



Mixed Effects Models for Resampled Network Statistics Improves Statistical Power to Find Differences in Multi-Subject Functional Connectivity

Manjari Narayan^{1*} and Genevera I. Allen^{1, 2, 3}

¹ Department of Electrical and Computer Engineering, Rice University, Houston, TX, USA, ² Department of Statistics, Rice University, Houston, TX, USA, ³ Jan and Dan Duncan Neurological Research Institute and Department of Pediatrics-Neurology at Baylor College of Medicine, Houston, TX, USA

Many complex brain disorders, such as autism spectrum disorders, exhibit a wide range of symptoms and disability. To understand how brain communication is impaired in such conditions, functional connectivity studies seek to understand individual differences in brain network structure in terms of covariates that measure symptom severity. In practice, however, functional connectivity is not observed but estimated from complex and noisy neural activity measurements. Imperfect subject network estimates can compromise subsequent efforts to detect covariate effects on network structure. We address this problem in the case of Gaussian graphical models of functional connectivity, by proposing novel two-level models that treat both subject level networks and population level covariate effects as unknown parameters. To account for imperfectly estimated subject level networks when fitting these models, we propose two related approaches $-R^2$ based on resampling and random effects test statistics, and R³ that additionally employs random adaptive penalization. Simulation studies using realistic graph structures reveal that R^2 and R^3 have superior statistical power to detect covariate effects compared to existing approaches, particularly when the number of within subject observations is comparable to the size of subject networks. Using our novel models and methods to study parts of the ABIDE dataset, we find evidence of hypoconnectivity associated with symptom severity in autism spectrum disorders, in frontoparietal and limbic systems as well as in anterior and posterior cingulate cortices.

Keywords: functional connectivity, Gaussian graphical models, Markov networks, covariates, mixed effects models, resampling methods, lasso, network statistics

1. INTRODUCTION

One of the goals of neuroimaging studies of intrinsic or "resting state" brain activity, is to discover specific and stable imaging based biomarkers or phenotypes of neuropsychiatric and neurological disorders. Typically, resting state studies seek to infer *functional connectivity* or functional relationships between distinct brain regions from observed neurophysiological activity. Advances in resting state studies using fMRI (Menon, 2011; Bullmore, 2012; Craddock et al., 2013;

OPEN ACCESS

Edited by:

Bertrand Thirion, Institut National de Recherche en Informatique et Automatique, France

Reviewed by:

Joshua T. Vogelstein, Johns Hopkins University, USA Felix Carbonell, Biospective Inc., Canada

*Correspondence: Manjari Narayan manjari.narayan@gmail.com

Specialty section:

This article was submitted to Brain Imaging Methods, a section of the journal Frontiers in Neuroscience

Received: 23 September 2015 Accepted: 07 March 2016 Published: 12 April 2016

Citation:

Narayan M and Allen GI (2016) Mixed Effects Models for Resampled Network Statistics Improves Statistical Power to Find Differences in Multi-Subject Functional Connectivity. Front. Neurosci. 10:108. doi: 10.3389/fnins.2016.00108

1

Smith et al., 2013) suggest that functional connectivity could yield neuroimaging biomarkers for diagnosis and personalized treatment for a wide range of disorders.

For instance, many studies have found differences either in individual functional connections or in overall patterns of connectivity in autism spectrum disorders (Di Martino et al., 2014a; Uddin, 2014), Alzheimer's (Buckner et al., 2009; Tam et al., 2014), Depression (Tao et al., 2013; Lui et al., 2014; Kaiser et al., 2015) and others (Meda et al., 2012; van den Heuvel et al., 2013; Palaniyappan et al., 2013). However, simple group level differences between two distinct samples are challenging to interpret in many disorders. Autism, for example, is a diagnostic label that masks many diverse clinical symptoms (Lenroot and Yeung, 2013; Insel, 2014). Thus, the biological relevance of group level differences in network structure between Autism and healthy populations is unclear for individual subjects. One solution to find more meaningful differences in network structure is to study whether behavioral and affective symptoms measured by cognitive scores are associated with variations in individual functional networks. This paper offers a novel and rigorous statistical framework to find and test such covariate effects on functional connectivity metrics, when functional connectivity is defined using Gaussian graphical models.

Functional connectivity refers to latent relationships that cannot be directly observed via any modality of functional neuroimaging. Instead, it must be estimated from observations of neurophysiological activity. In fMRI studies, we first observe changes in the BOLD response over time either across thousands of voxels or over hundreds of brain regions, defined anatomically or functionally. Then depending on the specific statistical definition for functional connectivity, we estimate a functional connectivity network per subject using within-subject BOLD observations. For example, in a pairwise correlation model of functional connectivity, if the mean time-series of two brain regions are correlated then they are functionally connected. Thus, one popular approach to estimate functional connectivity is to compute sample correlations between every pair of brain regions. An increasingly popular alternative is to use Gaussian graphical models (GGMs) based on partial correlations to define functional connectivity. Here, if two brain regions are partially correlated, that is if the mean time-series of two brain regions remain correlated after regressing out the time-series of other brain regions, then they are functionally connected. For multivariate normal data, a zero partial correlation between two brain regions is equivalent to independence between the activity of two brain regions conditional on the activity of all other intermediate brain regions. Thus, GGMs eliminate indirect connections between regions provided by pairwise correlations and are increasingly popular in neuroimaging (Marrelec et al., 2006; Smith et al., 2011; Varoquaux et al., 2012; Craddock et al., 2013). Consequently, employing GGMs for functional connectivity enables us to discover network differences that implicate nodes and edges directly involved in producing clinical symptoms and provide stronger insights into network structures truly involved in the disease mechanism. For the rest of this paper, we define functional connectivity in terms of GGMs and discuss approaches to conducting inference on network metrics for such network models.

The functional connectivity of a single experimental unit or subject is rarely the final object of interest. Rather, most neuroimaging studies (Bullmore, 2012; Bullmore and Sporns, 2012; Zuo et al., 2012) are interested in identifying network biomarkers, or broader patterns of functional connectivity shared across individuals who belong to some distinct population or display some clinical phenotype. A popular approach (Bullmore and Sporns, 2009) to find such network biomarkers is through topological properties of network structure. Common properties or metrics either measure specialization of network components into functionally homogenous modules, or measure how influential brain regions integrate information across distinct network components. However, recall that functional connectivity in individual subjects is unknown and unobserved. Consequently, many multi-subject fcMRI studies first estimate functional connectivity for every subject and then assuming these subject networks are fixed and known, compute topological metrics of these networks using the Brain Connectivity Toolbox (Rubinov and Sporns, 2010). Finally, they compare and contrast these estimated networks or estimated network metrics to infer group level network characteristics. Typical neuroimaging studies that seek to detect covariate effects on network structure (Warren et al., 2014; Hahamy et al., 2015) conduct a single level regression with network metrics as the response and cognitive scores as the covariate, and subsequently use standard F-tests for covariate testing. New methods to conduct such network inference either emphasize novel topological metrics (van den Heuvel and Sporns, 2011; Alexander-Bloch et al., 2012) or novel approaches to study covariate effects for known networks for complex experimental designs with longitudinal observations or multiple experimental conditions (Simpson et al., 2013; Ginestet et al., 2014; Kim et al., 2014). However, these existing approaches assume estimated functional networks are perfectly known quantities. In contrast, we seek to explicitly investigate the consequences of using estimated, and often imperfectly estimated, functional networks and their corresponding network metrics on subsequent inference for covariate effects.

Before considering the consequences of using estimated networks, one might ask why individual network estimates might be unreliable to begin with. Statistical theory informs us that estimated networks can be unreliable in two possible ways. First, high dimensional networks with a large number of nodes estimated from a limited number of fMRI observations in a session possess substantial sampling variability (Bickel and Levina, 2008; Rothman et al., 2008; Ravikumar et al., 2011; Narayan et al., 2015). Second, when assuming sparsity in the network structure in the form of thresholded or penalized network estimates to overcome high dimensionality, we often obtain biased network estimates in the form of false positive or false negative edges (Ravikumar et al., 2011). Such errors in estimating networks are particularly exacerbated (Narayan et al., 2015) when networks are well connected with modest degrees, as is the case in neuroimaging. Additionally, empirical evidence from neuroimaging studies also suggest that sample correlation based estimates of individual resting state networks

are unreliable. For instance test re-test studies (Shehzad et al., 2009; Van Dijk et al., 2010; Braun et al., 2012) that measure inter-session agreement of estimated functional networks within the same subject find that sample intra-class correlations vary between 0.3 and 0.7, indicating non-negligible within subject variability. While we expect many sources of variation contribute to such inter-session variability within a subject including natural variations due to differences in internal cognitive states, recent work by Birn et al. (2013); Hacker et al. (2013); Laumann et al. (2015) suggests that sampling variability due to limited fMRI measurements play a significant role. These studies find that increasing the length of typical fMRI sessions from 5-10 min to 25 min substantially improves inter-session agreement of functional networks. Given the accumulating theoretical and empirical evidence of these methodological limitations, we assume that obtaining perfect estimates of individual networks is unlikely in typical fMRI studies. Instead, we seek to highlight the importance of accounting for imperfect estimates of functional networks in subsequent inferential analyses.

Failure to account for errors in estimating statistical networks reduces both generalizability and reproducibility of functional connectivity studies. Statistical tests that compare functional networks but do not account for potentially unreliable network estimates lack either statistical power or type I error control or both. For instance, Narayan and Allen (2013); Narayan et al. (2015) investigate the impact of using estimated networks when testing for two-sample differences in edge presence or absence between groups. When individual subject graphical models cannot be estimated perfectly, Narayan et al. (2015) show that standard two-sample test statistics are both biased and overoptimistic, resulting in poor statistical power and type I error control. Though this paper is similar in spirit to previous work (Narayan et al., 2015) in emphasizing the adverse effects of using estimated networks to study differences in functional connectivity, the unique contribution of this work are as follows: (1) Whereas previous work considered simple two-sample tests, we consider general covariate effects (that include both binary and continuous covariates) to link symptom severity to individual variations in functional connectivity. (2) We propose methods relevant to network metrics beyond the edge level. Finally, we provide empirical results such as statistical power analyses that offer greater practical guidance on choosing sample size and planning data analysis for future studies.

The paper is organized as follows. In Section 2 we provide new statistical models that explicitly link subject level neurophysiological data to population level covariate effects for network metrics of interest and provide new statistical algorithms and test statistics using resampling and random penalization for testing covariate effects. While the models and methods we propose can detect covariate effects on many well behaved network metrics (Balachandran et al., 2013) at the edge level (Tomson et al., 2013), node level (Buckner et al., 2009; Zuo et al., 2012) and community level (Alexander-Bloch et al., 2012; Tomson et al., 2013), we investigate the benefits of our methods to discover covariate effects on connection density. Using realistic simulations of graph structure for GGMs in Section 3, we demonstrate our proposed resampling framework substantially

improves statistical power over existing approaches, particularly for typical sample size regimes in fMRI studies. Finally, in Section 4 we demonstrate that our proposed methods can detect biologically relevant signals in a resting state fMRI dataset for autism spectrum disorders.

2. MODELS AND METHODS

We seek new methods to detect covariate effects when populations of functional networks are unknown. To achieve this, we first need statistical models that describe how each measurement of brain activity denoted by $y_j^{(i)}$ arises from unknown functional brain network with *p* nodes in the *i*th subject and how individual variations in a population of brain networks are related to some population level mean. Thus, for any network model and any network metric under investigation, we propose the following general two-level models to investigate covariate effects in functional connectivity. In subsequent sections, we provide specific instances of these models investigated in this paper.

Subject Level:
$$y_j^{(i)} \stackrel{iid}{\sim} \mathcal{N}_p(0, \Sigma^{(i)})$$
 and
Population Level: $u(\text{Network}_{(i)}) \stackrel{iid}{\sim} \mathbb{P}_{\mu^{(i)}, \nu^2}$ (1)

where $\Sigma^{(i)}$ is the covariance, Network_i is an adjacency matrix derived from either the covariance, the inverse covariance $\Theta = (\Sigma^{(i)})^{-1}$ or their correlational counterparts and $u(\cdot)$ denotes some network metric over the brain network. In this paper, we assume the individual measurements of brain activity at the subject level follow a multivariate normal distribution. At the population level, we assume that the effect of covariates on the network metrics follows a generalized linear model (Searle et al., 2009) where the mean and variance of the relevant continuous or discrete probability distribution, \mathbb{P} , for the network metric of interest is given by $\mu^{(i)}$ and ν^2 .

