



Control of Neuronal Excitability by Cell Surface Receptor Density and Phosphoinositide Metabolism

Martin Kruse^{1,2}* and Rayne J. Whitten²

¹Department of Biology, Bates College, Lewiston, ME, United States, ²Program in Neuroscience, Bates College, Lewiston, ME, United States

Phosphoinositides are members of a family of minor phospholipids that make up about 1% of all lipids in most cell types. Despite their low abundance they have been found to be essential regulators of neuronal activities such as action potential firing, release and re-uptake of neurotransmitters, and interaction of cytoskeletal proteins with the plasma membrane. Activation of several different neurotransmitter receptors can deplete phosphoinositide levels by more than 90% in seconds, thereby profoundly altering neuronal behavior; however, despite the physiological importance of this mechanism we still lack a profound quantitative understanding of the connection between phosphoinositide metabolism and neuronal activity. Here, we present a model that describes phosphoinositide metabolism and phosphoinositide-dependent action potential firing in sympathetic neurons. The model allows for a simulation of activation of muscarinic acetylcholine receptors and its effects on phosphoinositide levels and their regulation of action potential firing in these neurons. In this paper, we describe the characteristics of the model, its calibration to experimental data, and use the model to analyze how alterations of surface density of muscarinic acetylcholine receptors or altered activity levels of a key enzyme of phosphoinositide metabolism influence action potential firing of sympathetic neurons. In conclusion, the model provides a comprehensive framework describing the connection between muscarinic acetylcholine signaling, phosphoinositide metabolism, and action potential firing in sympathetic neurons which can be used to study the role of these signaling systems in health and disease.

OPEN ACCESS

Edited by:

Murat Oz, Health Science Center, Kuwait, Kuwait

Reviewed by: Eamonn Dickson,

University of California, Davis, United States Raghu Padinjat, National Centre for Biological Sciences, India Christian R. Halaszovich, University of Marburg, Germany

> *Correspondence: Martin Kruse mkruse@bates.edu

Specialty section:

This article was submitted to Pharmacology of Ion Channels and Channelopathies, a section of the journal Frontiers in Pharmacology

> Received: 11 February 2021 Accepted: 29 March 2021 Published: 21 April 2021

Citation:

Kruse M and Whitten RJ (2021) Control of Neuronal Excitability by Cell Surface Receptor Density and Phosphoinositide Metabolism. Front. Pharmacol. 12:663840. doi: 10.3389/fphar.2021.663840 Keywords: phosphoinositides, neuronal excitability, superior cervical ganglion, PIP₂, ion channel

INTRODUCTION

Phosphoinositides are signaling molecules that affect different aspects of neuronal activity, ranging from regulating ion channel activity (Brown and Adams, 1980; Suh and Hille, 2002; Kruse et al., 2012; Hille et al., 2015), controlling neurotransmitter vesicle docking and release (Di Paolo and De Camilli, 2006; Martin, 2014) as well as endocytosis (Cremona and De Camilli, 2001; Posor et al., 2014), to organization of the cytoskeleton (Saarikangas et al., 2010).

Abbreviations: ATP, adenosine triphosphate; M_1R , muscarinic acetylcholine receptor type I; Oxo-M, oxotremorine methiodide; PI, phosphatidylinositol; PI(4)P, phosphatidylinositol 4-phosphate; PI(4,5)P₂, phosphatidylinositol 4,5-bisphosphate; PI4K, phosphatidylinositol 4-kinase; PIP5K, phosphatidylinositol 4-phosphate 5-kinase; PLC, phospholipase C; RACK1, receptor for Activated C-Kinase 1; RAMP, receptor-activity-modifying-protein; SCG, superior cervical ganglion; VSP, voltage-sensing phosphatase.

One of the most important members of the phosphoinositide family is phosphatidylinositol 4,5-bisphosphate (PI(4,5)P₂) (Saheki and De Camilli, 2017). PI(4,5)P2 is critically involved in the aforementioned processes and its levels can be depleted by more than 90% within seconds through activation of phospholipase C (PLC) in neurons, thereby altering neuronal activity (Reiner and Levitz, 2018; Weis and Kobilka, 2018). Phosphoinositide metabolism is highly dynamic and resynthesis of PI(4,5)P₂ occurs rapidly after the end of a PLCactivating stimulus via phosphorylation of phosphatidylinositol (PI) and phosphatidylinositol 4-phosphate (PI(4)P) through phosphatidylinositol 4- and 5-kinases, respectively (Willars et al., 1998; Cantley, 2002; Kruse et al., 2016). Interestingly, kinetics of $PI(4,5)P_2$ resynthesis after depletion are dependent on the cell type. Studies performed on human embryonic kidney cells have reported durations of 120 s for the restoration of PI(4,5)P₂ levels after activation of muscarinic acetylcholine receptors type 1 (M₁R) (Falkenburger et al., 2010a; Dickson et al., 2014; Dickson et al., 2016). In contrast, similar experiments performed on rat superior cervical ganglion (SCG) neurons reported resynthesis of PI(4,5)P2 in less than 60 s (Kruse et al., 2016). These differences provide evidence for the hypothesis that different types of cells have adjusted kinetics of PI(4,5)P₂ synthesis based on their physiological needs.

Work by many different groups has established a strong correlation between electrical activity of neurons and the control of ion channels by PI(4,5)P₂. For instance, members of the KCNQ family of voltage-gated potassium channels have been shown to be dependent on $PI(4,5)P_2$ and to be in control of electrical excitability of different types of neurons including sympathetic neurons such as superior cervical ganglion neurons (Suh and Hille, 2002; Brown et al., 2007; Hernandez et al., 2009; Zaika et al., 2011; Vivas et al., 2014). Members of the transient receptor potential (TRP) channel family as well as potassium channels have been shown to be regulated by breakdown of PI(4,5)P2 through phospholipase C in photoreceptors of Drosophila (Hardie et al., 2001; Hardie et al., 2004; Krause et al., 2008; Raghu and Hardie, 2009; Hardie and Franze, 2012; Randall et al., 2015; Liu et al., 2018), and lipid transfer proteins involved in phosphoinositide metabolism have been shown to be critical for the functionality of Drosophila photoreceptors (Yadav et al., 2015; Cockcroft et al., 2016; Cockcroft and Raghu, 2016; Nath et al., 2020; Basak et al., 2021). In addition, several voltage-gated Ca²⁺ channels are modulated in their activity by PI(4,5)P2 levels and influence neuronal excitability as well (Gamper et al., 2004; Suh et al., 2012; Hille et al., 2015). Lastly, while PI(4,5)P2 can regulate many ion channels directly, work by Balla and colleagues has provided evidence for a critical role of PI(4,5)P2 in control of Schwann cell activity and myelination (Alvarez-Prats et al., 2018; Baba et al., 2020). Many of the biophysical parameters of the interaction between PI(4,5)P2 and the aforementioned ion channels have been characterized in detail, however, we still lack an understanding of how dynamic changes of PI(4,5)P₂ levels influence neuronal excitability. What fraction of total $PI(4,5)P_2$ depletion is necessary to evoke action potential firing and how do kinetics of PI(4,5)P2 breakdown and resynthesis

influence neuronal activity? Currently, these questions can't be addressed experimentally as we lack tools to monitor phosphoinositide levels in a quantitative manner in a living neuron while also observing its action potential firing at the same time.

One solution for this problem is the development of mathematical models that allow for the simulation of both phosphoinositide metabolism and electrical activity of a neuron. Recently, several different groups have generated mathematical descriptions of phosphoinositide synthesis and breakdown in different types of cells including neurons (Xu et al., 2003; Brown et al., 2008; Dickson et al., 2013; Falkenburger et al., 2013; Hille et al., 2014; Kruse et al., 2016), however, all of these models lack a mathematical description of electrical activity. Recently, Mergenthal et al. published a first report of a mathematical model describing cholinergic modulation of action potential firing in CA1 pyramidal neurons (Mergenthal et al., 2020), however, we still lack such quantitative descriptions of phosphoinositide metabolism and its role for action potential firing for other types of neurons. Here, we report the generation of a new mathematical model that provides a description of phosphoinositide metabolism and muscarinic acetylcholine receptor signaling as well as action potential firing and underlying ion channel activity in rat superior cervical ganglion neurons. The model takes phosphoinositide dependence of ion channels into account and allows for a quantitative exploration of the connection between lipid metabolism, G protein-coupled receptor signaling, and action potential firing in a sympathetic neuron.

MATERIALS AND METHODS

We used a model of phosphoinositide metabolism of rat superior cervical ganglion neurons previously published by our group as well as a model of action potential firing in these neurons published by Zaika et al. as a starting point to develop a new model that describes neuronal activity of sympathetic neurons as phosphoinositide-dependent action potential firing in response to activation of muscarinic acetylcholine receptors (Zaika et al., 2006; Kruse et al., 2016). The following sections describe the procedures performed to acquire needed experimental data for the development of the model.

Animal Handling

Male adult Sprague-Dawley rats were obtained from The Jackson Laboratory (Bar Harbor, ME). All work with these animals described in this study has been approved and overseen by the Bates College Institutional Animal Care and Use Committee.

Cell Culture

Human embryonic kidney cells (HEK293, ATCC Cat# CRL-1573, RRID:CVCL_0045) were maintained at 50–70% confluency in Eagle's Minimum Essential Medium (EMEM, ATCC Cat# 30–2003)) supplemented with 10% (v/v) fetal bovine serum (Life Technologies Cat# 16000044), 100 units/ml Penicillin, and 100 µg/ml Streptomycin (Life Technologies Cat# 15140148) at 37 C and 5% CO₂. Transfection of HEK293 cells was carried out with Lipofectamine 3000[®] according to manufacturer instructions (Life Technologies Cat#L3000001).

Plasmids

A pcDNA3-PH_{PLC01}-RFP plasmid was provided by Kees Jalink (Netherlands Cancer Institute, Amsterdam, Netherlands) while Dr-VSP-IRES-GFP (encoding for Dr-VSP cloned into the pIRES2-GFP vector) was provided by Yasushi Okamura (Osaka University, Osaka, Japan). Plasmids encoding for rat KCNQ2/3 channels cloned into the pcDNA3 expression vector were obtained from D. McKinnon (State University of New York, Stony Brook, NY), M1R-YFP (coding sequence for mouse muscarinic acetylcholine receptor type one fused N-terminally to the coding sequence for the yellow fluorescent protein using the vector pEYFPN1) was provided by N. Nathanson (University of Washington, Seattle, WA), and a pcDNA3-M1R encoding plasmid was obtained from the cDNA Resource Center (Bloomsberg, PA). A plasmid encoding for the human KCNMA1 (Maxi-K a) subunit expressed via the pcDNA3 vector backbone was provided by R. Aldrich (University of Texas, Austin, TX). All expression plasmids utilized a CMV promotor for expression of cDNAs.

Solution and Reagents

Cells were superfused throughout all electrophysiological and confocal imaging experiments with extracellular recording solution (150.0 mM NaCl, 2.5 mM KCl, 2.0 mM CaCl₂, 1.0 mM MgCl₂, 10.0 mM HEPES, and 8.0 mM glucose, adjusted to pH 7.4 with NaOH). Pipette solution for electrophysiological recordings of KCNQ2/3 channels contained 175.0 mM KCl, 5.0 mM MgCl₂, 5.0 mM HEPES, 0.1 mM K₄BAPTA, 3.0 mM Na₂ATP, and 0.1 mM Na₃GTP, adjusted to pH 7.2 with KOH. Pipette solution for patch clamp recordings of KCNMA1 channels contained 95.0 mM KCl, 20.0 mM K₄-BAPTA, 19.8 mM CaCl₂, 1.0 mM MgCl₂, 5.0 mM HEPES, 3.0 mM Na2ATP, and 0.1 mM Na3GTP, adjusted to pH 7.2 with KOH. All chemicals used in this study were obtained from Sigma-Aldrich (St. Louis, MO) except for TRIzol reagent (Life Technologies Cat# 15596018) and Fluo-4 AM (Life Technologies Cat# F14201).

