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Measurement, spatial distribution dynamics, and influencing factors of forest ecological product value realization efficiency in China

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With the intensification of global climate change and ecological issues, the efficiency of forest ecological product value realization (FEPVRE) has become crucial in driving the green economy transformation. This paper, based on the Super-SBM model, measures FEPVRE across 30 Chinese provinces from 2012 to 2022. It employs methods such as spatial kernel density estimation, Markov chain analysis, the Gini coefficient method, the gravity model, and Quadratic Assignment Procedure (QAP) to assess its spatial distribution and dynamics. Additionally, spatial econometric models are applied from the perspective of the digital economy to explore the driving mechanisms of digital technologies, industries, and the digital environment on FEPVRE. The findings show: (1) FEPVRE in China exhibits fluctuating trends, with a convergence pattern from east to west. (2) FEPVRE associations shift from the eastern to the central regions, with stronger associations in the southeast. (3) FEPVRE will continue differentiating into two levels, with type IV regions prone to "level-locking" and club convergence. (4) Uneven digital technology distribution worsens regional disparities, but digital industries and environments help narrow the gap. (5) Eastern and Northeastern regions have higher FEPVRE due to better digital infrastructure and policies, while Central and Western regions face challenges, resulting in negative spillovers. High-efficiency regions positively influence neighboring areas. To achieve a balanced and sustainable green economy, bridging the digital divide in underdeveloped regions and promoting digital industries is key. Improving digital infrastructure will enhance FEPVRE and support an inclusive green economy.

KEYWORDS

forest ecosystem product value (FEPV), regional disparities, super-SBM model, value realization, digital technology, digital organization, digital environment

1 Introduction

The increasing forest ecological product value realization efficiency (FEPVRE) has expanded the value of forest ecosystem products (FEPV) beyond traditional economic dimensions, incorporating ecological, social, and cultural aspects. Forest ecosystem products refer to benefits derived from forests, such as wood, non-timber products, climate regulation, and biodiversity, while ecological products include all ecosystem services, such as water purification and carbon sequestration, provided by various

ecosystems like forests and wetlands. This transformation is analyzed through ecological economics and sustainable development theories, emphasizing the importance of forest ecosystem services in promoting environmental sustainability and socio-economic development at regional and national scales (Rusanen et al., 2024). The "Opinions on High-Level Protection and Efficient Utilization of Natural Resources to Promote Ecological Product Value Realization," released in December 2024, highlights the need to leverage the market's role, promote resource rights marketization, and ensure reasonable returns from protecting green mountains and clear waters. The policy also explores establishing a system for balancing the natural coastline and enforcing strict ecological protection red lines. Under this policy, entities may transfer supplementary arable land indicators generated by converting non-arable land to arable land. Pilot projects will focus on converting construction land within ecological protection red lines into forest land, grassland, or wetlands, and reclaimed land may be proportionally converted into new urban construction land without expanding the development boundary. This underscores the importance of measuring FEPVRE, as it helps assess how forest ecosystem products contribute to economic, ecological, and social benefits, ensuring ecosystem protection is both sustainable and economically viable.

The policy promotes market mechanisms, such as ecological compensation and carbon markets, to enhance forest ecosystem protection. Ecological compensation incentivizes local governments and businesses to engage in restoration and sustainable land use, ensuring the value of ecosystem services is recognized and financially supported. Carbon markets link the economic value of forest ecosystem services to market incentives, promoting forest protection and restoration. Together, these instruments improve FEPVRE by providing financial support for sustainable forest management, valuing services like climate regulation and carbon sequestration, and promoting both economic viability and environmental sustainability. FEPVRE aligns with the policy's aim to realize ecological product value by quantifying forest ecosystem services. Furthermore, it enhances social welfare, promotes public health, and carries cultural value (Lee et al., 2022; Riedl et al., 2024). Despite growing recognition of the FEPV, research on FEPVRE largely focuses on its economic dimension, often overlooking its ecological, social, and cultural impacts. This study addresses this gap by exploring how digital technologies and market mechanisms can enhance FEPVRE measurement, ensuring all dimensions are considered. FEPVRE measures how effectively forest ecosystem products-such as material supply, regulatory services, and cultural services—are transformed into economic and social benefits. Previous research has mainly focused on ecosystem service valuation and sustainable resource management, often overlooking the role of digital technologies and market mechanisms in improving FEPVRE. The "Two Mountains" theory, which stresses balancing economic development with environmental conservation, provides a new framework to understand the relationship between forest ecosystem services and socio-economic development. This theory advocates for integrating ecological health with economic growth to support green transformation for sustainable development.

Despite these contributions, there is a gap in the literature regarding the integration of digital technologies and market

mechanisms into FEPVRE measurement models. This gap limits the ability to fully optimize the efficiency of forest ecosystem products. This study aims to address this by applying the Technology-Organization-Environment (TOE) framework, which combines digital technologies, industry innovations, and environmental factors to provide a more comprehensive view of FEPVRE. The TOE framework highlights the role of digital technologies in driving sustainable development, offering new opportunities to improve forest ecosystem services' efficiency and effectiveness. Furthermore, while FEPVRE's economic aspects have been well explored, its ecological, social, and cultural dimensions are often overlooked. To fill these gaps, this study seeks to answer the following research question: How can FEPVRE be measured, and what are the key factors influencing its spatial and temporal development across regions in China? The study aims to: (1) measure the development level of FEPVRE, (2) analyze its spatiotemporal evolution and regional disparities, and (3) identify the factors influencing FEPVRE, particularly the role of digital technology, digital industries, and the digital environment. This approach will not only address the gaps in existing research but also offer a more comprehensive framework for improving FEPVRE.

2 Literature review

Existing research primarily focuses on the economic and ecological dimensions of FEPV, particularly in areas such as monetary valuation, market-based mechanisms, and the role of forestry in sustainable development (Grum and Boncina, 2024). However, studies rarely address how digital technologies, industrial modernization, and green development initiatives influence FEPVRE across space and time. This paper incorporates ecological economics and Green Growth theories to explore pathways for improving FEPVRE, including pure technical efficiency, enhancing the value of forestry's secondary and tertiary industries, increasing technology application, and improving human capital (Lou et al., 2024; Xu et al., 2025; Wang et al., 2023). Scientifically evaluating and realizing its comprehensive value has become a core task in promoting green development and ecological civilization. Methods for realizing the economic and social value of forest ecosystem products, such as establishing cross-regional ecological conversion mechanisms empowering forestry through the digital economy, are also explored (Hua et al., 2024; Li and Liu, 2024; Yao and Sun, 2023; Jiang et al., 2024). While existing research mainly focuses on combining green industry chain development with the marketization of ecological products to enhance FEPVRE (Wang et al., 2022; Huang H. et al., 2024), analytical methods like costbenefit analysis, ecosystem service evaluation, and distributed calculation are commonly used to assess FEPVRE (Yu et al., 2018; Li et al., 2023; Acharya et al., 2021). Additionally, measurement systems reflecting regional disparities in FEPVRE have been developed from perspectives such as new productive forces, digital villages, human capital, and the dual carbon goals (Chen et al., 2023; Zhang Y.-f. et al., 2023; Chen and Zhang, 2023; Su and Li, 2024). Despite this progress, there are areas for improvement: current measurement systems often rely on traditional productivity indicators, failing to fully account for the

impact of emerging technologies and industrial modernization. A more refined measurement framework that integrates ecological, economic, and social dimensions is needed to better reflect FEPVRE (Wang et al., 2022; X et al., 2023).

Moreover, most studies on regional disparities focus on county or local levels, often neglecting the inter-provincial and highdensity economic areas. The spatial distribution dynamics of FEPVRE, which examine how its efficiency evolves across different regions, remain underexplored. Few studies have analyzed the synergistic effects of technological, industrial, and policy factors on regional disparities in FEPVRE, particularly at larger spatial scales (Shi et al., 2021; Li et al., 2025; Zhang et al., 2023b). Furthermore, existing research seldom considers the synergistic effects of technological innovation, industrial modernization, and green productivity in driving the maximization of FEPVRE (Wang et al., 2023; Hu et al., 2023). Recent studies have introduced frameworks integrating ecological, economic, and social dimensions to improve FEPVRE measurement. Methods like Cost-Benefit Analysis, Ecosystem Service Evaluation, and Spatial Analysis (e.g., Super-SBM model, Markov chains, spatial Gini coefficient) examine FEPVRE's spatial distribution, highlighting regional disparities and trends. QAP Methods are used to analyze how technological, industrial, and policy factors influence FEPVRE (Ythier, 2022; Schultz et al., 2012; Li et al., 2020; Reb and er, 2013; Jones et al., 2023).

Based on these insights, a multidimensional FEPVRE measurement system has been constructed, considering economic, social, and ecological impacts (Barth and Doell, 2016; Bush et al., 2024; Chang et al., 2021; Chen et al., 2022; Guo et al., 2001; Kindler, 2016; Zandebasiri et al., 2023; Yang et al., 2023; Quoc Tuan et al., 2012; Ojea et al., 2010). This system, applied to the provincial and municipal levels in China, uses complex system interactions to provide new perspectives on FEPVRE. The main innovations of this paper are as follows: First, it develops a measurement system that combines the economic, ecological, and social dimensions of FEPV, enabling a comprehensive evaluation of forest ecosystem product values at the provincial and municipal levels in China. Second, by applying spatial analysis methods such as the Super-SBM super efficiency model, Markov chains, spatial Gini coefficient, and QAP methods, this paper analyzes FEPVRE disparities within and between provinces and cities in China, revealing trends in value efficiency changes at different spatial scales. These methods collectively provide a comprehensive understanding of regional disparities and their evolution over time. Third, this study constructs a measurement framework for FEPVRE using inputoutput methods and incorporates the TOE (Technology, Organization, and Environment) framework, Sustainable Development Goals (SDGs) theory and Green Growth models, to explore the interactions between digital technology, industry transformation, and ecological services in enhancing FEPVRE.

The contributions of this research are twofold: it introduces a multidimensional approach to FEPVRE measurement, expanding beyond traditional economic indicators to include ecological and social factors; and it broadens FEPVRE research by incorporating the role of digital technologies, industry transformation, and

sustainable development, providing valuable insights for policymakers aiming to improve forest ecosystem product efficiency and promote long-term sustainability. The specific research framework is shown in Figure 1.

3 Research design

3.1 Model specification

3.1.1 Super-SBM super efficiency

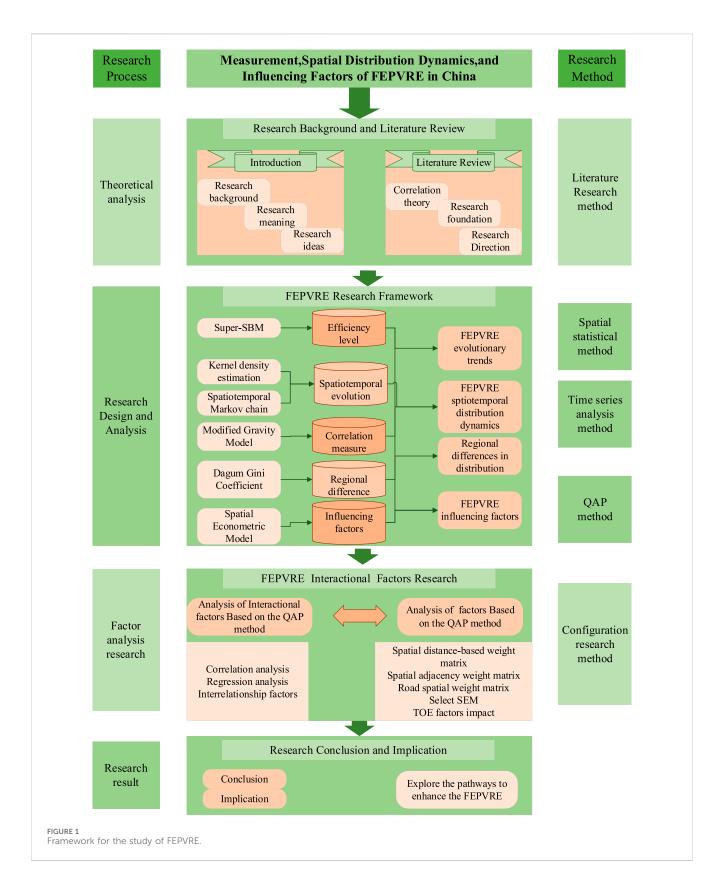
The Super-SBM model, proposed by Tone et al., which has its foundation in data envelopment analysis (DEA). This integration enables the effective evaluation of forest ecosystem products by considering both ecological efficiency and economic growth, ensuring a comprehensive analysis of FEPVRE (Tone, 2002; Zhang et al., 2023c). The Super-SBM model improves the identification and comparison of efficiency levels of different Decision-Making Units (DMUs) compared to traditional efficiency models. In this study, each province in China is considered a DMU, and efficiency analysis is performed using the non-oriented Super-SBM model. The FEPVRE for Chinese provinces from 2012 to 2022 is calculated using MATLAB software. The specific formula is as follows:

$$\rho = min = \frac{1 + \frac{1}{m} \sum_{q=1} \left(\frac{s_q}{x_{qk}}\right)}{1 - \frac{\sum_{r=1}^{s_1} \left(\frac{s_r^g}{y_{rk}^g}\right) + \sum_{t=1}^{s_2} \left(\frac{s_h^b}{y_{hk}^b}\right)}{s_1 + s_2}}$$

$$s.t. \begin{cases} x_{qk} \geqslant \sum_{j=1, j \neq k}^{n} x_{qj} \lambda_j - s_i^- \\ y_{rk}^g \leqslant \sum_{j=1, j \neq k}^{n} y_{rj}^g \lambda_j - s_i^g \\ y_{hk}^b \leqslant \sum_{j=1, j \neq k}^{n} y_{hj}^g \lambda_j - s_h^b \\ s_a^-, s_r^g, s_h^b, \lambda_j \geqslant 0 \end{cases}$$

$$(1)$$

In Equation 1, ρ represents the relative efficiency value, which indicates the FEPVRE of forest ecosystem products. If $\rho \ge 1$, it means that the decision-making unit (DMU) is relatively efficient and has reached the optimal production Frontier. If $0 < \rho < 1$, it indicates that the DMU is relatively inefficient and there is still a gap to the optimal production Frontier. In this model, m represents the number of input indicators for forest ecosystem product production, and s represents the number of output indicators for forest ecosystem products. x_{ik} denotes the value of the *i*-th forest ecosystem product input factor in decision-making unit k, while y_{rk} denotes the value of the r-th forest ecosystem product output factor in decision-making unit k. S_i^- and S_r^+ are the slack variables for inputs and outputs, respectively, representing the inefficient portions during the calculation process. Slack variables primarily reflect the efficiency loss of decision-making units. The weight vector λ_i represents the contribution of different decision-making units to the overall efficiency, and it satisfies $\lambda_i \ge 0$.