Suppose that we denote any network metric in the *i*th subject as $u^{(i)}$ and the vector of network metrics as $\mathbf{u} = (u^{(1)}, \ldots, u^{(n)})$, then the population mean is given by $\mu = \mathbb{E}(\mathbf{u})$ and population variance is given by $\operatorname{Var}(u^{(i)}) = v^2$. Then the generalized linear model for the population mean is given by

$$g(\mu) = X\beta + Z\gamma \tag{2}$$

Here $g(\mu)$ is a link function either reduces to $g(\mu) = \mu$ in linear models, or takes other forms such as the logit function for non-linear models; X is the $n \times (q + 1)$ matrix of the intercept and q covariates of interest with corresponding coefficients $\boldsymbol{\beta} = (\beta_0, \beta_1, \dots, \beta_q)$ while Z is the $n \times r$ matrix of nuisance covariates and corresponding regression coefficients $\boldsymbol{\gamma}$. X_i and Z_i denote the q dimensional explanatory covariate and r dimensional nuisance covariate for the *i*th subject, respectively.

In this paper, we seek to test the hypothesis that explanatory covariates have a statistically significant covariate effect on network metrics. Here $\beta_{\setminus 0}$ denotes the coefficients for

explanatory covariates. Thus, the null \mathcal{H}_0 and alternative hypothesis \mathcal{H}_1 are

$$\mathcal{H}_0: \boldsymbol{\beta}_{\setminus 0} = 0, \qquad \mathcal{H}_1: \boldsymbol{\beta}_{\setminus 0} \neq 0 \tag{3}$$

This section is organized as follows-In Section 2.1, we specifically employ Gaussian graphical model of functional connectivity at the subject level and investigate covariate effects using linear models for density based network metrics for the population level. Standard statistical analyses in neuroimaging studies estimate each level of these two level models separately. Thus, such approaches first estimate functional connectivity networks by fitting subject level models. However, they assume individual subject networks and their metrics are known when they fit the population level model and conduct inference on covariate effects. In Section 2.2 we discuss how such statistical procedures that assume functional connectivity networks are known lose statistical power to detect covariate effects. To address this problem, we introduce two related methods that utilize resampling, random adaptive penalization, and random effects that we call, R^2 and R^3 in Section 2.3. These methods ameliorate potential biases and sampling variability in estimated network metrics, thus improving statistical power to detect covariate effects.

2.1. Two Level Models for Covariate Effects

We begin by studying the earlier subject level network model in Equation (1) specifically for networks given by Gaussian graphical models. Recall that the *p*-variate random vector $y_j^{(i)}$ denotes BOLD observations or average BOLD observations within *p* regions of interest, at the *j*th time point for the *i*th subject. We assume $y_i^{(i)}$ has a multivariate normal distribution,

$$y_j^{(i)} \stackrel{iid}{\sim} \mathcal{N}_p(0, (\boldsymbol{\Theta}^{(i)})^{-1}), \tag{4}$$

where the network model of interest is derived from the inverse covariance or precision matrix $\Theta^{(i)}$, $j = 1, \ldots t$, and $i = 1, \ldots n$. In subsequent sections, we denote the $t \times p$ data matrix of observations by $\mathbf{Y}^i = (y_1^{(i)}, \ldots, y_t^{(i)})$ and the random variable associated with each brain region as Y_k . Although fMRI observations are autocorrelated across time and thus dependent (Woolrich et al., 2001; Worsley et al., 2002), we assume that these observations can be made approximately independent via appropriate whitening procedures discussed in our case study in Section 4.

Let $\mathcal{G}(\mathcal{V}, \mathcal{E})$ denote a Gaussian graphical model that consists of vertices $\mathcal{V} = \{1, 2, ..., p\}$ and edges $\mathcal{E} \subset \mathcal{V} \times \mathcal{V}$. Here, the presence of an edge $(k, l) \in \mathcal{E}$ implies that the random variables Y_k and Y_l at nodes/vertices k and l are statistically dependent conditional on all the other vertices $\mathcal{V} \setminus \{k, l\}$. For multivariate normal distributions, a non-zero value in the (k, l)entry of the inverse covariance matrix $\mathbf{\Theta}^{(i)}$ is equivalent to the conditional independence relationships, $Y_k \perp Y_l | Y_{\mathcal{V} \setminus \{k, l\}}$. Thus, we define functional connectivity networks where edges indicate *direct* relationships between two brain regions using the non-zero entries of $\Theta^{(i)}$. For a more thorough introduction to graphical models, we refer the reader to Lauritzen (1996).

Following the neuroimaging literature (Bullmore and Sporns, 2009), we consider network metrics to be functions of a binary adjacency matrix. The adjacency matrix of each individual subject network in our model (Equation 4) is given by the support of the inverse covariance matrix $\mathbb{I}\{\Theta^{(i)} \neq 0\}$. Network metrics that measure topological structure of networks are widely used in neuroimaging (Bullmore and Sporns, 2009; Rubinov and Sporns, 2010). While any of these network metrics can be incorporated into our two level models, we have found that many metrics originally proposed when studying a determinstic network are not suitable for covariate testing in the presence of individual variations in a population of networks. Recently, Balachandran et al. (2013) suggests that several discontinuous network metrics which include betweenness centrality, clustering coefficients defined at the node level and potentially many others are not suitable for inference. Thus, this paper focuses on well behaved topological metrics, namely density based metrics. Formally, the density or number of connections in any binary adjacency matrix A is given by $\sum_{k=1}^{p} \sum_{l=1}^{p} A_{kl}$. However, rather than defining density over the whole graph, the density can be restricted to a subnetwork (subnetwork density) or over a single node (node density or degree) or simply at the edge level (edge presence). At the node level, density is a simple measure of influence or centrality of a single brain region of interest (Rubinov and Sporns, 2010; Power et al., 2013). At the subnetwork level, density is popularly used (Honey et al., 2007; Bullmore and Sporns, 2009) to measure an excess or deficit of long range connections either within or between groups of brain regions with a distinct functional purpose. While we investigate node and subnetwork density in this paper, alternative network metrics amenable to inference include binary metrics such as edge presence (Meda et al., 2012; Narayan et al., 2015) or co-modularity relationships between nodes (Bassett et al., 2013; Tomson et al., 2013).

2.1.1. Population Model for Network Metrics

As described earlier, given the subject level model and a network metric of interest, we use a generalized linear model in Equation (2) to describe the deterministic relationship between the population mean for the network metrics and various covariates of interest. Depending on whether a network metric is continuous or binary valued, this general linear model takes the form of linear or logistic-linear models.

However, we also require a probability model to describe how a random sample of individual network metrics deviate from the population mean. When the network metric $u^{(i)}$ is continuous valued, the link function in Equation (2) reduces to the identity $g(\mu) = \mu$. For network metrics $u^{(i)}$ such as global, subnetwork or node density, we use the following linear model with normal errors,

$$u^{(i)} \stackrel{iid}{\sim} \mathcal{N}(X_i \boldsymbol{\beta} + Z_i \boldsymbol{\gamma}, \nu^2) \tag{5}$$

For metrics such as edge presence and co-modularity that take discrete binary values {0, 1}, a widely used link function (Williams, 1982; Agresti, 2002) for the generalized linear model

(Equation 2) is the logit function. The resulting logistic-linear model takes the following form

$$\mathbb{E}(u^{(i)}) = [1 + \exp(X_i \boldsymbol{\beta} + Z_i \boldsymbol{\gamma})]^{-1}$$
(6)

For the remainder of this paper, we consider normal models for node and subnetwork density.

2.2. Motivation for New Test Statistics

To understand why new statistical methods are necessary to fit our two-level models, consider the our covariate testing problem (Equation 3) for node and subnetwork density. Suppose the subject level networks in Equation (4) and corresponding metrics are known precisely for each subject. In this case, we employ standard least squares estimation with corresponding F-tests for linear regression to test our null hypothesis for covariate effects (Equation 3).

In practice however, not only is the covariate effect β unknown, the underlying graphical model $\Theta^{(i)}$ and the network metric $u^{(i)}$ is also unknown and are all estimated from data. In **Figure 1** we contrast the ideal scenario where the population of networks and corresponding network metrics are exactly known with the practical scenario where these network metrics are estimated from data. (See Section 3.1 for details on how we simulate data.) Applying a standard linear regression to known network metrics reveals an oracle estimate of the covariate effect (blue line). In contrast, when the standard approach described is applied to estimated network metrics (orange line), the size of the covariate effect is substantially reduced. However, by employing the R^3 approach (green line) that we introduce in the next section, we account for errors in estimating networks, thereby improving statistical power.

Two issues arise when we estimate network metrics from data. First, instead of true network metrics, $u^{(i)}$, our estimated network metrics, $\tilde{u}^{(i)}$, are a function of observations $\mathbf{Y}^{(i)}$. Thus, each estimate, $\tilde{u}^{(i)}$, possesses additional sampling variability. However, since we only acquire one network estimate per subject, standard least squares estimation cannot account for this additional variability. Additionally graph selection errors in network estimation potentially bias network metric estimates. Previously, Meinshausen and Bühlmann (2006); Ravikumar et al. (2011); Narayan et al. (2015) show that in finite sample settings where the number of independent observations t within a subject is comparable to the number of nodes p, we expect false positive and false negative edges in network estimates. Such graph selection errors increase with the complexity of the network structure, governed by factors such as the level of sparsity, maximum node degree as well as the location of edges in the network. Since functional connectivity networks are moderately dense and well connected with small world structure (Achard et al., 2006), edges in these networks might be selected incorrectly. Observe that in Figure 1, we obtain larger estimates of node and subnetwork density for individual networks where true node or subnetwork densities are small and the reverse for truly large node or subnetwork densities. As a result, individual variation in estimated metrics no longer reflects the true effect of the covariate, resulting in loss of statistical power. For a detailed overview of how selection errors in estimating network structure propagate to group level inferences, we refer the reader to Section 2 of Narayan et al. (2015).

To overcome these obstacles, we use resampling to empirically obtain the sampling variability of estimated network metrics, $\tilde{u}^{(i)}$, and propagate this uncertainty using mixed effects test statistics for the covariate effect $\hat{\beta}$. Moreover, by aggregating



FIGURE 1 | Motivation for new statistical framework R^3 . Here, we simulate covariate effects on the metric of interest, namely the degree centrality or node density (left) and subnetwork density (right) with (p = 50, n = 20, t = 200). We illustrate covariate effects in the ideal scenario where network metrics are known perfectly in blue. Unfortunately, in functional connectivity networks, statistical errors in estimating graphical models are inevitable and these propagate to estimates of network metrics. As a result, when we estimate node and subnetwork density for each subject and conduct tests for covariate effects using standard *F*-tests, we fail to see a clear relationship between metrics and covariate of interest (orange) using linear regression. This loss of statistical power occurs when standard test statistics assume that estimates of density are correct. In contrast, when we account for errors in graph estimation and selection using R^3 test statistics (green), we have greater statistical power to detect covariate effects on density metrics. Algorithmic details of the R^3 approaches can be found in Section 2.

network statistics across resamples and optionally incorporating adaptive penalization techniques, we sufficiently improve network estimates and corresponding network metrics to obtain more accurate estimates of the covariate effects.

2.3. Procedure for Testing Covariate Effects

In order to improve statistical power, we propose a resampling framework that integrates network estimation with inference for fixed covariate effects at the population level. We provide two related procedures to test covariate effects— R^2 that employs resampling (RS) and random effects test statistics (RE), and R^3 that employs resampling (RS), random adaptive penalization (RAP) and random effect test statistics (RE). Intuitively, our algorithm consists of first obtaining initial estimates of the sparsity levels in individual subject networks. Then, to estimate the sampling variability of each subject network empirically, we resample within subject observations and re-estimate the networks of each subject. Additionally, in the case of R^3 we simultaneously apply random adaptive penalties when reestimating the networks. Network metrics are computed on each of the resampled networks, giving us multiple pseudoreplicates of network metrics per subject. Finally, we model these resampled network statistics using simple mixed effects models to derive test statistics for population level covariate effects. After performing our procedure, one can use well known parametric or non-parametric approaches to obtain *p*-values and correct for multiplicity of test statistics when necessary. Thus, our resampling framework consists of three components, graph estimation and selection, resampling and optionally RAP, and covariate testing via mixed effects models. We discuss each of these ingredients separately before putting them together in Algorithm 1.