Electrophysiology

Whole-cell patch clamp recordings were carried out using an EPC10 patch clamp amplifier (HEKA Elektronik, EPC 10 USB Patch Clamp Amplifier, RRID:SCR_018399) and Patchmaster software for data acquisition (HEKA Elektronik, software version 2×90.5). Recording pipettes were manufactured from borosilicate glass (Sutter Instruments Cat# BF150-110-10) and fire-polished to a final resistance of 2–3 M Ω using a Sutter P-97 pipetter puller (Sutter P-97/PC Pipette Puller, RRID: SCR_018636). All recordings were performed at room temperature and under constant superfusion of cells with extracellular recording solution (see Solutions and Reagents) at a flow rate of 2 ml/min. Currents were sampled at 5 kHz, and series resistance was compensated by 50–70% after compensation of fast and slow capacitances. Low- and high-pass filters were set

to 2.8 and 10 kHz, respectively. KCNQ- or KCNMA1-channels were activated by a 500 ms long depolarization to a membrane potential of -20 mV from a holding potential of -60 mV. Channels were activated every 2 s. Dr-VSP was activated from a holding potential of -60 mV via three 400 ms long depolarizations to a membrane potential of 100 mV with a return to the holding potential of -60 mV for 100 ms between each depolarization. Recordings were analyzed using IGOR Pro 7.0 (WaveMetrics Inc., IGOR Pro, RRID:SCR_000325) and Patcher's Power Tools 2.18 (Patchers Power Tools, RRID: SCR_001950).

Confocal Imaging

All imaging experiments were carried out using a Leica SP8 microscope (Leica Microsystems Inc., Leica SP8 LIGHTNING confocal microscope, RRID:SCR_018169) at room temperature. Data acquisition was performed using LAS 4.1 software (Leica Microsystems Inc.). Cells were constantly superfused with extracellular recording solution (see Solutions and Reagents) at a flow rate of 2 ml/min. For calcium imaging experiments, cells were loaded with Fluo-4 AM (Life Technologies Cat# F14201) in extracellular recording solution prior to experiments according to manufacturer instructions. Fluo-4 was excited using light with a wavelength of 494 nm generated by a STELLARIS white light laser (Leica Microsystems Inc.) and emission was monitored between 510 and 550 nm by a hybrid detector (Leica Microsystems Inc.) while RFP was excited using light of a wavelength of 558 nm and its emission was detected between 580 and 600 nm. All data was acquired using a 63× oil-immersion objective (Leica Microsystems Inc.). Image analysis was performed with Fiji software 2.1.0 (https://imagej.net/Fiji).

Molecular Biology

Total RNA was isolated from superior cervical ganglia, heart, brain, and colon of adult male rats with TRIzol reagent (Life Technologies Cat# 15596018) according to manufacturer instructions. Total RNA underwent reverse transcription using the ProtoScript II First Strand cDNA Synthesis Kit (New England Biolabs Cat# E6560S) with D(T)23 VN oligonucleotides based on manufacturer instructions. Subsequently, synthesized cDNA was used in polymerase chain reactions with Q5 High-Fidelity DNA polymerase (New England Biolabs Cat# M0491S) and oligonucleotides for α - and β - subunits of rat KCNMA1 channels. Oligonucleotide sequences were as follows: rat KCNMA1 subunit (fwd: 5-CGAGACGGCTCTTAGAATGAG CAGC-3, rev: 5-CATTGGCTGCAATAAACCGCAAGCC-3), rat KCNMB1 subunit (fwd: 5-ATGGGGGAAGAAGCTGGTGATG-3, rev: 5-CTGGTACACAACACTGGTCTC-3), rat KCNMB2 subunit (fwd: 5-CCGGACCTCTTCATCTTACAG-3, rev: 5-TCTTCATGG TCTCTTCTGTGTG-3), rat KCNMB3 subunit (fwd: 5-GAATCA AACTGCACCACTGTC-3, rev: 5-CCTAACCAAACCAACAAT CAGAG-3), and rat KCNMB4 subunit (fwd: 5-ATGGCGAAG CTCAGGGTGTCTTACG-3, rev: 5-GAGGACCACGATGAG GACACCC-3).

Model Development

The model was developed in R and all programming code is publicly available (https://github.com/Martin-Kruse/SCG-PI-excitability).

Lipid Signaling Controls Neuronal Activity

The development and evaluation of the individual aspects of the model is described in the Results section.

RESULTS

Expression of KCNMA1 and KCNMB Subunits in Rat Superior Cervical Ganglia

Previous electrophysiological recordings of rat superior cervical ganglion neurons showed a critical role for both KCNQ and KCNMA1 potassium channels in controlling excitability of SCG neurons (Brown et al., 1982; Suh and Hille, 2002; Vivas et al., 2014). Both of these channel families have been shown to be regulated by PI(4,5)P₂, but while this dependence relies on an interaction of $PI(4,5)P_2$ with the α -subunits of KCNQ channels, any potential regulation of KCNMA1 channels by phosphoinositides seems to be caused by an interaction with KCNMA1 β-subunits (Vaithianathan et al., 2008; Hille et al., 2015). In order to develop a mathematical description of electrical activity and its regulation by phosphoinositides in SCGs, we needed to determine if any KCNMA1 channel β-subunits are expressed in SCG of adult rats. For this purpose, we isolated total RNA from SCGs and reverse transcribed it into cDNA. Polymerase chain reactions with oligonucleotides for rat KCNMA1 channel α -subunit showed a band at ~ 650 bp, consistent with the predicted fragment size of 641 bp (Figure 1A, left panel). This result indicates expression of KCNMA1 channel a-subunits in our preparation and agrees with previous studies (Vivas et al., 2014; Vivas et al., 2017). Polymerase chain reactions on cDNA from rat SCGs with oligonucleotides for KCNMA1 channel β-subunits showed no detectable fragments, indicating an absence of KCNMA1 channel β subunits in rat superior cervical ganglia neurons (Figure 1A, right panel). Given the absence of detectable PCR products for all four KCNMB subunits in cDNA isolated from total RNA of SCGs, we decided to isolate total RNA from rat tissues that had previously been described to express KCNMB subunits either in rodents or humans (Chang et al., 1997; Xia et al., 1999; Bautista et al., 2009; Fagerberg et al., 2014; Whitmire et al., 2017). Reverse transcription of these RNAs into cDNA with subsequent PCR on the cDNA showed PCR products of the expected size of 447 bp for KCNB1 in heart and brain (Figure 1B), a fragment of an expected size of 392 bp for KCNMB2 in heart and brain (Figure 1C), a fragment of an expected size of 414 bp for KCNMB3 in colon (Figure 1D), and a fragment of an expected size of 570 bp for KCNMB4 in brain (Figure 1E). We concluded that the chosen oligonucleotides for the detection of cDNA for the four KCNMB subunits are capable of allowing for amplification of PCR products for all four KCNMB subunits, thereby supporting our interpretation that KCNMB subunits are not expressed in SCGs.

Analysis of PI(4,5)P₂-Dependence of rat KCNMA1 Channels

We now turned our attention to the question of whether rat KCNMA1 channels depend on $PI(4,5)P_2$ for their activity. To

verify that we can successfully deplete plasma membrane PI(4,5)P2 in a transient manner, we transfected HEK293 cells with expression plasmids for mouse muscarinic acetylcholine receptor type I and PH_{PLC01}-RFP. Application of 10 µM oxotremorine methiodide (Oxo-M) for 20 s caused strong translocation of PHPLCo1-RFP from the plasma membrane into the cytoplasm, indicating net depletion of $PI(4,5)P_2$ at the plasma membrane (Figures 1F,G). To verify our result of successful activation of phospholipase C with a second, independent method, we loaded HEK293 cells with the membrane-permeable calcium-sensitive fluorescent dye Fluo-4-AM and activated endogenous purinergic receptors by a 20 s application of 100 µM ATP while monitoring Fluo-4indicated cytoplasmic calcium levels. We observed a strong increase in fluorescence intensity upon application of ATP, indicating an activation of phospholipase C (PLC) and depletion of PI(4,5)P2 at the plasma membrane while generating cytoplasmic inositol 1,4,5-trisphosphate and triggering calcium release from the endoplasmic reticulum (Figure 1H).

Having shown that SCG neurons seem to express only KCNMA1 channel α -, but not β -subunits, and that activation of PLC in HEK293 cells causes net depletion of $PI(4,5)P_2$, we asked whether a reduction of $PI(4,5)P_2$ levels would cause an alteration of KCNMA1 channel activity. We first expressed KCNQ2/3 channels and M1R in HEK293 cells and measured KCNQ2/3-mediated potassium current amplitudes by whole cell patch-clamp recordings. These channels have been shown to be strongly dependent on PI(4,5)P2 and can therefore serve as a positive control for electrophysiological detection of net PI(4,5)P₂ depletion (Suh and Hille, 2002; Brown et al., 2007; Kruse et al., 2012; Dickson et al., 2013). As expected, activation of M1R reduced KCNQ2/3-mediated current amplitudes by 79.7 ± 6.4% (mean \pm SEM, n = 16, p < 0.001, one-sample t-test), a finding that indicates strong net depletion of $PI(4,5)P_2$ by M₁R activation in HEK293 cells (Figures 2A,B). Next, we transfected HEK293 cells with expression plasmids for M1R and KCNMA1 channels. Measurement of KCNMA1 channel mediated current amplitudes before and after activation of M₁R by 10 µM Oxo-M showed no significant change in current amplitude (-3.0 \pm 4.4%, mean \pm SEM, n = 5, p =0.231, one-sample t-test) (Figures 2A,C). While this result indicated that KCNMA1 channels do not require $PI(4,5)P_2$ for full activity at the plasma membrane, we decided to repeat this test by using a different method of net $PI(4,5)P_2$ depletion. We transfected HEK293 cells with a voltagesensing lipid phosphatase, Dr-VSP, which has been shown to cause strong net depletion of $PI(4,5)P_2$ upon a depolarizing voltage pulse (Hossain et al., 2008; Iwasaki et al., 2008; Halaszovich et al., 2009; Falkenburger et al., 2010b). Interestingly, activation of Dr-VSP showed again no significant alteration of KCNMA1 channel activity $(-4.5 \pm 10.7\%, \text{ mean } \pm \text{ SEM}, n = 6, p = 0.328, \text{ one-sample}$ t-test) (Figures 2A,D). We concluded that net depletion of PI(4,5)P2 does not seem to significantly alter KCNMA1 channel activity.



isolated from rat SCG with oligonucleotides for KCNMA1 channel α -subunit. **Right:** Same as on left, but with oligonucleotides for KCNMA1 channel β -subunits. (**B**) - (**E**). RT-PCR on cDNA generated from total RNA isolated from indicated rat tissues with oligonucleotides for indicated KCNMB subunits. Arrows indicate expected molecular weight for PCR fragments. (**F**). Normalized cytoplasmic RFP-intensity in HEK293 cells expressing PH_{PLC81}-RFP and mouse M₁R in response to stimulation of cells with 10 μ M Oxo-M (n = 5). Error bars indicate SEM. Traces were normalized to the last timepoint before application of Oxo-M. (**G**). Representative gray-scale images of HEK293 cells expressing PH_{PLC81}-RFP before 1) and after 2) activation of muscarinic acetylcholine receptors by 10 μ M Oxo-M. (**H**). Normalized fluo-4 intensity in HEK293 cells in response to stimulation of cells with 100 μ M ATP (n = 6). Error bars indicate SEM. Traces were normalized to the last timepoint before application of the last timepoint before application of ATP.