3.1.2 Spatiotemporal evolution

Spatial kernel density estimation (SKDE) is a valuable tool for understanding FEPVRE and regional disparities. By incorporating both spatial and temporal factors, SKDE provides a more accurate

assessment of FEPVRE's distribution, revealing trends and variations across regions over time. Unlike traditional kernel density estimation, SKDE integrates spatial and temporal factors, allowing for a better estimation of the distribution of random

variables under spatiotemporal conditions (Hohl et al., 2022). The following formula illustrates the dynamic distribution of FEPV in China:

$$f(x,y) = \frac{1}{Nh_x h_y} \sum_{i=1}^{N} K_x \left(\frac{X_i - x}{h_x}\right) K_y \left(\frac{Y_i - y}{h_y}\right)$$

$$g(y \mid x) = \frac{f(x,y)}{f(x)}$$
(2)

In Equation 2, f(x, y) represents the joint kernel density function of the random variables x and y, where hx and hy are the bandwidth parameters for x and y, respectively, and K is the kernel function. He bandwidth parameters hx and hy correspond to the smoothing degrees of spatial data along the x-axis and y-axis, respectively. The selection of bandwidth is crucial because it controls the range of influence of the kernel function around each data point, which in turn affects the smoothness of the density estimate. If the bandwidth is too large, the density estimate becomes overly smooth, potentially masking important details in the data; if the bandwidth is too small, it may lead to overfitting, with the density estimate exhibiting excessive fluctuations. In SKDE, the bandwidth is typically determined using Silverman's formula, which is given by:

$$h_x = 0.9 \times min(\hat{\sigma}_x, \hat{\sigma}_y) \times n^{-\frac{1}{5}}$$

$$h_y = 0.9 \times min(\hat{\sigma}_x, \hat{\sigma}_y) \times n^{-\frac{1}{5}}$$
(3)

In Equation 3, $\hat{\sigma}_x$ and $\hat{\sigma}_y$ represent the standard deviations of the data along the x-axis and y-axis, respectively, and n is the sample size. This method provides an optimal balance in the bandwidth selection based on the data characteristics, ensuring an accurate and smooth estimation of the density function. By considering the combined effects of spatial and temporal factors, SKDE provides a more precise estimation of the distribution of random variables. Additionally, SKDE accounts for the conditional distribution state g(y|x), which estimates the distribution of variable y given a specific spatial variable x. This conditional density function is valuable for analyzing how FEPVRE changes over time and across regions under specific spatial conditions.

The spatiotemporal Markov chain analysis is a dynamic method for examining the transition trends of FEPVRE. It is essential for understanding the dynamics of FEPVRE and regional disparities. Building on SKDE, this approach helps identify transition trends and regional evolution in FEPVRE. By incorporating spatial lag, it effectively considers the impact of spatial effects and geographic context (Zhao et al., 2023), revealing the spatial dynamics of FEPV changes within regions. This method enables the analysis of the transition and evolution of ecological product value realization states between different provinces and cities, improving the accuracy of FEPVRE assessments for forest ecosystem products in China and deepening the understanding of spatiotemporal impacts. In this model, regional states are classified into k types, forming a $k \times k$ probability transition matrix. The element T_{kij} in the matrix represents the conditional probability of transitioning from state i at time t to state j at time (t + 1) within the neighborhood B of region A. The specific formula is as follows:

$$H = -2\log\left\{\prod_{l=1}^{k}\prod_{i=1}^{k}\prod_{j=1}^{k}\left[\frac{m_{ij}}{m_{ij}(S)}\right]^{n_{ij}(S)}\right\}$$
(4)

In Equation 4, k represents the number of FEPVRE types, where k = 4. $n_{ij}(S)$ denotes the number of transitions between provinces and cities in the spatial Markov chain of the neighborhood state type S while m_{ij} represents the probability of a Markov transition. $m_{ij}(S)$ refers to the transition probability of the Markov chain within the spatial domain S.

The Markov Chain method is used because it effectively models the temporal transitions of FEPVRE states across regions, accounting for spatial dependencies and the influence of previous states. This method is particularly suited for capturing dynamic processes and transition trends over time, making it more appropriate than other methods for analyzing FEPVRE, especially in the context of regional disparities. As shown in Table 1.

3.1.3 Modified gravity model

The traditional gravity model has limitations due to its reliance on a single indicator and the use of symmetric parameters, often set to 1. The modified gravity model, however, better aligns with actual conditions. To enhance the understanding of FEPVRE and regional disparities, the modified gravity model provides valuable insights. Building on SKDE and spatiotemporal Markov chain analysis, it quantifies spatial interactions between provinces and cities. By considering factors such as employment in the forestry sector, forestry industry value, and economic distance, the modified gravity model offers an objective measure of the correlation between FEPVRE across regions, complementing previous analyses (Huang Y. et al., 2024). The specific formula is as follows:

$$\frac{\sqrt[3]{FEPVRE_{i} \times P_{i} \times GI_{i}} \sqrt[3]{FEPVRE_{j} \times P_{j} \times GI_{j}}}{D_{ij}^{r}},$$

$$k = \frac{FEPVRE_{i}}{FEPVRE_{i} + FEPVRE_{j}}, D_{ij} = \frac{LD_{ij}}{PCG_{i} - PCG_{j}}$$
(5)

In Equation 5, F_{ij} represents the strength of the correlation between the FEPVRE of forest ecosystem products between provinces i and j. $FEPVRE_i$ refers to the FEPVRE of forest ecosystem products. P denotes the number of people employed in the forestry sector. GI_i represents the added value of the forestry industry in province i. r is the friction coefficient, set at 0.5. k is the gravity coefficient. D_{ij} represents the economic and geographic distance between provinces i and j, while LD_{ij} indicates the physical geographic distance between the two provinces. PCG refers to the real $per\ capita$ gross product.

3.1.4 Dagum Gini coefficient

The Dagum Gini coefficient is used to analyze regional disparities in FEPVRE in China (Huang et al., 2025). Building on methods like SKDE, spatiotemporal Markov chain analysis, and the modified gravity model, this approach quantifies FEPVRE differences across regions. By quantifying the differences between different regions, it helps to better understand the synergistic relationships within regions and across regions, as well as their impact on FEPVRE. This

TABLE 1 Comparison of Markov chain method and other dynamic analysis methods.

Method	Differences	Application
Spatiotemporal Markov Chain	Focuses on both spatial and temporal transitions, capturing state changes across time and geography	Models the transition of states across both time and space, with a focus on state-to-state probabilities
SKDE	SKDE does not model temporal transitions. It focuses purely on spatial patterns and densities	Estimates the density of a variable across a spatial region at one point in time
Super-SBM	Focuses on technical efficiency without incorporating spatiotemporal factors	Models efficiency at a single point in time, with no consideration of spatial or temporal transitions
QAP	Does not model temporal dynamics, only focuses on spatial relationships	Assesses the correlation between regions based on spatial data, without considering time-dependent changes
Cellular Automata	Cellular Automata does not model explicit state probabilities; instead, it uses a set of deterministic or probabilistic rules for each "cell."	Cells evolve based on predefined rules, often used in land-use change modeling
Agent-Based Models	Agent-Based Models agent behaviors, often ignoring the fixed probability transitions between states like Markov Chains	Models the interactions and behavior of multiple agents in a system, with space and sometimes time
System Dynamics	System Dynamics focuses on stocks, flows, feedback loops, and time-based system behavior rather than state transitions	Uses differential equations to model interactions and behavior of variables over time
Stochastic Differential Equations	SDE models continuous random processes, unlike the discrete state transitions of Markov Chains	Models continuous systems subject to random influences, often used for ecological or environmental processes
Vector Autoregressive (VAR) Models	VAR models relationships between multiple time series rather than discrete states in space and time	Analyzes the interdependencies between time series variables, does not directly model spatial dependencies

method is integrated with spatiotemporal Markov chain analysis and other techniques to offer a multidimensional view of FEPVRE, revealing trends in spatial efficiency and the factors driving regional disparities. This combined approach enhances our understanding of how FEPVRE evolves across different regions, providing a valuable framework for addressing disparities and promoting long-term sustainability. The specific formula is as follows:

$$G = \frac{\sum_{i=1}^{k} \sum_{m=1}^{k} \sum_{j=1}^{n_{i}} \sum_{r=1}^{n_{m}} |y_{ij} - y_{mr}|}{2n^{2}\mu}$$

$$G_{ii} = \frac{\sum_{j=1}^{n_{i}} \sum_{r=1}^{n_{i}} |y_{ij} - y_{ir}|}{2n_{i}^{2}\mu_{i}}$$

$$G_{im} = \frac{\sum_{j=1}^{n_{i}} \sum_{r=1}^{n_{m}} |y_{ij} - y_{mr}|}{n_{i}n_{m}(\mu_{i} + \mu_{m})}, \mu_{m} \leqslant \cdots \leqslant \mu_{i} \leqslant \cdots \leqslant \mu_{k}$$

$$G = G_{w} + G_{nb} + G_{l}, G_{gb} = G_{nb} + G_{l}, G_{w} = \sum_{i=1}^{k} G_{ii}p_{i}s_{i} \qquad (6)$$

$$G_{nb} = \sum_{i=2}^{k} \sum_{m=1}^{i-1} G_{im}(p_{i}s_{m} + p_{m}s_{i})D_{im}$$

$$G_{l} = \sum_{i=2}^{k} \sum_{m=1}^{i-1} G_{im}(p_{i}s_{m} + p_{m}s_{i})(1 - D_{im})$$

$$D_{im} = \frac{d_{im} - p_{im}}{d_{im} + p_{im}}$$

In Equation 6, G represents the overall Gini coefficient for the development level of FEPV. y_{ij} denotes the development level of FEPV in province j of region i, where k is the number of regions and n is the number of provinces. μ is the mean FEPV development level across all regions. G_{ii} is the Gini coefficient for region i, and G_{im} represents the Gini coefficient between region i and region m, indicating the relative impact of the development levels of

FEPVRE between these two regions. d_{im} is the difference in FEPV development levels between regions i and m, and p_{im} is the expected value of the sum of samples where $y_{mr} - y_{ij} > 0$ for regions i and m.

3.1.5 QAP method

The QAP method is used to analyze the correlation and dependence of spatial data. In this study, the QAP method is employed to assess the effects of T, O, and E on regional disparities in FEPVRE. Through correlation and regression analysis, it compares paired data to reveal interactions and spatial relationships between variables. Building on methods like SKDE, Markov chain analysis, the modified gravity model, and the Dagum Gini coefficient, the QAP method analyzes the effects of multiple variables on regional disparities (Jia et al., 2024). However, while the QAP method primarily identifies relationships and dependencies between regions, spatial econometric models, such as the SAR and SEM, go further by analyzing spatial causality and dependencies. These models help us understand how neighboring regions influence each other and identify spatial spillover effects, providing quantitative insights into spatial relationships. Together, these approaches offer a comprehensive understanding of regional disparities in FEPVRE, with QAP revealing spatial patterns and econometric models analyzing causal relationships.

3.1.6 Spatial econometric model

Based on the related studies (Li et al., 2022; Junru and Mingyang, 2024), the spatial econometric model is initially specified as follows:

$$Y_{it} = \rho \sum_{j=1}^{N} W_{ij} Y_{it} + \beta_0 + \beta_1 T_{it} + \beta_2 O_{it} + \beta_3 E_{it} + \gamma A_{it} + \alpha_i + \varepsilon_{it} + \nu_t$$
(7)

$$\varepsilon_{it} = \lambda \sum_{i=1}^{N} W_{ij} \varepsilon_{it} + \mu_{it}$$
 (8)

TABLE 2 The difference between the QAP method and spatial econometric models.

Aspect	QAP method	Spatial econometric models (SEM/SAR)
Concept	Non-parametric method for analyzing correlations between spatially distributed data	Parametric regression models for examining spatial dependencies and causality
Core Objective	Identifying spatial patterns and dependencies between regions	Quantifying spatial relationships, dependencies, and spillover effects
Handling of Problems	Focuses on comparing pairs of data to detect spatial correlations	Analyzes spatial causality and dependencies, focusing on spillover effects
Data Type	Pairwise data or spatially distributed network data	Continuous spatial data with explicit spatial relationships
Theoretical Basis	Network theory, correlation analysis	Spatial econometrics, spatial lag, and spatial error models
Dependence Structure	Relies on pairwise correlations without defining a causal relationship	Explicitly models spatial dependencies and causality between regions
Model Form	Non-parametric, based on correlation matrices	Parametric, with regression coefficients explaining spatial dependence
Role of Variables	Independent variables are compared in terms of spatial correlation, no specific focus on dependent variables	Dependent and independent variables are explicitly modeled, with spatial lags and errors
Main Output	Identifies spatial relationships and patterns in data	Provides regression coefficients, significance tests, and model fit
Results Interpretation	Focuses on spatial patterns and network structure	Focuses on quantifying spillover effects and explaining spatial causality
Hypothesis Testing	Not typically associated with hypothesis testing	Includes formal hypothesis testing (e.g., spatial lag and error effects)
Advantages	Ideal for detecting correlations in complex spatial networks	Provides quantitative insights into spatial dependencies and causality
Disadvantages	Limited ability to explain causality or infer relationships	Assumes a predefined model structure, which might not always fit the data well

The spatial econometric model is used to capture the spatial dependencies in FEPVRE across different regions. In the model, FEPVRE represents the forest ecosystem product value realization efficiency, and TOE represent digital technology, digital industry, and the digital environment, respectively. α_i denotes the regional effect, ν_t represents the time effect, and ε_{it} is the random disturbance term. W_{ij} is the spatial weight matrix, and ρ and λ represent the spatial error coefficient and spatial lag coefficient, respectively. A_{it} denotes the control variables.

