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Quantification of signal amplification for receptors: the K_d/EC_{50} ratio of full agonists as a gain parameter

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Concentration-response relationships connecting the concentration of ligands to the responses they produce are central to pharmacology in general and form the core of quantitative pharmacology. While typically they can be well-described by hyperbolic functions (sigmoid on commonly used semi-log scales) and characterized by half-maximal concentrations values (EC_{50}), their connection to receptor occupancy, characterized in a similar manner by the equilibrium dissociation constant K_d , can be complex due to the intermixing of the effects from occupancy-induced activation with those from partial agonism, constitutive activity, and pathway-specific signal amplification. Here, it is proposed that, as long as both occupancy and response follow such typical concentration-dependencies, signal amplification can be quantified using the gain parameter $g_K = \kappa = K_d/EC_{50}$ measured for full agonists. This is similar to the gain parameter used in electronics (e.g., $g_V = V_{out}/V_{in}$ for voltage). On customarily used semi-log representations, $\log g_K$ corresponds to the horizontal shift between the response and occupancy curves, $\log K_d - \log EC_{50}$, the presence of which (i.e., $K_d > EC_{50}$) is generally considered as evidence for the existence of “receptor reserve” or “spare receptors”. The latter is a misnomer that should be avoided since even if there are excess receptors, there is no special pool of receptors “not required for ordinary use” as *spare* would imply. For partial agonists, the $\kappa = K_d/EC_{50}$ shift is smaller than for full agonists as not all occupied receptors are active. The g_K gain parameter (full agonist K_d/EC_{50}) corresponds to the γ gain parameter of the SABRE receptor model, which includes parameters for Signal Amplification (γ), Binding affinity (K_d), and Receptor-activation Efficacy (ϵ); for partial agonists ($\epsilon < 1$), SABRE predicts a corresponding shift of $\kappa = \epsilon\gamma - \epsilon + 1$.

KEYWORDS

amplification, biased agonism, binding affinity, ligand efficacy, pharmacological shift ratio, signal transduction, spare receptor, receptor model

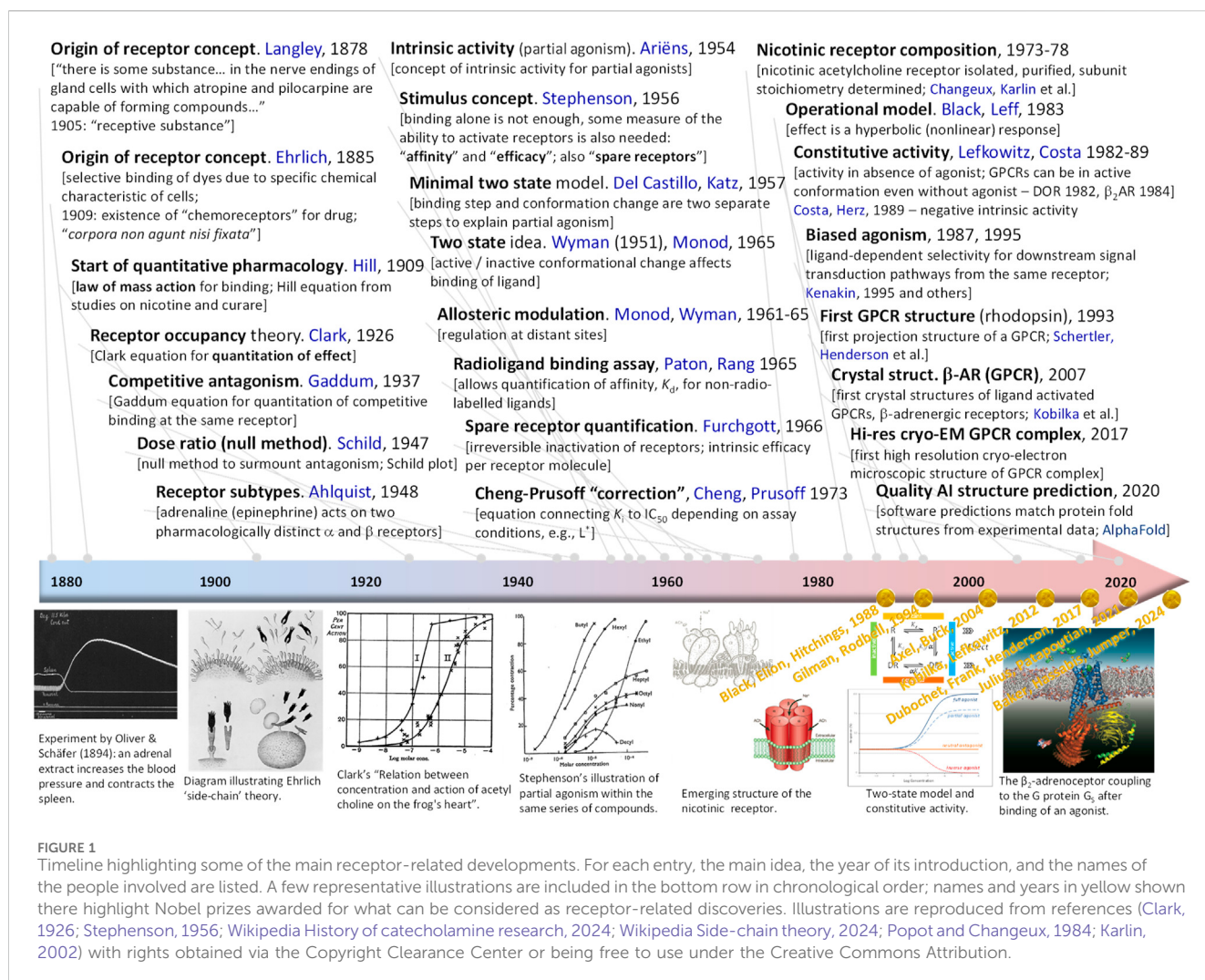


FIGURE 1

Timeline highlighting some of the main receptor-related developments. For each entry, the main idea, the year of its introduction, and the names of the people involved are listed. A few representative illustrations are included in the bottom row in chronological order; names and years in yellow shown there highlight Nobel prizes awarded for what can be considered as receptor-related discoveries. Illustrations are reproduced from references (Clark, 1926; Stephenson, 1956; Wikipedia History of catecholamine research, 2024; Wikipedia Side-chain theory, 2024; Popot and Changeux, 1984; Karlin, 2002) with rights obtained via the Copyright Clearance Center or being free to use under the Creative Commons Attribution.