Mathematical Description of Ion Channel Conductances in Rat SCG Neurons

In order to develop a mathematical model of action potential firing in superior cervical ganglion neurons, we expanded a previously published model by Zaika et al. (2006). Similar to

their model, we included a voltage-gated sodium conductance (Traub et al., 1991), a delayed rectifier potassium (KDR) conductance (Migliore et al., 1995), a high-threshold voltage-gated L-type calcium channel conductance (Migliore et al., 1995), a calcium-dependent



KCNMA1 channel conductance (Moczydlowski and Latorre, 1983; Migliore et al., 1995), and a M-current conductance (Borg-Graham, 1991; Migliore et al., 1995). In addition to these conductances, we also included a low-threshold L-type calcium conductance (Somjen et al., 2008) and mathematical descriptions of a sodium-calcium exchanger as well as a Ca²⁺ ATPase to simulate intracellular Ca²⁺ clearance mechanisms (Quadroni and Knopfel, 1994). Changes of the membrane potential were calculated by the following equation, where, I_{KM} , I_{BK} , I_{KDR} , I_{Na} , $I_{Ca(low)}$, $I_{Ca(high)}$, $I_{CaATPase}$, I_{NaCaEx} , and I_L are specific ionic currents representing KCNQ-, KCNMA1-, KDR-, high-threshold Ca²⁺-, low-threshold Ca²⁺-channels, respectively, as well as Ca²⁺-ATPase -, Na⁺-Ca²⁺-exchanger activities, and leak conductances. All parameters and constants used in the following equations are listed in **Supplemental Table S1**.

$$C\frac{av}{dt} = -I_{KM} - I_{BK} - I_{KDR} - I_{Na} - I_{Ca(high)} - I_{Ca(low)} - I_{CaATPase} - I_{NaCaEx} - I_L$$
(1)

In this equation, V represents the membrane potential, t is time, and C is the membrane capacitance. The ionic currents are described by the following equations:

1 7 7

$$I_{KM} = g_{KM}k \left(V - E_K\right) \tag{2}$$

$$I_{BK} = g_{BK}o \left(V - E_K\right) \tag{3}$$

$$I_{KDR} = g_{KDR} n^3 l (V - E_K)$$
(4)

$$I_{Na} = g_{Na} m^3 h (V - E_{Na})$$
 (5)

$$I_{Ca(high)} = g_{calbar} c^{2} \left(k_{i} \frac{k_{i}}{k_{i} + \frac{Ca_{c}}{1000}} \right) \cdot \left(-f \left(1 - \left(\frac{\left(\frac{Ca_{c}}{1000} \right)}{Ca_{ex}} \right) \right) \\ \cdot \exp \frac{V}{f} \right) \cdot efun\left(\frac{V}{f} \right) \right)$$
(6)

$$I_{Ca(low)} = g_{calbar2} c2 \left(k_i \frac{k_i}{k_i + \frac{Ca_c}{1000}} \right) \cdot \left(-f \left(1 - \left(\frac{\left(\frac{V}{1000} \right)}{Ca_{ex}} \right) \right) \\ \cdot \exp \frac{V}{f} \right) \cdot efun\left(\frac{V}{f} \right) \right)$$
(7)

$$I_{CaATPase} = K2f_{ATPase} \left(\frac{f_{ATPase} \cdot \frac{Ca_c}{1000}}{f_{ATPase} \cdot \frac{Ca_c}{1000} + b_{ATPase}} \right)$$
(8)

$$I_{NaCaEx} = -K2f_{ex} \cdot \left(Na_{C}^{3} \cdot Ca_{ex} \cdot \exp\left(E_{1} \cdot V\right) - Na_{ex}^{3} \cdot \frac{Ca_{c}}{1000} \right)$$
$$\cdot \exp\left(-E_{2} \cdot V\right)$$
(9)

$$I_L = g_L \left(V - E_L \right) \tag{10}$$

In these equations, g_x indicates the conductances per unit area of ion channel x, and Ca_c , Ca_{ex} , Na_C , and Na_{ex} represent the intraand extracellular concentration of Ca^{2+} and Na^+ , respectively. All activation and inactivation gating variables (described as x in the following equation) are expressed as stated in **Eq. (11)** based on the formulations by Hodgkin and Huxley (1952):

$$\frac{dx}{dt} = \frac{x_{\infty} - x}{\tau_x} \tag{11}$$

The function "efun" referenced in **Eqs. (6**, 7) is available in the program code listed under https://github.com/Martin-Kruse/SCG-PI-excitability and is listed in the **Supplemental Information**. All equations for the description of ion channel activities are listed in the **Supplemental Information**.

Mathematical Description of Phosphoinositide Metabolism in Rat SCG Neurons

The mathematical model of phosphoinositide metabolism of rat superior cervical ganglion neurons used in this model has



FIGURE 3 | Evaluation of model of action potential firing in rat superior cervical ganglion neurons. (**A**). Simulated membrane potential of rat SCG neurons in response to stimulation with 10 μM Oxo-M for 20 s. (**B**). Simulated action potentials representing time period from 40.0 s to 40.5 s in simulation shown in A. (**C**). Simulation of change in membrane potential to a 20 s application of 10 μM Oxo-M (**top panel**) under a condition of maximum L-type channel conductance over the entire simulation period. (**D**). Simulated membrane potential of rat SCG neurons over 60 s in response to 100% inhibition of KCNMA1 channel activity from 10 s to 50 s of the simulation. (**E**). KCNQ2/3 channel conductance (**top panel**), and PI(4,5)P₂ density (**middle panel**) under a condition of maximum L-type channel conductance over the entire simulation period (**bottom panel**). (**F**). Same as in E, but allowing for modification of L-type channel conductance in response to stimulation with Oxo-M (**bottom panel**).

been developed by our research group and has been described in a previous publication (Kruse et al., 2016). We have not modified this model for this study, so we refer the reader to our previous publication for a detailed description of the characteristics and development of this part of the model presented in this publication. Here, we will discuss the most essential principles of this model and introduce the equations of the model that are of greatest relevance for this study. The most relevant parameters for the description of phosphoinositide metabolism in this model are listed in **Supplemental Table S2**. We refer the reader to our previous publication for a full description of all parameters (Kruse et al., 2016).

The relative contributions of phosphatidylinositol (PI), phosphatidvlinositol 4-phosphate (PIP), and phosphatidylinositol 4,5-bisphosphate ($PI(4,5)P_2$) to the overall phosphoinositide pool of rat SCG neurons were determined by lipid mass spectrometry (Kruse et al., 2016; Traynor-Kaplan et al., 2017). The kinetics of breakdown of PIP and PIP₂ by phospholipase C (PLC) after activation of muscarinic acetylcholine receptors type I as well as their resynthesis were measured using fluorescent lipid-binding domains such as P4M for PIP (Hammond et al., 2014), and PH_{PLC01} and Tubby-R332H for PI(4,5)P₂, respectively (van der Wal et al., 2001; Hughes et al., 2007). Changes in levels of active PLC were described by the following equation in the model:

$$\frac{d_{PLC}(G\alpha GTP)}{dt} = \left(\left(Kf_{PLC_{assoc}}PLC \cdot G\alpha GTP \right) - \left(Kr_{PLC_{assoc}} \cdot PLC \left(G\alpha GTP \right) \right) \right) + \left(Kf_{NE_{GaP}} \cdot G\alpha GDP_{PLC} \right) - \left(Kf_{GTPase_{GaP}} \cdot PLC \left(G\alpha GTP \right) \right)$$
(12)

Rates of changes of PIP were calculated using the following equation:

$$\frac{d_{PIP}}{dt} = (k4_{rest} \cdot foldPIP_2 * PI) - (k4P \cdot PIP) -(k5k_{rest} \cdot foldPIP_2 \cdot PIP) + (k5P_{rest} \cdot foldPIP_2 \cdot PIP_2) -(PIP \cdot PLC_{efficiency}PIP) \cdot (PLC_{basal} + K_{PLC} \cdot PLC (G\alpha GTP)) -((speed_{P4M_{PIP}} \cdot P4M \cdot PIP) - (speed_{P4M_{PIP}} \cdot KD_{P4M_{PIP}} \cdot P4M_{PIP})) (13)$$

Similarly, rates of changes of $PI(4,5)P_2$ were calculated by the following equation:

$$\frac{d_{PIP_{2}}}{dt} = (k5k_{rest} \cdot foldPIP_{2} \cdot PIP) - (k5P_{rest} \cdot foldPIP_{2} \cdot PIP_{2})$$

$$\frac{d_{boundPIP2}}{dt} - ((speed_{Tubby_{PIP2}} \cdot Tubby \cdot PIP_{2}) - (speed_{Tubby_{PIP2}})$$

$$\cdot KD_{Tubby_{PIP2}} \cdot Tubby_{PIP2})) - ((speed_{PH_{PIP2}} \cdot PH_{PLC\delta} \cdot PIP_{2})$$

$$- (KD_{PH_{PIP2}} \cdot speed_{PH_{PIP2}} \cdot PH_{PIP2})) - (PIP_{2} \cdot (PLC_{basal})$$

$$+ foldPIP_{2} \cdot PLC(G\alpha GTP))) - ((speed_{PIP2_{KCNQ}} \cdot KCNQ \cdot PIP_{2}))$$

$$- (speed_{PIP2_{KCNQ}} \cdot KD_{KCNQ_{PIP2}} \cdot KCNQ_{PIP2}))$$

$$(14)$$

The rates of changes of bound $PI(4,5)P_2$ were calculated using the following equation:



FIGURE 4 | Dose-dependence of I_{KM} and I_{Ca} inhibition. (A). Simulated and measured inhibition of KCNQ2/3 channel activity in response to 0.1–10.0 μ M Oxo-M. Measured I_M data for SCG neurons taken from (Kruse et al., 2016). (B). Simulated inhibition of KCNQ2/3 and L-type calcium channels in response to 0.1–10.0 μ M Oxo-M.

$$\frac{d_{boundPIP2}}{dt} = \left(\left(\left(-1.0 + foldPIP_2 \right) \cdot speed_{buffering} \right) \cdot PIP_2 \right) - \left(speed_{buffering} \cdot boundPIP_2 \right)$$
(15)

Rates of changed of free KCNQ channels or KCNQ channels in a complex with $PI(4,5)P_2$ were calculated by the following two equations:

$$\frac{d_{KCNQ}}{dt} = -\begin{pmatrix} (speed_{PIP2_{KCNQ}} \cdot KCNQ \cdot PIP_2) \\ -(speed_{PIP2_{KCNQ}} \cdot KD_{KCNQ_{PIP2}} \cdot KCNQ_{PIP2}) \end{pmatrix}$$
(16)
$$\frac{d_{KCNQ_{PIP2}}}{dt} = \begin{pmatrix} (speed_{PIP2_{KCNQ}} \cdot KCNQ \cdot PIP_2) \\ -(speed_{PIP2_{KCNQ}} \cdot KD_{KCNQ_{PIP2}} \cdot KCNQ_{PIP2}) \end{pmatrix}$$
(17)

Model Evaluation

In order to generate a model of action potential firing of rat SCG neurons that simulates action potential firing in response to activation of muscarinic acetylcholine receptors, we combined the mathematical descriptions of the aforementioned conductances with our previously published model of phosphoinositide metabolism and muscarinic acetylcholine receptor activity in superior cervical ganglion neurons (Kruse et al., 2016), and added a dependence of KCNQ channels on PI(4,5)P₂ levels based on previously described affinities of these channels for PI(4,5)P₂ (Falkenburger et al., 2010b).

The newly generated model reproduced several key properties of electrical activity in SCG neurons. First, the model predicted a stable resting membrane potential of ~ -60.5 mV and an absence of spontaneous action potential firing without activation of muscarinic acetylcholine receptors (**Figure 3A**). These properties are in line with experimental observations from rat SCG neurons obtained by perforated patch-clamp recordings from isolated SCG neurons (Vivas et al., 2014). Second, simulated activation of M_1R causes an initial slow depolarization that eventually causes a train of action potentials lasting for approximately 20–30 s before the membrane potential returns to its resting value (**Figure 3A**),



which again aligns well with previously obtained experimentally observed electrical behavior of rat SCG neurons (Vivas et al., 2014). Lastly, properties of individual simulated action potentials such as threshold of depolarization, firing frequency, and kinetics of de- and repolarization closely resembled action potentials recorded from primary rat SCG neurons (**Figure 3B**) (Vivas et al., 2014).

to a virtual application of 10 µM Oxo-M for 20 s at indicated densities of M1R.