The QAP and Spatial Econometric Models both analyze spatial relationships and dependencies but differ significantly in their approach and application. The QAP method is a non-parametric technique that identifies correlations and dependencies between spatially distributed variables, focusing on detecting patterns without assuming a specific model structure. It is particularly useful for exploring interactions in complex systems, especially with networked data. In contrast, Spatial Econometric Models are parametric regression models that quantify spatial relationships by accounting for spatial dependence and lag effects. These models provide a more comprehensive understanding of spatial causality and spillover effects, revealing both direct and indirect influences between regions. As shown in Table 2.

3.1.7 The entropy method

The use of the entropy method to measure the levels of digital technology, digital industry, and digital environment not only avoids the randomness and arbitrariness of subjective weighting methods but also resolves the issue of information overlap among multiple indicators. Therefore, it is considered an objective and scientific method for determining weights. Specifically, the greater the data dispersion, the smaller the information entropy, and the greater the impact and weight of the indicator on the overall evaluation. Conversely, the smaller the data dispersion, the greater the information entropy, and the lower the weight of the indicator. The specific steps and calculation formula of the entropy method are as follows.

 Data Standardization. Since the units and value ranges of different indicators may vary, it is necessary to standardize the raw data to eliminate the impact of units. The standardization formula is as follows:

positive indicators:

$$X'_{ij} = \frac{X_{ij} - min(X_j)}{max(X_i) - min(X_i)}$$

$$(9)$$

negative indicators:

$$X'_{ij} = \frac{max(X_j) - X_{ij}}{max(X_j) - min(X_j)}$$
(10)

In the Equations 9, 10, X_{ij} represents the value of the j indicator for the i sample; X'_{ij} represents the standardized value; $min(X_j)$ and $max(X_j)$ denote the minimum and maximum values of the j indicator, respectively.

2. Calculating Information Entropy. Information entropy reflects the amount of information contained in an indicator. The smaller the information entropy, the greater the information content, and the higher the weight of the indicator should be. The formula for calculating information entropy is as follows:

$$e_j = \frac{-1}{\ln n} \sum_{1}^{n} \left(P_{ij} \times \ln P_{ij} \right) \tag{11}$$

In the Equation 11 formula, e_j represents the information entropy of the j indicator; n denotes the number of samples; P_{ij} represents the weight of the i sample in the j indicator, calculated as (Equation 12):

$$P_{ij} = \frac{X'_{ij}}{\sum_{1}^{n} X'_{ij}} \tag{12}$$

3. Calculation of Redundancy. Redundancy is the opposite of information entropy and reflects the degree of redundancy in the indicator information. The Formula 13 for calculating redundancy is as follows:

$$d_i = 1 - e_i \tag{13}$$

Calculation of Weights. The weights of each indicator are calculated based on redundancy, and the formula is as follows:

$$w_{j} = \frac{d_{j}}{\sum_{j=1}^{m} d_{j}} \tag{14}$$

In the Formula 14, w_j represents the weight of the j indicator, and m represents the number of indicators.

5. The composite evaluation index is obtained by performing a weighted sum of each decision unit's performance across various indicators, according to the weight of each indicator, to derive a composite score. The composite evaluation index C_i for each decision unit is calculated as follows:

$$C_{i} = \sum_{j=1}^{n} w_{j} \cdot X'_{ij} \tag{15}$$

In Formula 15, C_i is the composite evaluation index of the i-th decision unit. w_j is the weight of the j-th indicator (calculated using the entropy method). X_{ij}' is the normalized value of the i-th decision unit for the j-th indicator.

3.1.8 The number of broadband internet access ports

In the China Statistical Yearbook, the statistics for broadband internet access ports consider various types of access methods, aggregating the port numbers of different technologies to derive a total. Generally, the calculation formula is:

Number of broadband Internet access ports

$$= \sum (Port number for various access methods)$$
 (16)

In Formula 16, the port numbers for various access methods mainly include ADSL (Asymmetric Digital Subscriber Line) access

ports, Fiber optic access (such as FTTH, FTTB, FTTC) ports, Wireless broadband access (such as 4G, 5G access) ports and Other broadband access technologies (such as Hybrid Fiber-Coaxial (HFC), satellite broadband, etc.). Among these, In Formula 17, the number of ADSL access ports is primarily based on the ADSL ports in the fixed telephone network. The formula for this can be expressed as:

ADSL Access Ports =
$$\sum$$
 (ADSL Access Ports in each region) (17)

In Formula 18, fiber optic access ports (FTTx), fiber optic access port statistics are usually subdivided into FTTH, FTTB, FTTC, and so on, with separate statistics for each type of access. The formula is:

Fiber Optic Access Ports =
$$\sum$$
 (Fiber Optic Access Ports in each region) (18)

The number of wireless broadband access ports includes wireless access based on mobile networks (such as 4G, 5G, etc.). The statistical method typically determines the number of ports based on the number of base stations, access points, and other factors related to each technology. The Formula 19 is:

Wireless Broadband Access Ports =
$$\sum$$
 (Wireless Broadband Access Ports in each region) (19)

3.2 FEPVRE indicator system construction

3.2.1 Dependent variable

This study measures FEPVRE using input-output methods based on scientific accuracy, comprehensiveness, and operability. The selection of input and output indicators follows a systematic process informed by prior research and expert recommendations (Xu et al., 2025). Input indicators primarily reflect the resources and investments directed towards forest ecosystems, which are essential for sustainable forest management and ecosystem service provision. For instance, Forest Material Preservation Value represents the value of timber and non-timber products, directly influencing the forest's ability to provide materials for economic use and aligning with the Forest Product Value indicator. These resources also support other vital ecosystem services, such as Water Yield Value and Carbon Sequestration Service Value, contributing to ecological stability. The Forestry Fixed Asset Investment indicator represents capital directed towards forest infrastructure, machinery, and technological advancements, ensuring effective management and enhancing the quality and scale of forest products and services. It complements Forest Material Preservation Value by facilitating sustainable resource extraction and boosting productivity. The Number of People Employed in Forestry reflects human capital investment, supporting effective forest management, conservation, and sustainable utilization, while directly contributing to the Forest Recreation Value and other ecosystem services. These indicators highlight the role of human and financial resources in improving forest ecosystem outcomes and advancing the broader goals of FEPVRE. Data for input indicators, such as forest product value, water yield, and carbon sequestration, focus on the tangible and intangible

TABLE 3 Indicator system for measuring FEPVRE.

Category	Primary indicator	Secondary indicator	Unit
Input Indicators	Forest Material Preservation Value Forest Product Value		Ten Thousand RMB
		Water Yield Value	Ten Thousand RMB
		Carbon Sequestration Service Value	Ten Thousand RMB
	Ecological Regulation Conversion Value	Oxygen Release Value	Ten Thousand RMB
		Air Purification Value	Ten Thousand RMB
		Soil Conservation Value	Ten Thousand RMB
	Cultural Service Conversion Value	Forest Recreation Value	Ten Thousand RMB
	Material Capital	Forestry Fixed Asset Investment	Ten Thousand RMB
	Labor Force	Number of People Employed in Forestry	Ten Thousand People
Output Indicators	Forestry Industry Output Value	Forestry Primary Industry Output	Ten Thousand RMB
		Forestry Secondary Industry Output	Ten Thousand RMB
		Forestry Tertiary Industry Output	Ten Thousand RMB

benefits derived from forests, including their role in water regulation and carbon mitigation. Other indicators, like oxygen release, air purification, and soil conservation, emphasize critical ecological services like maintaining oxygen levels, improving air quality, and preventing soil erosion. Forest recreation value underscores the socio-cultural benefits provided by eco-tourism and recreational services. Additionally, forestry fixed asset investment and employment in forestry serve as key indicators for assessing the economic activities and human resources invested in forest ecosystems (Huang et al., 2025).

Output indicators evaluate the economic impact of forest ecosystems through different sectors. The forestry primary industry output represents economic contributions from timber production and harvesting, while the secondary industry output reflects the value derived from processing and transforming forest products. The tertiary industry output includes services linked to forests, such as eco-tourism and wellness services. These indicators were selected based on their relevance to forest ecosystem services and their availability in national and provincial data sources. The study uses the China Statistical Yearbook (2012–2022) and the China Forestry Statistical Yearbook to ensure comprehensive data coverage, focusing on consistent and comparable data across provinces. Based on these input and output indicators, this study constructs a measurement framework for FEPVRE that includes 12 indicators, as shown in Table 3.

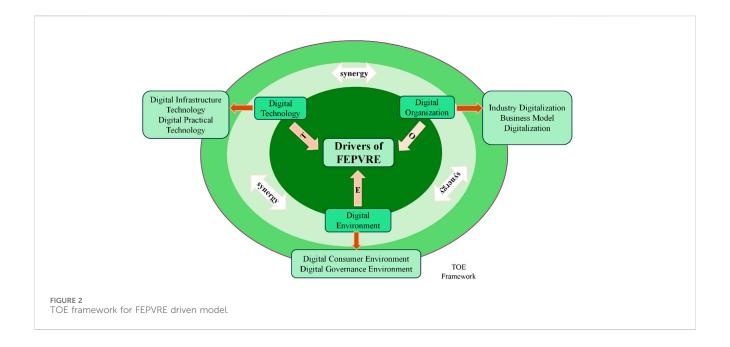
3.2.2 Explanatory variables

The TOE framework consists of three components: Digital Technology (T), Digital Organization (O), and Digital Environment (E). Based on research by scholars (Miao and Zhao, 2023), this framework has been widely applied in green development, particularly for analyzing how digital technologies, organizational structures, and the digital environment influence economic and ecological systems. The TOE framework is selected for analyzing factors influencing FEPVRE because it offers a comprehensive approach to assess how digital advancements drive environmental, organizational, and technological changes

that impact forest ecosystem services and their value realization. The rapid growth of digital technologies and the digital economy plays a crucial role in shaping FEPVRE. By focusing on the digital economy, this study explores how innovations in digital technology, organizational structures, and the digital environment influence the utilization, conservation, and management of forest ecosystem products. This perspective provides a deeper understanding of digitalization's role in green development, which may not be fully captured by broader ecological, economic, and social viewpoints. Analyzing FEPVRE through the digital economy lens helps assess how digital transformation impacts forest ecosystem efficiency. This approach aligns with the study's objective of understanding the influence of digital technologies and organizational structures on FEPVRE, supporting more sustainable and efficient forest resource management. The model highlights key drivers of FEPVRE within the digital economy, addressing current and future challenges in forest ecosystem management. Therefore, the study focuses on the dimensions of digital economy-digital technology (T), digital organization (O), and digital environment (E)—and constructs a FEPVRE-driven development model, as shown in Figure 2.

Digital Technology (T). Based on the research (Xu et al., 2025), this study identifies digital infrastructure technologies and digital practice technologies as key driving factors of digital technology. Digital infrastructure indicators include long-distance optical cable line density (km/km²), number of broadband Internet access ports (per 10,000 people), and network connection addresses (per 10,000 people). Digital practice technologies include mobile phone penetration rate (%), Internet penetration rate (%), and telecom business revenue (million RMB). A composite digital technology index is calculated using the entropy method, integrating both digital infrastructure and digital practice technologies. This method assigns weights to each variable based on its contribution to the overall digital technology index, mitigating the impact of multicollinearity and ensuring each indicator contributes uniquely.

Digital Organization (O). this research focuses on digital industries and the digitalization of business models. Digital industry indicators



include total telecom services, information technology service revenue (million RMB), and software revenue (million RMB). The digitalization of business models is represented by e-commerce sales volume, the proportion of e-commerce transaction activities conducted by enterprises (%), and the number of websites per 100 enterprises. A composite digital industry index is computed using the entropy method, integrating both digital industry and business model digitalization.

Digital Environment (E). Based on the research by scholars (Huang et al., 2025), this study considers the digital consumer environment and the digital government environment as key factors. The digital consumer environment includes indicators like total household consumption expenditure (million RMB) and online retail sales (million RMB), reflecting digital adoption and e-commerce activity. The digital government environment is represented by the online government service capability index (%), which measures the effectiveness of digital government platforms in delivering services to the public. A composite digital environment index is calculated using the entropy method, integrating both digital consumer behavior and government service capabilities.

While other factors, such as governance and institutional environments, could offer deeper insights, these selected indicators are directly relevant to assessing the impact of the digital landscape on FEPVRE. They connect digital technology to economic activities (digital consumer behavior) and governance (digital government services), providing a measurable understanding of how digital resources enhance forest ecosystem services.

3.2.3 Control variables

The control variables include urbanization development level, economic development level, infrastructure level, fiscal expenditure scale, and technological innovation level. These were selected based on a thorough literature review and their established influence on FEPVRE (Kaoru, 1800). Data were gathered from the China Statistical Yearbook, with criteria based on their relevance across provinces and their significance in shaping regional economic and

ecological conditions. The urbanization development level is measured by the proportion of the urban population in the total permanent population. It influences the demand for forest ecosystem services, urban pressure on forest ecosystems, and resource management. The economic development level is represented by the logarithm of per capita GDP, reflecting the region's economic growth. The infrastructure level is quantified by the ratio of road mileage to the administrative area. Welldeveloped infrastructure facilitates the transport of forest products, efficient delivery of ecosystem services, and the economic development of forest-dependent regions. The fiscal expenditure scale is measured by the ratio of government fiscal expenditure to GDP. The technological innovation level is represented by the product of the ratio of total agricultural machinery power to forestry industry output value and the ratio of forestry value-added. This captures technological progress in agriculture and forestry, reflecting mechanization and innovation that improves productivity and resource allocation in forest ecosystems. Total agricultural machinery power represents technological innovation in agriculture and forestry. It improves resource allocation and productivity, particularly important for forest ecological product production. Including this variable enhances the analysis accuracy by accounting for technological advancements and eliminating regional disparities.

In summary, these control variables are widely recognized for their relevance and ensure a comprehensive analysis of the factors affecting FEPVRE, resulting in a more accurate evaluation of regional disparities.

3.3 Data sources

Data for this study were sourced from publicly available statistical yearbooks, including the China Statistical Yearbook (2012–2022), China Forestry Statistical Yearbook, and China Forestry and Grassland Statistical Yearbook, covering

TABLE 4 Descriptive statistics.