2.3.1. Graphical Model Estimation

Many approaches such as sparse regularized regression (Meinshausen and Bühlmann, 2006), sparse penalized maximum likelihood (ML) or the graphical lasso (Yuan and Lin, 2007; Friedman et al., 2008) and others (Cai et al., 2011; Zhou et al., 2011) can be used to estimate $\Theta^{(i)}$ in our subject level model (Equation 4). We use the QuIC solver (Hsieh et al., 2011, 2013) to fit a weighted graphical lasso to obtain estimates of $\Theta^{(i)}$.

$$\hat{\boldsymbol{\Theta}}_{\Lambda^{(i)}}^{(i)}(\mathbf{Y}^{(i)}) = \arg\min_{\boldsymbol{\Theta} \succ 0} \operatorname{Tr}(\hat{\boldsymbol{\Sigma}}^{(i)}\boldsymbol{\Theta}) - \log\det(\boldsymbol{\Theta}) + \|\Lambda^{(i)} \circ \boldsymbol{\Theta}\|_{1,\text{off}}$$
(7)

where $\hat{\boldsymbol{\Sigma}}^{(i)}$ is the empirical sample covariance, $\hat{\boldsymbol{\Sigma}}^{(i)} = \frac{1}{t}(\mathbf{Y}^{(i)\top}\mathbf{Y}^{(i)})$, and \circ denotes the Hadamard dot product. The term $\|\boldsymbol{\Theta}\|_{1,\text{off}} = \sum_{k < l} |\theta_{k,l}|$ is the ℓ_1 penalty on the off-diagonals entries. Since the sample correlation rather than covariance is commonly used in neuroimaging, we employ sample correlation matrix, $\tilde{\boldsymbol{\Sigma}}^{(i)}$. The two are equivalent when $\mathbf{Y}^{(i)}$ has been centered and scaled. Given any estimate of the inverse covariance matrix $\widehat{\boldsymbol{\Theta}}^{(i)}$, the estimated adjacency matrix for each subject is thus given by $\mathbb{I}(\widehat{\boldsymbol{\Theta}}^{(i)} \neq 0)$ and network statistics can be computed

accordingly. For our R^3 procedure, we employ a symmetric weight matrix of penalties $\Lambda^{(i)}$ obtained by randomly perturbing an initial penalty parameter $\lambda^{(i)}$. For our R^2 this weight matrix $\Lambda^{(i)}$ reduces to a scalar value $\lambda^{(i)}$ for all off-diagonal entries, giving us the standard graphical lasso. In order to estimate these initial penalty parameters $\lambda^{(i)}$, we employ StARS (Liu et al., 2010), a model selection criterion that is asymptotically guaranteed to contain the true network, and works well with neuroimaging data. The *beta* parameter of StARS is set to 0.1 in our work.

2.3.2. Resampling and Random Adaptive Penalization

Since network estimates depend on the underlying observations $\mathbf{Y}^{(i)}$, we employ resampling techniques to estimate the sampling variability of $\tilde{u}^{(i)}$. Recall that estimates of a network metric, $\tilde{u}^{(i)}$, are a function of estimated networks $\mathbb{I}\{\widehat{\Theta}^{(i)}(\mathbf{Y}^{(i)}) \neq 0\}$. Unfortunately, closed form finite sample distributions for sparse penalized estimates of $\widehat{\Theta}^{(i)}$ (Berk et al., 2013) as well as sampling distributions of network metrics (Balachandran et al., 2013) are still an emerging area of research. Thus, our problem differs from standard univariate GLM analyses employed in both voxel-wise activation studies and seed-based correlational analysis (Penny et al., 2003; Fox et al., 2006) where closed form asymptotic formulas for sample variance at the subject level are incorporated into the group level analyses. To tackle the issue of unknown sampling variability we build an empirical distribution of network statistics, where we perturb the data by sampling mout of t observations with replacement (bootstrap) (Efron and Tibshirani, 1993) or without replacement (subsampling) (Politis et al., 1999) and re-estimate the network metrics per resample. By aggregating network statistics across resamples within each subject (Breiman, 1996a), we gain the additional benefit of variance reduction (Bühlmann and Yu, 2002) for individual subject metrics. Many variations of resampling techniques exist to handle dependencies (Lahiri, 2013) in spatio-temporal data. Since we assume approximately independent observations, from here on our resampling consists of sampling t out of t observations with replacement.

Recall that our method R^2 is a variant of R^3 , that only involves resampling without random adaptive penalties. Here we obtain a bootstrapped network estimate $\widehat{\Theta}^{*(i,b)}$, and a corresponding network metric $\tilde{u}^{*(i,b)}$ in Step 1 of our Algorithm 1 for each of B = 100 resamples. For our alternative procedure, R^3 , however, we not only use resampling, but simultaneously perturb the initial regularization parameters $\lambda^{(i)}$ for every resample. This amounts to solving a weighted graphical lasso to re-estimate the network, where the weights are given by random adaptive penalties. Our motivation to use R^3 is based on previous work in the context of two-sample tests for edge differences. Narayan et al. (2015) show that random penalization significantly improved power over pure resampling to detect differential edges when the networks were moderately dense. Given this result, we sought to investigate the benefits of random penalization for more general network metrics. Intuitively, we anticipate that density based metrics beyond the edge level are immune to some graph selection errors. For instance, when false negatives are compensated by an equal number of false positive edges within the same node or subnetwork, node or subnetwork density values remain unchanged. However, graph selection errors that do not cancel each other out result in a net increase or decrease in density, thus contributing to loss of power. In these scenarios, we expect R^3 to offer additional statistical power to test covariate effects.

Whereas general network metrics, require global properties of the network structure be preserved, the standard randomized graphical lasso (Meinshausen and Buhlmann, 2010) penalizes every edge randomly such that topological properties of the network could be easily destroyed within each resample. Thus, we seek to randomly perturb selected models in a manner less destructive to network structure. To achieve this, we adaptively penalize (Zhou et al., 2011) entries of $\Theta^{(i)}$. Strongly present edges are more likely to be true edges and should thus be penalized less, whereas weak edges are more likely to be false and should be penalized more. As long as we have a good initial estimate of where the true edges in the network are, we can improve network estimates by adaptively re-estimating the network, while simultaneously using random penalties to account for potential biases in the initial estimates. In order to obtain a reliable initial estimate of network structure, we take advantage of the notion of stability as a measure of confidence popularized by Breiman (1996b); Meinshausen and Buhlmann (2010). Here the stability of an edge within a network across many resamples measures how strongly an is edge present in the network. When an edge belongs to the true network with high stability we randomly decrease the associated penalty by a constant κ . Conversely, we randomly increase the penalty by κ for an edge with low stability. Similar to Narayan et al. (2015), we fix the constant κ to $0.25\lambda_{max}^{(i)}$. Here $\lambda_{max}^{(i)}$ is the regularization parameter that results in the all zero graph for a subject. We call this approach random adaptive penalization (RAP) as it builds on the previous random penalization approach of Narayan et al. (2015) but adaptively perturbs the regularization parameters using initial stability scores along the lines of the random lasso (Wang et al., 2011).

Since, random adaptive penalization depends on an initial estimate of the stability of every edge in the network, we take advantage of the basic resampling step in Algorithm 1 to obtain a stability score matrix $\hat{\Pi}^{(i)}$ for each subject. The entries of this matrix provide a proportion that takes values in the interval (0, 1). Once we have the stability scores, we consider an additional set of B = 100 resamples to implement RAP. Thus, in step 2 of Algorithm 1, we form an matrix of random penalties $\Lambda_{RAP}^{(i,b)}$ per resample b. For each edge (k, l) the corresponding adaptive penalty is determined by perturbing initial $\hat{\lambda}^{(i)}$ by an amount κ using a Bernoulli random variable. The probability of success of each Bernoulli r.v is determined by the corresponding stability score for that edge.

$$\Lambda_{RAP}^{(i,b)} = \begin{cases} \hat{\lambda}^{(i)} + \kappa & \text{Ber}(1 - \Pi_{kl}^{(i)}) \\ \hat{\lambda}^{(i)} - \kappa & \text{Ber}(\Pi_{kl}^{(i)}) \end{cases}$$
(8)

Putting these components together, R^3 consists of first running Step 1 of Algorithm 1 to obtain stability scores and then using an additional B resamples based on random adaptive penalization,

summarized in Step 2 of Algorithm 1 to obtain nB resampled network metrics $\tilde{u}^{(i,b)}$. Note that in subsequent steps we omit the superscripts in $\Lambda_{RAP}^{(i,b)}$ for notational convenience.

Algorithm 1 : R^2 and R^3 Procedures for Testing Covariates Effects on Network Metrics

Step 0: Initial Parameters Input: $\mathbf{Y}^{(i)}$, Output: $\hat{\lambda}^{(i)}$

Estimate $\hat{\lambda}^{(i)}$ using graphical model estimation and selection (StARS) for each subject *i*.

Step 1: Subject Level Resampling

Input: $(\mathbf{Y}^{(i)}, \hat{\lambda}^{(i)}, B = 100)$, **Output:** Either $\tilde{u}^{*(i,b)}$ or $\hat{\Pi}^{(i)}$

- (a) FOR b = 1, ..., B in the *i*th subject
 - (i) Bootstrap the data $\mathbf{Y}^{(i)}$ to get $\mathbf{Y}^{*(i,b)}$ and sample correlation matrix $\tilde{\boldsymbol{\Sigma}}^{*(i,b)}$
 - (ii) Perform a standard graphical lasso $\widehat{\Theta}_{\hat{\lambda}^{(i)}}^{*(i,b)}(\tilde{\Sigma}^{*(i,b)})$ in Equation (7)
 - (iii) If R^2 : Compute network statistic $\tilde{u}^{*(i,b)}$ defined in Section 2.1

END

(b) If R^3 : $\hat{\Pi}^{(i)}$ Estimate stability scores _ $\frac{1}{B}\sum_{b}^{B}\mathbb{I}(\widehat{\boldsymbol{\Theta}}_{\hat{\boldsymbol{\lambda}}^{(i)}}^{(i)}(\tilde{\boldsymbol{\Sigma}}^{*(i,b)})\neq 0)$

Step 2: Subject Level Resampling & Random Adaptive Penalization (R^3 only)

Input: $(\mathbf{Y}^{(i)}, \hat{\Pi}^{(i)}, \hat{\lambda}^{(i)}, B = 100)$, Output: $\tilde{u}^{*(i,b)}$

- (a) FOR b = 1, ..., B in the i^{th} subject
 - (i) Bootstrap the data $\mathbf{Y}^{(i)}$ to get $\mathbf{Y}^{*(i,b)}$ and sample correlation matrix $\tilde{\boldsymbol{\Sigma}}^{*(i,b)}$
 - (ii) Using stability scores from Step 1(b), compute random adaptive penalties $\Lambda_{RAP}^{(i,b)}$ in Equation (8) (iii) Using a weighted graphical lasso,
 - estimate $\widehat{\boldsymbol{\Theta}}_{\Lambda_{RAP}}(\widetilde{\boldsymbol{\Sigma}}^{*(i,b)}) \text{ in Equation (7)}$ (iv) Compute network statistic $\widetilde{u}^{*(i,b)}$ defined in Section 2.1
 - END

Step 3: Population Level Inference for $\hat{\beta}$ using Random Effects

Input: $\{\{\tilde{u}^{*(i,b)}\}_{h=1}^B\}_{i=1}^n$, **Output:** $\hat{\boldsymbol{\beta}}$ and *p*-values

- (a) Estimate fixed covariate effects $\hat{\beta}$ using mixed effects models. (Section B.1)
- (b) Compute mixed effects test statistic and p-values in Equation (B.1)

2.3.3. Test Statistics for Network Metrics

Both R^2 and R^3 yield a total of *nB* resampled network statistics that possess two levels of variability. If we applied single level regression techniques to test the covariate effect in Equation (3), we would in effect assume that all the nB resampled

statistics were independent. Test statistics that assume nB independent observations, despite the availability of only n independent clusters of size B are known to be overoptimistic (Laird and Ware, 1982; Liang and Zeger, 1993). To address this overoptimism, a more reasonable assumption is that resampled statistics between any two subjects are independent, whereas within subject resampling statistics are positively correlated. Just as we commonly employ mixed effects models to account for two levels of variation in repeated measures data, we employ similar two-level models to derive test statistics for resampled network metrics.

