quantiles are rather narrow. The RRMSE was 1.256 or 0.0649 when the two worst predicted validation data points were not taken into account. The RRMSE for log(ka, -30 kPa) and log(ka, -10 kPa) were around 0.800 with one bad validation data point, and the RRMSE for log(ka, -7 kPa) was very high (8.154) with three



FIGURE 5 | (A) Logarithmic air permeability measured at a water matric potential of -70 kPa (ka) vs. the average pore volume of the smallest pores (Avg_Svol). Black and white circles represent the observations from the calibration and validation data sets, respectively. Crosses represent the predicted validation data points and the dotted lines the 25 and 75% regression model quantiles. **(B)** The predicted logarithmic air permeability from the average pore volume of the smallest pores vs. the observed logarithmic air permeability. Error bars represent the 75% regression model quantiles.

badly predicted data points out of five. The combination of Avg_Svol and average pore volume of all pores (Avg_Vol) performed slightly better in some cases, and slightly worse in others. **Figure 5B** shows the predicted log(ka) from Avg_Svol vs. the observed log(ka) values. Although the RRMSE were acceptable, the regression model distributions (the error bars represent the 75% regression models quantiles) were high which induce large uncertainty. That combination of two explaining variables was, in all cases, the best regression model of two explaining variables. Other important explaining variables were the average coordination number (Avg_Z), the proportion of isolated porosity (IPO), the average pore volume of the biggest pores (Avg_Bvol) and the combination of μ CT_PO and Large_PO.

With soil air diffusivity, soil air permeability is one of the main processes governing the exchange of gases with the atmosphere, including therefore soil aeration. Through our experimentations, we aimed at unraveling the main physical drivers of air fluxes through the soil. We have previously observed that subdividing the pore volume averages into three categories (all of the pores, the biggest, and smallest) was not informative; in this study, we have shown the opposite. Avg_Svol was the average volume of the pores having a volume between 4×10^5 and $\pm 8 \times 10^7 \ \mu \text{m}^3$, in contrast to other cited studies; those pores were visible because of our high resolution (43 μ m). Eventually, we suggested that Avg_Svol worked as a limiting factor.

CONCLUSION

X-ray microtomography, among other visualization techniques, has brought new insight into the study and the understanding of soil function. The challenge, however, is the representativeness of the studied soil samples (Vogel et al., 2010) and, to that purpose, the analysis of the same soil samples at two scales has become more prevalent. The resulting next challenge is the resolution at which the soil samples should be studied. To our knowledge, very few studies dealt with equivalent voxel size ($43^3 \ \mu m^3$) and, we did not find any micro-macro correlations such as the ones we observed.

Starting with the comparison of the calculated visible porosity for all pores and for those of at least 1,000 voxels in volume, it appeared that the difference was rather small but positively correlated to indicators of the pore network complexity. The uncommon relationships we observed might be due to the higher resolution we worked with and the resulting finer details of the pore network structure. For example, the calculated fractal dimension and degree of anisotropy are both global indicators of the pore network complexity and both were positively correlated to the saturated hydraulic conductivity, although with some limitations. The global connectivity showed interesting results although highly dependent on the decomposition software used to extract the pore size distribution. Identifying the key parameters that convey the complexity of the pore network is a motivating goal to reach. Pore network modeling has already proven useful (e.g., Vogel and Roth, 1998, or more recently, Köhne et al., 2011), and those three indicators are values that could be used for the generation of a phenomenological model.

Furthermore, we have reported various positive correlations between the air permeability measured at several water matric potentials and microscopic measurements. The average volume of the smallest pores (as small as \pm 4 \times 10⁵ μ m³) showed the best link with air permeability. Due to our high resolution, we observed a higher number of pores than in other studies and consequently more isolated pores. The Euler number based on the connected space was expected to correlate well with air permeability, but this was not the case. Other measures that provide similar types of information (total pore length, total number of branches, and junctions) proved equally unsatisfactory. In fact, a pertinent link was the positive relationship between the average pore volume of the biggest pores and that of the smallest ones, suggesting dependence between pores of different volumes.

We also reported that the soil water retention curve was better predicted near saturation with the pore size distribution extracted from the X-ray µCT data. Indicators can be derived from the SWRC to characterize soil quality or extrapolate microorganism development (Rabot et al., 2018); its accurate description is therefore a prerequisite. The degree of saturation is also important in the modeling of microbial growth, the dissolution of O₂, the soil respiration, the NO and N₂O production. These processes are affected by the so-called water filled pore space, by soil oxygen content and by soil temperature, which all vary with the volumetric water content (Smith et al., 2003). Blagodatsky and Smith (2012) concluded that the microbial growth models (and we add to this statement: "among others") including "an explicit description of microbial growth, i.e., growth rate and efficiency, humidification ratios and their relationship with N availability, need to be coupled with well-developed soil transport models." The fluid transport predictions for a continuous range of water contents and from discrete measurements are possible through models that are, today, mostly not physically-based. From the pore space structures analyzed, we aimed at contributing to a better understanding of the potential influences of the pore network topology on the physical hydrodynamic properties of soil. Strong unequivocal conclusions could not be drawn because of the limited number of repetitions; image processing and analysis are time-consuming and will be increase with increasing resolution. The comparisons to others studies, as discussed multiple times, depends on many factors and we, therefore, strongly urge the open access to gray scale X-ray µCT images.

DATA AVAILABILITY

Grayscale images and soil physical properties data are available upon request (contact the corresponding author).

AUTHOR CONTRIBUTIONS

SS conceived and designed the research, acquired and analyzed the X-ray images, analyzed and interpreted the data, and wrote the manuscript. EB provided the general X-ray μ CT images processing scheme. EP implemented the 3D morphological quantification's code in Avizo. SS, EB, EP, AL, and AD edited the manuscript.

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fenvs. 2018.00020/full#supplementary-material

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Conflict of Interest Statement: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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