Variable Category	Variable name	Variable	Mean	Std.Dev	Min	Max	Obs
Dependent Variable	FEPVRE	Y	0.907	0.612	0.001	2.948	330
Explanatory Variables	T	X_1	0.195	0.029	0.616	330	330
	0	X ₂	0.0926	-0.004	0.801	330	330
	E	X ₃	0.132	0.006	0.858	330	330
Control Variables	Urbanization Level	A_1	0.608	0.118	0.363	0.909	330
	Economic Development Level	A_2	10.906	0.445	9.849	12.156	330
	Infrastructure Level	A_3	0.959	0.522	0.091	2.259	330
	Fiscal Expenditure Scale	A_4	0.252	0.104	0.105	0.675	330
	Technological Innovation Level	A_5	8.512	1.286	4.747	10.854	330

30 provinces in China. Tibet, Hong Kong, Macau, and Taiwan were excluded due to missing or inconsistent data, which could affect the reliability of the analysis. The selected sources were chosen based on their comprehensiveness and consistency over time, ensuring reliable and comparable data. In addition, remote sensing data were incorporated from the Resource and Environmental Science and Data Center of the Chinese Academy of Sciences and the National Meteorological Data Center, providing a more granular view of ecological changes across regions. Remote sensing data for green economy products at the provincial and municipal levels were sourced from the Resource and Environmental Science and Data Center, National Tibetan Plateau Science Data Center, National Meteorological Data Center, Geospatial Data Cloud, and the National Earth System Science Data Center. These data are crucial for studying forest ecosystem product environmental changes, ecosystem services, and resource utilization efficiency. Soil data were derived from the World Soil Database (HWSD), jointly constructed by the Food and Agriculture Organization (FAO) and the International Institute for Applied Systems Analysis (IIASA). The soil data for China, available at a 1: 1,000,000 scale, cover the period from 2012 to 2022, with missing values supplemented using interpolation methods. Descriptive statistics for each variable are presented in Table 4.

4 Results

4.1 Forest ecosystem product value realization efficiency

FEPVRE serves as the basis for studying regional efficiency disparities across China. The analysis of efficiency development trends highlights the specific differences and evolution of FEPVRE in the country's four major regions. The results indicate a fluctuating trend in FEPVRE development across regions. Significant fluctuations from 2012 to 2020 reflect the early stages of China's green transformation and ecological civilization strategy. Policymakers should address these regional disparities, especially in the western and northeastern regions, where FEPVRE lags behind. The measurement results are presented in Table 5, and the efficiency evolution trend is shown in Figure 3.

From 2012 to 2022, the national average FEPVRE showed a fluctuating trend with significant regional disparities. The Eastern region outperformed the Western and Northeastern regions due to higher investments in green technology and ecological development. Policymakers should prioritize digital infrastructure and green innovation to enhance efficiency in lagging regions, especially the Western and Northeastern areas. In 2016, the FEPVRE peaked at 30.81%, indicating highly efficient utilization of forest ecosystem products in China. However, between 2016 and 2020, a decline occurred due to pressures from China's "dual carbon goals." Regions heavily reliant on traditional industries faced challenges aligning with the green transformation. Policymakers should support these areas, fostering a balanced transition to a low-carbon economy with targeted policies and incentives. A noticeable convergence trend emerged, with the Western region's FEPVRE gradually approaching that of the Central region, while the Northeastern region remained relatively low and grew slowly. The Eastern region's higher FEPVRE values were driven by investments in ecological construction and green industry innovation. The Central region showed larger fluctuations due to challenges in economic transitions, such as significant population movements and industrialization. The Western region, particularly provinces like Guizhou, Guangxi, and Sichuan, displayed fluctuating growth linked to abundant natural resources and successful green development strategies. The Northeast region, with low FEPVRE values and minimal improvement, struggled with imbalanced resource development due to structural adjustments in industrialization.

4.2 Association of FEPVRE

Regional disparities between the East and West are the primary drivers of differences in FEPVRE across China. This study employs a modified gravity model to measure the degree of association in FEPVRE among the 30 provinces and cities, aiming to identify the intensity of regional connections. Figures 4(a-k) illustrates the FEPVRE association from 2012 to 2022. The analysis reveals that the Eastern region is closely linked with the Central region, indicating potential for inter-regional cooperation in green development. Conversely, the Western and Northeastern regions show weaker connections, presenting

TABLE 5 Measurement results of FEPVRE in China.

No.	Region	Province	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021	2022	均值
1	Eastern Region	Beijing	1.450	1.530	1.503	1.522	1.522	1.530	1.549	1.532	1.551	1.566	1.589	1.450
2		Tianjin	0.028	0.023	0.099	1.199	0.018	1.015	1.288	1.574	1.528	1.592	1.589	0.028
3		Hebei	0.310	0.706	0.431	0.475	0.407	0.483	0.510	0.240	0.177	1.321	0.321	0.310
9		Shanghai	1.543	1.591	1.188	1.305	1.186	1.569	1.577	1.206	1.236	0.327	1.039	1.543
10		Jiangsu	1.583	1.588	1.582	1.585	1.587	1.591	1.516	1.169	1.290	1.243	1.321	1.583
11		Zhejiang	1.140	1.586	1.429	1.584	1.580	1.516	1.208	1.545	1.405	1.598	1.467	1.140
13		Fujian	1.279	2.771	1.142	1.109	2.172	2.948	2.322	1.273	1.255	1.175	1.146	1.279
15		Shandong	1.505	1.600	1.580	1.503	1.600	1.592	0.926	1.520	0.979	1.595	1.599	1.505
19		Guangdong	1.588	1.060	1.501	1.595	1.595	1.596	1.544	1.556	1.841	1.596	1.468	1.588
21		Hainan	1.590	1.320	1.576	1.566	1.586	1.571	1.600	0.176	1.470	1.623	1.731	1.590
4	Central Region	Shanxi	0.310	0.337	0.352	0.266	0.276	0.260	0.042	0.125	0.091	0.077	0.103	0.310
12		Anhui	1.106	1.542	1.111	1.832	1.588	1.499	1.950	1.542	1.794	1.597	1.534	1.106
14		Jiangxi	0.827	1.471	1.109	1.104	0.473	0.486	1.375	1.133	0.753	1.059	1.451	0.827
16		Henan	0.343	1.114	0.681	1.088	1.024	0.893	0.612	0.824	0.692	0.590	0.866	0.343
17		Hubei	0.536	0.943	1.015	1.401	1.188	1.067	0.733	0.819	0.631	0.980	0.728	0.536
18		Hunan	0.708	1.502	1.572	1.547	1.093	1.036	1.033	0.707	0.826	0.631	0.832	0.708
5	Western Region	Inner Mongolia	1.081	1.087	0.192	1.055	1.316	1.244	0.190	0.041	1.205	0.065	0.031	1.081
20		Guangxi	0.689	0.921	0.477	0.537	0.860	0.770	0.589	1.144	1.260	1.432	1.397	0.689
22		Chongqing	0.269	0.323	0.856	0.698	0.757	0.664	1.178	1.226	1.138	1.375	1.290	0.269
23		Sichuan	0.332	0.375	1.000	1.000	1.009	0.655	0.124	0.579	0.634	0.405	0.433	0.332
24		Guizhou	0.203	0.156	1.347	1.424	1.587	1.694	1.344	1.501	1.485	1.405	1.506	0.203
25		Yunnan	1.361	1.576	1.537	1.535	1.503	1.307	1.523	1.410	1.563	1.495	1.338	1.361
27		Shaanxi	0.284	0.327	0.373	0.435	0.192	0.188	0.001	0.148	0.108	0.083	0.084	0.284
28		Gansu	0.085	0.148	0.129	0.116	0.054	0.058	0.538	0.044	0.029	0.026	0.029	0.085
29	_	Qinghai	0.001	0.001	0.006	0.007	1.507	1.535	0.133	0.008	0.023	0.002	0.005	0.001
30		Ningxia	0.292	0.711	0.343	0.782	1.144	0.312	0.022	0.093	0.120	0.111	0.120	0.292
31		Xinjiang	0.115	0.145	0.105	0.106	0.064	0.161	0.013	1.526	0.019	0.030	0.031	0.115
6	Northeastern Region	Liaoning	0.846	1.496	0.911	0.969	0.616	0.598	1.372	1.506	0.896	0.598	1.206	0.846
7		Jilin	0.373	0.009	0.461	0.219	0.224	0.196	0.583	0.445	0.102	0.248	0.431	0.373
8		Heilongjiang	0.025	0.035	0.186	0.161	1.085	0.110	0.170	0.095	0.042	0.098	0.095	0.025

opportunities for enhanced regional cooperation. Policymakers could foster partnerships to improve FEPVRE in less developed regions by promoting knowledge and resource sharing. Using the natural breakpoints classification method, regions are divided into four levels based on cooperation strength. The Western region has fewer intensive connections, resulting in lower cooperation in FEPVRE compared to the Eastern and Central regions. Over time, high-level cooperation has been concentrated in the Southeastern region, with Guangdong leading the way. In contrast, the Western region lacks inter-regional cooperation or collaborative cities. The FEPVRE cooperation network in China demonstrates a "Matthew Effect," where provinces and cities with higher cooperation

intensities cluster together, reinforcing the unequal distribution of FEPVRE development.

4.3 Spatial distribution of FEPVRE

Since the southeastern region significantly influences regional differences in FEPVRE across China, this study employs SKDE to explore the spatial distribution dynamics of FEPVRE and assess its temporal and spatial evolution. The static spatial kernel density and contour map of FEPVRE (Figures 5(a,b)) reveal that the overall efficiency values of the forest ecosystem product value realization

show a rightward shift and concentration trend, with expanded coverage. This indicates an overall improvement in FEPVRE across China, with a more concentrated distribution. The performance of different provinces has become more consistent, and the range of distribution has widened. The curve polarization trend suggests a dominant peak, indicating that regional differences in FEPVRE are expected to persist and even widen during the sample period. The contour map reveals peaks aligned parallel to the y-axis, located at the upper left and lower right of the 45-degree diagonal, suggesting significant regional differences, with some provinces exhibiting relatively low FEPVRE. The spatial distribution of FEPVRE is concentrated in the Eastern and Southeastern regions, while the Western and Northeastern regions lag behind. To address these disparities, the government can invest in regional capacity building and promote technologies in lagging areas, which will help reduce spatial disparities and support more balanced green development.

From the spatial dynamic kernel density and contour map of FEPVRE across China's four major regions (Figures 6(a-e)), it is evident that severe polarization exists in both time and space, particularly in terms of spatial spillover effects. In the Eastern region, the peaks are aligned parallel to the y-axis, with one section of the primary peak located just below the 45-degree diagonal and the other section above it. This suggests a polarization trend: after a 3-year period, some provinces experience high FEPVRE, while others show a decline, reflecting instability in the region's development. In the Western region, the peaks are above the 45-degree diagonal, indicating a positive shift in FEPVRE, suggesting that these areas have significant potential for growth, especially during the green transformation process. In the Central region, the peaks are below the 45-degree diagonal, indicating that after 3 years, FEPVRE tends to stabilize and concentrate, with little room for further growth. This may be due to the full development of forest resources and a slower pace of green transformation. In the Northeastern region, there are two segments: one with a large peak above the 45-degree diagonal, indicating improvement in FEPVRE in some provinces after 3 years, and the other segment, a trough, lying below the diagonal, where provinces exhibit lower FEPVRE. For these provinces, strengthening ecological protection policies, promoting green development, and improving forest resource management are essential.

4.4 Markov chain analysis

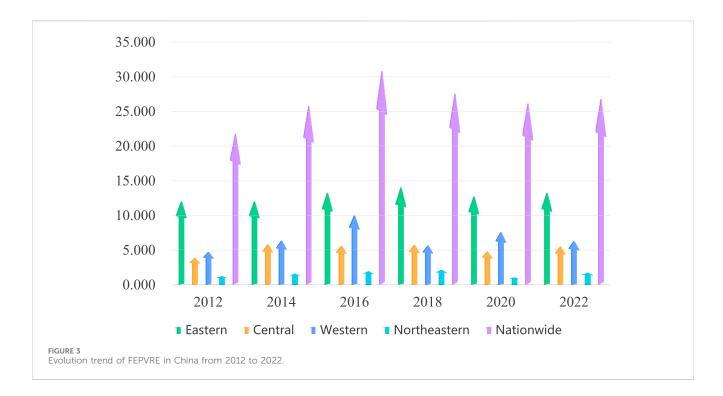
Due to the significant dual-level development of FEPVRE in China, Markov chain analysis is employed to analyze the dynamic transition trends of FEPVRE. The comprehensive scores during the sample period are categorized into four types: Low (I), Low-Medium (II), Medium-High (III), and High (IV). The results are presented in Table 6.

The analysis in Table 7 reveals that FEPVRE dynamics exhibit both stability and dynamism. The values on the main diagonal are generally higher than those on the off-diagonal, with the maximum value being 0.790 and the minimum 0.547. The probability of FEPVRE remaining unchanged for most provinces is at least 55%, indicating high stability across the majority of provinces. For FEPVRE transitions, provinces in Category I (inefficient) have a transition probability of 0.789 to remain in their status,

while provinces in Category IV (highly efficient) have a transition probability of 0.747, indicating strong stability in both low-efficiency and high-efficiency provinces. However, provinces in intermediate categories (II and III) face greater challenges in terms of transition. Specifically, Category I provinces (low-efficiency) have a 0.125 probability of moving up to Category II, reflecting the difficulty in improving efficiency. In contrast, Category III provinces (moderately high-efficiency) have a 0.227 probability of advancing, suggesting significant potential for improvement. These provinces are in the "sweet spot," with the capability and potential to further enhance efficiency. Category II provinces (moderately lowefficiency) face a 0.125 probability of downgrading to Category I, highlighting the risk of significant decline. Even Category IV provinces (high-efficiency) face a 0.190 probability of transitioning downward, indicating downward pressure on even the most efficient regions.