Let \mathbf{U}_i^* denote the vector $B \times 1$ vector of resampled statistics per subject { $\tilde{u}^{*(i,b)}$ } In the case of real valued density metrics, we use a linear mixed effects (LME) model for repeated measures (Laird and Ware, 1982) to account for the two levels of variability in resampled statistics.

$$\mathbf{U}_{i}^{*} = \beta_{0} + \underbrace{X_{i}\boldsymbol{\beta}_{\backslash 0} + Z_{i}\boldsymbol{\gamma}}_{\text{Between Subject}} + \underbrace{R_{i}a_{i}}_{\text{Within Subject}} + e_{i}^{*}$$
(9)
$$\operatorname{Var}(\mathbf{U}_{i}^{*}) = V_{i} = \phi^{*2} + R_{i}v^{2}R_{i}^{\top}$$
(10)

Here a_i are *i.i.d* subject level random intercepts with variance $Var(a_i) = v^2$, $R_i = \mathbf{1}_{B \times 1}$ is the random effect design matrix, and e_i^* is independent of a_i and captures within subject sampling variability with variance $Var(e_i) = \phi^{\star 2} \mathbf{I}_B$ where \mathbf{I} denotes

the identity. From hereon, we ignore the intercept β_0 , and assume that β denotes the $(q \times 1)$ vector of explanatory fixed effects.

Estimation and inference for linear mixed effect models are well covered in the neuroimaging literature in the context of functional activation studies and longitudinal designs (Beckmann et al., 2003; Bernal-Rusiel et al., 2013). We employ standard estimators and test statistics for linear mixed effects models including generalized least squares estimators for $\hat{\beta}$ and corresponding restricted maximum likelihood (ReML) estimators of variance to obtain *F*-test statistics to test the null hypothesis regarding β , the covariate effects. A thorough review of mixed effects models can be found in Agresti (2015) and we also spell these out in more detail for our methods in Supplementary Materials.

3. SIMULATION STUDY

In this section, we seek to evaluate our framework for testing covariate effects by conducting a rigorous power analysis using realistic fMRI network structures. We obtain realistic network structures for fMRI functional connectivity by using networks estimated from real data as the basis of our simulated networks. First, we synthetically create multivariate data according to our two-level models using realistic graph structures in Section 3.1. Since we know the true structure of graphical models and their network metrics we empirically measure statistical power and type-I error for all methods. Then, in Section 3.2 we offer two key results. First, by employing simulations using two-level models of variability in Equation (4) that reflect how functional networks are analyzed in practice, we provide a more realistic assessment of when we lose statistical power due to sample sizes (t, n) and covariate signal-to-noise (SNR) controlled by population variance v^2 . Second, we show that both R^2 and R^3 mitigate the challenges discussed in Section 2.2 and improve statistical power over standard test statistics under various sample sizes and covariate SNR regimes.

3.1. Simulation Setup for Node and Subnetwork Density

We simulate multivariate data according to our two level models in Section 2.1. We know from previous work that the graph structure or location of non-zeros in the inverse covariance (Narayan et al., 2015) influences the difficulty of estimating individual subject networks accurately. Using a group level empirical inverse correlation matrix obtained from 90 healthy subjects in the Michigan sample of the ABIDE dataset, preprocessed in Section 4, we threshold entries smaller than $\tau = |.25|$ to create a baseline network A_0 that contributes to the intercept term β_0 of our model (Equation 4). Illustrations of this baseline network can be found in Figure A.0 in the Supplementary Materials. Then we create individual adjacency matrices and network metrics $u^{(i)}$ according to the linear model (Equation 5). We create inverse correlation matrices $\Theta^{(i)}$ using the graph structure provided by A_0 and ensure $\Theta^{(i)}$ is positive definite.

Our main focus in the simulation study is to conduct a rigorous power analysis to detect covariate effects on node density and subnetwork density under a range of sample sizes and population variability and demonstrate the benefits of using R^3 and R^2 over standard approaches. Recall from Section 2.1 that node density is the degree of a node, while the subnetwork density is the number of connections between sets of nodes that make up a submatrix or subnetwork of the inverse covariance matrix. We obtain empirical estimates of statistical power by measuring the proportion of times we successfully reject $\hat{\boldsymbol{\beta}}_{\setminus 0} = 0$ at level $\alpha = .05$, in the presence of a true covariate effect $\boldsymbol{\beta}_{\setminus 0} \neq 0$, across 150 monte-carlo trials for a simulation scenario. Similarly, we obtain an empirical estimate of type I error by measuring the proportion of times we reject $\hat{\boldsymbol{\beta}}_{\setminus 0} = 0$ at level $\alpha = .05$ in the presence of a null covariate effect of $\boldsymbol{\beta}_{\setminus 0} = 0$.

Although one could choose to vary a large number of parameters for these simulations, we focus on the parameters most important for a power analysis, sample sizes and population variance, (t, n, v^2) , while fixing other parameters such as number of covariates to q = 1, r = 0 and number of nodes to p = 50. We present a 3×3 panel of 9 power analyses of node density in Figure 2 where we vary $t = \{p, 2p, 4p\}$ along the y-axis and $v^2 = \{0.1, 0.25, 0.5\}$ along the x-axis. Then within each sub-panel, we evaluate statistical power at subject sample sizes of $n = \{5, 10, \dots, 95\}$. For the entire 3×3 panel we hold the intercept and covariate effect fixed at $\beta_0 = 2, \beta_1 = 1$. Thus, each sub-panel illustrates statistical power as a function of subject sample size *n* for a fixed value of (t, v^2) . Similarly, in Figure 3 we present power analyses for subnetwork density where we hold the intercept and covariate fixed at $\beta_0 = 5$, $\beta_1 =$ 2 and use subnetworks of size 0.1p = 10 nodes. We use



FIGURE 2 | Statistical power analysis for node density. When node density varies with an explanatory covariate (q = 1), statistical power to detect this covariate effect improves with subject sample size *n* but crucially depends on the number of independent fMRI samples *t* from a single session and relative size of the covariate effect, $\beta_1 = 1$, to population variance v^2 (covariate SNR). When $t \approx p$, estimates of node density are both highly variable and potentially biased. By accounting for these issues, R^3 and R^2 improve estimates of network metrics, thus exceeding 80% power, whereas the standard *F*-test is substantially less powerful. Note that R^3 and R^2 are more powerful at smaller sample sizes compared to the standard approach. However, when fMRI samples become sufficiently large at $t \approx 4p$, all methods become similarly powerful for detecting covariate effects of node density. Empirical statistical power is defined as $\frac{\# \text{ of times reject } \mathcal{H}_0}{\# \text{ of Monte Carlo Trials}}}$ when the alternative is true in Equation (3).

larger values for covariate effects to ensure that the number of edges in a subnetwork are realistically large for a subnetwork with 10 nodes. While the sample sizes (t, n) are identical to those in node density, we increase $\nu^2 = \{0.4, 1, 2\}$ to match β . This ensures that covariate signal to noise ratio $\frac{\|X\beta_1\|_2^2}{\nu^2}$ is similar for both metrics. Note that that the intercept values β_0 in both power analyses were based on the average node degree in A_0 or average subnetwork density for subnetworks of size 10 in A_0 . For each power analysis, we have a corresponding simulation of type-I error, obtained by setting $\beta_1 = 0$ while keeping all other parameters equivalent. The full set of type-I error control results are presented in Supplementary Materials, and one representative simulation for each metric is presented in **Figure 4**.

3.2. Simulation Results

In these simulations, our methods, R^3 and R^2 , empirically outperform standard methods in terms of statistical power, particularly when within subject observations are comparable to the dimension of the network, and subject networks are harder to estimate correctly. Recall from Section 2.2 that we expect to lose statistical power when individual subject networks are difficult to estimate correctly, due to additional sampling variability and bias in network metrics. As expected, power analyses for both metrics in **Figures 2**, **3** reveal that statistical power deteriorates as observations *t* available for subject network estimation reduces. Moreover, this loss of statistical power cannot always be compensated by larger subject sample sizes *n*. For example, the best achievable statistical power at large subject



FIGURE 3 | Statistical power for subnetwork density. When subnetwork density varies with an explanatory covariate (q = 1), statistical power to detect this effect improves with subject sample size *n* but crucially depends on the number of independent fMRI samples *t* from a single session and the relative size of the covariate effect, $\beta_1 = 2$, to the population variance v^2 (covariate SNR). For many values of (t, p) estimates of subnetwork density are both highly variable and potentially biased. By accounting for these issues, both R^3 and R^2 test statistics substantially improve statistical power across all regimes at smaller subject sample sizes, whereas the standard *F*-test is substantially less powerful. We note that covariate effects on subnetwork metrics are particularly hard to detect when $t \approx p$, with statistical power often below 60%. Empirical statistical power is defined as $\frac{\# of Monte Carlo Trials}{\# of Monte Carlo Trials}$ when the alternative is true in Equation (3).

samples of $n \approx 100$ begins to deteriorate when t = p. While, the best achievable statistical power often exceeds 90% for node density when t > p, it drops as low as 80% for R^3 and R^2 . The standard approach in contrast drops below 60% node density. In the case of subnetwork density, statistical power for R^3 and R^2 exceed 80% when t = 4p, this drops as low as 60% at more modest sample sizes of t = 2p and further down to 40% at t = p. The standard approach falls to below 40% more quickly at t = 2p and below 20% when t = p.

Just as with subject sample size, when individual network estimation is easy in our simulations with larger within subject observations of t = 4p, the covariate signal to noise ratio or SNR has an almost negligible impact on statistical power. However, as t decreases, network estimation becomes harder and consequently, all methods become much more sensitive to SNR. For example, in

regimes where t = 2p, network estimation is moderately hard but detecting covariate effects is achievable at high SNR. However, we observe that all methods lose power as covariate SNR decreases. We also observe that loss of statistical power due to SNR is more pronounced at smaller subject sample sizes of n < 60. Such a result is expected since sampling variability of covariate effect β_1 is proportional to population variance ν^2 and decreases with larger subject sample sizes n.

We noted earlier in Section 2.3 that we expect the benefits of R^3 over R^2 to be the greatest for finest scale metrics at the edge level which are most sensitive to graph selection errors and decrease as metrics measure density at more global levels. Whereas, random penalization improves statistical power relative to R^2 for two-sample differences at the edge level Narayan et al. (2015), they share similar statistical power for



node and subnetwork density in most simulations presented here, with some marginal benefits for node density. R^3 offers greater benefits over R^2 at small sample sizes t for networks that are more sparse and where the stability of true edges over false edges can be improved via random penalties. All methods, including R^3 and R^2 are unable to detect covariate effects when estimation of individual networks becomes unreliable under high density regimes. We provide additional simulations that vary the sparsity of baseline networks in Figure A.3 in the Supplementary Materials.

Finally, in **Figure 4**, we provide evidence that type-I error is controlled by all methods for both node and subnetwork density. The full panel of simulations that complement **Figures 2**, **3** are included in Supplementary Materials.

From these simulations we conclude that resampling based approaches are more efficient, i.e., they have higher statistical power for both node and subnetwork density at smaller subject sample sizes n, particularly for smaller t and lower covariate SNR. Another insight from these simulations is that given a fixed budget of fMRI session time, it is preferable to increase the number of within session observations t per subject for fewer number of subjects n in order to maximize statistical power. For studies where each fMRI session consists of observations comparable to the size of networks ($t, p \in [100, 200]$), as well as for studies that cannot recruit a large number of subjects, our methods, R^3 and R^2 , make better use of available data and improve statistical power compared to standard approaches to network analysis.

4. CASE STUDY

A number of recent studies on autism spectrum disorders (ASD) have found differences in functional connectivity that were correlated with symptom severity as measured by Autism Diagnostic Interview (ADI) or Autism Diagnostic Observation Schedule (ADOS). However, the majority of these studies that

link symptom severity to functional connectivity derive networks using pairwise correlations (Supekar et al., 2013; Uddin et al., 2013b). An important shortcoming of studying differences in pairwise correlation networks is that edges in a true correlational network might be present due to the effect of "common causes" elsewhere in the brain and do not necessarily represent a direct flow of information. Thus, while correlational networks can provide network biomarkers for autism (Supekar et al., 2013), it is more problematic to infer network mechanisms of behavioral deficits in ASD exclusively using correlational networks. However, by studying previously implicated regions and subnetworks using Gaussian graphical models (GGMs), we strengthen the interpretation of variations in network structure linked to autism severity. Thus, by employing our two level models (Equation 1) based on GGMs to detect covariate effects, we enable scientists to infer that any network differences linked with behavioral deficits implicate nodes and edges directly involved in the disease mechanism. Guided by the successes of our simulation study, we employ R^3 to investigate the relationship between cognitive scores on node and subnetwork densities in autism spectrum disorders. In particular, we conduct tests for covariate effects on two density metrics, the node density and subnetwork density. Node density counts the number of connections between a single region of interest to all other regions where as subnetwork density counts the number of connections between sets of regions or subnetworks. We investigate nodes and subnetworks hypothesized in the literature (Uddin, 2014) to be involved in regulating attention to salient events and explanatory for behavioral deficits in ASD.