Introduction

Receptors and concentration- or dose-response curves

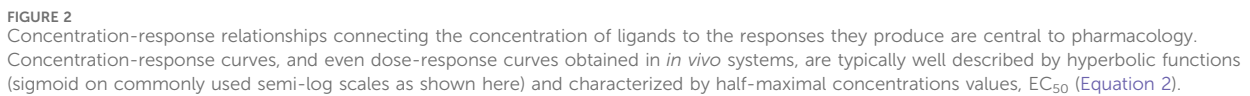
Receptors, “pharmacology’s big idea” (Rang, 2006), are at the core of our current understanding of mechanism of drug action (Figure 1) (Maehle et al., 2002; Winquist et al., 2014; Heldin et al., 2016; Finlay et al., 2020). In a general context, receptors are used to denote any target of a substance that is responsible for initiating a biological response, but in a stricter pharmacological sense, receptors are protein molecules whose function is to recognize and respond to endogenous chemical signals; as such, they are one of the four common drug targets (receptors, enzymes, carriers, and ion channels) (Ritter et al., 2020). Binding of a ligand to the receptor initiates a sequential process termed signal transduction that culminates in one or more specific cellular response. Unequivocally connecting the concentration of a ligand of interest to the response it produces is of obvious interest; thus, concentration-response relationships are central to pharmacology in general and quantitative pharmacology in particular. Typically, the concentration-

dependence of both receptor response and occupancy can be well described by hyperbolic functions (sigmoid on commonly used semi-log scales) characterized by half-maximal concentrations values, i.e., $K_{obs} = EC_{50}$ and K_d for response and occupancy, respectively (Figure 2). These are determined from single-parameter equations such as those shown below for fractional occupancy (f_{occup}) and response (f_{resp}), respectively:

$$f_{occup}([L]) = R_{occup}/R_{max} = \frac{[L]}{[L] + K_d} \quad (1)$$

$$f_{resp}([L]) = E/E_{max} = \frac{[L]}{[L] + EC_{50}} = \frac{[L]}{[L] + K_{obs}} \quad (2)$$

With the evolution of the field (see summary timeline of Figure 1) (Maehle et al., 2002; Winquist et al., 2014; Finlay et al., 2020; Ruffolo, 1982; Colquhoun, 1998), it became clear that the connection between receptor occupancy and response can be quite complex, as in addition to occupancy, it also has to account for partial agonism, receptor reserve, constitutive activity, and other effects. The overall efficiency of the transduction process that links occupancy to response, i.e., the occupancy-response coupling (Katzung, 2018), is



2023). Hence, even if the simple Clark equation (Equation 2), which has been published a century ago in 1926 (Figure 1) (Clark, 1926)¹, works well and forms the basis of most concentration-response or dose-response relationship fittings to this day, a quantitative model that can form the basis of a true concentration-response relationships and connect the concentration of a ligand to the response(s) that it produces should account for all these and, thus, have a

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minimum of five independent parameters (Buchwald, 2023). Most likely, even more parameters are needed for dose-response relationships (*in vivo* systems), where the pharmacokinetic aspects determining the amount (concentration) of drug ultimately reaching the receptor also have to be accounted for (Aronson, 2007; Gabrielsson and Weiner, 2000).

Quantifying signal amplification for receptors

Along these lines, it has been clearly recognized since the mid-1950s (Figure 1) that, for some receptors, maximal or close to maximal response can be achieved when only a much smaller fraction of the receptors is occupied—a recognition that led to the notion of “spare receptors” or “receptor reserve” (Stephenson, 1956; Nickerson, 1956). A method to quantify the fraction of occupied receptors (occupancy) from measurements of response (effect) data alone was introduced by Furchgott about a decade later (Furchgott, 1966; Furchgott and Bursztyn, 1967), and versions of it are still in use (Buchwald, 2022). Quantitative studies comparing occupancy and response have been done for a number of cases, most of them involving G-protein coupled receptors (GPCRs), and some found quite extreme cases of activation. For example, guinea pig ileal response, where histamine can produce close to 100% response at only ~2% occupancy ($f_{\text{resp}} \approx 1.00$ at $f_{\text{occup}} = 0.02$), or rat heart β -adrenergic receptors, where epinephrine can produce half-maximal increase of muscle contractility at only ~2% occupancy ($f_{\text{resp}} \approx 0.50$ at $f_{\text{occup}} = 0.02$) (see (Buchwald, 2019) for additional references). This implies that significant signal amplification has to take place downstream—typically via some cascade mechanism involving second messengers such as cyclic AMP (cAMP) or other systems (Koshland et al., 1982; Strickland and Loeb, 1981; Ferrell, 1996); a classic textbook illustration for GPCRs can be found in Figure 36 here (El-Fakahany and Merkey, 2020). Sensory systems in particular need to rely on high gain, low noise amplification processes to be able to convert even very weak stimuli into detectable and reliable signals (Kleene, 1997). Many GPCRs can generate ultra-sensitive responses to ligands at concentrations below picomolar levels ($<10^{-12}$ M) (Civciristov and Halls, 2019), and there are examples of diverse chemical agents capable of engaging receptors/intracellular signaling systems in a variety of species to elicit effects at ultra-low concentrations (in the 10^{-18} to 10^{-24} M range, i.e., approaching the one molecule per cell ratio) (Calabrese and Giordano, 2021). Along these lines, in phototransduction a single photon has been shown to activate around 60 G proteins from rod photoreceptors in frogs, which can lead to hydrolysis of up to 70,000 cGMP molecules downstream (Arshavsky and Burns, 2014). Consequently, humans seem to be able to detect a single-photon incident on the cornea (Tinsley et al., 2016). Another well-known example is the mechanism by which epinephrine (adrenaline) or glucagon sets off a cascade of phosphorylation leading to the production of glucose resulting in a very strong amplification of the initial signal, possibly as high as 10^7 – 10^8 -fold as (sub)nanomolar changes ($<10^{-9}$ M) in these signals can lead to millimolar changes ($\sim 10^{-3}$ M) in glucose (Nelson and Cox, 2012; Lodish et al., 2003). Signal amplification has been confirmed not only for GPCRs, but also for kinase-linked receptors (Heldin et al., 2016) and ligand-

gated ion channels (for example, for insect olfactory receptors whereby receptor excitation allows for direct influx of Ca^{2+} serving as second messenger and thereby amplify responses (Ng et al., 2019)). It is therefore important to have a well-defined method and corresponding parameter(s) that can be used to quantify receptor signal amplification.