Generation of action potential firing in rat SCG neurons has been shown to require a simultaneous inhibition of both KCNQ and KCNMA1 channels (Vivas et al., 2014). Inhibition of KCNQ channels is caused by net depletion of $PI(4,5)P_2$ while inhibition of KCNMA1 channels is dependent on a reduction of calcium influx through L-type calcium channels (Vivas et al., 2014; Vivas et al., 2017). We tested our model to determine if it would reproduce these key characteristics of action potential firing in SCG neurons. In order to evaluate this, we first simulated activation of acetylcholine receptors by a 20 s application of 10 µM Oxo-M while clamping the conductance of L-type calcium channels at its starting value, thereby not allowing for a virtual suppression of calcium channel activity due to activation of acetylcholine receptors. The model predicted a small depolarization of the membrane potential of about 2 mV and a subsequent recovery back to the resting membrane potential, a depolarization that was well below the threshold potential for action potential firing (Figure 3C). While the observed depolarization was very small, closely resembling experimental data (Vivas et al., 2014), the model predicted a strong inhibition of KCNQ channels and substantial net PI(4,5)P₂ depletion (Figure 3E, top and middle panels). This finding shows that our model correctly predicts that an inhibition of KCNQ channels alone is insufficient to cause action potential firing if calcium channels are not inhibited as well (Figure 3E, bottom panel). Next, we tested the predicted outcome of an inhibition of KCNMA1 channels alone. Experimental data had shown that inhibition of KCNMA1 channels without inhibition of KCNQ channels does not evoke action potential firing in rat SCG neurons (Vivas et al., 2014). We tested this by performing a 60 s long simulation of the membrane potential during which we set the conductance of KCNMA1 channels to 0 between 10 s and 50 s while keeping KCNQ channel conductance at 100%. Closely resembling experimental data, the membrane potential barely depolarized (Figure 3D). Interestingly, if we compared simulations that allowed for inhibition of L-type calcium channels by activation of muscarinic acetylcholine receptors (Figure 3F, bottom panel) which caused a strong depolarization of the membrane potential and eventually action potential firing (Figure 3A) with simulations that kept L-type channel conductance constant while activating muscarinic acetylcholine receptors (Figure 3E, bottom panel), the amounts of PI(4,5)P2 and KCNQ channel inhibition were identical in both simulations (Figures 3E,F, top and middle panels). These simulation results show that our model correctly predicts a simultaneous control of electrical activity of rat SCG neurons by KCNQ and KCNMA1 channels with a strong dependence of KCNQ channels on PI(4,5)P2 while KCNMA1 channel activity is controlled by influx of Ca²⁺ through L-type calcium channels.

Patch-clamp recordings on isolated rat SCG neurons had allowed for the experimental determination of an IC₅₀ value of M current inhibition by Oxo-M of 1.2 \pm 0.2 µM (Kruse et al., 2016). We used this value to test whether our model would provide us with a similar prediction as a way to evaluate the quality of the newly generated model. Our model predicted an IC₅₀ value of 0.7 µM (**Figure 4A**), a value that is slightly lower than our experimentally determined IC₅₀, however, the modelled IC₅₀ is in agreement with a previously published IC₅₀ value for inhibition of M current by Oxo-M in SCG neurons by Winks et al. who reported an IC₅₀ of 0.7 \pm 0.1 µM (Winks et al., 2005). In addition, we determined the IC₅₀ for inhibition of L-type calcium



FIGURE 6 Influence of PIP5K activity on electrical activity and second messenger generation in rat SCG neurons. (A). Simulated membrane potential in response to an application of 10 μ M Oxo-M for 20 s under conditions of reduction of PIP5K activity by 50%. (B) – (D). Same as in A, but under conditions of 75, 150, and 200% activity of PIP5K, respectively. (E) – (H). Normalized reductions or membrane densities and concentrations for levels of PI(4,5)P₂ (E), PI(4)P (F), diacylglycerol (G), and inositol 1,4,5-trisphosphate (H) in response to an application of 10 μ M Oxo-M for 20 s with indicated levels of PIP5K activity. (I) – (J). Same as in G and H, but for indicated levels of M₁R surface density (molecules/ μ m²) under conditions of 100% PIP5K activity.



channels by Oxo-M as predicted by our model and compared it with previously published data. Our model predicted an IC₅₀ for L-type calcium channels of 2.1 μ M (**Figure 4B**), which is in agreement with previously published IC₅₀ values of 2.0 μ M (Bernheim et al., 1992; Zhang et al., 2011). We concluded that our model shows a dose-dependence of KCNQ- and L-type calcium channel inhibition through activation of muscarinic acetylcholine receptors that resembles previously published experimental observations.

Altering M₁R Surface Density and PI(4)P 5-kinase Activity Levels as Tools to Uncouple Action Potential Firing and Intracellular Signaling Pathways

Previous biochemical analysis has shown that superior cervical ganglion neurons have a resting surface density of approximately 16 receptors/ μ m² (Kruse et al., 2016). Receptor turnover in

neuronal cells is highly dynamic though (Devreotes and Fambrough, 1975; Rudell and Ferns, 2013) and variations in receptor density are therefore likely to cause different amounts of phospholipase C activation and subsequent hydrolysis of PI(4,5)P₂ as well as generation of second messengers such as diacylglycerol and inositol 1,4,5-trisphosphate. We used our model to develop predictions how alterations in M1R surface density would influence hydrolysis of PI(4,5)P2 and action potential generation. For this purpose, we applied a virtual stimulus of 10 µM Oxo-M for a duration of 20 s and altered M_1R density ranging from 0 to 30 receptors/ μ m². Increasing receptor density from 0 to 16 receptors/µm² led to a sharp increase in the amount of PI(4,5)P2 being hydrolyzed by activation of phospholipase C, and simulations with the experimentally determined receptor density of 16 receptors/ μ m² showed levels of ~800 molecules/ μ m² PI(4,5)P₂ remaining at the end of the Oxo-M stimulation (Figure 5A), indicating a depletion of ~ 75% of resting $PI(4,5)P_2$ levels. Interestingly, increasing the receptor density further did not lead to a strong additional increase in PI(4,5)P2 hydrolysis, which indicates that the biochemical signaling pathway seems to reach saturation at this point and synthesis of $PI(4,5)P_2$ can mostly compensate for the additional hydrolysis of PI(4,5)P2 by phospholipase C (Figure 5A). Next, we asked how a variation in M_1R density influences electrical excitability of SCG neurons. We utilized the same stimulation protocol and observed a strong correlation between the ability of a stimulus to cause action potential firing and M₁R surface density (Figure 5B). Our simulations showed that receptor densities up to 12.5 receptors/µm² were insufficient to trigger action potential firing and the membrane potential showed very little depolarization upon a stimulation with 10 µM Oxo-M for 20 s (Figure 5B). Increasing the receptor density to 15 receptors/ μ m² on the other hand caused action potential firing (Figure 5B), which indicates that this density of M₁R seems to cause sufficient inhibition of KCNQ and L-type calcium channels if stimulated with the aforementioned application protocol. It is striking that an alteration of very few receptor molecules per μm^2 is sufficient to seemingly function as a switch for the generation of action potential firing and that the physiological resting receptor density seems to be just above this threshold, thereby potentially allowing a SCG neuron to switch between "non-firing" and "firing" by adjusting M₁R surface density by very few molecules (Figure 5C). Interestingly, activation of phospholipase C through surface densities below 15 receptors/µm² was still capable of hydrolyzing more than 50% of PI(4,5)P₂ (Figures 5A,D), which provides potential to generate second messengers such as DAG and IP₃ without causing the SCG neuron to fire action potentials.

We hypothesized that if small alterations of M_1R surface density are sufficient to modify phospholipase C activation to an extent that allows for switching between a "firing" and "nonfiring" mode of electrical activity, an alteration in PI(4,5)P₂ synthesis pathways might have a similar effect and provide an equivalent level of control over electrical activity of SCG neurons. We tested this hypothesis by either reducing PI(4)P 5-kinase activity in our model to levels of 50 and 75% of original activity or



FIGURE 8 | Relationship of PIP5K activity, PI(4,5)P₂ levels, and electrical excitability. A. Simulations of PI(4,5)P₂ densities in response to a 30 s application of 10 μM Oxo-M for indicated levels of PIP5K activity and stimulus durations. All stimulations were simulated for a frequency of 10 Hz. **(B)**. Same as **(A)**, but for KCNQ channel conductance. **(C)**. Simulation of PI(4,5)P₂ levels under conditions of unmodified PIP5K activity (white background) or reduction of PIP5K activity by 50% (gray background). **(D)**. Simulation of membrane potential and PI(4,5)P₂ density in response to 30 s applications of 10 μM Oxo-M at a stimulus frequency of 10 Hz and a stimulus duration of 10 ms. Red bar indicates simulation period with a 50% reduction of PIP5K activity.

by increasing it to 150 or 200% of its original activity while keeping M_1R density at 16 molecules/ μm^2 . Given that PI(4)P 5kinases catalyze the last reaction step in the synthesis of $PI(4,5)P_2$ from phosphatidylinositol (PI) (Figure 9B) we considered them a reasonable biochemical target and a potential modulator of electrical activity (Di Paolo et al., 2004). In agreement with our hypothesis, a virtual application of 10 µM Oxo-M for 20 s under conditions of reduced PI(4)P 5-kinase activity caused increased action potential firing compared to control conditions (Figures 6A,B, control data shown in Figure 5C, black trace). Increasing PI(4)P 5-kinase activity to 150 or 200% of its original activity on the other hand rendered the stimulus insufficient to evoke action potential firing and led to only a small depolarization of the membrane potential (Figures 6C,D). These simulation results support our hypothesis that small modifications of PI(4)P 5-kinase activity can serve as "switches" in the same way as a modification of M1R surface density can do. This switch-like behavior is not caused by differences in the speed at which PI(4,5)P2 and PI(4)P are hydrolyzed by phospholipase C as can be seen by comparing normalized traces of PI(4,5)P2 and PI(4)P depletion under conditions of 50, 75, 100, 150, or 200% of PI(4)P 5-kinase activity, respectively (Figures 6E,F). A critical property of reductions of either M1R surface density or PI(4)P 5-kinase activity is the ability of SCG neurons to still produce significant amounts of important second messengers that are

generated as products of PLC-mediated PI(4,5)P₂ hydrolysis. Simulations with 50 or 75% reduced PI(4)P 5-kinase activities showed levels of DAG or IP₃ that were still sufficient to trigger the activation of protein kinases in the case of DAG or cause release of calcium from intracellular calcium stores in the case of IP₃ (Figures 6G,H). Similarly, varying the surface density of M₁R from 10 to 20 molecules/µm² showed significant production of DAG and IP₃ under all tested conditions (Figures 6I,J). These results indicate that small variations in the surface density of M1R or PI(4)P 5-kinase activity are predicted to lead to a switch between firing and non-firing of action potentials while the production of second messengers such as DAG and IP₃ follows a more gradual progression under these conditions. A reduction of M1R surface density or PI(4)P 5-kinase activity could therefore serve as an aforementioned switch that uncouples electrical activity from intracellular signaling pathways and allows SCG neurons to utilize PLC-mediated hydrolysis of $PI(4,5)P_2$ to generate second messenger molecules without evoking action potential firing.

Influence of PI(4,5)P₂ Levels on Electrical Excitability of SCG Neurons in Response to Varying Levels of PI(4)P 5-Kinase Activity

Activation of M_1R by Oxo-M in a laboratory setting is usually accomplished by prolonged continuous application of the



amplitude of low-threshold L-type calcium channels plotted against membrane potential. **(B)**. Illustration of regulation of action potential firing of rat SCG neurons by phosphoinositide metabolism (yellow background) and ion channel activity (green background). Blue arrows indicate activation of KCNQ2/3 channels by Pl(4,5)P₂ or of KCNMA1 channels by Ca²⁺ ions entering the cell through L-type calcium channels. Red lines indicate that noninhibited activity of KCNQ2/3 and KCNMA1 channels prevents action potential firing.

agonist, e.g. continuous stimulation for 20-30 s (Suh and Hille, 2002; Dickson et al., 2016; Kruse et al., 2016). While these stimulation patterns are well suited for a variety of experiments, they do not reproduce physiological situations in which acetylcholine is present for only a few milliseconds, but might stimulate a neuron several times per second at frequencies of 2-10 Hz (Brown and Selyanko, 1985; Ivanov and Purves, 1989). Such stimulation frequencies are difficult to reproduce experimentally, so we decided to apply such stimulation patterns to our model to analyze how $PI(4,5)P_2$ levels and electrical activity would develop under such conditions. For this purpose, we applied virtual stimuli of 10 µM Oxo-M at a frequency of 10 Hz for a duration of 30 s and varied the length of an individual stimulus from 5 to 30 ms. We first focused on electrical activity and observed that under conditions of unmodified PI(4)P 5-kinase activity the membrane potential reacted with only small subthreshold depolarizations to

individual stimuli that were 5, 10, or 20 ms long. However, a duration of 30 ms for an individual application of 10 μ M Oxo-M evoked action potential firing (**Figure 7A**). Next, we reduced PI(4)P 5-kinase activity by 50% and repeated our virtual experiment. Under these conditions, individual stimuli as short as 10 ms evoked action potential firing, indicating a strongly increased electrical excitability of the neurons (**Figure 7B**).