4.1. ABIDE Data Collection and Preprocessing

We use resting state fMRI data collected from the Autism Brain Imaging Data Exchange (ABIDE) project (Di Martino et al., 2014b) and preprocessed by the Preprocessed Connectomes Project (PCP) (Craddock and Bellec, 2015) using the configurable-pipeline for analysis of connectomes or (C-PAC) toolbox (Craddock, 2014; Giavasis, 2015). In order to properly account for site effects, we choose to focus on two major sites with relatively large samples, UCLA and Michigan, resulting in 98 and 140 subjects per site. While both ADOS and ADI-R cognitive scores are available for these sites, we focus on ADOS scores obtained using the Gotham algorithm (Gotham et al., 2009), which is known to be comparable across different age groups.

The ABIDE data was acquired (Di Martino et al., 2014b) using T2 weighted functional MRI images with scan parameters TR = 2 at the Michigan site and TR = 3 at the UCLA site. Subsequently, this data was minimally preprocessed using the C-PAC utility (Craddock and Bellec, 2015; Giavasis, 2015), including slice timing correction, motion realignment and motion correction using 24 motion parameters, and normalization of images to Montreal Neurological Institute (MNI) 152 stereotactic space at $3 \times 3 \times 3$ mm³ isotropic resolution. The pipeline was also conFigured to regress out nuisance signals from the fMRI time-series. The nuisance variables included were physiological confounds such as heart beat and respiration, tissue signals

and low frequency drifts in the time-series. We did not regress out the global signal as this operation is known to introduce artifacts in the spatial covariance structure (Murphy et al., 2009). Additionally, we did not apply band pass filtering as this would interfere with subsequent temporal whitening that we describe later in thisSection. Preprocessed data without bandpass filtering and global signal regression is available using the noglobalnofilt option in the PCP project. Finally, the spatial time-series was parcellated into times-series × regions of interest using the Harvard-Oxford atlas distributed with FSL (http://fsl.fmrib.ox. ac.uk/fsl/fslwiki/). Here we included p = 110 regions of interest including 96 cortical regions and 14 subcortical regions. Regions corresponding to white matter, brain stem and cerebellum were excluded. The resulting time-series \times regions data matrix for each individual subject is (t = 116, p = 110) for UCLA subjects and (t = 300, p = 110) for Michigan subjects. This preprocessed dataset has been archived in a public repository (http://dx.doi. org/10.6084/m9.figshare.1533313).

4.2. Previously Implicated Subnetworks and Regions

Distinct lines of evidence suggest the involvement of limbic, fronto-parietal, default mode and ventral attention regions in ASD. Uddin (2014) summarize the evidence in favor of a salience-network model to explain behavioral dysfunction in responding to external stimuli. According to this model, the salience network regions that span traditional limbic and ventral attention systems play a vital role in coordinating information between the default mode regions involved in attending to internal stimuli and the fronto-parietal regions involved in regulating attention to external stimuli. Together, these interactions enable appropriate behavioral responses to "salient" or important events in the external environment. Uddin et al. (2013a) conducted a network-based prediction study and found that connectivity features of the anterior cingulate cortex, and the anterior insula, predict an increase ADOS repetitive behavior scores. Similarly, another study by Di Martino et al. (2009) also implicates connectivity of anterior insula and anterior cingulate cortex to deficits in social responsiveness in Autism. Cherkassky et al. (2006); Monk et al. (2009) implicate posterior cingulate connectivity within the default mode network in ASD. Alaerts et al. (2013) show that deficits in emotion recognition were correlated with network features in the right posterior superior temporal sulcus, a result also supported in the wider literature (Uddin et al., 2013b).

Additionally, we also major findings from previous analyses of the ABIDE dataset that include the UCLA or Michigan subject samples. Whole brain voxelwise analysis by Di Martino et al. (2014b) revealed covariate effects associated with the mid insula, posterior insula, posterior cingulate cortex and thalamus. Group level two-sample tests of functional segregation and integration in seed based functional connectivity (Rudie et al., 2012a,b) reveal differences in the amygdyla, IFG right pars opercularis.

Based on our review of existing literature, we seek to detect covariate effects with respect to 23 hypotheses regarding the density of connections. Of these 23 hypotheses, 13 correspond to density of connections of nodes or brain regions with respect to the whole brain, and 10 correspond to the density within and between 4 large scale functional subnetworks. These regions are defined using the Harvard-Oxford atlas with large scale subnetworks provided by Yeo et al. (2011). **Figure 5** illustrates the volumes associated with the 13 regions of interest. **Figure 6** illustrates the four large scale functional brain networks we consider, namely, the default mode, the frontoparietal, the limbic and the ventral attention networks as defined by Yeo et al. (2011). By explicitly testing the density of long-range connections in brain regions and networks previously linked with ASD, we aim to identify network structures at the node and subnetwork level that are directly involved in behavioral deficits.

4.2.1. Testing for Covariate Effects via R³

We employ the linear model from Equation (5) for node and subnetwork density to test the null hypothesis that ADOS covariates have no effect on density. For this analysis, we jointly consider two related explanatory covariates, the ADOS Social Affect (SA) and the ADOS Restricted, Repetitive Behavior (RRB) scores (q = 2), while accounting for differences in clinical evaluation across sites, by incorporating site as a nuisance covariate (r = 1). We eliminate subjects without ADOS cognitive scores, leaving us with n = 100 autism subjects. Thus, the final data tensor for covariate tests contains either t = 116 (UCLA) or t = 300 (Michigan) time-points for p = 110 brain regions in n = 100 subjects.

Before applying the R^3 procedure from Section 2.3 to the preprocessed ABIDE dataset, we need to ensure fMRI observations are approximately independent. By whitening temporal observations, we ensure that estimating individual subject networks is more efficient. We achieve this by first estimating the temporal precision matrix $\hat{\Omega} = \sum_{i=1}^{n} \mathbf{Y}^{(i)} (\mathbf{Y}^{(i)})^{\top}$ using the banded regularization procedure of Bickel and Levina (2008) for autoregressive data and whitening the fMRI timeseries of each subject $\tilde{\mathbf{Y}}^{(i)} = \hat{\Omega}^{1/2} \mathbf{Y}^i$. To choose the number of lags, we conduct model selection via cross-validation (Bickel and Levina, 2008). Given these whitened observations, we apply the R^3 procedure outlined in Algorithm 1. We initialize regularization parameters using StARS and subsequently perturb these parameters according to RAP as described in Section 2.3. Since we have a total of 23 node density and subnetwork density hypotheses, we control the false discovery rate at the 5% level using the Benjamini-Yekutieli procedure (Benjamini and Yekutieli, 2001).

4.3. ABIDE Data Analysis: Results

Tables 1, 2 show statistically significant covariate effects for 3 subnetwork hypotheses and 5 regions of interest. Notable findings amongst subnetwork hypotheses in **Table 1** are that an increase in behavioral deficits indicated by restricted and repetitive behavior scores (RRB) and social affect (SA) is associated with a decrease in connection densities in frontoparietal-based subnetworks. The 3 prominent findings involve connection densities between the frontoparietal to limbic subnetworks, between the default mode and limbic







covariate effects in **Table 1**. Using previous studies discussed in Section 4.2, we seek to test whether symptom severity is associated with individual differences in the density or number of connections within and between these sub-networks. Panels (**A**–**D**) illustrate subnetwork components of the full group level network in panel (**E**). The network structure in Panel (**A**) shows links within the limbic subnetwork as well as between the limbic regions and all other brain regions. Similarly, each of the other panels emphasize connectivity of fronto-parietal (**B**), ventral attention (**C**), and default mode (**D**) regions, respectively, to the whole brain. For the purposes of illustration, this group level network is obtained using individually estimated graphical models from the procedure in Section 2.3.1. Nodes correspond to anatomical regions in the Harvard Oxford Atlas (Fischl et al., 2004). The subnetworks correspond to resting state networks provided by Yeo et al. (2011). We first threshold weak edges with stability scores less than 0.8 in individual subject networks and then obtain a group level network by aggregating edge presence across all subjects. Note that we use this group network exclusively for illustrative purposes and not for statistical inference. The color gradient for edges in group network in panel (**E**) corresponds to proportion of stable edges found across all subjects.

TABLE 1	Joint ADOS	covariate effects	on subnetwork density.
---------	------------	-------------------	------------------------

Subnetwork 1	Subnetwork 2	pval (RRB + SA)	RRB	CI (L)	CI (U)	SA	CI (L)	CI (U)	SITE	CI (L)	CI (U)
Default	Default	0.061200	-2.66	-7.10	1.78	-0.66	-2.92	1.59	0.22	-5.85	6.30
Default	Frontoparietal	0.010000	-2.34	-4.97	0.29	-0.18	-1.52	1.15	-0.52	-4.12	3.08
Default	Limbic	0.004530*	-1.51	-3.06	0.04	-0.10	-0.89	0.69	-0.30	-2.42	1.82
Default	Ventral attention	0.038000	-0.83	-1.76	0.10	0.08	-0.40	0.55	0.37	-0.91	1.64
Frontoparietal	Frontoparietal	0.007030	-1.36	-3.23	0.52	-0.51	-1.47	0.44	-0.47	-3.04	2.10
Frontoparietal	Limbic	0.000088*	-1.15	-1.98	-0.31	0.00	-0.43	0.43	0.23	-0.92	1.38
Frontoparietal	Ventral attention	0.003793*	-0.61	-1.16	-0.06	0.03	-0.25	0.31	0.75	0.00	1.50
Limbic	Limbic	0.530000	-0.19	-1.70	1.32	-0.35	-1.11	0.42	-0.77	-2.83	1.29
Limbic	Ventral attention	0.955000	0.01	-0.45	0.46	-0.05	-0.28	0.18	-0.69	-1.31	-0.06
Ventral attention	Ventral attention	0.196000	-0.05	-0.50	0.40	-0.21	-0.44	0.02	-0.24	-0.86	0.37

We jointly test the effects of two ADOS covariates on subnetwork density while accounting for site effects as a nuisance covariate. Here, the most prominent findings suggest that a decrease in the number of direct connections between frontoparietal to limbic, between frontoparietal to ventral attention subnetworks and between default to limbic subnetworks is linked with increased ADOS symptom severity. This result is consistent with the hypothesis that abnormalities within the salience network, comprising anterior cingulate cortex (a region within our frontoparietal network) and insula (a region within our ventral attention network), results in a failure to regulate between attention to external stimuli vs. attention to internal thoughts. A total of three subnetworks, denoted by *, survive corrections for multiplicity, using false discovery control over all 23 hypotheses tested at the 5% level using Benjamini-Yekuteli. Although estimates of site effects were non-zero, individual confidence intervals for most site effects are close to or include zero and were thus not statistically significant after corrections for multiplicity. Results are discussed further in Section 4.3

TABLE 2 | Joint ADOS covariate effects on node density.