Methods of gain quantification

Gain quantification based on analogy with electronic amplifiers

Since the cascade mechanisms of physiological signal amplification resembles in many ways those occurring in electronic circuits (Grubelnik et al., 2009), it makes sense to define a signal amplification factor in a manner similar to that used there. In a very general perspective, for a transfer function, $y = f_{\text{tr}}(x)$ that links the magnitude of the output response y to the input signal x , the gain (or amplification factor) g is defined as the ratio of output to input at a given value of input x (Elowitz et al., 2022):

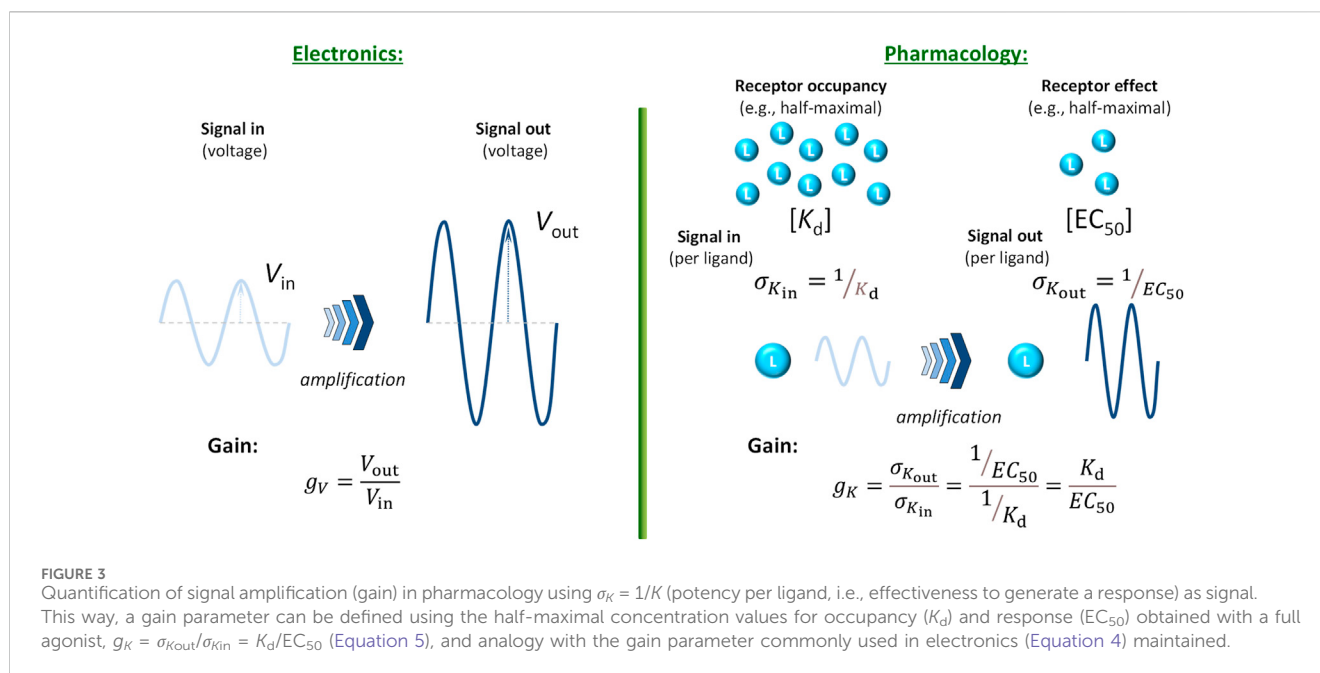
$$g = \frac{f_{\text{tr}}(x)}{x} \quad (3)$$

The input and output signals have to be of the same type (i.e., measured in the same units); therefore, the gain for voltage as a common example from electronics is:

$$g_V = \frac{V_{\text{out}}}{V_{\text{in}}} \quad (4)$$

For linear amplifiers, the simplest case, the gain is constant over the entire range of the input, but in general, the value of the gain g depends on the input level, x . In such cases, the derivative of the transfer curve, df_{tr}/dx , is of interest as it represents the change in output (dy) produced by a small change in input (dx) at level x (Elowitz et al., 2022). For linear amplifiers, this is identical to the gain g itself, as in this case, $f_{\text{tr}}(x) = gx$ for all x values with g being constant, so that $df_{\text{tr}}/dx = g$.

In physiological/pharmacological signaling, there can be significant increase in the number (concentration) of molecules due to downstream amplification from possibly only a few ligands that bind to the receptor (“input”) to a much larger number of generated molecules where the response or readout takes place (“output”) – a few well-known illustrative cases, such as that of epinephrine $\rightarrow$ glucose, have been mentioned earlier. The corresponding increase ratio could be used to calculate a concentration gain, $g_C = C_{\text{out}}/C_{\text{in}}$; however, concentrations are rarely measured (or even measurable) along signaling pathways. On the other hand, responses are commonly measured (often normalized to their maximum) and quantified using EC_{50} , the ligand concentration that causes half-maximal response ($f_{\text{resp}} = 0.5$; Equation 2). Thus, it makes sense to quantify amplification using them, especially as they are also measured in concentration units. One way to do so is to consider the signal that is amplified to be not the ligand concentration, but the effectiveness of the ligand to generate a response, i.e., the signaling power per unit input (molecule). Since potency quantification is done by



concentrations corresponding to half-maximal responses (e.g., K_d and $K_{obs} = EC_{50}$ in Equations 1, 2, respectively), one can consider the respective potency per ligand as proportional with the inverse of them. Thus, the signal per ligand is inversely proportional with the concentration of ligands needed to achieve a given, e.g., half-maximal effect, $\sigma_K = 1/K$, and then the corresponding gain g_K is the ratio of these, i.e., $\sigma_{K_{in}}$ at the level of occupancy as the “in” signal and $\sigma_{K_{out}}$ at the level of measured response as the “out” signal (Figure 3):

$$g_K = \frac{\sigma_{K_{out}}}{\sigma_{K_{in}}} = \frac{1/EC_{50}}{1/K_d} = \frac{K_d}{EC_{50}} \quad (5)$$

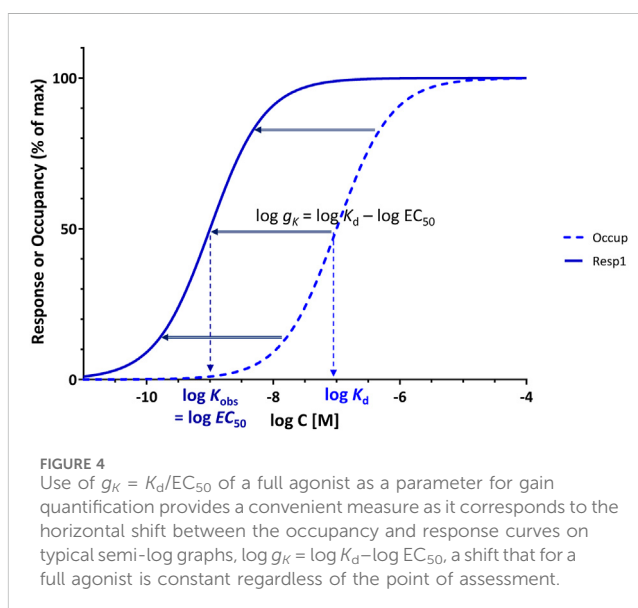
Gain quantification based on the shift in transfer functions

One can also arrive at the same by considering that, as already mentioned, the classic Clark equation (or its more general form the Hill equation) serves well as transfer function (f_{tr} , Equation 3) for most pharmacological responses (Figure 2). Thus, for normalized responses, the transfer function can be written as:

$$f_{resp}([L]) = \frac{[L]}{[L] + K} = \frac{\left(\frac{[L]}{K}\right)}{1 + \left(\frac{[L]}{K}\right)} \Rightarrow f_{tr}(x) = \frac{\left(\frac{x}{K}\right)}{1 + \left(\frac{x}{K}\right)} \quad (6)$$