Could this increased excitability under conditions of reduced PI(4)P 5-kinase activity be caused by $PI(4,5)P_2$ levels that are prior to activation of M1R already only slightly above the threshold for decreasing KCNQ channel sufficiently to evoke action potential firing? We addressed this question by analyzing $PI(4,5)P_2$ levels for conditions of unmodified and reduced PI(4)P 5-kinase levels. Interestingly, before activation of M_1R we observed $PI(4,5)P_2$ levels that are above a density of ~ 800 molecules/ μ m² (Figure 8A) which we had determined to be approximately the threshold for enough reduction of KCNQ channel activity to evoke action potential firing (Figure 5A). It is important to note though that under conditions of reduced PI(4)P 5-kinase activity the observed $PI(4,5)P_2$ density is only twice the threshold density while the $PI(4,5)P_2$ density under control conditions is four times larger than the threshold density (Figure 8A). Under control conditions, stimulation with the aforementioned duration times at a frequency of 10 Hz causes only the $PI(4,5)P_2$ curve for a stimulation of 30 ms length of an individual pulse to drop below this threshold, but the curves for shorter stimulus durations remain above it (Figure 8A). This is in line with the observed firing behavior for unmodified levels of PI(4)P 5-kinase activity (Figure 7A). On the other hand, the $PI(4,5)P_2$ curves under conditions of reduced PI(4)P 5-kinase activity all drop below this threshold except for the curve for a 5 ms long stimulation (Figure 8A), again following exactly the observed pattern of electrical activity (Figure 7B). Similarly, levels of M current conductance followed the same pattern (Figure 8B) and allowed us to conclude that reduced $PI(4,5)P_2$ levels due to a reduction of PI(4)P 5-kinase activity seemingly render SCG neurons significantly more excitable.

These findings led us to the hypothesis that transient reductions in PI(4)P 5-kinase activity could be a regulatory switch for SCG neurons that would allow them to flip back and forth between responding to a stimulus with action potential firing and activation of intracellular signaling pathways that depend on DAG and IP₃, or to remain electrically silent, but allow for second messenger generation. This hypothesis requires that adjustments in $PI(4,5)P_2$ levels can happen quickly enough to make this switch-like behavior physiologically reasonable for a neuron. We tested this hypothesis by simulating $PI(4,5)P_2$ levels over a time period of 800 s during which we reduced PI(4)P 5kinase activity levels by 50% for the time period of 180 s-480 s. Interestingly, our simulations showed that such transient switches in activity for very few minutes are sufficient to equilibrate PI(4,5)P2 to a new steady-state (Figure 8C), thereby allowing for the cell to quickly adjust

resting PI(4,5)P₂ levels within short time periods. Next, we asked whether such an adjustment of PI(4)P 5-kinase activity would indeed produce the aforementioned patterns of electrical activity. For this purpose, we simulated both $PI(4,5)P_2$ and electrical activity over a time period of 600 s and kept PI(4)P 5-kinase activity at its control level for the first 180 s. Afterwards, we reduced its activity by 50% for the rest of the simulation (red bar in Figure 8D). In this simulation, we applied virtual stimuli of 10 µM Oxo-M at a frequency of 10 Hz for 10 ms durations between 10 and 40 s of the simulation and again between 360 and 390 s (Figure 8D). In line with our hypothesis, the first stimulation which occurred under conditions of unmodified PI(4)P 5-kinase activity decreased PI(4,5)P2 levels and generated second messengers, but failed to depolarize the neuron sufficiently to evoke action potential firing (Figure 8D). The second stimulus though which was applied under conditions of reduced PI(4)P 5-kinase activity and after equilibration of $PI(4,5)P_2$ densities to a new and reduced steady-state caused not only $PI(4,5)P_2$ hydrolysis, but evoked action potential firing (Figure 8D). These observations support the hypothesis that transient alterations in PI(4)P 5-kinase activity could serve as a switch for neurons to temporarily alter between stimulus responses that combine second messenger generation with action potential firing or ones that evoke only second messenger generation.

Simulation of L-type Channel Activity Shows Activation near Resting Membrane Potential

Activation of KCNMA1 channels through Ca²⁺-influx mediated by L-type calcium channels requires these channels to be active at membrane potentials near the resting membrane potential. Electrophysiological recordings of KCNMA1 channels coexpressed with Ca_V1.3 channels have provided evidence that co-expression of these channels shifts their activation thresholds to membrane potentials around -50 mV (Vivas et al., 2017) which is well in line with membrane potential depolarizations evoked by closure of KCNQ channels upon muscarinic stimulation (Vivas et al., 2014). Simulations of I/V curves of low-threshold calcium channels in our model show activation of these channels around a membrane potential of -50 mV (Figure 9A), thereby reproducing experimental results obtained by our other groups (Vivas et al., 2017) and providing an explanation for the experimentally observed dependence of KCNMA1 channels on L-type calcium channel activity at membrane potentials near the resting membrane potential.

DISCUSSION

Validation of Model

Generation of action potential firing in superior cervical ganglion neurons has been shown to be controlled by several different factors. First, voltage-gated potassium channels such as KCNQ and KCNMA1 channels conduct a potassium efflux that stabilizes the resting membrane potential, thereby requiring an inhibition of both channels to allow for the generation of action potential firing (Suh and Hille, 2002; Zaika et al., 2006; Brown et al., 2007; Vivas et al., 2014). Both KCNQ and KCNMA1 channels are also ligand-activated, with KCNQ channels requiring interaction with $PI(4,5)P_2$ and KCNMA1 channels with Ca²⁺ (Suh and Hille, 2002; Vivas et al., 2017). Our model reproduces these dependencies, and action potential firing is only evoked in the model if both KCNQ and KCNMA1 channels are inhibited due to a loss of interaction with $PI(4,5)P_2$ and Ca^{2+} , respectively. Second, current-clamp recordings on SCG neurons have shown that stimulation of SCG neurons with Oxo-M at supramaximal concentrations leads to a slow (20-40 s) sub-threshold depolarization before the membrane potential reached the threshold for activation of voltage-gated sodium channels (Vivas et al., 2014). This slow depolarization has been explained by ongoing net depletion of $PI(4,5)P_2$ that causes an accumulation of deactivated KCNQ channels (Suh and Hille, 2002). Our newly developed model recapitulates this important property (see Figure 3C for an example of this slow depolarization) and places action potential firing under the control of PI(4,5)P2 if Ca2+ levels are sufficiently low to deactivate KCNMA1 channels. Third, Ca2+ needed for activation of KCNMA1 channels enters SCG neurons through L-type Ca²⁺ channels that are located in close proximity of KCNMA1 channels and is not provided by release of Ca²⁺ from intracellular stores (Vivas et al., 2014; Vivas et al., 2017). The model reproduces this interplay between L-type Ca²⁺ channel and KCNMA1 channel activity and places the activity of L-type Ca²⁺ channels under the control of muscarinic acetylcholine receptors. In addition, our model reproduces depolarization as well as repolarization kinetics as observed by perforated patch-clamp recordings from rat SCG neurons, and correctly simulates peak amplitudes and firing frequencies of action potentials evoked by activation of muscarinic acetylcholine receptors (Vivas et al., 2014). In conclusion, the newly generated model resembles all known characteristics of experimentally observed action potential firing of rat SCG neurons and combines this description of electrical activity with a previously published quantitative simulation of phosphoinositide metabolism of these neurons (Kruse et al., 2016), therefore allowing for a simulation of electrical activity of rat SCG neurons under the control of muscarinic acetylcholine receptors and phosphoinositide metabolism.

Regulation of Action Potential Firing by Surface Density of Muscarinic Acetylcholine Receptors and PI(4,5)P₂ Synthesis Kinetics

Our simulations showed that small variations in the surface density of muscarinic acetylcholine receptors or kinetics of $PI(4,5)P_2$ synthesis changed electrical excitability of rat SCG neurons significantly. Are such modulations of surface density and $PI(4,5)P_2$ synthesis kinetics plausible and if so, what physiological consequences does such a modulation have? We

first turn our attention to mechanisms that govern surface density of muscarinic acetylcholine receptors. Several different studies have provided evidence that surface localization of muscarinic acetylcholine receptors is neither uniform nor stable in different kinds of neurons, but can change in a short amount of time based on the physiological situation of the specific neuron. Bernard et al. showed that the localization of M4R in striatal neurons depends on the cholinergic environment and that stimulation of these neurons with oxotremorine triggers translocation of M4R from the cell surface to endosomes (Bernard et al., 1999). In addition, several groups have shown that PDZ domain-containing proteins such as LARG, RGS3, PDZ-RhoGEF, and Spinophilin function as regulators of trafficking and surface density of practically all different types of muscarinic acetylcholine receptors (Dunn and Ferguson, 2015). In addition to these mechanisms, proteins such as receptor-activity-modifying-proteins (RAMPs) and RACK1 (Receptor for Activated C-Kinase 1) have been linked to regulation of cell surface density of several different types of GPCRs (Achour et al., 2008). While this list is far from being complete it highlights that GPCR cell surface density has been shown to be dynamic and controlled by a variety of different mechanisms.

Similar to rapid changes in cell surface receptor density, kinetics of PI(4,5)P₂ synthesis have been shown to be dynamic and adjustable to the specific needs of a cell in a given physiological situation. One example of such a transient adjustment of PI(4,5)P₂ synthesis kinetics is activation of the Wnt3a pathway. Qin et al. showed that activation of the cell surface receptor Frizzled followed by recruitment of the cytoplasmic protein Dishevelled led to stimulation of PI(4,5)P₂ synthesis via activation of both phosphatidylinositol 4-kinase (PI4K) and PI(4)P 5-kinases (Pan et al., 2008; Qin et al., interaction between Dishevelled 2009). The and phosphatidylinositol 4-phosphate 5-kinase seems to be mediated by the DIX domain of Dishevelled, which allows for a rapid and transient control of phosphatidylinositol 4-phosphate 5-kinase activity (Hu et al., 2015). The lipid environment of the plasma membrane itself has been shown to be another regulator of phosphatidylinositol 4-phosphate 5-kinase activity. Recent work by Nishimura et al. showed that Osh proteins generate nanodomains in the plasma membrane that are enriched in unsaturated phosphatidylserine and sterols which synergistically stimulate phosphatidylinositol 4-phosphate 5kinase activity (Nishimura et al., 2019). Small variations in Osh protein levels can alter this microenvironment and lead to alterations of PI(4,5)P2 levels. Lastly, protein levels of PIP5Ks are dynamic and alterations of PIP5K amounts or of proteins that activate PIP5Ks such as Ras associated domain family 4 (RASSF4) have been shown to change cellular phosphoinositide levels (de la Cruz et al., 2020). It should be noted that kinetics of PI(4,5)P₂ synthesis are not only controlled by activity levels of phosphatidylinositol 4- and 5-kinases and phosphatidylinositol as 4,5-bisphosphate 5-phosphatases well as by phosphatidylinositol 4-phosphate phosphatases, but also by levels of substrates such as phosphatidylinositol and phosphatidylinositol 4-phosphate (Dai et al., 2016). In conclusion, transient adjustments of PI(4,5)P2 synthesis

kinetics have been shown for various different cell types and mechanisms, and make it likely that such dynamic adjustments of $PI(4,5)P_2$ levels can be used by neurons and other cell types to regulate their activity and responses to stimuli that activate pathways which involve phosphoinositide signaling.