Subnetwork	Region	pval (RRB + SA)	RRB	CI (L)	CI (U)	SA	CI (L)	CI (U)	SITE	CI (L)	CI (U)
Default	L. Cingulate post.	0.004600*	-0.68	-1.35	-0.02	-0.01	-0.34	0.33	-0.05	-0.96	0.86
Default	R. Cingulate post.	0.009000	-0.49	-0.96	-0.01	0.03	-0.21	0.27	0.39	-0.26	1.03
Default	R. pSTG	0.010900	-0.41	-0.85	0.04	-0.02	-0.24	0.21	0.08	-0.53	0.69
Frontoparietal	R. Cingulate ant.	0.002100*	-0.30	-0.65	0.04	-0.08	-0.26	0.10	0.62	0.14	1.09
Frontoparietal	R. IFG pars oper	0.004100*	-0.69	-1.30	-0.09	0.06	-0.25	0.36	0.05	-0.78	0.88
Frontoparietal	L. Cingulate ant.	0.005400*	-0.55	-1.14	0.05	-0.06	-0.36	0.24	-0.05	-0.86	0.76
Frontoparietal	L. IFG pars oper	0.058000	-0.29	-0.70	0.11	-0.01	-0.22	0.19	0.07	-0.48	0.62
Limbic	R. Thalamus	0.004200*	-0.46	-1.02	0.10	-0.12	-0.41	0.16	-0.65	-1.41	0.12
Limbic	L. Thalamus	0.037700	-0.49	-1.20	0.21	-0.08	-0.43	0.28	-0.57	-1.53	0.39
Limbic	R. Amygdyla	0.092500	-0.29	-0.23	0.21	-0.01	-0.72	0.14	-0.26	-0.85	0.33
Limbic	L. Amygdyla	0.175100	-0.14	-0.49	0.21	-0.07	-0.25	0.11	0.30	-0.19	0.78
Ventral attention	L. Insula	0.223300	-0.11	-0.46	0.24	-0.08	-0.26	0.09	-0.24	-0.72	0.23
Ventral attention	R. Insula	0.306800	-0.13	-0.60	0.34	-0.10	-0.34	0.14	-0.76	-1.40	-0.12

We jointly test the effects of two ADOS covariates on node density while accounting for site effects as a nuisance covariate. Notably, we find that a decrease in the number of direct connections between left posterior cingulate cortex (PCC) and anterior cingulate cortex (ACC) with all other regions is linked with an increase in ADOS symptom severity. This result corroborates previous findings that ACC (a component of the salience network) and PCC connectivity might be directly involved behavioral deficits ASD. A total of five regions, denoted by *, survive corrections for multiplicity, using false discovery control over all 23 hypotheses tested at the 5% level using Benjamini-Yekutieli. Although estimates of site effects were non-zero, individual confidence intervals for most site effects are close to or include zero and were thus not statistically significant after corrections for multiplicity. Results are discussed further in Section 4.3.

subnetworks. Individual regression coefficients and confidence intervals for RRB and SA suggest that of the two covariates, RRB scores particularly dominate the decrease in subnetwork density for two of these results, particularly the frontoparietallimbic subnetwork. The most prominent results amongst region of interest hypotheses in **Table 2** suggest that ADOS symptom severity is again associated with hypoconnectivity or a decrease in the number of connections between each of the following regions with the rest of the network—bilateral pairs of anterior cingulate cortex (ACC); left posterior cingulate cortex(PCC); the right inferior frontal gyrus (IFG); and the thalamus. Note that we use a conservative Benjamini-Yekutieli procedure (Benjamini and Yekutieli, 2001) to control for FDR at the 5% level under arbitrary dependence amongst the 23 hypotheses tested. Under a less conservative procedure, Benjamini-Hochberg (Benjamini and Hochberg, 1995), four additional hypotheses including the within-frontoparietal subnetwork and the right PCC are statistically significant at 5% FDR control. While the regression coefficients for site effects are non-zero in both analyses, most confidence intervals either contain zero or are very close to zero and not statistically significant. The one exception amongst our prominent findings, the right ACC, shows statistically significant site effects. We also find site effects for two hypotheses where we did not detect ADOS effects, namely, the limbic to ventral attention subnetwork and right insula. However, these site effects are not statistically significant after correcting for multiplicity.

Our analysis strongly implicates the frontoparietal-limbic subnetwork, and frontoparietal-ventral attention subnetworks, as well as posterior/anterior cingulate cortical connections with the rest of the brain, in behavioral deficits of ASD. Since we identify these regions and subnetworks using partial correlation measures of functional connectivity, our results provide strong evidence that these network components are directly involved in ASD. In particular, since the salience network (Buckner et al., 2013; Uddin et al., 2013a) is thought to comprise the ACC, which falls within our frontoparietal network, and insular regions that overlap limbic and ventral attention networks in our analysis, our subnetwork findings are consistent with the salience network explanation for behavioral deficits in autism. Additionally, our findings strongly implicate frontoparietal-limbic relationships. While our region of interest analysis found abnormalities in thalamar connectivity, a component of the limbic network, other limbic regions could also be directly involved in ASD and thus warrant further study.

We contrast our findings on the 23 a-priori hypotheses in Section 4.2 with previous analyses that were obtained by conducting network analyses on correlational networks, including previous analyses of the same ABIDE dataset. Our analysis detects only a subset of previous covariate effects on ASD network structure when using GGM based networks via R^3 . Correlational network analysis using the UCLA and UM samples of ABIDE (Rudie et al., 2012b; Di Martino et al., 2014b) as well as those form alternative sites (Uddin et al., 2013b) link insular, amygdylar connectivity with autism symptoms, whereas we do not detect strong effects for these regions for density metrics. The absence of strong covariate effects using GGMs suggests that the insular and amygdylar connections might be associated with behavioral deficits in autism only due to indirect correlations with other regions of interest. Similarly, although we find abnormalities in the PCC, a region within the default mode network, and between the default-mode and the limbic regions, we failed to find abnormalities linking the default mode with frontoparietal or ventral attention networks. This suggests that previous findings involving the default mode network could have been the result of indirect pairwise correlations, possibly driven by PCC and limbic regions. Although we use novel functional connectivity models and methods to analyze the ABIDE dataset, some of our choices of a-priori hypotheses for this analysis, notably, the inclusion of IFG pars opercularis and the amygdyla for node density, were guided by alternative analyses of the ABIDE dataset (Rudie et al., 2012b; Di Martino et al., 2014b). Thus, we need further validation of the purported effects of ADOS on IFG pars opercularis density.

5. DISCUSSION

This paper investigates an understudied issue in neuroimaging the impact of (often imperfectly) estimated functional networks on subsequent population level inference to find differences across functional networks. Using an important class of network models for functional connectivity, Gaussian graphical models, we demonstrate that neglecting errors in estimated functional networks reduces statistical power to detect covariate effects for network metrics. While lack of statistical power due to small subject sizes is well documented in neuroimaging (Button et al., 2013), recent test re-test studies (Birn et al., 2013; Laumann et al., 2015) suggest that typical fMRI studies of 5-10 min are highly susceptible to lack of statistical power. This paper provides additional evidence that within subject sample size, t, is important for well powered studies. For typical studies where t is comparable to the number of nodes p, errors in estimating functional networks can be substantial and not accounted for by standard test statistics. We show that our methods to mitigate this problem, R^2 and R^3 , are always at least as powerful if not substantially more powerful than standard test statistics under a variety of sample sizes and covariate signal-to-noise regimes. Additionally, regardless of the methods employed, our power analyses suggest that in many scenarios, particularly when subject level networks are large, a more efficient use of a fixed experimental budget would be to collect more within subject measurements and fewer subject samples in order to maximize statistical power to detect covariate effects. While we demonstrate this result on the joint importance of within and between subject sample sizes using density based network metrics, we expect such results to hold more generally whenever population level functional connectivity analyses are conducted in a two-step manner where subject level networks are estimated initially and population level metrics then explicitly depend on the quality of subject level network estimates. In practice, we additionally need to incorporate other considerations beyond statistical power in choosing within subject scan length such as increase in movement or the discomfort to participants particularly in patient populations. These issues related to statistical power warrant further investigation in future work.

This paper also highlights the scientific merits of employing explicit density based metrics in graphical models of functional connectivity to gain insights into disease mechanisms at a macroscopic level using the ABIDE dataset (Di Martino et al., 2014b). In Section 4, we sought to detect covariate effects on the density of direct, long range functional connections in Austism Spectrum Disorders (ASD). Notably, our results in Section 4.3, at both the subnetwork and node level favor the hypoconnectivity hypothesis for behavioral deficits in ASD. Specifically, we find that a reduction in directly involved long-range functional connections between parcellated regions of interest increases ADOS symptom severity. Assuming that the salience network model of autism dysfunction is correct (Uddin, 2014), our results suggest that reduced interactions between the executive control network and the salience network, as well as default mode to the salience network might be responsible for ASD symptoms. Since we employ GGM based models, a plausible interpretation of such hypoconnectivity is that regions in ventral attention and limbic systems fail to adequately communicate with frontoparietal regions that participate in executive control and default mode regions that participate in internal attention. A previous study found evidence of hyperconnectivity when counting the number of local voxelwise connections in Keown et al. (2013). Our results

do not contradict this finding since a network architecture of ASD could involve both reduced long range connections as well as increased density of local connections (Rudie and Dapretto, 2013). Other results on hyperconnectivity (Supekar et al., 2013; Uddin et al., 2013a) do not explicitly employ degree or density of connections to measure hyper or hypo-conectivity but measure the strength of the mean pairwise correlation within and between regions and subnetworks. While the effect in Supekar et al. (2013) appears to be a large and robust finding, the correlational model of connectivity employed in their analysis could be misleading since it includes both direct and indirect functional connections and does not explicitly measure the density of connections. While further studies are needed to resolve the questions raised by Rudie and Dapretto (2013) on this matter, we emphasize that since graphical models of functional connectivity capture direct functional connections, such models enable stronger scientific conclusions regarding functional network mechanisms compared to purely correlational models where edges do not necessarily reflect direct communication between regions.

As we discuss in the simulation results in Section 3.2, our ability to detect covariate effects in populations of graphical models deteriorates in highly dense regimes of network structure where the density or number of edges in the network increases substantially while the number of within subject observations remains limited, or when the individual networks contain a large number of hub-like structures (Ravikumar et al., 2011; Zhou et al., 2011). Since our resampling based methods are a framework that employ existing graph estimation algorithms (Section 2.3), they inherit the strengths and limitations of the specific graph estimation algorithm in such high density regimes. By incorporating new and improved estimators (Yang et al., 2014) for graphical models at the level of individual subjects, we expect corresponding variants of our resampling framework to detect covariate effects under a wider range of network density regimes.

While this paper specifically considers network models (Equation 1) where neuroimaging data is distributed according to a multivariate normal, alternative distributions can be employed for the subject level model in Equation (1), including matrix variate distributions (Allen and Tibshirani, 2012; Zhou et al., 2014) that can account for the serial correlation in temporal observations, and non-parametric graphical models (Lafferty et al., 2012) that relax assumptions of normality. Furthermore, while we focus on resting state functional connectivity in fMRI in this work, our concern regarding errors in estimating large functional networks is applicable to other imaging modalities including EEG/MEG studies. In fact, our two level models (Equation 1) and R^3 framework can be easily extended to functional network analyses based on partial coherence (Sato

REFERENCES

Achard, S., Salvador, R., Whitcher, B., Suckling, J., and Bullmore, E. (2006). A resilient, low-frequency, small-world human brain functional network with highly connected association cortical hubs. J. Neurosci. 26, 63–72. doi: 10.1523/JNEUROSCI.3874-05.2006 et al., 2009) networks or vector autoregressive models (Koenig et al., 2005; Schelter et al., 2006) that are popular in EEG/MEG studies. Additionally, our results are highly relevant to dynamic functional connectivity (Chang and Glover, 2010) analyses where studies estimate separate time-varying functional networks per subject using short sliding-windows of 30-60 s rather than 5-10 min. In such a high dimensional setting where $t \ll p$, our power analyses in Figures 2, 3 suggest that such dynamic network analyses will be highly underpowered and could benefit from our methods. Thus, extensions of the R^3 framework for dynamic connectivity analyses as well as other multivariate network models is a promising avenue of research. Other areas of investigation include inference for partial correlation strength and corresponding weighted network analysis, as well as including high dimensional covariates in our general linear model (Equation 2). Overall, this work reveals that accounting for imperfectly estimated functional networks dramatically improves statistical power to detect population level covariate effects, thus highlighting an important new direction for future research.

6. DATA SHARING

The preprocessed ABIDE dataset used in this paper is available at http://dx.doi.org/10.6084/m9.figshare.1533313. Software for reproducing our analysis is be provided at https://bitbucket.org/gastats/monet/downloads.

AUTHOR CONTRIBUTIONS

MN and GA conceived and designed the research. MN conducted data analysis. MN and GA wrote and revised the paper.

FUNDING

MN and GA are supported by NSF DMS 1264058. MN is supported an AWS (Amazon Web Services) research grant for computational resources.

ACKNOWLEDGMENTS

The authors thank Steffie Tomson for helpful discussions and advice on preprocessing the ABIDE dataset.

SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: http://journal.frontiersin.org/article/10.3389/fnins. 2016.00108

Agresti, A. (2002). Categorical Data Analysis, Vol. 359. Hoboken, NJ: John Wiley & Sons.