Rearranging Equations 1, 2 to have a form similar to this (Equation 6), they can be written as:

$$f_{occup}([L]) = \frac{\left(\frac{[L]}{K_d}\right)}{1 + \left(\frac{[L]}{K_d}\right)} \quad (7)$$



$$f_{resp}([L]) = \frac{\left(\frac{[L]}{K_{obs}}\right)}{1 + \left(\frac{[L]}{K_{obs}}\right)}; \quad K_{obs} = EC_{50} \quad (8)$$

Comparing these, it is clear that the measured response, the “out” signal (Equation 8), follows the same pattern as the occupancy, the “in” signal (Equation 7), but with an amplified input x (assuming that the response runs “ahead” of occupancy, $K_{obs} < K_d$). The ratio of these two x s can be considered as the gain factor of the corresponding signal transduction giving the same result as Equation 5:

$$g_K = \frac{\frac{[L]}{K_{obs}}}{\frac{[L]}{K_d}} = \frac{K_d}{EC_{50}} \quad (9)$$

Not only is this definition of gain for receptor signal transduction (Equation 5 or 9) similar to that used in other fields such as electronics (Equation 4), but it also has the advantage that on the semi-log scales customarily used to plot concentration-response curves, it corresponds to the horizontal shift between $\log K_d$ and $\log K_{obs}$ ($\log EC_{50}$), so that it has an intuitive visual interpretation as well (Figure 4):

$$\log g_K = \log K_d - \log EC_{50} \quad (10)$$

Furthermore, if both concentration-dependencies follow the same hyperbolic form (sigmoid on semi-log scale), a central assumption here, the horizontal shift between occupancy and response is the same everywhere as it is at the midpoint (K_d and EC_{50}) as evident from comparing the functional forms in Equations 7, 8 (see also detailed derivation for the general case in Supplementary Information, Supplementary Appendix 1). Thus, $\log g_K$, as defined here (Equation 10) is a particularly useful concept since for full agonists, the shift along the horizontal axis on the typical semi-log graph is the same everywhere, i.e., $\log g_K$ is the separation not just at the midpoint (at K_d and EC_{50} where $f_{occup} = f_{resp} = 50\%$) but at any other arbitrary crosscut (e.g., at $f_{resp} = f_{occup} = 25\%$ or 90% ; see Supplementary Appendix 1, Supplementary Information). Note, however, that all these require full agonism, as response and occupancy need to run in parallel and both must reach 100% as maximum (Figure 4); partial agonists are discussed in the next section. Regarding this definition of gain for the presence of signal amplification (Equation 5), it should also be noted that it corresponds to what is generally considered as evidence for the existence of “*spare receptors*” (i.e., $EC_{50} < K_d$) – see discussion later. In fact, this parameter (K_d/EC_{50}) corresponds to the *pharmacological shift ratio* introduced by Macfarlane in 1982 to “denote the ratio between the concentrations of agonist giving half-maximal occupancy and half-maximal effect” (Macfarlane, 1982) that has been used in a few publications since then, e.g., (Morey et al., 1998; Zsuga et al., 2017).

Partial agonist

Partial agonists cannot produce maximal response even at full occupancy. According to the official IUPHAR definition, a partial agonist is an “agonist that in a given tissue, under specified conditions, cannot elicit as large an effect (even when applied at high concentration, so that all the receptors should be occupied) as can another agonist acting through the same receptors in the same tissue” (Neubig et al., 2003). Thus, a partial agonist can only produce a maximum response (denoted as e_{max} on a normalized scale) that is less than that of the full agonist, $e_{max} < 100\%$, even if occupancy has the same plateau of 100% receptor sites (denoted as e_{100}). Hence, to accommodate partial agonists, Equation 2 needs to be modified to allow maximum responses that are less than 100% (Buchwald, 2023):

$$f_{occup}([L]) = e_{100} \frac{[L]}{[L] + K_d}; e_{100} = 1 \quad (11)$$

$$f_{resp}([L]) = e_{max} \frac{[L]}{[L] + EC_{50}} \quad (12)$$

Note that for partial agonists, the half-maximal concentration K_{obs} is commonly denoted as EC_{50} , and it is the concentration at which half-maximal response compared to the achievable maximum is produced (i.e., $e_{max}/2$, which is less than 50%). Thus, if the partial agonist can only produce an $e_{max} = 60\%$ (compared to 100% for the full agonist), then its EC_{50} is at the concentration where it produces 30% response ($e_{max}/2$) and not where it produces 50% response (see, e.g., Figure 5B for an illustration). The ratio of K_d and $K_{obs} = EC_{50}$ will be denoted as κ for the general case (as it has been done before (Buchwald, 2023)):

$$\kappa = \frac{K_d}{K_{obs}} \quad (13)$$

For partial agonists, κ will in general be smaller than that of the full agonist, which corresponds to the gain parameter for this response, $\kappa < \kappa_{full\ agon} = g_K$, and it can be used to obtain an estimate of the relative efficacy. As shown before (Buchwald, 2022), for typical hyperbolic responses (sigmoid on semi-log scale), relative ligand efficacies can be compared using the $E_{max} \cdot K_d/EC_{50}$ ratios:

$$\frac{\varepsilon_2}{\varepsilon_1} = \frac{E_{max,2} \frac{K_{d,2}}{EC_{50,2}}}{E_{max,1} \frac{K_{d,1}}{EC_{50,1}}} \quad (14)$$

This formula was derived earlier for sigmoid responses from the assumption that at conditions that produce equal responses at low enough concentrations, the ratio of efficacies is the reverse of the ratio of occupied receptors producing it; see (Buchwald, 2022) for details. Use of the same formula to compare relative efficacies ($E_{max} \cdot K_d/EC_{50}$, Equation 14) has been also suggested by others based on different considerations (Ehlert et al., 1999; Trzeciakowski, 1999; Strange, 2008). Introducing κ and assuming normalized responses (with e_{max} maxima), Equation 14 with the present notation becomes:

$$\frac{\varepsilon_2}{\varepsilon_1} = \frac{e_{max,2} \cdot \kappa_2}{e_{max,1} \cdot \kappa_1} \quad (15)$$

Thus, relative efficacies can be estimated by comparing $e_{max} \cdot \kappa$ products (Equation 15). Consequently, for a partial agonist, its relative efficacy compared to the full agonist that produces 100% maximum response (and has an efficacy of one) can be obtained as:

$$\varepsilon_{rel} = e_{max} \frac{\kappa}{\kappa_{full\ agon}} = e_{max} \frac{\kappa}{g_K} \quad (16)$$

Finally, in addition to looking at responses as a function of ligand concentration, i.e., concentration-response curves, $f_{resp} = f([L])$, it is also informative to look at them as a function of occupancy as well, $f_{resp} = f(f_{occup})$, especially in the present context of connecting receptor occupancy and response. Accordingly, for all examples below, a response versus occupancy graph will also be included for illustration. It has been shown before that if both occupancy and response follow hyperbolic relationships, as assumed here, fractional response (f_{resp}) is a hyperbolic function