The Markov chain analysis results, presented in Table 6, show that the transition probabilities for spatial lag types I and IV are 0.790 and 0.747, respectively. For spatial lag type I, the probability of maintaining the original state is significantly higher than the probabilities of upward or downward transitions. Similarly, in spatial lag type IV (high-efficiency provinces), the probability of maintaining the original state is also high, indicating the higher stability of ecological efficiency in these provinces. Both lowefficiency and high-efficiency provinces tend to maintain their existing ecological efficiency levels, especially when the efficiency gap with neighboring provinces is small or stable. In contrast, spatial lag types II and III show more instability, with most off-diagonal elements non-zero. This suggests that provinces in these types have a higher potential for transitioning to either better or worse efficiency levels. Notably, in spatial lag types III and IV, the off-diagonal elements are 0.100 and 0.250, respectively, indicating that the efficiency of these provinces is more susceptible to external shocks and the transition processes of neighboring provinces. The differences in upward and downward transition probabilities under different lag conditions are significant. In spatial lag type III, the probability of a type I province transitioning upward to type II is 0.140, while a type III province has a 0.227 probability of moving upward to type IV, highlighting the significant improvement potential for provinces in type III. Conversely, in spatial lag type IV, the probability of a type II province transitioning upward to type III is 0.250, while the downward transition probability for highefficiency provinces in type IV is 0.190, demonstrating that highefficiency provinces show strong resistance to decline, maintaining relatively stable efficiency. These findings indicate that ecological efficiency transitions under different lag states are strongly influenced by the current efficiency status of a province. Provinces in type II and III are at a critical point for upward transitions. If they can leverage external support, such as provinces' experiences and technological neighboring advancements, there is potential for overcoming existing bottlenecks. On the other hand, provinces in type IV exhibit strong stability and low transition risks.

Overall, the Markov chain analysis of FEPVRE suggests that most provinces maintain their efficiency levels, but provinces in the intermediate efficiency range have significant upward mobility potential. Future research should explore the factors driving these transitions and identify the elements contributing to upward

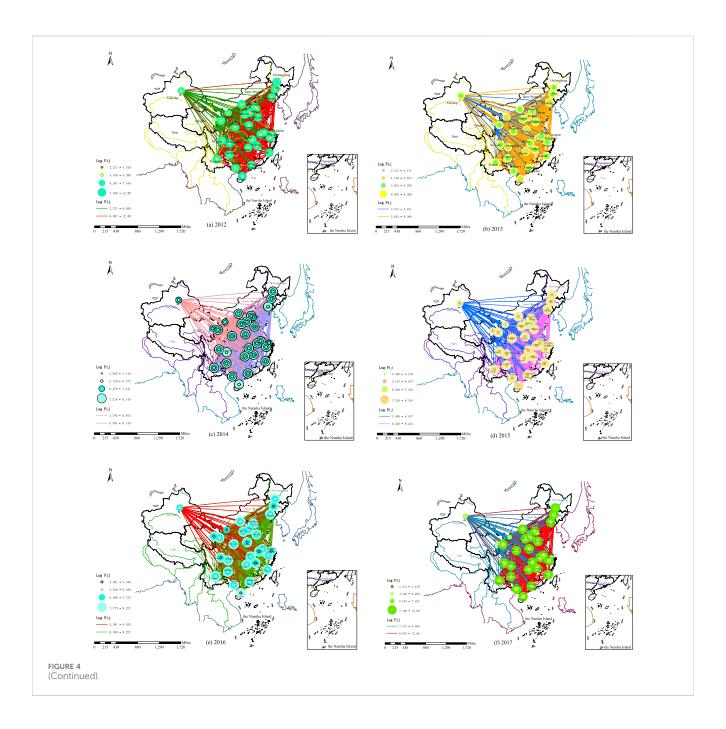


mobility. Policymakers can use these insights to support provinces with improvement potential through targeted interventions.

4.5 Regional disparity analysis

The analysis of the FEPVRE Gini coefficient (GT) from 2012 to 2022 reveals significant regional disparities across China, reflecting the dynamic interaction of political, economic, and social factors that influence forest ecosystem product value realization efficiency. The following sections provide an overview of national trends and a detailed regional analysis, comparing the development trends in the Eastern, Central, Western, and Northeastern regions. Nationally, the Gini coefficient fluctuated, starting at 0.592 in 2012 and decreasing steadily to 0.417 by 2015, signaling a narrowing of regional disparities. However, from 2015 to 2021, the coefficient rose to 0.572, indicating an increase in the regional gap. In 2022, it dropped to 0.485, reflecting some improvement, particularly in the central and western regions, due to policy interventions. In the Eastern region, the Gini coefficient continuously improved, declining from 0.217 in 2012 to 0.148 in 2022, driven by investments in green technology and infrastructure. In contrast, the Western region experienced significant fluctuations, rising from 0.494 in 2012 to 0.574 in 2022. This reflects challenges like underdeveloped infrastructure, slower economic growth, and limited technological innovation. The Central region had moderate fluctuations, with its Gini coefficient moving from 0.244 in 2012 to 0.283 in 2022, showing gradual progress despite challenges in infrastructure and industrial development. The Northeastern region exhibited large fluctuations, with the Gini coefficient peaking at 0.644 in 2013, then dropping to 0.310 in 2014, and stabilizing at 0.428 by 2022, highlighting struggles with industrial restructuring and the slow transition to green industries. In conclusion, while the Eastern region has made significant progress, other regions like the Western and Northeastern areas continue to face substantial challenges in improving FEPVRE. This underscores the need for targeted policies and investments in green technologies and infrastructure to foster more balanced and sustainable development across the country, as shown in Figure 7.

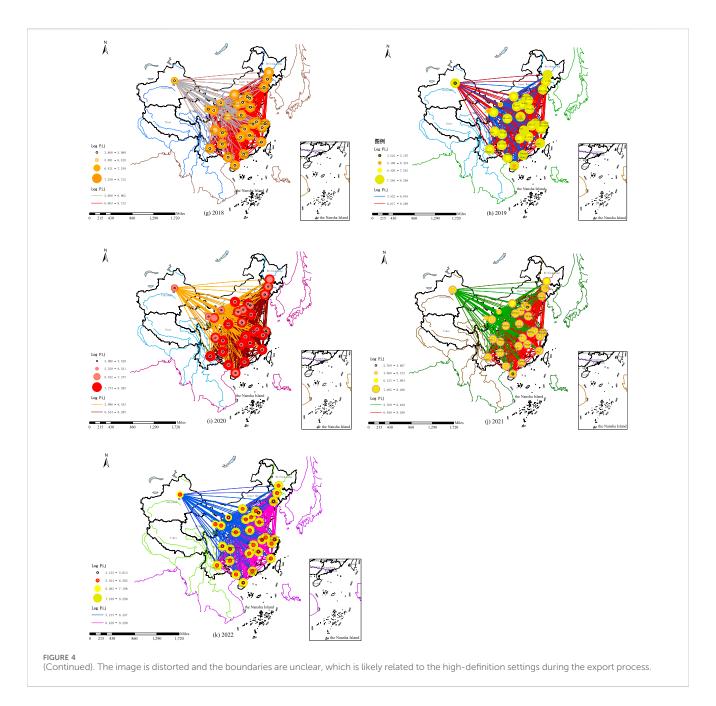
The decomposition of the Gini coefficient for FEPVRE highlights the key sources of regional disparities. The value of Gw has remained relatively stable, starting at 0.136 in 2012, peaking at 0.138 in 2021, and decreasing to 0.120 in 2022. This suggests that regional disparities have fluctuated only slightly during the study period. The stability of Gw indicates that, despite minor changes in regional balance, the efficiency of forest ecosystem product utilization within regions has generally remained consistent. Contributing factors could include policies promoting more equitable resource distribution and improvements in ecological protection measures, although localized disparities still exist. Gnb shows a fluctuating pattern, starting at 0.394 in 2012 and gradually decreasing to 0.244 by 2022, with a peak of 0.357 in 2021. The decreasing trend of Gnb after 2020 indicates some success in efforts to reduce regional disparities in FEPVRE, particularly in improving the performance of less efficient regions. Policies supporting the digital economy, ecological development, and technological advancements have positively impacted lowefficiency regions, helping reduce the gap. However, the sharp rise in Gnb in 2021 suggests that regional disparities intensified, possibly due to uneven technological adoption or industrial development. Gt fluctuated during the period, starting at 0.0628 in 2012, rising to 0.139 in 2019, and gradually decreasing to 0.121 by 2022. Gt peaked at 0.139 in 2019, followed by a decline in 2020 and 2021. While Gt reflects disparities between high-efficiency and low-efficiency regions, its changes more directly reflect structural differences, particularly in resource distribution and



technology adoption. The fluctuations in Gt highlight the gap between leading and lagging regions, while Gnb emphasizes the fundamental disparities between regions and the improvements driven by policy interventions, as shown in Figure 8.

The within-group Gini changes from 2012 to 2022 (Table 8) reveal fluctuating trends in FEPVRE across China, reflecting the changing nature of internal disparities within regions at different stages. In the eastern region, the within-group Gini coefficient gradually decreased from 2012 to 2015, indicating a narrowing of internal disparities and an improvement in internal balance. However, from 2016 to 2021, the Gini coefficient began to rise, reflecting fluctuating internal disparities due to unbalanced ecological protection and resource management. The central region showed relatively stable changes in the within-group Gini

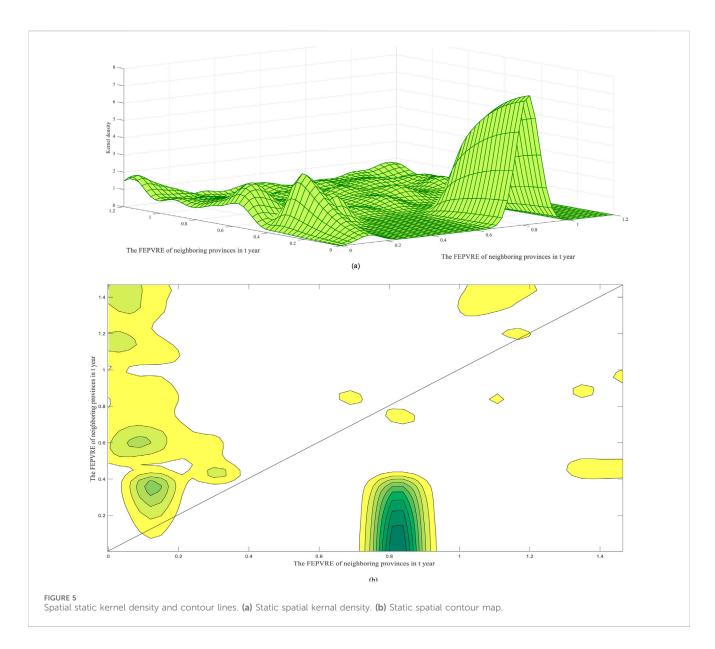
but experienced a slight upward fluctuation from 2016 to 2022, suggesting that internal disparities in this region have slightly intensified. This can be attributed to uneven economic development in some provinces, widening internal disparities. The western region exhibited large fluctuations in the withingroup Gini coefficient, initially decreasing and then increasing. This pattern indicates that internal differences in FEPVRE in the western region narrowed at first, but expanded after the disruptions caused by the 2019 pandemic, highlighting significant internal disparities. The northeastern region showed large fluctuations from 2012 to 2015, with a decrease and peak in 2018. This indicates intensifying internal disparities, and while the internal FEPVRE improved by 2022, it remained in a state of significant disparity, suggesting a lag in the development resources required.



Overall, the Gini analysis reveals growing regional disparities in FEPVRE, with widening gaps between the Eastern, Western, and Northeastern regions. Policymakers should focus on closing these gaps through green policies, equitable investment distribution, and enhanced cross-regional collaboration to promote more balanced and sustainable development.

As inter-group differences are the primary source of regional disparities, this section analyzes the trend in inter-group Gini across regions to reflect dynamic disparities in FEPVRE in China. The results, shown in Table 9, reveal that from 2012 to 2022, the intergroup Gini between the Eastern region and the Central, Western, and Northeastern regions exhibited an overall downward trend. In contrast, the inter-group Gini between the Central and Western, Central and Northeastern, and Western and Northeastern regions showed an increasing trend, indicating significant and uneven

disparities. From 2012 to 2015, the inter-group Gini between the Eastern and Central regions continued to decrease, with slight rebounds in 2016 and 2021 before decreasing again, signaling a gradual narrowing of the gap between these regions. The inter-group Gini between the Eastern and Western regions also showed a decreasing trend from 2012 to 2022, though the gap between the Central and Western regions remained larger. Meanwhile, the intergroup Gini between the Eastern and Northeastern regions was higher, reflecting greater differences in FEPVRE between these regions. However, their regional development remained more stable than that between the Eastern and Western regions. From 2013 to 2018, the inter-group Gini between the Central and Western regions showed a fluctuating downward trend, followed by a rapid increase until 2022. Despite this, the inter-group Gini between the Central and Western regions was much lower than that between the



Eastern and Western regions, indicating that the Eastern region's FEPVRE is higher than those of the Central and Western regions, with a larger gap. The inter-group Gini between the Central and Northeastern regions showed slow, fluctuating growth, while the inter-group Gini between the Western and Northeastern regions was higher, suggesting that the gap between the Central and Northeastern regions was smaller than the gap between the Western and Northeastern regions.