What are the potential benefits of adjustments of cell surface receptor density and PI(4,5)P2 levels for a SCG neuron? Our simulations show that relatively modest alterations in either of these parameters can act like a switch for the SCG neuron that either triggers action potential firing in response to a stimulation with acetylcholine, or prevents it. We showed that this switch-like behavior can uncouple the generation of the second messengers inositol 1,4,5-trisphosphate and diacylglycerol from generation of action potential firing, thereby allowing the SCG neuron to use muscarinic acetylcholine receptors either only for the activation of intracellular signaling pathways or for a dual generation of electrical activity and second messenger molecules. In addition, these adjustments allow for a dosed response to acetylcholine and can transiently alter the sensitivity of a neuron to an incoming stimulus, thereby providing flexibility for the neuron receiving the stimulus. Achieving this level of flexibility with adjustments of just two parameters while using only one signaling system provides robustness and reduces the need for the cell to provide separate signaling systems for different physiological needs and conditions.

Analysis of PI(4,5)P₂ Dependence of KCNMA1 Channels in SCG Neurons

Our expression analysis showed that KCNMA1 channels in rat SCG neurons are composed of only a-subunits. Given both previous reports that any PI(4,5)P2 dependence of KCNMA1 channels is caused by interaction of KCNMA1 a-subunits with β -subunits (Hille et al., 2015) and our own correlating finding that KCNMA1 channel a-subunits do not show alterations of their activity by net $PI(4,5)P_2$ depletion, the question can be raised what physiological advantage it could have for SCG neurons to control action potential firing through two potassium channels that are regulated by different ligands? The answer to this question might be the generation of a control system that provides enhanced flexibility for the neuron. Placing both potassium channels under the control of PI(4,5)P₂ would lead to a situation in which net depletion of PI(4,5)P₂ almost always causes action potential generation. Placing KCNQ potassium channels under the control of $PI(4,5)P_2$ and KCNMA1 α -subunits under the control of intracellular Ca²⁺ levels though allow for a SCG neuron to control whether a signal evokes both electrical activity and second messenger generation or only activation of intracellular signaling pathways. Under these conditions, receptor activation can cause net depletion of PI(4,5)P2 that deactivates KCNQ channels, however, if L-type Ca²⁺ channels are not inhibited simultaneously, KCNMA1 channels would remain active and prevent action potential firing, therefore allowing for activation of intracellular signaling pathways in response to muscarinic stimulation without evoking action potential firing. A simultaneous depletion of PI(4,5)P2 and inhibition of L-type

Ca²⁺ channels would inhibit both KCNQ and KCNMA1 channels though, and cause action potential firing of the SCG neuron.

Future Uses and Expansion of Model

Our model provides a kinetic description of electrical activity and phosphoinositide metabolism in rat superior cervical ganglion neurons; however, it does not contain spatial information. Currently, phosphoinositide metabolism is mathematically described as a series of biochemical reactions in one compartment and it does not simulate the synthesis of phosphoinositides in different compartments and the transport processes of these phospholipids between different intracellular organelles (Saheki and De Camilli, 2017) (Figure 9B). It would be of great interest to expand the model to include such spatial information. Recent work by Zewe et al. and Pemberton et al. using newly developed fluorescent biosensors for the most prominent member of the phosphoinositide family, phosphatidylinositol (PI), revealed a very low presence of PI at the plasma membrane, but provided evidence for pools of PI in the endoplasmic reticulum, cytosolic leaflets of the Golgi complex, peroxisomes, and the outer mitochondrial membrane (Pemberton et al., 2020; Zewe et al., 2020). These new fluorescent biosensors will allow us to not only acquire experimental data needed for the simulation of compartmental transport of PI, but also provide the possibility to determine kinetics of PI synthesis and breakdown, thereby significantly enhancing the mathematical description of phosphoinositide metabolism in our current model. The addition of spatial information to the model would also allow to describe the interplay of KCNMA1 and L-type calcium channels in a stochastic manner as previously described by Cox (Cox, 2014). Lastly, it would be of great interest to expand the description of regulation of L-type calcium channel activity in our model. Work by Suh et al. has shown that the association of certain β-subunits with a-subunits of L-type calcium channels renders them partly sensitive to PI(4,5)P₂ levels (Suh et al., 2012), and Liu et al. have shown that arachidonic acid can serve as a modulator of L-type calcium channel activity (Liu et al., 2006). Currently, our model uses a simplified approach to calculate L-type calcium channel inhibition by multiplying the maximum conductance of L-type calcium channels with the ratio of activated muscarinic acetylcholine receptors divided by the total number of receptors. This calculation does not take the aforementioned regulatory mechanisms of L-type calcium channels into account, but gaining more information about the molecular nature of regulation of these channels in SCG neurons would allow for a more detailed mathematical description of their activity in a model. An inclusion of these regulatory mechanisms would therefore provide an opportunity to use such an expanded version of our model for testing of more detailed hypotheses regarding the regulation of action potential firing by phosphoinositide metabolism.

The model presented here consists of two components, the first one being a description of phosphoinositide metabolism and muscarinic acetylcholine receptor type I signaling in rat SCG neurons (highlighted in the yellow box in Figure 9B), and the second component being a mathematical description of ion channel activities in rat SCG neurons which are responsible for action potential firing in the neurons (highlighted in the green box in Figure 9B). As illustrated by the background color coding in Figure 9B, these two components of the model can be treated as two separate mathematical descriptions, but they are linked via the regulation of KCNQ channel activity through $PI(4,5)P_2$ (indicated by blue arrow in **Figure 9B**). Mathematically, this relationship is provided by Eqs. (16, 17) listed in the Results section. As can be seen from this equation, our model assumes an interaction of one PI(4,5)P2 molecule per KCNQ channel subunit. This is in contrast to the results published by Falkenburger et al. (Falkenburger et al., 2010b) which suggested an interaction of more than one molecule PI(4,5)P2 per channel subunit. Our decision to simulate this interaction with just one molecule $PI(4,5)P_2$ per channel subunit is based on 1) a better reproduction of experimental data, e.g. kinetics of membrane potential depolarization after activation of M1R and duration of action potential firing upon PI(4,5)P2 depletion, compared to simulations that assumed the interaction of more than molecule PI(4,5)P₂ per KCNQ channel subunit, and 2) recently published data by Sun and MacKinnon that analyzed the structural basis of human KCNQ1 channel modulation and gating by $PI(4,5)P_2$ (Sun and MacKinnon, 2020). Their work showed the interaction of just one molecule PI(4,5)P₂ with KCNQ1 channels in a region of the protein that is highly conserved among KCNQ channels. Sun and MacKinnon concluded that their data provides evidence that the findings obtained from KCNQ1 channels apply to other members of the KCNQ channel family as well. This structural analysis of KCNQ channel interaction with PI(4,5)P2 supported our observation that simulations assuming the interaction of only one molecule PI(4,5)P2 per KCNQ channel subunit resulted in a better reproduction of previously published experimental data (Vivas et al., 2014).

As mentioned before, L-type calcium activity is regulated in a complex manner that involves a small, diffusible second messenger signaling pathway as described by Mathie et al. (Mathie et al., 1992), but our model does not include such signaling due to a lack of a more detailed molecular characterization of this pathway. A mathematical description of this pathway would result in a second molecular link between the model of muscarinic signaling in the top part of **Figure 9B** and L-type calcium channel activity (depicted as "I_{Ca}" in **Figure 9B**), thereby indicating how signaling through muscarinic acetylcholine signaling regulates both KCNQ- and KCNMA1 channel activity.

In conclusion, our model allowed us to identify small alterations of surface density of muscarinic acetylcholine receptors type I or changes of PI(4)P 5-kinase activity as potential molecular switches that can uncouple the generation of second messengers such as diacylglycerol and inositol 1,4,5-trisphosphate from action potential firing. Previous work from our group and others have identified PI 4kinases and lipid transfer processes as molecular targets that can alter their activity depended on the physiological needs of a cell (Kruse et al., 2016; Dickson, 2019; Myeong et al., 2020). Our model provides a framework that allows for an analysis of the predicted outcomes of alterations in these pathways, thereby providing a toolkit that can aid not only in the development of new hypotheses and the design of targeted experiments to gain a better understanding of the connection of phosphoinositide metabolism and electrical activity of SCG neurons, but also provide further insight into the mechanisms governing the regulation of activity of sympathetic neurons in health and disease.

DATA AVAILABILITY STATEMENT

Publicly available datasets were analyzed in this study. This data can be found here: https://github.com/Martin-Kruse/SCG-PI-excitability.

ETHICS STATEMENT

The animal study was reviewed and approved by the Bates College Institutional Animal Care and Use Committee.

AUTHOR CONTRIBUTIONS

RW: culture of HEK293 cells, electrophysiological recordings of KCNQ and KCNMA1 channels, Ca²⁺-imaging and confocal microscopy, and data analysis. RW and MK: isolation of RNA from rat superior cervical ganglia and RT-PCR. MK: culture of HEK293 cells, electrophysiological recordings of KCNQ channels,

REFERENCES

- Achour, L., Labbé-Jullié, C., Scott, M. G. H., and Marullo, S. (2008). An escort for GPCRs: implications for regulation of receptor density at the cell surface. *Trends Pharmacol. Sci.* 29, 528–535. doi:10.1016/j.tips.2008.07.009
- Alvarez-Prats, A., Bjelobaba, I., Aldworth, Z., Baba, T., Abebe, D., Kim, Y. J., et al. (2018). Schwann-cell-specific deletion of phosphatidylinositol 4-kinase alpha causes aberrant myelination. *Cel Rep.* 23, 2881–2890. doi:10.1016/j.celrep.2018.05.019
- Baba, T., Alvarez-Prats, A., Kim, Y. J., Abebe, D., Wilson, S., Aldworth, Z., et al. (2020). Myelination of peripheral nerves is controlled by PI4KB through regulation of Schwann cell Golgi function. *Proc. Natl. Acad. Sci. USA.* 117, 28102–28113. doi:10.1073/pnas.2007432117
- Basak, B., Krishnan, H., and Raghu, P. (2021). Interdomain interactions regulate the localization of a lipid transfer protein at ER-PM contact sites. *Biol. Open.* 10, bio057422. doi:10.1242/bio.057422
- Bautista, L., Castro, M. J., López-Barneo, J., and Castellano, A. (2009). Hypoxia inducible factor-2α stabilization and maxi-K + channel β 1 -subunit gene repression by hypoxia in cardiac myocytes. *Circ. Res.* 104, 1364–1372. doi:10. 1161/circresaha.108.190645
- Bernard, V., Levey, A. I., and Bloch, B. (1999). Regulation of the subcellular distribution of m4 muscarinic acetylcholine receptors in striatal NeuronsIn vivoby the cholinergic environment: evidence for regulation of cell surface receptors by endogenous and exogenous stimulation. *J. Neurosci.* 19, 10237–10249. doi:10.1523/jneurosci.19-23-10237.1999
- Bernheim, L., Mathie, A., and Hille, B. (1992). Characterization of muscarinic receptor subtypes inhibiting Ca2+ current and M current in rat sympathetic neurons. *Proc. Natl. Acad. Sci.* 89, 9544–9548. doi:10.1073/ pnas.89.20.9544

data analysis and mathematical modeling, supervision of project, and drafting of the manuscript. Both RW and MK contributed to the article and approved the submitted version.

FUNDING

Research reported in this project was supported by an Institutional Development Award (IDeA) from the National Institute of General Medical Sciences of the National Institutes of Health under grant number P20GM103423.

ACKNOWLEDGMENTS

We would like to thank all colleagues who have generously provided us with plasmids (see Material and Methods). We are also thankful to Dr. Bavis for providing us with tissue from rats and to Drs. Hill, Dearborn, and Castro for comments on the manuscript, and to all members of the Kruse lab and the members of the Department of Biology and Program in Neuroscience at Bates College for discussions and experimental advice. The authors declare no competing financial interests.

SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fphar.2021.663840/full#supplementary-material.