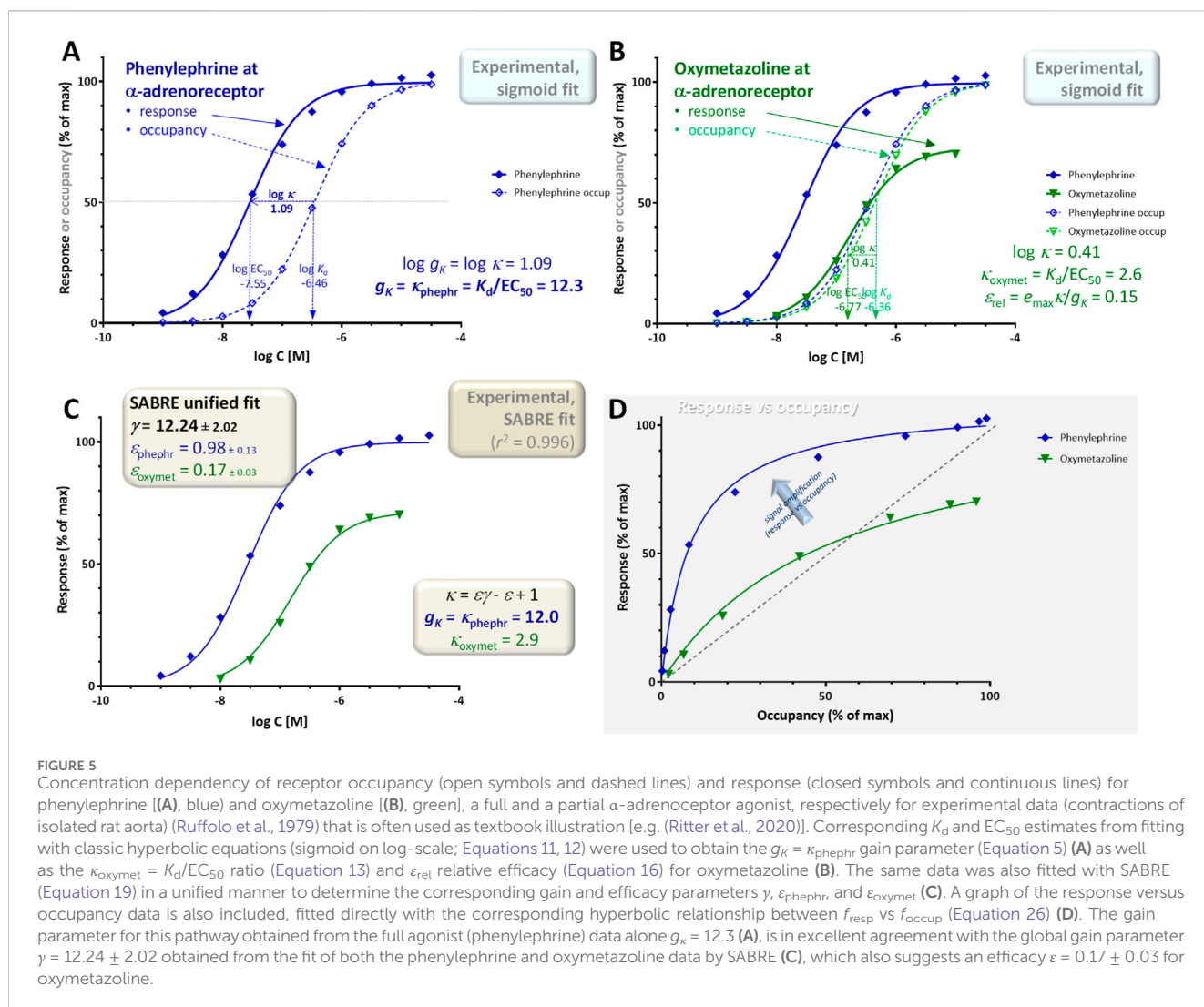


FIGURE 5

Concentration dependency of receptor occupancy (open symbols and dashed lines) and response (closed symbols and continuous lines) for phenylephrine (A), blue and oxymetazoline (B), green, a full and a partial α -adrenoreceptor agonist, respectively for experimental data (contractions of isolated rat aorta) (Ruffolo et al., 1979) that is often used as textbook illustration [e.g. (Ritter et al., 2020)]. Corresponding K_d and EC_{50} estimates from fitting with classic hyperbolic equations (sigmoid on log-scale; Equations 11, 12) were used to obtain the $g_K = \kappa_{\text{phepr}}$ gain parameter (Equation 5) (A) as well as the $\kappa_{\text{oxymet}} = K_d/EC_{50}$ ratio (Equation 13) and ε_{rel} relative efficacy (Equation 16) for oxymetazoline (B). The same data was also fitted with SABRE (Equation 19) in a unified manner to determine the corresponding gain and efficacy parameters γ , $\varepsilon_{\text{phepr}}$, and $\varepsilon_{\text{oxymet}}$ (C). A graph of the response versus occupancy data is also included, fitted directly with the corresponding hyperbolic relationship between f_{resp} vs f_{occup} (Equation 26) (D). The gain parameter for this pathway obtained from the full agonist (phenylephrine) data alone $g_K = 12.3$ (A), is in excellent agreement with the global gain parameter $\gamma = 12.24 \pm 2.02$ obtained from the fit of both the phenylephrine and oxymetazoline data by SABRE (C), which also suggests an efficacy $\varepsilon = 0.17 \pm 0.03$ for oxymetazoline.

of occupancy (f_{occup}) even for partial agonists that can only produce a maximum response of $e_{\text{max}} < 100\%$ (Buchwald, 2023):

$$f_{\text{resp}} = e_{\text{max}} \frac{\kappa}{(\kappa - 1)} \frac{f_{\text{occup}}}{f_{\text{occup}} + \frac{e_{100}}{\kappa - 1}} \quad (17)$$

Gain quantification using the SABRE receptor model

The gain quantification method discussed so far relies entirely on parameters derived from fitting the experimental data with standard concentration-response curves (K_d , EC_{50}) and the gain parameter g_K derived from them (Equation 5). Thus, it only relies on the assumption that both response and occupancy follow classic hyperbolic concentration dependencies (sigmoid on the commonly used semi-log scale) characterizable by the corresponding half-maximal concentrations values, K_d and EC_{50} , respectively (Equations 11, 12) and that they were determined for a true full agonist.