4.6 QAP analysis

4.6.1 QAP correlation analysis

To explore the key factors contributing to regional differences in FEPVRE, the QAP method was applied. This method is particularly effective for examining spatial relationships and dependencies between variables, allowing for a deeper understanding of how factors such as T, O, and E contribute to regional disparities in FEPVRE. The results of the analysis are presented in Table 10. Based on the QAP correlation

analysis for the entire sample period (2012-2022), the results show that the correlation coefficients between FEPVRE and T, urbanization level, economic development level, and infrastructure level are positive. In contrast, the correlation coefficients between FEPVRE and O, E, fiscal expenditure, and technological innovation level are negative, suggesting that these factors are inversely related to FEPVRE in the studied regions. Specifically, T and economic development level (with a coefficient of 0.512) show significant positive correlations with FEPVRE, indicating that technological progress and economic growth are key drivers of FEPVRE across regions. Conversely, the negative correlation between FEPVRE and O and E suggests that organizational and environmental factors, such as regional policy alignment or ecological protection practices, can hinder forest ecosystem product efficiency in some areas. Significant intercorrelations were observed among variables. For example, O, E, technological innovation, economic development, infrastructure, and fiscal expenditure are closely related, demonstrating their collective influence on regional differences in FEPVRE. Notably, infrastructure level and fiscal expenditure are strongly correlated with urbanization, implying that urban development plays a critical role in

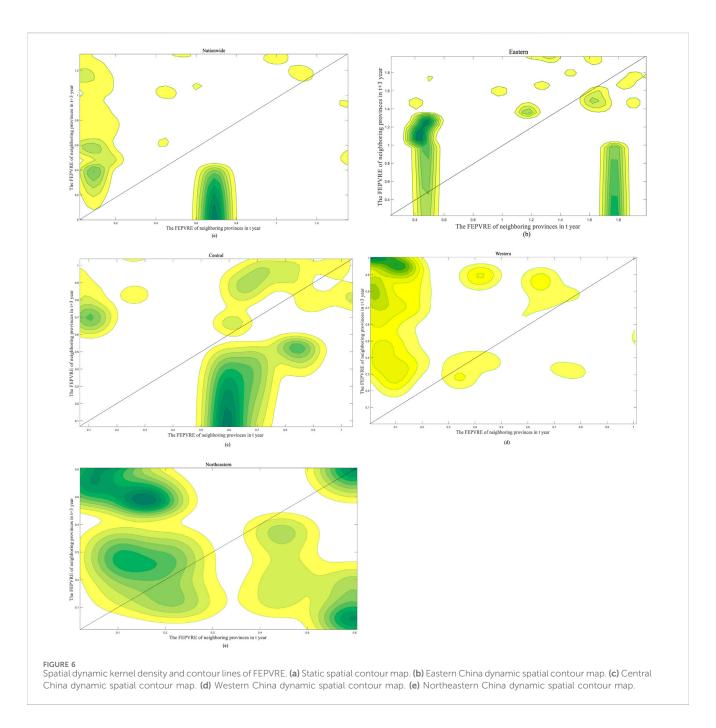


TABLE 6 Transition probabilities of the traditional Markov chain from 2012 to 2022.

t/t+1			Ш	IV	Observations
I	0.789	0.079	0.105	0.026	76
II	0.125	0.6625	0.1875	0.025	80
III	0.067	0.16	0.547	0.227	75
IV	0.038	0.025	0.190	0.747	79

shaping the efficiency of the forest ecosystem. To address multicollinearity and ensure the reliability of the results, a QAP regression analysis was performed. This analysis helped isolate the

effects of T, O, and E, providing a clearer understanding of their individual contributions to regional disparities in FEPVRE.

In summary, the QAP method is crucial for analyzing the impact of T, O, and E on regional differences in FEPVRE. It offers valuable insights into how these factors interact and influence the efficiency of forest ecosystem products. The regression analysis will further clarify the causal relationships and highlight the importance of each factor in driving FEPVRE disparities.

4.6.2 QAP regression analysis

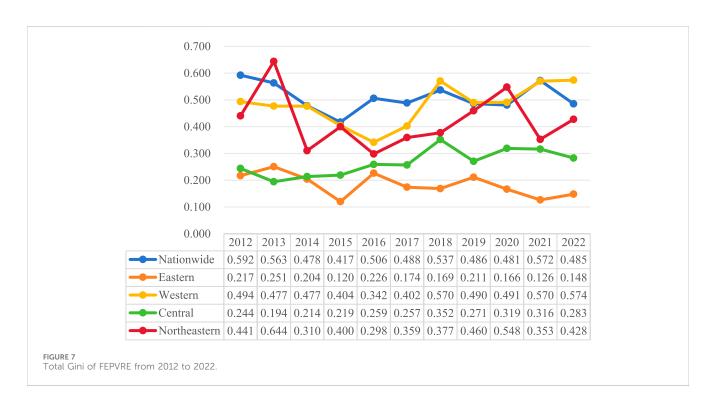
As digital technology is a primary factor influencing the efficiency of FEPVRE, this study further examines the impact of various factors on regional disparities in FEPVRE using QAP regression analysis. The QAP method, a statistical tool used to

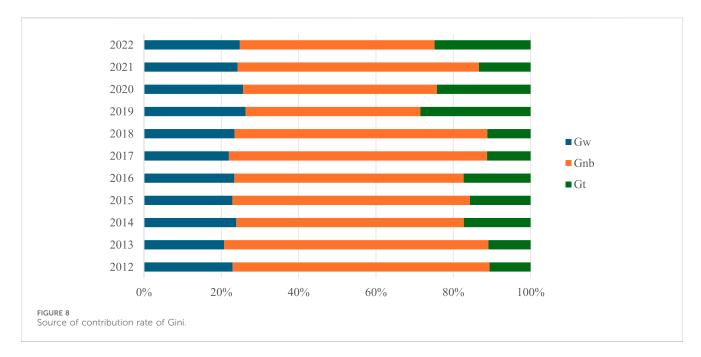
TABLE 7 Spatial Markov chain transition matrix (2012-2022).

Spa lag	itial type	I	II	III	IV	Observations
I	I	0.789	0.079	0.105	0.026	76
	II	0.125	0.663	0.188	0.025	80
	III	0.067	0.16	0.547	0.227	75
	IV	0.038	0.025	0.190	0.747	79
II	I	0.000	0.000	0.000	0.000	0
	II	0.000	0.000	0.000	0.000	0
	III	0.000	0.000	0.000	0.000	0
	IV	0.000	0.000	0.000	0.000	0
III	I	0.865	0.027	0.081	0.027	37
	II	0.140	0.721	0.140	0.000	43
	III	0.045	0.227	0.636	0.091	22
	IV	0.100	0.000	0.100	0.800	10
IV	I	0.743	0.143	0.086	0.029	35
	II	0.107	0.571	0.250	0.071	28
	III	0.069	0.138	0.586	0.207	29
	IV	0.030	0.061	0.152	0.758	33

analyze the correlation and dependencies among spatial data, is particularly suitable for understanding how T, O, and E contribute to the regional disparities in FEPVRE. By applying QAP regression, we can isolate and evaluate the effects of each of these factors on regional differences in FEPVRE. The QAP regression results for the

entire sample period (2012-2022) are shown in Table 11. The standardized coefficient for T is 0.581, statistically significant at the 10% level, indicating that the imbalance in digital technology across regions contributes to the widening of regional disparities in FEPVRE. In contrast, the standardized regression coefficients for O and E are -0.157 and -0.326, respectively, both significant at the 5% level. These results suggest that regional differences in digital industry and digital environment help reduce regional disparities in FEPVRE. Specifically, the regional gap in T positively affects regional disparities in FEPVRE, highlighting the role of digital technology in enhancing efficiency. On the other hand, the regional gaps in O and E have a negative impact, implying that the current development of the digital economy in these regions has not effectively addressed the needs of FEPVRE. Factors such as structural mismatches, low levels of innovation, policy gaps, and institutional barriers contribute to this issue. Among the control variables, the standardized regression coefficient for economic development level is 0.701, significant at the 5% level, suggesting that regional disparities in economic development positively influence regional disparities in FEPVRE. Reducing the imbalance in economic development across regions is an effective way to narrow the regional disparities in FEPVRE. In terms of impact, the influence of economic development on FEPVRE is greater than that of the digital economy. From the full-sample regression results, urbanization level, fiscal expenditure scale, and technological innovation level are not statistically significant. Regarding model fit, the adjusted R² is 0.552, passing the 1% significance level test, indicating that the selected variables can explain 55.2% of the causes of regional disparities in FEPVRE in China. The results of this study have significant practical implications for policymakers and stakeholders. Given the importance of FEPVRE for sustainable regional development, policymakers should focus on improving digital infrastructure





and green technologies, particularly in regions where efficiency remains low. Additionally, targeted support, such as subsidies for green industries and improved resource management systems, could help bridge regional gaps in efficiency. Stakeholders should also invest in capacity-building programs for the Western and Northeastern regions to foster green innovation.

5 Analysis of the factors influencing the FEPVRE in China

5.1 Selection of spatial econometric model

The spatial autocorrelation test was conducted using Moran's I index, which yielded a value of 0.600, indicating a positive spatial effect. This result is statistically significant at the 1% level, suggesting that from 2012 to 2022, there is a positive spatial effect on the FEPVRE. Therefore, spatial variables are introduced for further analysis, as shown in Table 12.

To further investigate the influencing factors of the spatiotemporal FEPVRE in various provinces and municipalities of China, three spatial weight matrices are constructed: the spatial adjacency weight matrix, the digital finance weight matrix, and the economic geography weight matrix.

The spatial distance weight matrix is calculated using the latitude and longitude of different provinces, measuring the square of the geographical distance between provinces. d_{ij}^2 represents the square of the geographical distance between two provinces. The Formula 20 for the spatial distance weight matrix is expressed as:

$$W_{ij} = \frac{1}{\left|\bar{D}_i - \bar{D}_j\right|} \left(i \neq j\right) \tag{20}$$

The spatial adjacency weight matrix is the reciprocal of the square of the geographical distance between the central cities of different provinces in China. This matrix is used to determine the adjacency relationship between regions. The distance between region i and region j is denoted by d_{ij} . The Formula 21 for the spatial adjacency weight matrix is expressed as:

$$W_{ij} = \begin{cases} 1 & d_{ij} < d \\ 0 & d_{ij} \ge d \end{cases}$$
 (21)

The digital economy spatial weight matrix, by analyzing the spatial interactions between digital economy and geographical factors on FEPVRE, helps to understand how the digital economy drives regional green transformation through spatial spillover effects. This matrix provides a quantitative tool for analyzing the mutual influences between different regions, particularly in the context of significant differences in digital economy levels, revealing the spatial disparities in green economic transformation. In turn, it supports the formulation of more targeted policies, promoting the coordinated and sustainable development of green economy across regions in China. The Digital Economy Spatial Weight Matrix W_{ij} is obtained by the product of the digital economy composite index and the square of the geographical distance. Each element W_{ij} in the matrix represents the mutual influence intensity between region i and region j. The digital economy composite index DEI is calculated through the entropy method, using multiple digital economy indicators such as the scale of mobile phone facilities, the length of long-distance optical fiber cables, the number of web pages, the number of domain names, information transmission capacity, the number of legal entities in software and information technology services, the number of domestic patent applications, and digital inclusive finance. Geographical distance d_{ij} is a key factor in measuring the spatial relationships between different regions. In this paper, the geographical distance is calculated based on the latitude and longitude distances between provinces and cities. The Digital Economy Spatial Weight Matrix is obtained by the product of the digital economy composite index and the square of the geographical distance. The calculation Formula 22 is as follows:

TABLE 8 Within-group Gini coefficient.

Year	Eastern region	Central region	Western region	Northeastern region
2012	0.438	0.244	0.441	0.535
2013	0.372	0.275	0.644	0.520
2014	0.353	0.282	0.515	0.310
2015	0.259	0.294	0.450	0.400
2016	0.374	0.390	0.410	0.298
2017	0.289	0.349	0.469	0.359
2018	0.374	0.352	0.377	0.601
2019	0.346	0.271	0.578	0.460
2020	0.289	0.319	0.578	0.548
2021	0.385	0.364	0.645	0.353
2022	0.282	0.362	0.651	0.428

TABLE 9 Inter-group Gini.

	J .					
Year	Eastern & central	Eastern & western	Eastern & northeastern	Central & western	Central & northeastern	Western & northeastern
2012	0.618	0.729	0.743	0.381	0.451	0.524
2013	0.481	0.743	0.748	0.568	0.534	0.657
2014	0.390	0.613	0.604	0.480	0.434	0.447
2015	0.303	0.509	0.614	0.459	0.550	0.485
2016	0.537	0.612	0.685	0.435	0.428	0.418
2017	0.478	0.578	0.789	0.441	0.588	0.574
2018	0.493	0.579	0.685	0.399	0.537	0.519
2019	0.464	0.554	0.551	0.479	0.420	0.547
2020	0.441	0.514	0.681	0.507	0.540	0.652
2021	0.537	0.665	0.783	0.568	0.550	0.675
2022	0.378	0.579	0.528	0.567	0.477	0.588

$$W_{ij} = \begin{cases} \frac{DEI_i \cdot DEI_j}{d_{ij}^2} & i \neq j \\ 0 & i = j \end{cases}$$
 (22)

The SDM, SAR, and SEM are three commonly used spatial econometric models. For the purpose of model selection and assessing spatial dependence, spatial distance weight matrix, the spatial adjacency weight matrix and the digital economy spatial weight matrix were employed to properly assess the spatial dependence in the model selection, and the LM error and LR are performed. These tests are crucial in diagnosing whether spatial dependence exists and determining which form of dependence—error or lag—is more significant. The LM and the LR p-values for all three matrices are below the 10%, 5% and 1% significance levels, indicating the presence of spatial dependence and confirming that the models pass the significance test. In addition, Wald tests are conducted to further refine the model selection. These

tests evaluate the adequacy of the selected models by testing the null hypothesis regarding the restrictions on the coefficients. The Wald test results for all three spatial weight matrices show strong significance, providing additional confirmation of the robustness of the chosen models. This combination of LM, LR, and Wald tests ensures the appropriate selection of the most suitable spatial econometric model for analyzing spatial dependence in the context of FEPVRE. As shown in Table 13.

In the robustness test of spatial effects in Table 13, both the SEM and the SAR were applied to test spatial effects under different spatial weight matrices. For the Spatial Distance Weight Matrix, both the Lagrange Multiplier (LM) test for spatial error and the LM test for spatial lag are significant at the 1% level, indicating the presence of both spatial error and spatial lag effects. This suggests that a combination of the SEM and SAR models would be appropriate. Given the presence of both effects, the SDM, which combines features of both the SEM and SAR models, is selected as

TABLE 10 QAP correlation results.