- Borg-Graham, L. (1991). Modelling the non-linear conductances of excitable membranes. Oxford: Oxford University Press
- Brown, D. A., Adams, P. R., and Constanti, A. (1982). Voltage-sensitive K-currents in sympathetic neurons and their modulation by neurotransmitters. J. Auton. Nervous Syst. 6, 23–35. doi:10.1016/0165-1838(82)90019-4
- Brown, D. A., and Adams, P. R. (1980). Muscarinic suppression of a novel voltagesensitive K+ current in a vertebrate neurone. *Nature* 283, 673–676. doi:10.1038/ 283673a0
- Brown, D. A., Hughes, S. A., Marsh, S. J., and Tinker, A. (2007). Regulation of M(Kv7.2/7.3) channels in neurons by PIP2and products of PIP2hydrolysis: significance for receptor-mediated inhibition. J. Physiol. 582, 917–925. doi:10. 1113/jphysiol.2007.132498
- Brown, D. A., and Selyanko, A. A. (1985). Membrane currents underlying the cholinergic slow excitatory post-synaptic potential in the rat sympathetic ganglion. J. Physiol. 365, 365–387. doi:10.1113/jphysiol. 1985.sp015777
- Brown, S.-A., Morgan, F., Watras, J., and Loew, L. M. (2008). Analysis of phosphatidylinositol-4,5-bisphosphate signaling in cerebellar Purkinje spines. *Biophysical J*. 95, 1795–1812. doi:10.1529/biophysj.108.130195
- Cantley, L. C. (2002). The phosphoinositide 3-kinase pathway. *Science* 296, 1655–1657. doi:10.1126/science.296.5573.1655
- Chang, C.-P., Dworetzky, S. I., Wang, J., and Goldstein, M. E. (1997). Differential expression of the α and β subunits of the large-conductance calcium-activated potassium channel: implication for channel diversity. *Mol. Brain Res.* 45, 33–40. doi:10.1016/s0169-328x(96)00230-6
- Cockcroft, S., Garner, K., Yadav, S., Gomez-Espinoza, E., and Raghu, P. (2016). RdgBa reciprocally transfers PA and PI at ER-PM contact sites to maintain PI(4,5)P2 homoeostasis during phospholipase C signalling in *Drosophila* photoreceptors. *Biochem. Soc. Trans.* 44, 286–292. doi:10.1042/bst20150228

- Cockcroft, S., and Raghu, P. (2016). Topological organisation of the phosphatidylinositol 4,5-bisphosphate-phospholipase C resynthesis cycle: PITPs bridge the ER-PM gap. *Biochem. J.* 473, 4289–4310. doi:10.1042/bcj20160514c
- Cox, D. H. (2014). Modeling a Ca 2+ channel/BK Ca channel complex at the singlecomplex level. *Biophysical J.* 107, 2797–2814. doi:10.1016/j.bpj.2014.10.069
- Cremona, O., and De Camilli, P. (2001). Phosphoinositides in membrane traffic at the synapse. J. Cel Sci. 114, 1041–1052.
- Dai, G., Yu, H., Kruse, M., Traynor-Kaplan, A., and Hille, B. (2016). Osmoregulatory inositol transporter SMIT1 modulates electrical activity by adjusting PI(4,5)P2 levels. *Proc. Natl. Acad. Sci. USA*. 113, E3290–9. doi:10. 1073/pnas.1606348113
- De La Cruz, L., Traynor-Kaplan, A., Vivas, O., Hille, B., and Jensen, J. B. (2020). Plasma membrane processes are differentially regulated by type I phosphatidylinositol phosphate 5-kinases and RASSF4. *J. Cel Sci* 133. doi:10. 1242/jcs.233254
- Devreotes, P. N., and Fambrough, D. M. (1975). Acetylcholine receptor turnover in membranes of developing muscle fibers. J. Cel Biol. 65, 335–358. doi:10.1083/jcb. 65.2.335
- Di Paolo, G., and De Camilli, P. (2006). Phosphoinositides in cell regulation and membrane dynamics. *Nature* 443, 651–657. doi:10.1038/nature05185
- Dickson, E. J. (2019). Recent advances in understanding phosphoinositide signaling in the nervous system. *F1000Res.* 8, F1000 Faculty Rev-278. doi:10. 12688/f1000research.16679.1
- Dickson, E. J., Falkenburger, B. H., and Hille, B. (2013). Quantitative properties and receptor reserve of the IP3 and calcium branch of Gq-coupled receptor signaling. J. Gen. Physiol. 141, 521–535. doi:10.1085/jgp.201210886
- Dickson, E. J., Jensen, J. B., and Hille, B. (2014). Golgi and plasma membrane pools of PI(4)P contribute to plasma membrane PI(4,5)P2 and maintenance of KCNQ2/3 ion channel current. *Proc. Natl. Acad. Sci.* 111, E2281–E2290. doi:10.1073/pnas.1407133111
- Dickson, E. J., Jensen, J. B., Vivas, O., Kruse, M., Traynor-Kaplan, A. E., and Hille, B. (2016). Dynamic formation of ER-PM junctions presents a lipid phosphatase to regulate phosphoinositides. J. Cel Biol. 213, 33–48. doi:10.1083/jcb.201508106
- Dunn, H. A., and Ferguson, S. S. G. (2015). PDZ protein regulation of G proteincoupled receptor trafficking and signaling pathways. *Mol. Pharmacol.* 88, 624–639. doi:10.1124/mol.115.098509
- Fagerberg, L., Hallström, B. M., Oksvold, P., Kampf, C., Djureinovic, D., Odeberg, J., et al. (2014). Analysis of the human tissue-specific expression by genomewide integration of transcriptomics and antibody-based proteomics. *Mol. Cell Proteomics.* 13, 397–406. doi:10.1074/mcp.m113.035600
- Falkenburger, B. H., Dickson, E. J., and Hille, B. (2013). Quantitative properties and receptor reserve of the DAG and PKC branch of G_q-coupled receptor signaling. *J. Gen. Physiol.* 141 (5), 537–555. doi:10.1085/jgp.201210887
- Falkenburger, B. H., Jensen, J. B., and Hille, B. (2010a). Kinetics of M1 muscarinic receptor and G protein signaling to phospholipase C in living cells. J. Gen. Physiol. 135, 81–97. doi:10.1085/jgp.200910344
- Falkenburger, B. H., Jensen, J. B., and Hille, B. (2010b). Kinetics of PIP2 metabolism and KCNQ2/3 channel regulation studied with a voltage-sensitive phosphatase in living cells. J. Gen. Physiol. 135, 99–114. doi:10.1085/jgp.200910345
- Gamper, N., Reznikov, V., Yamada, Y., Yang, J., and Shapiro, M. S. (2004). Phosphotidylinositol 4,5-bisphosphate signals underlie receptor-specific gq/ 11-mediated modulation of N-type Ca2+ channels. *J. Neurosci.* 24, 10980–10992. doi:10.1523/jneurosci.3869-04.2004
- Halaszovich, C. R., Schreiber, D. N., and Oliver, D. (2009). Ci-VSP is a depolarization-activated phosphatidylinositol-4,5-bisphosphate and phosphatidylinositol-3,4,5-trisphosphate 5'-phosphatase. J. Biol. Chem. 284, 2106–2113. doi:10.1074/jbc.m803543200
- Hammond, G. R. V., Machner, M. P., and Balla, T. (2014). A novel probe for phosphatidylinositol 4-phosphate reveals multiple pools beyond the golgi. J. Cel Biol. 205, 113–126. doi:10.1083/jcb.201312072
- Hardie, R. C., and Franze, K. (2012). Photomechanical responses in *Drosophila* photoreceptors. *Science* 338, 260–263. doi:10.1126/science.1222376
- Hardie, R. C., Gu, Y., Martin, F., Sweeney, S. T., and Raghu, P. (2004). *In vivo* lightinduced and basal phospholipase C activity in *Drosophila* photoreceptors measured with genetically targeted phosphatidylinositol 4,5-bisphosphatesensitive ion channels (Kir2.1). *J. Biol. Chem.* 279, 47773–47782. doi:10. 1074/jbc.m407525200

- Hardie, R. C., Raghu, P., Moore, S., Juusola, M., Baines, R. A., and Sweeney, S. T. (2001). Calcium influx via TRP channels is required to maintain PIP2 levels in *Drosophila* photoreceptors. *Neuron* 30, 149–159. doi:10.1016/s0896-6273(01) 00269-0
- Hernandez, C. C., Falkenburger, B., and Shapiro, M. S. (2009). Affinity for phosphatidylinositol 4,5-bisphosphate determines muscarinic agonist sensitivity of Kv7 K+ channels. J. Gen. Physiol. 134, 437–448. doi:10.1085/ jgp.200910313
- Hille, B., Dickson, E. J., Kruse, M., Vivas, O., and Suh, B.-C. (2015). Phosphoinositides regulate ion channels. *Biochim Biophys. Acta.* 1851, 844–856. doi:10.1016/j.bbalip.2014.09.010
- Hille, B., Dickson, E., Kruse, M., and Falkenburger, B. (2014). Dynamic metabolic control of an ion channel. Prog. Mol. Biol. translational Sci. 123, 219–247. doi:10.1016/b978-0-12-397897-4.00008-5
- Hodgkin, A. L., and Huxley, A. F. (1952). A quantitative description of membrane current and its application to conduction and excitation in nerve. J. Physiol. 117, 500–544. doi:10.1113/jphysiol.1952.sp004764
- Hossain, M. I., Iwasaki, H., Okochi, Y., Chahine, M., Higashijima, S., Nagayama, K., et al. (2008). Enzyme domain affects the movement of the voltage sensor in ascidian and zebrafish voltage-sensing phosphatases. *J. Biol. Chem.* 283, 18248–18259. doi:10.1074/jbc.m706184200
- Hu, J., Yuan, Q., Kang, X., Qin, Y., Li, L., Ha, Y., et al. (2015). Resolution of structure of PIP5K1A reveals molecular mechanism for its regulation by dimerization and dishevelled. *Nat. Commun.* 6, 8205. doi:10.1038/ ncomms9205
- Hughes, S., Marsh, S. J., Tinker, A., and Brown, D. A. (2007). PIP2-dependent inhibition of M-type (Kv7.2/7.3) potassium channels: direct on-line assessment of PIP2 depletion by Gq-coupled receptors in single living neurons. *Pflugers Arch.* 455, 115–124. doi:10.1007/s00424-007-0259-6
- Ivanov, A., and Purves, D. (1989). Ongoing electrical activity of superior cervical ganglion cells in mammals of different size. J. Comp. Neurol. 284, 398–404. doi:10.1002/cne.902840307
- Iwasaki, H., Murata, Y., Kim, Y., Hossain, M. I., Worby, C. A., Dixon, J. E., et al. (2008). A voltage-sensing phosphatase, Ci-VSP, which shares sequence identity with PTEN, dephosphorylates phosphatidylinositol 4,5bisphosphate. *Proc. Natl. Acad. Sci.* 105, 7970–7975. doi:10.1073/pnas. 0803936105
- Krause, Y., Krause, S., Huang, J., Liu, C.-H., Hardie, R. C., and Weckström, M. (2008). Light-dependent modulation of shab channels via phosphoinositide depletion in *Drosophila* photoreceptors. *Neuron* 59, 596–607. doi:10.1016/j. neuron.2008.07.009
- Kruse, M., Hammond, G. R. V., and Hille, B. (2012). Regulation of voltage-gated potassium channels by PI(4,5)P2. J. Gen. Physiol. 140, 189–205. doi:10.1085/jgp. 201210806
- Kruse, M., Vivas, O., Traynor-Kaplan, A., and Hille, B. (2016). Dynamics of phosphoinositide-dependent signaling in sympathetic neurons. J. Neurosci. 36 (4), 1386–1400. doi:10.1523/jneurosci.3535-15.2016
- Liu, C. H., Bollepalli, M. K., Long, S. V., Asteriti, S., Tan, J., Brill, J. A., et al. (2018). Genetic dissection of the phosphoinositide cycle in *Drosophila* photoreceptors. *J. Cel Sci.* 131. doi:10.1242/jcs.214478
- Liu, L., Zhao, R., Bai, Y., Stanish, L. F., Evans, J. E., Sanderson, M. J., et al. (2006). M1 muscarinic receptors inhibit L-type Ca2+ current and M-current by divergent signal transduction cascades. *J. Neurosci.* 26, 11588–11598. doi:10. 1523/jneurosci.2102-06.2006
- Martin, T. F. (2014). PI(4,5)P₂-binding effector proteins for vesicle exocytosis. Biochim. Biophys. Acta. 14, S1388–S1981. doi:10.1016/j.bbalip.2014.09.017
- Mathie, A., Bernheim, L., and Hille, B. (1992). Inhibition of N- and L-type calcium channels by muscarinic receptor activation in rat sympathetic neurons. *Neuron* 8, 907–914. doi:10.1016/0896-6273(92)90205-r
- Mergenthal, A., Bouteiller, J. C., Yu, G. J., and Berger, T. W. (2020). A computational model of the cholinergic modulation of CA1 pyramidal cell activity. *Front. Comput. Neurosci.* 14, 75. doi:10.3389/fncom.2020.00075
- Migliore, M., Cook, E. P., Jaffe, D. B., Turner, D. A., and Johnston, D. (1995). Computer simulations of morphologically reconstructed CA3 hippocampal neurons. J. Neurophysiol. 73, 1157–1168. doi:10.1152/jn.1995.73.3.1157
- Moczydlowski, E., and Latorre, R. (1983). Gating kinetics of Ca2+-activated K+ channels from rat muscle incorporated into planar lipid bilayers. Evidence for

two voltage-dependent Ca2+ binding reactions. J. Gen. Physiol. 82, 511-542. doi:10.1085/jgp.82.4.511