Gain quantification of pharmacological signaling can also be done in a different, model-based approach using the recently introduced SABRE model (Signal Amplification, Binding affinity, and Receptor-activation Efficacy) – the first quantitative receptor model that explicitly includes parametrization for signal amplification (Buchwald, 2019; Buchwald, 2020; Buchwald, 2023). SABRE, in its full general form (Equation 18), employs a total of five parameters to cover the full spectrum of parameters listed earlier in the Introduction – K_d for binding affinity, ε for efficacy, ε_{R0} for the efficacy of constitutive activity, γ for the gain of signal amplification, and n for Hill coefficient (for details, see (Buchwald, 2019; Buchwald, 2020; Buchwald, 2023)):

$$E/E_{\text{max}} = \frac{\varepsilon \gamma [L]^n + \varepsilon_{R0} \gamma K_d^n}{(\varepsilon \gamma - \varepsilon + 1) [L]^n + (\varepsilon_{R0} \gamma - \varepsilon_{R0} + 1) K_d^n} \quad (18)$$

Here, only the simplified three-parameter version of SABRE will be used, which assumes that there is no constitutive activity ($\varepsilon_{R0} = 0$) and the regular law of mass action holds (Hill slope $n = 1$), but allows partial agonism (ε) and signal amplification (γ):

$$E/E_{\max} = f_{\text{resp}} = \frac{\varepsilon\gamma[L]}{(\varepsilon\gamma - \varepsilon + 1)[L] + K_d} = \frac{\varepsilon\gamma}{\varepsilon\gamma - \varepsilon + 1} \frac{[L]}{[L] + \frac{K_d}{\varepsilon\gamma - \varepsilon + 1}} \quad (19)$$

Comparing this equation (Equation 19) in its the rearranged form on the right side with Equation 12 describing the typical concentration-response curve, makes it clear that the assumptions of SABRE also result in a classic hyperbolic (sigmoid on the semi-log scale) relationship between (fractional) response, $E/E_{\max}$, and ligand concentration, $[L]$, with apparent EC_{50} (K_{obs}) and $e_{\max}$ ($0 < e_{\max} \leq 100\%$) values that are:

$$K_{\text{obs}} (= EC_{50}) = \frac{K_d}{\varepsilon\gamma - \varepsilon + 1} \quad (20)$$

$$e_{\max} = \frac{\varepsilon\gamma}{\varepsilon\gamma - \varepsilon + 1} \quad (21)$$

Accordingly, the κ ratio of K_d/K_{obs} for a given agonist (Equation 13), can be expressed in terms of SABRE parameters using Equation 20 as:

$$\kappa = \frac{K_d}{K_{\text{obs}}} = \varepsilon\gamma - \varepsilon + 1 \quad (22)$$

Notably, considering that for a full agonist ($\varepsilon = 1$), this κ ratio equals the gain parameter, $g_K = \kappa$, it becomes obvious that g_K corresponds exactly to the gain parameter γ of SABRE:

$$\varepsilon = 1 \Rightarrow g_K = \kappa_{\text{full agon}} = \gamma \quad (23)$$

This is particularly encouraging, as it shows that the gain parameter (g_K) obtained from concentration-response based considerations that led to Equations 5, 9 corresponds to the gain parameter of SABRE (γ), which, however, was introduced based on different considerations (i.e., $\gamma = [R_{\text{tot}}]/K_y$ to extend the range of the input of the hyperbolic response function linking the concentration of active receptors to response; see (Buchwald, 2019)). Accordingly, if data obtained with multiple agonists can be fitted adequately within the unified framework of SABRE (i.e., response data are adequately fitted while using the experimental K_d values as affinity parameters in SABRE, Equation 19), then the γ parameter of SABRE can provide a more reliable gain estimate than the g_K value obtained from the full agonist data alone—several illustrative examples are provided below.

Furthermore, fit with SABRE also provides direct estimates of ligand efficacies, ε , for all agonists with response data included. In fact, if its assumptions hold, the relative efficacy of partial agonists derived earlier for hyperbolic responses (Equation 16) yields exactly the ε of SABRE using substitutions from Equations. 21–23 as shown below (Equation 24):

$$\varepsilon_{\text{rel}} = e_{\max} \frac{\kappa}{g_K} = \frac{\varepsilon\gamma}{\varepsilon\gamma - \varepsilon + 1} \frac{\varepsilon\gamma - \varepsilon + 1}{\gamma} = \varepsilon \quad (24)$$

On the other hand, Equation 22 also provides a different formula (Equation 25) to estimate ε_{rel} as long as the assumptions of SABRE are valid. Expressing ε as ε_{rel} of a partial agonist from Equation 22 (and using Equation 23 to replace γ with g_K):

$$\varepsilon_{\text{rel}} = \frac{\kappa - 1}{\gamma - 1} = \frac{\kappa - 1}{g_K - 1} \quad (25)$$

Finally, within the formalism of SABRE, the response versus occupancy relationship of Equation 17 can be written as:

$$\begin{aligned} f_{\text{resp}} &= e_{\max} \frac{\kappa}{(\kappa - 1) f_{\text{occup}} + \frac{e_{100}}{\kappa - 1}} = \frac{\varepsilon\gamma}{(\varepsilon\gamma - \varepsilon + 1)} \frac{\varepsilon\gamma - \varepsilon + 1}{\varepsilon\gamma - \varepsilon} \frac{f_{\text{occup}}}{f_{\text{occup}} + \frac{1}{\varepsilon\gamma - \varepsilon}} \\ &= \frac{\gamma}{\gamma - 1} \frac{f_{\text{occup}}}{f_{\text{occup}} + \frac{1}{\varepsilon(\gamma - 1)}} \end{aligned} \quad (26)$$

In the examples included in Results, this was used to fit the corresponding response versus occupancy curves.

Data and model fitting

Experimental data and corresponding K_d and EC_{50} values used here are from published works as referenced for each case; response data values used for model fittings were obtained from the figures using WebPlotDigitizer (Rohatgi, 2022). All data used here were normalized to be in the 0%–100% range and fitted using GraphPad Prism (GraphPad, La Jolla, CA, USA, RRID:SCR_002798). Fittings with SABRE were done with a custom implementation corresponding to the general Equation 19 (available for download, see (Buchwald, 2020)), and with parameters constrained as indicated for each case. Response versus occupancy data were fitted with a custom GraphPad model corresponding to Equation 26.

Illustrative examples—results and discussion

A number of illustrative examples from published data involving both full and partial agonists acting on various receptors are provided to illustrate the gain quantification process described above. There is only relatively limited data where both receptor binding (occupancy) and response were measured in parallel in the same system as needed here; nevertheless, the examples below should be sufficient to support the concept of signal amplification at pharmacological receptors and the advantages of using $g_K = K_d/EC_{50}$ as a gain parameter for its quantification.