- Agresti, A. (2015). *Foundations of Linear and Generalized Linear Models*. Hoboken, NJ: John Wiley & Sons.
- Alaerts, K., Woolley, D. G., Steyaert, J., Di Martino, A., Swinnen, S. P., and Wenderoth, N. (2013). Underconnectivity of the superior temporal sulcus

predicts emotion recognition deficits in autism. Soc. Cogn. Affect. Neurosci. 9, 1589–1600. doi: 10.1093/scan/nst156

- Alexander-Bloch, A., Lambiotte, R., Roberts, B., Giedd, J., Gogtay, N., and Bullmore, E. (2012). The discovery of population differences in network community structure: new methods and applications to brain functional networks in schizophrenia. *NeuroImage* 59, 3889–3900. doi: 10.1016/j.neuroimage.2011.11.035
- Allen, G. I., and Tibshirani, R. (2012). Inference with transposable data: modelling the effects of row and column correlations. J. R. Stat. Soc. Ser. B 74, 721–743. doi: 10.1111/j.1467-9868.2011.01027.x
- Balachandran, P., Airoldi, E., and Kolaczyk, E. (2013). Inference of network summary statistics through network denoising. arXiv:1310.0423.
- Bassett, D. S., Porter, M. A., Wymbs, N. F., Grafton, S. T., Carlson, J. M., and Mucha, P. J. (2013). Robust detection of dynamic community structure in networks. *Chaos Interdiscipl. J. Nonlin. Sci.* 23, 013142. doi: 10.1063/1. 4790830
- Beckmann, C. F., Jenkinson, M., and Smith, S. M. (2003). General multilevel linear modeling for group analysis in fmri. *Neuroimage* 20, 1052–1063. doi: 10.1016/S1053-8119(03)00435-X
- Benjamini, Y., and Hochberg, Y. (1995). Controlling the false discovery rate: a practical and powerful approach to multiple testing. *J. R. Stat. Soc. Ser. B* 57, 289–300.
- Benjamini, Y., and Yekutieli, D. (2001). The control of the false discovery rate in multiple testing under dependency. Ann. Stat. 29, 1165–1188. doi: 10.1214/aos/ 1013699998
- Berk, R., Brown, L., Buja, A., Zhang, K., and Zhao, L. (2013). Valid post-selection inference. Ann. Stat. 41, 802–837.
- Bernal-Rusiel, J. L., Greve, D. N., Reuter, M., Fischl, B., Sabuncu, M. R., Initiative, A. D. N., et al. (2013). Statistical analysis of longitudinal neuroimage data with linear mixed effects models. *Neuroimage* 66, 249–260. doi: 10.1016/j.neuroimage.2012.10.065
- Bickel, P. J., and Levina, E. (2008). Regularized estimation of large covariance matrices. Ann. Stat. 36, 199–227. doi: 10.1214/009053607000000758
- Birn, R. M., Molloy, E. K., Patriat, R., Parker, T., Meier, T. B., Kirk, G. R., et al. (2013). The effect of scan length on the reliability of resting-state fmri connectivity estimates. *Neuroimage* 83, 550–558. doi: 10.1016/j.neuroimage.2013.05.099
- Braun, U., Plichta, M. M., Esslinger, C., Sauer, C., Haddad, L., Grimm, O., et al. (2012). Test-retest reliability of resting-state connectivity network characteristics using fmri and graph theoretical measures. *Neuroimage* 59, 1404–1412. doi: 10.1016/j.neuroimage.2011.08.044
- Breiman, L. (1996a). Bagging predictors. Mach. Learn. 24, 123–140. doi: 10.1007/BF00058655
- Breiman, L. (1996b). Heuristics of instability and stabilization in model selection. *Ann. Stat.* 24, 2350–2383. doi: 10.1214/aos/1032181158
- Buckner, R. L., Krienen, F. M., and Yeo, B. T. (2013). Opportunities and limitations of intrinsic functional connectivity mri. *Nat. Neurosci.* 16, 832–837. doi: 10.1038/nn.3423
- Buckner, R. L., Sepulcre, J., Talukdar, T., Krienen, F. M., Liu, H., Hedden, T., et al. (2009). Cortical hubs revealed by intrinsic functional connectivity: mapping, assessment of stability, and relation to alzheimer's disease. *J. Neurosci.* 29, 1860–1873. doi: 10.1523/JNEUROSCI.5062-08.2009
- Bühlmann, P., and Yu, B. (2002). Analyzing bagging. Ann. Stat. 30, 927–961. doi: 10.1214/aos/1031689014
- Bullmore, E. (2012). Functional network endophenotypes of psychotic disorders. *Biol. Psychiatry* 71, 844. doi: 10.1016/j.biopsych.2012.03.019
- Bullmore, E., and Sporns, O. (2009). Complex brain networks: graph theoretical analysis of structural and functional systems. *Nat. Rev. Neurosci.* 10, 186–198. doi: 10.1038/nrn2575
- Bullmore, E., and Sporns, O. (2012). The economy of brain network organization. Nat. Rev. Neurosci. 13, 336–349. doi: 10.1038/nrn3214
- Button, K. S., Ioannidis, J. P., Mokrysz, C., Nosek, B. A., Flint, J., Robinson, E. S., et al. (2013). Power failure: why small sample size undermines the reliability of neuroscience. *Nat. Rev. Neurosci.* 14, 365–376. doi: 10.1038/ nrn3475
- Cai, T., Liu, W., and Luo, X. (2011). A constrained ℓ1 minimization approach to sparse precision matrix estimation. JASA 106, 594–607. doi: 10.1198/jasa.2011.tm10155

- Chang, C., and Glover, G. H. (2010). Time-frequency dynamics of restingstate brain connectivity measured with fmri. *Neuroimage* 50, 81–98. doi: 10.1016/j.neuroimage.2009.12.011
- Cherkassky, V. L., Kana, R. K., Keller, T. A., and Just, M. A. (2006). Functional connectivity in a baseline resting-state network in autism. *Neuroreport* 17, 1687–1690. doi: 10.1097/01.wnr.0000239956.45448.4c
- Craddock, C. (2014). "Preprocessed connectomes project: open sharing of preprocessed neuroimaging data and derivatives," in 61st Annual Meeting (AACAP), (San Diego, CA: AACAP).
- Craddock, R. C., and Bellec, P. (2015). Preprocessed Connectomes Project: Abide. Availbel online at: http://preprocessed-connectomes-project.github.io/abide/
- Craddock, R. C., Jbabdi, S., Yan, C.-G., Vogelstein, J. T., Castellanos, F. X., Di Martino, A., et al. (2013). Imaging human connectomes at the macroscale. *Nat. Methods* 10, 524–539. doi: 10.1038/nmeth.2482
- Di Martino, A., Fair, D. A., Kelly, C., Satterthwaite, T. D., Castellanos, F. X., Thomason, M. E., et al. (2014a). Unraveling the miswired connectome: a developmental perspective. *Neuron* 83, 1335–1353. doi: 10.1016/j.neuron.2014.08.050
- Di Martino, A., Yan, C.-G., Li, Q., Denio, E., Castellanos, F. X., Alaerts, K., et al. (2014b). The autism brain imaging data exchange: towards a large-scale evaluation of the intrinsic brain architecture in autism. *Mol. Psychiatry* 19, 659–667. doi: 10.1038/mp.2013.78
- Di Martino, A., Shehzad, Z., Kelly, C., Roy, A. K., Gee, D. G., Uddin, L. Q., et al. (2009). Relationship between cingulo-insular functional connectivity and autistic traits in neurotypical adults. *Am. J. Psychiatry* 166, 891–899. doi: 10.1176/appi.ajp.2009.08121894
- Efron, B., and Tibshirani, R. J. (1993). An Introduction to the Bootstrap. London, UK: Chapman & Hall.
- Fischl, B., van der Kouwe, A., Destrieux, C., Halgren, E., Ségonne, F., Salat, D. H., et al. (2004). Automatically parcellating the human cerebral cortex. *Cereb. Cortex* 14, 11–22. doi: 10.1093/cercor/bhg087
- Fox, M. D., Corbetta, M., Snyder, A. Z., Vincent, J. L., and Raichle, M. E. (2006). Spontaneous neuronal activity distinguishes human dorsal and ventral attention systems. *Proc. Natl. Acad. Sci. U.S.A.* 103, 10046–10051. doi: 10.1073/pnas.0604187103
- Friedman, J., Hastie, T., and Tibshirani, R. (2008). Sparse inverse covariance estimation with the graphical lasso. *Biostatistics* 9, 432–441. doi: 10.1093/biostatistics/kxm045
- Giavasis, S. (2015). Configurable-Pipeline for the Analysis of Connectomes Version 0.3.8. Available online at: http://dx.doi.org/10.5281/zenodo.14298
- Ginestet, C. E., Fournel, A. P., and Simmons, A. (2014). Statistical network analysis for functional mri: summary networks and group comparisons. *Front. Comput. Neurosci.* 8:51. doi: 10.3389/fncom.2014.00051
- Gotham, K., Pickles, A., and Lord, C. (2009). Standardizing ados scores for a measure of severity in autism spectrum disorders. J. Autism Dev. Disord. 39, 693–705. doi: 10.1007/s10803-008-0674-3
- Hacker, C. D., Laumann, T. O., Szrama, N. P., Baldassarre, A., Snyder, A. Z., Leuthardt, E. C., et al. (2013). Resting state network estimation in individual subjects. *Neuroimage* 82, 616–633. doi: 10.1016/j.neuroimage.2013.05.108
- Hahamy, A., Behrmann, M., and Malach, R. (2015). The idiosyncratic brain: distortion of spontaneous connectivity patterns in autism spectrum disorder. *Nat. Neurosci.* 18, 302–309. doi: 10.1038/nn.3919
- Honey, C. J., Kötter, R., Breakspear, M., and Sporns, O. (2007). Network structure of cerebral cortex shapes functional connectivity on multiple time scales. *Proc. Natl. Acad. Sci. U.S.A.* 104, 10240–10245. doi: 10.1073/pnas.0701519104
- Hsieh, C.-J., Sustik, M. A., Dhillon, I. S., and Ravikumar, P. (2011). Sparse inverse covariance matrix estimation using quadratic approximation. *Adv. Neural Inf. Proces. Syst.* 24, 2330–2338. arXiv:1306.3212
- Hsieh, C.-J., Sustik, M. A., Dhillon, I. S., Ravikumar, P. K., and Poldrack, R. (2013). Big & quic: Sparse inverse covariance estimation for a million variables. *Adv. Neural Inf. Proces. Syst.* 26, 3165–3173.
- Insel, T. R. (2014). The nimh research domain criteria (rdoc) project: precision medicine for psychiatry. Am. J. Psychiatry 171, 395–397. doi: 10.1176/appi.ajp.2014.14020138
- Kaiser, R. H., Andrews-Hanna, J. R., Wager, T. D., and Pizzagalli, D. A. (2015). Large-scale network dysfunction in major depressive disorder a meta-analysis of resting-state functional connectivity. *JAMA Psychiatry* 72, 603–611. doi: 10.1001/jamapsychiatry.2015.0071