Variables	Υ	X ₁	X ₂	X ₃	A ₁	A ₂	A ₃	A ₄	A ₅
Y	1	0.286	-0.113	-0.093	0.32	0.512	0.542	-0.533	-0.016
X_1	0.286	1	0.741	0.651	0.34	0.213	0.102	-0.012	0.109
X_2	-0.113	0.741	1	0.9	0.299	0.072	-0.163	0.451	0.126
X_3	-0.093	0.651	0.9	1	0.498	0.257	-0.042	0.277	-0.206
A_1	0.32	0.34	0.299	0.498	1	0.878	0.404	-0.305	-0.53
A_2	0.512	0.213	0.072	0.257	0.878	1	0.545	-0.529	-0.397
A_3	0.542	0.102	-0.163	-0.042	0.404	0.545	1	-0.605	-0.079
A_4	-0.533	-0.012	0.451	0.277	-0.305	-0.529	-0.605	1	0.241
A ₅	-0.016	0.109	0.126	-0.206	-0.53	-0.397	-0.079	0.241	1

the most suitable model for this matrix. Additionally, the LR test for SAR and LR test for SEM are significant at the 5% level, confirming that the SDM cannot degrade into either the SAR or SEM models. This result is consistent with the Wald test, further validating the use of the SDM for the Spatial Distance Weight Matrix. Contrast, the Spatial Adjacency Weight Matrix and the Digital Economy Geographic Weight Matrix are best modeled by the SAR, but the reasoning behind the model selection differs. For the Spatial Adjacency Weight Matrix, the LM test for spatial error is significant at the 10% level, while the LM test for spatial lag is highly significant at the 1% level. These results indicate the presence of both spatial error and spatial lag effects, making it suitable to apply both SEM and SAR. Since both models are relevant, the SDM, which combines features of both, is the best choice. However, the LR test for SAR and SEM for the Spatial Adjacency Weight Matrix are not significant at the 10% level, supporting the null hypothesis that the SDM can be simplified to either SAR or SEM. This aligns with the Wald test results, confirming that either model could be chosen. Since the LM test for SAR yields a more rational result, the SAR model is considered the most appropriate for this matrix. For the Digital Economy Geographic Weight Matrix, the LM test for the Lagrange multiplier is not significant at the 5% level (p > 0.05), while the LM test for spatial lag is highly significant at the 1% level (p < 0.01), indicating that the spatial lag effect is dominant. Therefore, the SAR model is more suitable for this matrix. Furthermore, the LR test for SAR and SEM for the Digital Economy Geographic Weight Matrix are both insignificant at the 10% level, supporting the hypothesis that the SDM can be simplified to the SAR model. This is consistent with the results from the Wald test for SAR and SEM, which also suggest that the SAR model is the most appropriate choice.

5.2 Measurement results

Using Stata 15 software, the random effects model, time fixed effects model, and double fixed effects model were estimated, incorporating the three spatial weight matrices into the spatial econometric models. The calculation results are shown in Table 14.

The Hausman test results confirm that the fixed effects model is the most suitable for all three spatial weight matrices—spatial distance, spatial adjacency, and digital economy geographic matrices. With a p-value of 0.000, the fixed effects model is preferred over the random effects model due to significant differences in coefficients and standard errors. The time fixed effects model is better suited for capturing temporal variations in FEPVRE, effectively controlling for time-specific factors, while the two-way fixed effects model, though capable of considering both regional and time effects, is more complex and less precise. In the Spatial Distance Weight Matrix's double fixed effects model, the LogL is -94.252, indicating a good fit. The coefficient for λ is -0.048, statistically significant at the 5% level, and the R-squared value is 0.073, suggesting reasonable reliability for this model. The coefficients for the TOE variables show that both T and E have negative coefficients with respect to FEPVRE, indicating that digital technology and the digital environment exhibit negative spillover effects. In contrast, O has a positive coefficient of 0.951, suggesting a positive spillover effect of the digital industry on FEPVRE. This suggests that weak technology adoption and environmental adaptability hinder the benefits from technological and environmental improvements, potentially causing negative spillover effects due to the unequal distribution of digital infrastructure, technology access, and policy support. On the other hand, digital industries, especially green technology innovation, positively impact green transformation. When developed in certain regions, digital industries not only enhance local green transformation but also promote it in neighboring areas through spillover effects. Therefore, policies should focus on supporting digital industries in less efficient regions to improve overall green economic performance. The maximum LogL values for the Spatial Adjacency Weight Matrix and the Digital Economy Geographic Weight Matrix are -111.685 and -97.652, respectively, with λ values of 0.370 and -0.091, and σ^2 values of 0.219 and 0.236. The p-values are significant at the 1% level, indicating that the SAR model fits the data well. In both matrices, the effects of digital technology and the digital industry on FEPVRE exhibit positive spatial spillover effects, while the impact of the digital environment shows negative spatial spillover effects. These negative effects tend to weaken over time. This suggests that digital technology and industries generate positive spillover effects on FEPVRE, driving green transformation in neighboring regions through technological diffusion and industrial chain collaboration.

TABLE 11 QAP regression results.

Independent	Un-stdized coefficient	Stdized coefficient	Significance	As large	As large			
X1	9.435	0.581	0.010	0.010	0.991			
X2	-2.445	-0.157	0.401	0.599	0.401			
Х3	-4.358	-0.326	0.233	0.767	0.233			
a1	-1.816	-0.395	0.149	0.852	0.149			
a2	0.981	0.701	0.023	0.023	0.977			
a3	0.241	0.245	0.077	0.077	0.924			
a4	0.222	0.046	0.413	0.413	0.587			
a5	-0.109	-0.050	0.421	0.579	0.421			
Intercept	-0.012	0.000						
R-square		0.556						
Adj R-Sqr		0.552(0.000)						
obs		870						

TABLE 12 Moran's I index results for one-time output from 2012 to 2022.

Year	- 1	E(I)	Sd(I)	z	p-value
2012	0.189	-0.034	0.097	2.290	0.022
2013	0.229	-0.034	0.095	2.760	0.006
2014	0.229	-0.034	0.098	2.700	0.007
2015	0.373	-0.034	0.097	4.198	0.000
2016	-0.010	-0.034	0.097	0.256	0.798
2017	0.159	-0.034	0.094	2.061	0.039
2018	0.282	-0.034	0.097	3.269	0.001
2019	0.272	-0.034	0.098	3.137	0.002
2020	0.385	-0.034	0.097	4.315	0.000
2021	0.313	-0.034	0.098	3.554	0.000
2022	0.375	-0.034	0.098	4.196	0.000

Conversely, the digital environment causes negative spillover effects, mainly due to the environmental burdens and resource distribution imbalances associated with digitalization. Over time, policy adjustments and technological advancements help mitigate these negative effects, promoting a more sustainable green transformation.

5.3 Heterogeneity analysis

To explore the impact of T, O, and E on FEPVRE across different regions, China's provinces are categorized into four regions: Eastern, Central, Western, and Northeastern. The analysis reveals significant regional disparities in FEPVRE, with the Eastern region exhibiting higher efficiency levels compared to the Western and Northeastern regions. These disparities reflect the complex interaction of technological, organizational, and environmental factors, as

supported by ecological economics and Green Growth theories. The calculation results show that the SDM model for the Spatial Distance Weight Matrix has relatively high LogL and R-square values for all four regions, indicating a good model fit. Similarly, the Spatial Adjacency Weight Matrix and Digital Economy Geographic Weight Matrix also show higher LogL and R-square values, suggesting a good fit for the SAR model. The spatial autoregressive coefficients are significant at the 10%, 5%, and 1% levels, further validating the appropriateness of these models, as shown in Table 15.

In the Spatial Distance Weight Matrix, T and E exhibit negative spillover effects on FEPVRE in the Eastern and Western regions, while showing positive spillover effects in the Central and Northeastern regions. O only has a negative spillover effect in the Central region, with positive spillover effects in all other regions. The Eastern and Western regions face challenges in digital green transformation due to technology adoption gaps, inadequate infrastructure, and regional resistance, which hinder FEPVRE. In contrast, the Central and Northeastern regions benefit from better integration of digital technologies and sustainable policies, leading to positive spillover effects and stronger FEPVRE. Digital industry shows a negative spillover effect only in the Central region, possibly due to industrial overcapacity or lack of green innovation. The Central region should focus on fostering green digital innovation, while other regions can scale up digital industry growth with a sustainability focus. In the Spatial Adjacency Weight Matrix, T generates negative spillover effects on FEPVRE in the Eastern and Western regions, while generating positive spillover effects in the Central and Northeastern regions. This is primarily due to uneven technology diffusion and industrial structure differences, with lower technology adoption rates in some areas of the Eastern region, limiting the positive impacts of digital technology. In the Western region, infrastructure deficiencies and delays in technological innovation hinder effective diffusion, restricting the green transformation of surrounding areas. In contrast, O shows positive spillover effects on FEPVRE across all regions, promoting green industry development and enhancing forest ecosystem product value, particularly in the Central, Eastern,

TABLE 13 Spatial econometric model selection.

Test method	Spatial distance weight matrix			Spatial adjacency weight matrix			Digital economy geographic weight matrix			
	Statistic	df	р	Statistic	df	р	Statistic	df	р	
Spatial error:										
Moran's I	3.479	1	0.001	1.740	1	0.082	1.720	1	0.085	
Lagrange multiplier	8.869	1	0.003	33.018	8 1 0.000		1.705	1	0.192	
Robust Lagrange multiplier	4.468 1 0.035		42.567	2.567 1 0.000		7.511	1	0.006		
Spatial lag:							1			
Lagrange multiplier	15.571	1	0.000	2.610	1	0.000	7.319	1	0.007	
Robust Lagrange multiplier	11.170	1	0.001	12.160	1	0.002	13.125	1	0.000	
Hausman test	0.10			2.19			-7.63			
Wald test for SAR	0.011			0.135			0.130			
Wald test for SEM	0.011			0.119			0.124			
LR test for SAR	0.014			0.144			0.139			
LR test for SEM	0.013			0.122			0.131			
Model Selection	SDM/SEM/SAR			SDM/SEM/SAR			SAR			
Model Specification	SDM			SAR			SAR			

Northeastern, and Western regions. However, E produces negative spillover effects across all regions, mainly because digitalization has exacerbated resource over-exploitation and ecological pressure, especially in digital infrastructure construction. Uneven distribution of environmental resources and a lack of sustainable management have intensified environmental burdens, hindering improvements in FEPVRE.

In the Digital Economy Geographic Weight Matrix, O exhibits negative spillover effects in the Central region, while showing positive effects in other regions. Conversely, T has a positive spillover effect in the Central region but negative spillover effects in other regions. This highlights that regional disparities in digital development and green transformation are influenced by varying spillover effects. In the Central region, where digital infrastructure and technology adoption lag, negative spillovers reflect barriers such as resource inequality, technological gaps, and lack of green innovation. In contrast, the Eastern and Western regions benefit from positive spillovers, indicating better integration of digital solutions aligned with green transformation goals. The negative spillover effect of the digital environment across regions suggests challenges in leveraging environmental improvements, often hindered by insufficient ecological policies and uneven resource distribution. Therefore, regions with negative spillovers should focus on improving digital infrastructure, adopting green technologies, and implementing region-specific innovations to enhance FEPVRE.

5.4 Robustness test

To verify the reliability and stability of the conclusions regarding the impact of T, O, and E on FEPVRE, robustness tests are

conducted using multiple spatial weight matrices. The LM test, Wald test, Hausman test, and LR test are employed to evaluate the stability and robustness of the spatial econometric models (Zheng et al., 2025). These tests assess whether the results remain consistent across different spatial structures and model specifications.

First, the LM and LR test results are compared using the spatial distance weight matrix, spatial adjacency weight matrix, and digital economy geographic matrix. The p-values for these tests are all below 5%, 10% or 1%, confirming that the Spatial Distance Weight Matrix is best modeled by the SDM model, while the Spatial Adjacency Weight Matrix and Digital Economy Geographic Weight Matrix are best modeled by the SAR model, effectively capturing spatial dependencies in all three matrices. The LM test diagnoses spatial dependence due to error correlations, while the LR test assesses lag dependence across regions. Both tests help identify the nature of spatial relationships, thereby refining the choice of the spatial econometric model. Specifically, for the Spatial Distance Matrix, the LM test for both Spatial Error and Spatial Lag shows p-values below 1%. For the Spatial Adjacency Matrix, the LR test results for both SEM and SAR are significant at the 5% level, consistent with the Wald test conclusions, rejecting the possibility of the SDM degenerating into the SEM or SAR models. The Digital Economy Geographic Matrix shows that the LM test for Spatial Lag is significant below the 1% level, and both the LR and Wald tests support the SDM degenerating into the SAR model, further confirming the applicability of the SAR model for all regions. Although the LM test for the Spatial Adjacency Weight Matrix initially suggests the SDM model, the LR and Wald test results are not significant at the 10% level, supporting the selection of the SEM and SAR models. Next, the Hausman test is conducted to compare the fixed effects model and the random effects model. The statistics

TABLE 14 Measurement results.

Variable	Spatial di	stance weig	ht matrix	Spatial adj	jacency weig	ght matrix	Digital economy geographic weight matrix			
	Ind	Time	Both	Ind	Time	Both	Ind	Time	Both	
Т	0.053 (0.14)	0.148 (0.280)	-0.065 (-0.170)	0.326 (1.130)	0.576 (1.300)	0.384 (1.270)	0.179 (0.550)	0.712 (1.510)	0.024 (0.070)	
O	0.752 (1.54)	0.880 (1.26)	0.951 (1.960)	0.513 (1.340)	0.479 (0.860)	0.459 (1.140)	0.477 (1.200)	0.469 (0.810)	0.663 (1.660)	
Е	-0.411 (-1.05)	-0.517 (-0.940)	-0.461 (-1.200)	-0.654** (-1.920)	-0.887* (-1.830)	-0.630* (-1.770)	-0.529 (-1.460)	-1.006 (-1.920)	-0.602 (-1.660)	
Control Variables	yes	yes	yes							
λ	0.031 (0.320)	0.195* (2.050)	-0.048 (-0.480)	0.027 (0.350)	0.370*** (6.200)	0.111 (1.470)	0.004 (0.040)	0.054 (0.500)	-0.091 (-0.850)	
σ2	0.109*** (12.840)	0.225*** (12.790)	0.104*** (12.840)	0.115*** (12.840)	0.219*** (12.680)	0.127*** (12.190)	0.109*** (12.85)	0.236*** (12.84)	0.106*** (12.83)	
LogL	-102.773	-223.392	-94.252	-111.685	-223.038	-167.380	-102.950	-230.052	-97.652	

Note: denotes p < 0.1, ** denotes p < 0.05, *** denotes p < 0.01; standard errors are presented in parentheses; same below.

for the Spatial Distance Weight Matrix and the Spatial Adjacency Weight Matrix are positive, while the statistics for the Digital Economy Geographic Weight Matrix are negative. The prob>chi2 values for the Spatial Distance Matrix is 1.000, for the Spatial Adjacency Matrix is 0.975, and for the Digital Economy Geographic Matrix is 0.982. These results do not significantly support the null hypothesis, indicating that the random effects model is not appropriate.