- Myeong, J., De La Cruz, L., Jung, S. R., Yeon, J. H., Suh, B. C., Koh, D. S., et al. (2020). Phosphatidylinositol 4,5-bisphosphate is regenerated by speeding of the PI 4-kinase pathway during long PLC activation. *J. Gen. Physiol.* 152. doi:10.1085/jgp.202012627
- Nath, V. R., Mishra, S., Basak, B., Trivedi, D., and Raghu, P. (2020). Extended synaptotagmin regulates membrane contact site structure and lipid transfer function *in vivo*. *EMBO Rep.* 21, e50264. doi:10.15252/embr.202050264
- Nishimura, T., Gecht, M., Covino, R., Hummer, G., Surma, M. A., Klose, C., et al. (2019). Osh proteins control nanoscale lipid organization necessary for PI(4,5) P2 synthesis. *Mol. Cel.* 75, 1043–1057.e8. doi:10.1016/j.molcel.2019.06.037
- Pan, W., Choi, S.-C., Wang, H., Qin, Y., Volpicelli-Daley, L., Swan, L., et al. (2008). Wnt3a-mediated formation of phosphatidylinositol 4,5-bisphosphate regulates LRP6 phosphorylation. *Science* 321, 1350–1353. doi:10.1126/science.1160741
- Paolo, G. D., Moskowitz, H. S., Gipson, K., Wenk, M. R., Voronov, S., Obayashi, M., et al. (2004). Impaired PtdIns(4,5)P2 synthesis in nerve terminals produces defects in synaptic vesicle trafficking. *Nature* 431, 415–422. doi:10.1038/nature02896
- Pemberton, J. G., Kim, Y. J., Humpolickova, J., Eisenreichova, A., Sengupta, N., Toth, D. J., et al. (2020). Defining the subcellular distribution and metabolic channeling of phosphatidylinositol. *J. Cel Biol.* 219, e201906130. doi:10.1083/jcb.201906130
- Posor, Y., Eichhorn-Grunig, M., and Haucke, V. (2014). Phosphoinositides in endocytosis. *Biochim. Biophys. Acta.* 14, S1388–S1981. doi:10.1016/j.bbalip. 2014.09.014
- Qin, Y., Li, L., Pan, W., and Wu, D. (2009). Regulation of phosphatidylinositol kinases and metabolism by Wnt3a and Dvl. J. Biol. Chem. 284, 22544–22548. doi:10.1074/jbc.m109.014399
- Quadroni, R., and Knopfel, T. (1994). Compartmental models of type A and type B Guinea pig medial vestibular neurons. J. Neurophysiol. 72, 1911–1924. doi:10. 1152/jn.1994.72.4.1911
- Raghu, P., and Hardie, R. C. (2009). Regulation of *Drosophila* TRPC channels by lipid messengers. *Cell Calcium*. 45, 566–573. doi:10.1016/j.ceca.2009.03.005
- Randall, A. S., Liu, C.-H., Chu, B., Zhang, Q., Dongre, S. A., Juusola, M., et al. (2015). Speed and sensitivity of phototransduction in *Drosophila* depend on degree of saturation of membrane phospholipids. *J. Neurosci.* 35, 2731–2746. doi:10.1523/jneurosci.1150-14.2015
- Reiner, A., and Levitz, J. (2018). Glutamatergic signaling in the central nervous system: ionotropic and metabotropic receptors in concert. *Neuron* 98, 1080–1098. doi:10.1016/j.neuron.2018.05.018
- Rudell, J. B., and Ferns, M. J. (2013). Regulation of muscle acetylcholine receptor turnover by β subunit tyrosine phosphorylation. *Devel Neurobio.* 73, 399–410. doi:10.1002/dneu.22070
- Saarikangas, J., Zhao, H., and Lappalainen, P. (2010). Regulation of the actin cytoskeleton-plasma membrane interplay by phosphoinositides. *Physiol. Rev.* 90, 259–289. doi:10.1152/physrev.00036.2009
- Saheki, Y., and De Camilli, P. (2017). Endoplasmic reticulum-plasma membrane contact sites. Annu. Rev. Biochem. 86, 659–684. doi:10.1146/annurev-biochem-061516-044932
- Somjen, G. G., Kager, H., and Wadman, W. J. (2008). Computer simulations of neuron-glia interactions mediated by ion flux. J. Comput. Neurosci. 25, 349–365. doi:10.1007/s10827-008-0083-9
- Suh, B.-C., and Hille, B. (2002). Recovery from muscarinic modulation of M current channels requires phosphatidylinositol 4,5-bisphosphate synthesis. *Neuron* 35, 507–520. doi:10.1016/s0896-6273(02)00790-0
- Suh, B.-C., Kim, D.-I., Falkenburger, B. H., and Hille, B. (2012). Membranelocalized -subunits alter the PIP2 regulation of high-voltage activated Ca2+ channels. Proc. Natl. Acad. Sci. 109, 3161–3166. doi:10.1073/pnas.1121434109
- Sun, J., and Mackinnon, R. (2020). Structural basis of human KCNQ1 modulation and gating. *Cell* 180, 340–347. doi:10.1016/j.cell.2019.12.003
- Traub, R. D., Wong, R. K., Miles, R., and Michelson, H. (1991). A model of a CA3 hippocampal pyramidal neuron incorporating voltage-clamp data on intrinsic conductances. J. Neurophysiol. 66, 635–650. doi:10.1152/jn.1991.66.2.635
- Traynor-Kaplan, A., Kruse, M., Dickson, E. J., Dai, G., Vivas, O., Yu, H., et al. (2017). Fatty-acyl chain profiles of cellular phosphoinositides. *Biochim Biophys Acta Mol Cell Biol Lipids*. 1862, 513–522. doi:10.1016/j.bbalip.2017.02.002

- Vaithianathan, T., Bukiya, A., Liu, J., Liu, P., Asuncion-Chin, M., Fan, Z., et al. (2008). Direct regulation of BK channels by phosphatidylinositol 4,5bisphosphate as a novel signaling pathway. J. Gen. Physiol. 132, 13–28. doi:10.1085/jgp.200709913
- Van Der Wal, J., Habets, R., Várnai, P., Balla, T., and Jalink, K. (2001). Monitoring agonist-induced phospholipase C activation in live cells by fluorescence resonance energy transfer. J. Biol. Chem. 276, 15337–15344. doi:10.1074/jbc. m007194200
- Vivas, O., Kruse, M., and Hille, B. (2014). Nerve growth factor sensitizes adult sympathetic neurons to the proinflammatory peptide bradykinin. J. Neurosci. 34, 11959–11971. doi:10.1523/jneurosci.1536-14.2014
- Vivas, O., Moreno, C. M., Santana, L. F., and Hille, B. (2017). Proximal clustering between BK and Ca_V1.3 channels promotes functional coupling and BK channel activation at low voltage. *Elife* 6, 1–18. doi:10.7554/elife.28029
- Weis, W. I., and Kobilka, B. K. (2018). The molecular basis of G protein-coupled receptor activation. Annu. Rev. Biochem. 87, 897–919. doi:10.1146/annurevbiochem-060614-033910
- Whitmire, L. E., Ling, L., Bugay, V., Carver, C. M., Timilsina, S., Chuang, H. H., et al. (2017). Downregulation of KCNMB4 expression and changes in BK channel subtype in hippocampal granule neurons following seizure activity. *PLoS One* 12, e0188064. doi:10.1371/journal.pone.0188064
- Willars, G. B., Nahorski, S. R., and Challiss, R. A. J. (1998). Differential regulation of muscarinic acetylcholine receptor-sensitive polyphosphoinositide pools and consequences for signaling in human neuroblastoma cells. J. Biol. Chem. 273, 5037–5046. doi:10.1074/jbc.273.9.5037
- Winks, J. S., Hughes, S., Filippov, A. K., Tatulian, L., Abogadie, F. C., Brown, D. A., et al. (2005). Relationship between membrane phosphatidylinositol-4,5bisphosphate and receptor-mediated inhibition of native neuronal M channels. J. Neurosci. 25, 3400–3413. doi:10.1523/jneurosci.3231-04.2005
- Xia, X.-M., Ding, J. P., and Lingle, C. J. (1999). Molecular basis for the inactivation of Ca2+and voltage-dependent BK channels in adrenal chromaffin cells and rat insulinoma tumor cells. J. Neurosci. 19, 5255–5264. doi:10.1523/jneurosci.19-13-05255.1999
- Xu, C., Watras, J., and Loew, L. M. (2003). Kinetic analysis of receptor-activated phosphoinositide turnover. J. Cel Biol. 161 (4), 779–791. doi:10.1083/jcb. 200301070
- Yadav, S., Garner, K., Georgiev, P., Li, M., Gomez-Espinosa, E., Panda, A., et al. (2015). RDGB , a PtdIns-PtdOH transfer protein, regulates G-protein-coupled PtdIns(4,5)P2 signalling during *Drosophila* phototransduction. *J. Cel Sci.* 128, 3330–3344. doi:10.1242/jcs.173476
- Zaika, O., Lara, L. S., Gamper, N., Hilgemann, D. W., Jaffe, D. B., and Shapiro, M. S. (2006). Angiotensin II regulates neuronal excitability via phosphatidylinositol 4,5-bisphosphate-dependent modulation of Kv7 (M-type) K+channels. *J. Physiol.* 575, 49–67. doi:10.1113/jphysiol.2006.114074
- Zaika, O., Zhang, J., and Shapiro, M. S. (2011). Functional role of M-type (KCNQ) K+channels in adrenergic control of cardiomyocyte contraction rate by sympathetic neurons. J. Physiol. 589, 2559–2568. doi:10.1113/jphysiol.2010.204768
- Zewe, J. P., Miller, A. M., Sangappa, S., Wills, R. C., Goulden, B. D., and Hammond, G. R. V. (2020). Probing the subcellular distribution of phosphatidylinositol reveals a surprising lack at the plasma membrane. *J. Cel Biol.* 219, e201906127. doi:10.1083/jcb.201906127
- Zhang, J., Bal, M., Bierbower, S., Zaika, O., and Shapiro, M. S. (2011). AKAP79/150 signal complexes in G-protein modulation of neuronal ion channels. *J. Neurosci.* 31, 7199–7211. doi:10.1523/jneurosci.4446-10.2011

Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

Copyright © 2021 Kruse and Whitten. This is an open-access article distributed under the terms of the Creative Commons Attribution License (CC BY). The use, distribution or reproduction in other forums is permitted, provided the original author(s) and the copyright owner(s) are credited and that the original publication in this journal is cited, in accordance with accepted academic practice. No use, distribution or reproduction is permitted which does not comply with these terms.