- Keown, C. L., Shih, P., Nair, A., Peterson, N., Mulvey, M. E., and Müller, R.-A. (2013). Local functional overconnectivity in posterior brain regions is associated with symptom severity in autism spectrum disorders. *Cell Rep.* 5, 567–572. doi: 10.1016/j.celrep.2013.10.003
- Kim, J., Wozniak, J. R., Mueller, B. A., Shen, X., and Pan, W. (2014). Comparison of statistical tests for group differences in brain functional networks. *NeuroImage* 101, 681–694. doi: 10.1016/j.neuroimage.2014. 07.031
- Koenig, T., Studer, D., Hubl, D., Melie, L., and Strik, W. (2005). Brain connectivity at different time-scales measured with eeg. *Philos. Trans. R. Soc. B Biol. Sci.* 360, 1015–1024. doi: 10.1098/rstb.2005.1649
- Lafferty, J., Liu, H., and Wasserman, L. (2012). Sparse nonparametric graphical models. Statist. Sci. 27, 519–537. doi: 10.1214/12-STS391
- Lahiri, S. N. (2013). Resampling Methods for Dependent Data. New York, NY: Springer Science & Business Media
- Laird, N. M., and Ware, J. H. (1982). Random-effects models for longitudinal data. Biometrics 38, 963–974. doi: 10.2307/2529876
- Laumann, T. O., Gordon, E. M., Adeyemo, B., Snyder, A. Z., Joo, S. J., Chen, M.-Y., et al. (2015). Functional system and areal organization of a highly sampled individual human brain. *Neuron* 87, 657–670. doi: 10.1016/j.neuron.2015.06.037
- Lauritzen, S. L. (1996). *Graphical Models*, Vol. 17, New York, NY: Oxford University Press.
- Lenroot, R. K., and Yeung, P. K. (2013). Heterogeneity within autism spectrum disorders: what have we learned from neuroimaging studies? *Front. Hum. Neurosci.* 7:733. doi: 10.3389/fnhum.2013.00733
- Liang, K.-Y., and Zeger, S. L. (1993). Regression analysis for correlated data. *Annu. Rev. Public Health* 14, 43–68. doi: 10.1146/annurev.pu.14.050193.000355
- Liu, H., Roeder, K., and Wasserman, L. (2010). Stability approach to regularization selection (stars) for high dimensional graphical models. *Adv. Neural Inf. Process. Syst.* 24, 1432, arXiv:1006.3316.
- Lui, S., Wu, Q., Qiu, L., Yang, X., Kuang, W., Chan, R. C., et al. (2014). Resting-state functional connectivity in treatment-resistant depression, *Am. J. Psychiatry* 168, 642–648. doi: 10.1176/appi.ajp.2010.10101419
- Marrelec, G., Krainik, A., Duffau, H., Pélégrini-Issac, M., Lehéricy, S., Doyon, J., et al. (2006). Partial correlation for functional brain interactivity investigation in functional MRI, *Neuroimage* 32, 228–237. doi: 10.1016/j.neuroimage.2005. 12.057
- Meda, S. A., Gill, A., Stevens, M. C., Lorenzoni, R. P., Glahn, D. C., Calhoun, V. D., et al. (2012). Differences in resting-state functional magnetic resonance imaging functional network connectivity between schizophrenia and psychotic bipolar probands and their unaffected first-degree relatives, *Biol. Psychiatry* 71, 881–889. doi: 10.1016/j.biopsych.2012.01.025
- Meinshausen, N., and Bühlmann, P. (2006). High-dimensional graphs and variable selection with the lasso. Ann. Stat. 34, 1436–1462. doi: 10.1214/009053606000000281
- Meinshausen, N., and Buhlmann, P. (2010). Stability selection. J. R. Stat. Soc. Ser. B 72, 417–473. doi: 10.1111/j.1467-9868.2010.00740.x
- Menon, V. (2011). Large-scale brain networks and psychopathology: a unifying triple network model. *Trends Cogn. Sci.* 15, 483–506. doi: 10.1016/j.tics.2011.08.003
- Monk, C. S., Peltier, S. J., Wiggins, J. L., Weng, S.-J., Carrasco, M., Risi, S., et al. (2009). Abnormalities of intrinsic functional connectivity in autism spectrum disorders. *Neuroimage* 47, 764–772. doi: 10.1016/j.neuroimage.2009.04.069
- Murphy, K., Birn, R. M., Handwerker, D. A., Jones, T. B., and Bandettini, P. A. (2009). The impact of global signal regression on resting state correlations: are anti-correlated networks introduced? *Neuroimage* 44, 893–905. doi: 10.1016/j.neuroimage.2008.09.036
- Narayan, M., and Allen, G. I. (2013). "Randomized approach to differential inference in multi-subject functional connectivity," in *Pattern Recognition in Neuroimaging (PRNI), 2013 International Workshop on (IEEE)* (Philadelphia, PA), 78–81. doi: 10.1109/PRNI.2013.29
- Narayan, M., Allen, G. I., and Tomson, S. (2015). Two sample inference for populations of graphical models with applications to functional connectivity. arXiv:1502.03853.
- Palaniyappan, L., Simmonite, M., White, T. P., Liddle, E. B., and Liddle, P. F. (2013). Neural primacy of the salience processing system in schizophrenia, *Neuron* 79, 814–828. doi: 10.1016/j.neuron.2013.06.027

- Penny, W. D., Holmes, A., and Friston, K. (2003). Random effects analysis. Hum. Brain Funct. 2, 843–850. doi: 10.1016/B978-012264841-0/50044-5
- Politis, D., Romano, J., and Wolf, M. (1999). Subsampling. New York, NY: Springer.
- Power, J. D., Schlaggar, B. L., Lessov-Schlaggar, C. N., and Petersen, S. E. (2013). Evidence for hubs in human functional brain networks. *Neuron* 79, 798–813. doi: 10.1016/j.neuron.2013.07.035
- Ravikumar, P., Wainwright, M. J., Raskutti, G., and Yu, B. (2011). High-dimensional covariance estimation by minimizing *l*₁-penalized log-determinant divergence. *Electron. J. Statist.* 5, 935–980. doi: 10.1214/11-EJS631
- Rothman, A. J., Bickel, P. J., Levina, E., and Zhu, J. (2008). Sparse permutation invariant covariance estimation. *Electron. J. Statist.* 2, 494–515. doi: 10.1214/08-EJS176
- Rubinov, M., and Sporns, O. (2010). Complex network measures of brain connectivity: uses and interpretations. *Neuroimage* 52, 1059–1069. doi: 10.1016/j.neuroimage.2009.10.003
- Rudie, J., Brown, J., Beck-Pancer, D., Hernandez, L., Dennis, E., Thompson, P., et al. (2012a). Altered functional and structural brain network organization in autism. *NeuroImage* 2, 79–94. doi: 10.1016/j.nicl.2012.11.006
- Rudie, J. D., and Dapretto, M. (2013). Convergent evidence of brain overconnectivity in children with autism? *Cell Rep.* 5, 565–566. doi: 10.1016/j.celrep.2013.10.043
- Rudie, J. D., Shehzad, Z., Hernandez, L. M., Colich, N. L., Bookheimer, S. Y., Iacoboni, M., et al. (2012b). Reduced functional integration and segregation of distributed neural systems underlying social and emotional information processing in autism spectrum disorders. *Cereb. Cortex* 22, 1025–1037. doi: 10.1093/cercor/bhr171
- Sato, J. R., Takahashi, D. Y., Arcuri, S. M., Sameshima, K., Morettin, P. A., and Baccalá, L. A. (2009). Frequency domain connectivity identification: an application of partial directed coherence in fmri. *Hum. Brain Mapp.* 30, 452– 461. doi: 10.1002/hbm.20513
- Schelter, B., Winterhalder, M., Eichler, M., Peifer, M., Hellwig, B., Guschlbauer, B., et al. (2006). Testing for directed influences among neural signals using partial directed coherence. *J. Neurosci. Methods* 152, 210–219. doi: 10.1016/j.jneumeth.2005.09.001
- Searle, S. R., Casella, G., and McCulloch, C. E. (2009). Variance Components, Vol. 391, Hoboken, NJ: Wiley-Interscience.
- Shehzad, Z., Kelly, A. C., Reiss, P. T., Gee, D. G., Gotimer, K., Uddin, L. Q., et al. (2009). The resting brain: unconstrained yet reliable. *Cereb. Cortex* 19, 2209–2229. doi: 10.1093/cercor/bhn256
- Simpson, S. L., Bowman, F. D., and Laurienti, P. J. (2013). Analyzing complex functional brain networks: fusing statistics and network science to understand the brain. *Statist. Surv.* 7, 1–36. doi: 10.1214/13-SS103
- Smith, S. M., Miller, K. L., Salimi-Khorshidi, G., Webster, M., Beckmann, C. F., Nichols, T. E., et al. (2011). Network modelling methods for fmri. *NeuroImage* 54, 875–891. doi: 10.1016/j.neuroimage.2010.08.063
- Smith, S. M., Vidaurre, D., Beckmann, C. F., Glasser, M. F., Jenkinson, M., Miller, K. L., et al. (2013). Functional connectomics from resting-state fmri. *Trends Cogn. Sci.* 17, 666–682. doi: 10.1016/j.tics.2013.09.016
- Supekar, K., Uddin, L. Q., Khouzam, A., Phillips, J., Gaillard, W. D., Kenworthy, L. E., et al. (2013). Brain hyperconnectivity in children with autism and its links to social deficits. *Cell Rep.* 5, 738–747. doi: 10.1016/j.celrep.2013.10.001
- Tam, A., Orban, P., Dansereau, C., Belleville, S., Benoit, S., Dagher, A., et al. (2014). Connectome-wide analysis of differences between normal aging, mild cognitive impairment, and dementia of the alzheimer's type using resting-state fmri connectivity. *Alzheimer Dement.* 10, P827–P828. doi: 10.1016/j.jalz.2014.05.089
- Tao, H., Guo, S., Ge, T., Kendrick, K. M., Xue, Z., Liu, Z., et al. (2013). Depression uncouples brain hate circuit. *Mol. Psychiatry* 18, 101–111. doi: 10.1038/mp.2011.127
- Tomson, S. N., Narayan, M., Allen, G. I., and Eagleman, D. M. (2013). Neural networks of colored sequence synesthesia. J. Neurosci. 33, 14098–14106. doi: 10.1523/JNEUROSCI.5131-12.2013
- Uddin, L. Q. (2014). Salience processing and insular cortical function and dysfunction. *Nat. Rev. Neurosci.* doi: 10.1038/nrn3857
- Uddin, L. Q., Supekar, K., Lynch, C. J., Khouzam, A., Phillips, J., Feinstein, C., et al. (2013a). Salience network-based classification and prediction of symptom severity in children with autism. *JAMA Psychiatry* 70, 869–879. doi: 10.1001/jamapsychiatry.2013.104

- Uddin, L. Q., Supekar, K., and Menon, V. (2013b). Reconceptualizing functional brain connectivity in autism from a developmental perspective. *Front. Hum. Neurosci.* 7:458. doi: 10.3389/fnhum.2013. 00458
- van den Heuvel, M. P., and Sporns, O. (2011). Rich-club organization of the human connectome. *J. Neurosci.* 31, 15775–15786. doi: 10.1523/JNEUROSCI.3539-11.2011
- van den Heuvel, M. P., Sporns, O., Collin, G., Scheewe, T., Mandl, R. C., Cahn, W., et al. (2013). Abnormal rich club organization and functional brain dynamics in schizophrenia. *JAMA Psychiatry* 70, 1–10. doi: 10.1001/jamapsychiatry.2013. 1328
- Van Dijk, K. R., Hedden, T., Venkataraman, A., Evans, K. C., Lazar, S. W., and Buckner, R. L. (2010). Intrinsic functional connectivity as a tool for human connectomics: theory, properties, and optimization. *J. Neurophysiol.* 103, 297– 321. doi: 10.1152/jn.00783.2009
- Varoquaux, G., Gramfort, A., Poline, J., and Thirion, B. (2012). Markov models for fmri correlation structure: is brain functional connectivity small world, or decomposable into networks? *J. Physiol.* 106, 212–221. doi: 10.1016/j. jphysparis.2012.01.001
- Wang, S., Nan, B., Rosset, S., and Zhu, J. (2011). Random lasso. *Ann. Appl. Stat.* 5, 468. doi: 10.1214/10-AOAS377
- Warren, D. E., Power, J. D., Bruss, J., Denburg, N. L., Waldron, E. J., Sun, H., et al. (2014). Network measures predict neuropsychological outcome after brain injury. *Proc. Natl. Acad. Sci. U.S.A.* 111, 14247–14252. doi: 10.1073/pnas.1322173111
- Williams, D. A. (1982). Extra-binomial variation in logistic linear models. Appl. Statist. 31, 144–148. doi: 10.2307/2347977
- Woolrich, M. W., Ripley, B. D., Brady, M., and Smith, S. M. (2001). Temporal autocorrelation in univariate linear modeling of fmri data. *Neuroimage* 14, 1370–1386. doi: 10.1006/nimg.2001.0931

- Worsley, K. J., Liao, C. H., Aston, J., Petre, V., Duncan, G., Morales, F., et al. (2002). A general statistical analysis for fmri data. *Neuroimage* 15, 1–15. doi: 10.1006/nimg.2001.0933
- Yang, E., Lozano, A. C., and Ravikumar, P. K. (2014). Elementary estimators for graphical models. Adv. Neural Inf. Proces. Syst. 2159–2167.
- Yeo, B. T. T., Krienen, F. M., Sepulcre, J., Sabuncu, M. R., Lashkari, D., Hollinshead, M., et al. (2011). The organization of the human cerebral cortex estimated by intrinsic functional connectivity. *J. Neurophysiol.*, 106, 1125–1165. doi: 10.1152/jn.00338.2011
- Yuan, M., and Lin, Y. (2007). Model selection and estimation in the gaussian graphical model. *Biometrika* 94, 19–35. doi: 10.1093/biomet/asm018
- Zhou, S., Rütimann, P., Xu, M., and Bühlmann, P. (2011). High-dimensional covariance estimation based on gaussian graphical models, *J. Mach. Learn. Res.* 12, 2975–3026. arXiv:1009.0530
- Zhou, S. et al. (2014). Gemini: graph estimation with matrix variate normal instances. *Ann. Stat.* 42, 532–562. doi: 10.1214/13-AOS1187
- Zuo, X.-N., Ehmke, R., Mennes, M., Imperati, D., Castellanos, F. X., Sporns, O., et al. (2012). Network centrality in the human functional connectome. *Cereb. Cortex* 22, 1862–1875. doi: 10.1093/cercor/bhr269

Conflict of Interest Statement: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

Copyright © 2016 Narayan and Allen. This is an open-access article distributed under the terms of the Creative Commons Attribution License (CC BY). The use, distribution or reproduction in other forums is permitted, provided the original author(s) or licensor are credited and that the original publication in this journal is cited, in accordance with accepted academic practice. No use, distribution or reproduction is permitted which does not comply with these terms.