Example 1: single receptor (α -adrenergic), pathway, and readout (rat aorta contraction) with multiple agonists

A first illustration is provided with data that is frequently used as textbook illustration of the possible complex relationship between receptor occupancy and response (for example, in Rang and Dale's *Pharmacology* (Ritter et al., 2020)): the concentration-dependent contractions of isolated rat aorta induced by imidazoline-type α -adrenoceptor agonists including phenylephrine, oxymetazoline, and others (Ruffolo et al., 1979). Contractions of isolated rat aortic strips were measured as response using isometric transducers, and receptor binding affinities (dissociation constants, K_d s) were assessed separately by two different methods using Furchgott-type (Furchgott and Burszty, 1967) and Schild-plot based methods (Arunlakshana and Schild, 1959), respectively (Ruffolo et al., 1979); the average of these two affinity estimates were used

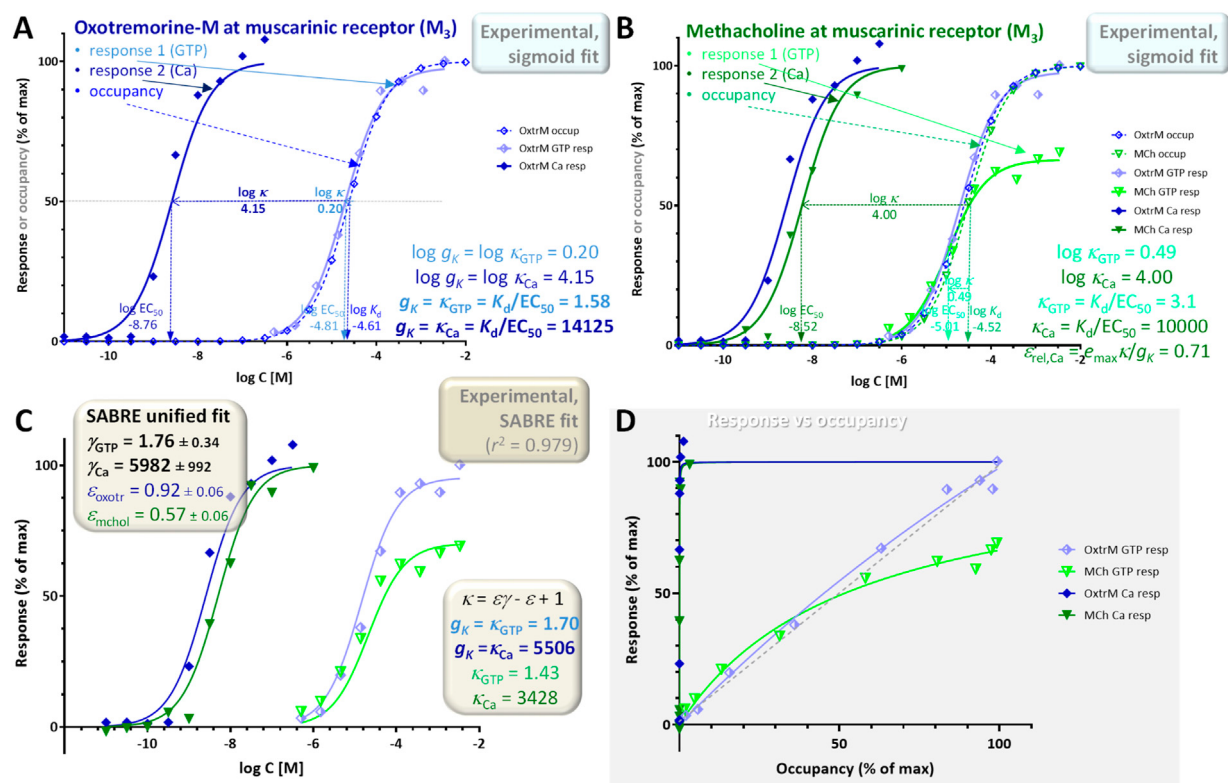


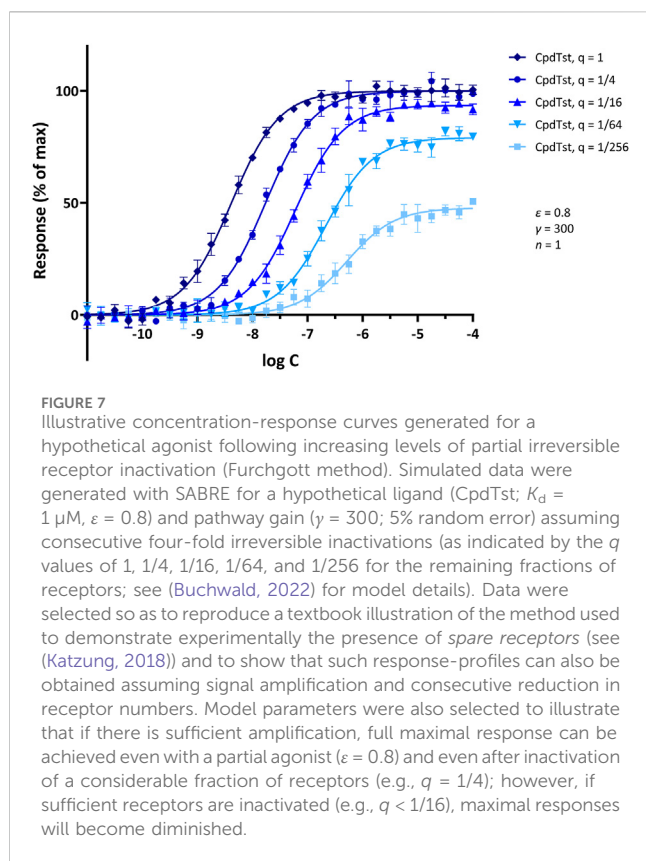
FIGURE 6 Concentration dependency of receptor occupancy (open symbols and dashed lines) and two different responses (stimulation of GTP binding to G_a subunits and subsequent increase in intracellular Ca levels after M_3 receptor activation; lighter half-closed and darker closed symbols, respectively with continuous lines) for the muscarinic agonists oxotremorine-M [(A), blue] and methacholine [(B), green]. Experimental data (Sykes et al., 2009) and the corresponding K_d and EC_{50} estimates from fitting with classic hyperbolic equations (sigmoid on log-scale; Equations 11, 12) were used to obtain the two different g_K gain parameter (Equation 5) (A) and κ values (Equation 13) (B). Fit of the full agonist (oxotremorine-M) data alone indicates gains g_K of 1.6 and ~14,000 for GTP and Ca, respectively (A). As in Figure 5, the data was also fitted with SABRE (Equation 19) in a unified manner to determine the corresponding gain (γ_{GTP} , γ_{Ca}) and efficacy parameters (ϵ_{oxotr} , ϵ_{mchol}) (C). Values obtained this way for the gain parameters (C) are in general agreement with those from the sigmoid fit (A); they also suggest an efficacy $\epsilon = 0.57 \pm 0.06$ for methacholine. A graph of the response versus occupancy data is also included, fitted directly with the corresponding hyperbolic relationship between f_{resp} vs f_{occup} (Equation 26) (D).