6 Conclusion

Through SKDE, Markov chain analysis, and spatial Gini coefficient analysis of the FEPVRE across various provinces in China from 2012 to 2022, the following conclusions can be drawn:

1. From the perspective of super-efficiency, the average FEPVRE in China showed a fluctuating development trend between 2012 and 2022, with notable changes between 2014 and 2020. This fluctuation reflects the early stages of China's green transition, where ecological civilization strategies influenced efficiency variations. FEPVRE peaked in 2016 but then declined due to pressures from green transformation goals, which aligns with findings from previous studies (Liu et al., 2023). Regionally, the Eastern region demonstrates higher FEPVRE, while the Western and Northeastern regions show slower growth, confirming the convergence trend observed in earlier research (Xu and Ding, 2024). Policymakers should address these regional disparities by promoting green technologies and sustainable practices, especially in the Western and Northeastern regions, to overcome transitional challenges (Zhu et al., 2025). This study contributes theoretically by integrating economic, ecological, and technological factors into the FEPVRE evaluation, highlighting the importance of considering these dimensions when analyzing regional differences in forest ecosystem product efficiency. From a policy perspective, targeted

- interventions in underperforming regions are essential for achieving an inclusive green transformation and ensuring sustainable development.
- 2. From the perspective of spatial kernel density, FEPVRE in China shows a rightward shift and concentration, indicating a growing efficiency gap between high-efficiency and lowefficiency provinces. High-efficiency provinces exert spatial spillover effects on neighboring low-efficiency provinces (Cheng and Xiong, 2024), resulting in polarization between low-efficiency (Type I) and high-efficiency (Type IV) provinces, with intermediate regions (Types II and III) showing potential for upward mobility. These findings highlight that provinces in middle-efficiency categories have significant improvement potential, especially through crossregional cooperation and knowledge transfer, which can play a critical role in enhancing FEPVRE (Wolf et al., 2007). The theoretical contributions of this study emphasize the role of spatial spillover effects and inter-regional collaboration in improving FEPVRE. By integrating spatial dependencies with regional development strategies, this study provides a novel framework for addressing regional disparities. From a policy perspective, fostering cooperation between high- and low-efficiency provinces is crucial. Promoting knowledge transfer and resource sharing through cross-regional agreements is essential for enhancing FEPVRE and fostering more sustainable and balanced development across regions.
- 3. From the perspective of regional spatiotemporal development, significant disparities in FEPVRE across China highlight regional challenges, particularly the widening gap between the eastern, western, and northeastern provinces. The Gini analysis shows that the eastern region maintains relatively stable FEPVRE, while the western and northeastern regions experience larger fluctuations, especially post-2021. This reflects differences in policy, resource allocation, and industrial development speeds, consistent with previous research, which emphasizes the need for targeted policy interventions (Niu et al., 2024). To address these disparities,

TABLE 15 Heterogeneity measurement results for the eastern, central, western, and northeastern regions.

Variable	Eastern			Central			Western			Northeast		
	Spatial matrix	Adjacency matrix	Digital matrix	Spatial matrix	Adjacency matrix	Digital matrix	Spatial matrix	Adjacency matrix	Digital matrix	Spatial matrix	Adjacency matrix	Digital matrix
Т	-0.367 (-0.490)	-0.194 (-0.290)	-0.413 (-0.560)	0.223 (0.40)	1.157*** (2.760)	0.198 (0.360)	-0.808 (-1.72)	-0.398 (-0.820)	-0.264 (-0.540)	7.682 * (2.270)	0.661 (0.330)	-5.765** (-3.070)
0	0.806 (0.800)	1.572* (1.920)	1.575 (1.650)	-2.812*** (-3.29)	0.126 (0.150)	-2.147* (-2.230)	0.989 (1.480)	1.113 (1.490)	0.597 (0.730)	12.42*** (3.330)	3.312 (1.600)	23.160*** (7.500)
Е	-0.152 (-0.260)	-0.783 (-1.300)	-0.717 (-1.23)	1.202* (2.270)	-1.425*** (-2.850)	0.526 (0.940)	-0.136 (-0.190)	-0.624 (-0.880)	-0.370 (-0.520)	-9.322*** (-3.550)	-0.527 (-0.300)	-4.937** (-2.620)
Control Variables	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
λ	-0.149 (-1.140)	-0.022 (-0.210)	-0.009 (-0.060)	-0.856*** (-4.560)	0.207* (1.690)	-0.162 (-0.990)	-0.507** (-3.240)	-0.091 (-0.700)	-0.403** (-2.640)	-0.448* (-2.290)	-0.263 (-1.51)	-0.344 (-1.930)
σ2	0.096*** (7.380)	0.150*** (7.030)	0.096*** (7.420)	0.015*** (5.280)	0.043*** (5.410)	0.023*** (5.720)	0.070*** (7.740)	0.093*** (7.760)	0.077*** (7.540)	0.010*** (3.830)	0.035*** (3.990)	0.005*** (4.420)
LogL	-27.784	-61.962	-26.866	38.790	22.474	30.079	-15.306	-28.071	-18.666	26.544	7.485	20.672

Note: * denotes p < 0.1, ** denotes p < 0.05, *** denotes p < 0.01; Standard errors are in parentheses.

policymakers should prioritize promoting green industries, improving infrastructure, and encouraging digital technology adoption in the western and northeastern regions (Lu et al., 2025). Theoretical contributions from this study emphasize the importance of integrating spatiotemporal analysis with policy and technological factors to better understand FEPVRE. From a policy perspective, the findings underscore the need for strategies that narrow the efficiency gap and ensure sustainable forest management across regions. Future research should explore the long-term impacts of these disparities on the sustainability of China's forest resources.

- 4. The QAP analysis results show that digital technology significantly impacts FEPVRE, with regional variations in its effect. In the Eastern region, rapid digital technology development has led to resource misallocation, as observed in previous studies. Conversely, in the Northeastern region, digital technology positively impacts FEPVRE, driven by policy-led digitalization that optimizes resource use in traditional forestry (Yu et al., 2025). While the digital industry has positive effects in the Eastern and Northeastern regions, it shows negative impacts in the Central and Western regions, where infrastructure and ecosystem development are still evolving. These results highlight the importance of strong infrastructure and technology in improving FEPVRE, especially in less-developed areas. Additionally, the negative impact of the digital environment in some regions underscores the need for careful management of digital transformation to ensure sustainable forest resource management. Theoretical contributions of this study emphasize the complex relationship between digital technologies and FEPVRE, noting that integrating digitalization with traditional forestry practices can significantly improve resource utilization, particularly in regions with adequate technological infrastructure. From a policy perspective, the study suggests promoting digital technology adoption in underdeveloped regions, especially the Central and Western regions, while addressing infrastructural gaps. This approach will help improve FEPVRE and enhance the sustainability of forest ecosystems, contributing to green growth and ecological civilization goals.
- 5. The spatial econometric model results reveal significant regional differences in FEPVRE. In the Eastern and Northeastern regions, better digital infrastructure and policy support lead to positive spillover effects, enhancing FEPVRE. In contrast, the Central and Western regions face challenges due to slower technology adoption and inadequate digital infrastructure, resulting in negative spillover effects on FEPVRE. This aligns with previous research, which emphasizes that regions with established infrastructure experience more efficient resource utilization and greater FEPVRE. T and O are crucial for driving green transformation, but their impact varies across regions. The Central and Western regions show weaker spillover effects due to underdeveloped digital infrastructure and slower technology adoption (Thida et al., 2025). While the Eastern and Northeastern regions benefit from positive spillovers, the Central region needs targeted strategies to foster green

digital innovation. The negative spillover effects of the digital environment underscore the need for stronger ecological policies and balanced resource distribution. Slower technology adoption and inadequate infrastructure limit FEPVRE in these regions, as reflected in the negative impact of O on FEPVRE. Limited infrastructure in the Western region further hinders efficiency. The findings suggest that improving digital infrastructure and technology adoption, particularly in less-developed regions, is key to enhancing FEPVRE. This approach will promote regional cooperation, optimize resource use, and support green growth and ecological sustainability. Strengthening digital industries and environments will ensure more balanced and efficient forest ecosystem management.

6.1 Implications

- 1. There are significant disparities in FEPVRE across regions in China, particularly between the eastern and central/western regions. To promote a comprehensive regional green transformation, cross-provincial and cross-regional cooperation should be enhanced. This can be achieved through information sharing, technical support, and experience exchange. By learning from the successful experiences of more efficient regions, less efficient areas can improve their FEPVRE. In this context, leadership coaching can play a key role in fostering collaboration and enhancing team-level knowledge creation, ultimately supporting better environmental performance. Leadership coaching positively influences knowledge creation within teams, leading to improved environmental outcomes (Khan et al., 2024). By promoting such knowledge exchange, regions with lower FEPVRE can enhance their efficiency. Additionally, local regions should strengthen policy coordination between the eastern and central/western regions, increasing investment in green development technologies and financial support to accelerate the green transformation in the central and western regions. This approach will help narrow the regional disparities further.
- Promoting the green transformation and technological innovation in low-efficiency provinces is essential for improving FEPVRE. Technological progress plays a key role in driving FEPVRE, and sectoral differences significantly impact CO2 emissions and forest resource utilization. Specifically, the manufacturing and agriculture sectors contribute substantially to emissions, while the services sector has a more positive impact on FEPVRE (Khan et al., 2020). To address these challenges, policymakers should focus on encouraging technological innovation and green energy development in low-efficiency provinces, particularly those in the western and central regions. These provinces face significant barriers in improving ecological efficiency, and thus, financial subsidies, tax incentives, and other supportive policies are necessary to promote green industries. Additionally, efforts should be made to optimize production processes, enhance resource utilization, and adopt modern technologies in ecological product production. Strengthening

green technological innovation and infrastructure is crucial to boosting FEPVRE in these regions. By leveraging modern technology, improving resource efficiency, and promoting sustainable practices, low-efficiency provinces can accelerate their green transformation.

- 3. To improve regional differentiated green transformation strategies, national and local governments should tailor their approaches based on each province's resource endowment, economic foundation, and technological capabilities. For highefficiency provinces, particularly those in the eastern region, greater incentives for technological innovation and green development funds should be provided to promote advancements in ecological protection and green industries. In contrast, low-efficiency provinces in the western and central regions should receive targeted interventions that address their specific challenges. Drawing on principles of transformational leadership and green dedication, local governments in these low-efficiency regions should focus on enhancing employee and stakeholder engagement in green practices. This approach is crucial for fostering organizational commitment and improving green performance (Khan and Khan, 2022). By adopting these tailored strategies, regions can more effectively drive green transformation and narrow efficiency gaps across provinces.
- 4. To strengthen the incentive mechanism for the ecological products market, policymakers should refine market frameworks such as the carbon trading market, ecological compensation mechanisms, and the pricing system for green products. These adjustments will help ensure that the ecological values of forest products are accurately reflected in market prices. The Gini analysis and results from the Markov chain analysis indicate significant regional disparities in FEPVRE, which may stem from inadequate market pricing mechanisms and policy implementation gaps. Market-based incentive mechanisms should also encourage the sustainable use of forest resources and promote green investments. Future research could explore the long-term effects of these market incentives on FEPVRE and assess how such mechanisms can integrate forest products into both national and international green economy models.
- 5. To enhance the recognition of the green value and social cognition of forest ecological products, it is essential to raise awareness of their multidimensional value, such as carbon sequestration, ecological protection, and cultural services. Improving FEPVRE in China depends not only on technological and policy support but also on broad societal acceptance. The government can foster understanding and support for green FEPV through public education, active participation, and guidance on green consumption. Similar to consumer behavior in the hotel industry, factors like commitment, trust, and attitude significantly shape attitudes toward green products. These behaviors can greatly influence the societal recognition of ecological products. Additionally, strengthening public policy support for forest ecological products can increase public recognition of their value. By raising societal awareness of environmental sustainability, the government can drive green transformation, enhancing both the social value and economic benefits of forest ecological products.

6. The positive impact of digital technology and the negative role of digital environment misalignment on FEPVRE are crucial findings. However, further investigation into the reasons behind the negative impact of digital environment misalignment is necessary. Factors such as inadequate digital infrastructure, low digital literacy, and inefficient implementation of digital policies in certain regions may contribute to this issue. For example, regions with poor digital infrastructure may struggle to effectively use digital technologies, resulting in inefficiencies in forest ecosystem management. Additionally, a lack of digital skills and awareness can prevent local stakeholders from fully leveraging digital tools in forest resource management, exacerbating regional disparities. Misaligned digital policies that do not match local needs or capacities may also limit the effectiveness of digital technologies, reducing their potential benefits. Future research should focus on these underlying issues to provide a comprehensive understanding of the digital environment's role in FEPVRE, guiding more targeted and effective policy interventions.

The study has limitations, such as the exclusion of factors like the institutional environment and governance performance, which could provide a more comprehensive understanding of FEPVRE. Additionally, the focus on China limits the applicability of the findings to other regions with different ecological, economic, and technological contexts. Despite these limitations, the study makes significant contributions by integrating digital technologies into the analysis of FEPVRE, particularly in low-efficiency regions, and exploring the role of regional policies. This approach differentiates it from existing studies, which often overlook digital innovation and policy aspects. By combining digital, ecological, and policy factors, the study offers a more holistic perspective. Future research should explore the role of digital technologies in improving FEPVRE, the integration of ecological protection with green economic development, and the long-term dynamics of FEPVRE, considering policy, technology, and market factors. Cross-country comparisons would further enhance FEPVRE policies in China, advancing both research and policymaking in the field.

Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding authors.

Author contributions

LZ: Writing – original draft, Resources, Writing – review and editing, Investigation, Formal Analysis, Data curation, Conceptualization. JZ: Supervision, Writing – review and editing, Funding acquisition, Formal Analysis. LS: Writing – review and editing, Project administration, Methodology, Investigation, Visualization. WY: Data curation, Conceptualization, Writing – review and editing, Formal Analysis. XS: Supervision, Software, Writing – original draft, Visualization, Validation.

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Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

Generative Al statement

The author(s) declare that no Generative AI was used in the creation of this manuscript.

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Supplementary material

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fenvs.2025.1658104/full#supplementary-material

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