here. From the whole dataset obtained originally with ten compounds (Ruffolo et al., 1979), here, only the data of phenylephrine as full agonist and oxymetazoline as representative partial agonist are used to avoid overcrowding the figures (Figure 5). Experimental data obtained with the full agonist phenylephrine (log $K_d = -6.46$, log $EC_{50} = -7.55$), indicate a shift between the semi-log curves of response and occupancy of log $\kappa = \log K_d - \log EC_{50} = 1.09$; thus, a corresponding gain parameter for this readout that is $g_K = \kappa_{full\ agonist} = K_d/EC_{50} = 12.3$ (Figure 5A). The shift between the response and occupancy curves for the partial agonist is smaller; here, log $\kappa = 0.41$ (green in Figure 5B with log $K_d = -6.36$, log $EC_{50} = -6.77$), thus $\kappa = K_d/EC_{50} = 2.6$ for oxymetazoline, as the response it generates is running less “ahead” of occupancy than for the full agonist (is less left-shifted) as clearly noticeable in Figure 5D. In fact, oxymetazoline illustrates nicely one of the confusing cases when comparing (fractional) response and occupancy for a partial agonist acting on a pathway with amplification as its response actually runs both “ahead” and “behind” the occupancy: $f_{resp} > f_{occup}$ until about 60% occupancy ($f_{occup} < 0.6$), but then reverses and $f_{resp} < f_{occup}$ when $f_{occup} > 0.6$ (Figure 5D). According to this data, using Equation 16, the relative efficacy of oxymetazoline compared to phenylephrine is $\epsilon_{rel} = 0.73 \times 2.6/12.3 = 0.15$ (Figure 5B).

These estimates (signal transduction gain $g_K = 12.3$ and relative efficacy of oxymetazoline $\epsilon_{rel} = 0.15$) are solely based on fitting of the experimental data with individual sigmoid response curves and the corresponding K_d and EC_{50} values. As the data in its entirety can be fitted with SABRE as a single, unified model (see (Buchwald, 2019) for a detailed fit including for multiple partial agonists), estimates can also be obtained from fit of the entire data with a single set of model parameters. Overall, SABRE (Equation 19) fits the data very well, accounting for more than 99% of the variability ($r^2 = 0.996$; Figure 5C). Unified fitting of the entire dataset results in a gain parameter, $\gamma = 12.24 \pm 2.02$, and an efficacy for oxymetazoline, $\epsilon = 0.17 \pm 0.03$, that are both in excellent agreement with the estimates obtained simply from the experimental K_d and EC_{50} values using Equations 5, 16, respectively indicating that very consistent estimates can be obtained for this data.

Example 2: single receptor (M_3 muscarinic) and pathway with multiple readouts (G_a -GTP binding and intracellular Ca increase)

A second illustration is provided with a dataset involving responses by the M_3 muscarinic receptor elicited by agonists



including oxotremorine-M and methacholine (Sykes et al., 2009). It is included as an illustration for a case where two different responses are measured at consecutive vantage points downstream on the same pathway: here, the stimulation of GTP binding to G_α and the subsequent increase in intracellular calcium, Ca (Figure 6; shown as lighter half-closed and darker closed symbols, respectively). GTP binding assays were performed using [^{35}S]GTP γS in 96-well optiplates, agonist-induced changes in Ca^{2+} concentration were measured using a fluorometric imaging plate reader, and binding affinity estimates (K) were obtained from equilibrium competition experiments with N -methyl- [^3H]scopolamine (following Cheng-Prusoff corrections (Cheng and Prusoff, 1973)) (Sykes et al., 2009). As immediately evident from a quick comparison of the $\log K_d$ and $\log \text{EC}_{50}$ values in Figure 6A, the amplifications of the two responses assessed here are very different with that of the GTP binding being close to unity ($\log \kappa_{\text{GTP}} = 0.20$; $g_{K,\text{GTP}} = \kappa_{\text{GTP,full agon}} = 1.6$) and that of the Ca increase being very large, around four orders of magnitude ($\log \kappa_{\text{Ca}} = 4.15$; $g_{K,\text{Ca}} = \kappa_{\text{Ca,full agon}} \approx 14,000$). Such a large discrepancy makes it difficult to obtain well-defined fittings and parameter estimates, but the partial agonist character of methacholine is clearly observable in the GTP response ($e_{\text{max}} = 0.66$) and the decreased shift in the Ca response ($e_{\text{rel,Ca}} = 0.71$) (Figure 6B).

For the same reason, fit of the entire dataset with SABRE (Equation 19) as a single model is particularly challenging; nevertheless, it still accounts for most of the variability ($r^2 = 0.979$; Figure 6C) suggesting gain (amplification) parameters ($\gamma_{\text{GTP}} = 1.76 \pm 0.34$, $\gamma_{\text{Ca}} = 5982 \pm 992$) and an efficacy for the partial agonist methacholine ($\epsilon = 0.57 \pm 0.06$) in reasonable

agreement with those from the previous sigmoid-based estimates. Due to the strong amplification in the Ca responses, the corresponding response versus occupancy curve is strongly distorted as even minimal occupancy already results in essentially maximum response (Figure 6D). Nevertheless, these data still provide an illustration of a case with two different responses measured along the same downstream pathway with two different amplifications corresponding to the two different assessment points. It also highlights an issue that often causes confusion: partial agonists are typically recognized as not being able to elicit maximum responses; however, in pathways with strong amplification, even relatively weak partial agonists can cause full responses as nicely evidenced here by the Ca response of methacholine (versus the corresponding GTP response; closed vs half-closed green symbols in Figure 6). A more detailed illustration of the effect of intermixing the effect of partial agonism and different amplification/receptor levels is shown in Figure 7 and discussed below.

Example 3: single receptor (muscarinic), pathway, and readout (adenylate cyclase, rabbit myocardium) with multiple levels of partial irreversible inactivation (furchgott method)

The third illustration is for a set of Furchgott type experiments that allow the quantification of receptor binding affinity by comparing concentration-response curves obtained at different receptor levels, e.g., following partial irreversible inactivation. One advantage of such experiments is that they require the measurement of response data only and use that to estimate binding affinity; thus, they avoid the need of having to set up separate ligand binding experiments (Furchgott and Bursztyn, 1967; Buchwald, 2022). A set of illustrative concentration-response curves obtained from simulations of such an experiment assuming increasing levels of partial irreversible receptor inactivation is shown in Figure 7. Simulation parameters were selected so as to reproduce textbook illustrations of the Furchgott method used to demonstrate experimentally the presence of *spare receptors* (e.g., (Katzung, 2018)). The data from such multiple concentration-response curves can be used to estimate both the K_d of the ligand and the fraction of remaining receptors after each inactivation (q) (Buchwald, 2022). Thus, such Furchgott-type approaches are particularly well-suited for quantitative pharmacology characterization as they allow the concurrent estimation of the binding affinity and relative efficacy of the ligand as well as the characteristics of the pathway as long as multiple concentration-response curves can be obtained at different levels of receptor levels (Buchwald, 2022) either via the classic method of partial irreversible receptor inactivation as introduced by Furchgott (Furchgott, 1966; Furchgott and Bursztyn, 1967) or via different levels of receptor expression, which are now possible (see, e.g., (Jakubik et al., 2019), for a recent implementation).

The experimental data used for illustration here were all also obtained using muscarinic receptors and oxotremorine-M as full agonist as in example 2 but involve muscarinic receptor-mediated

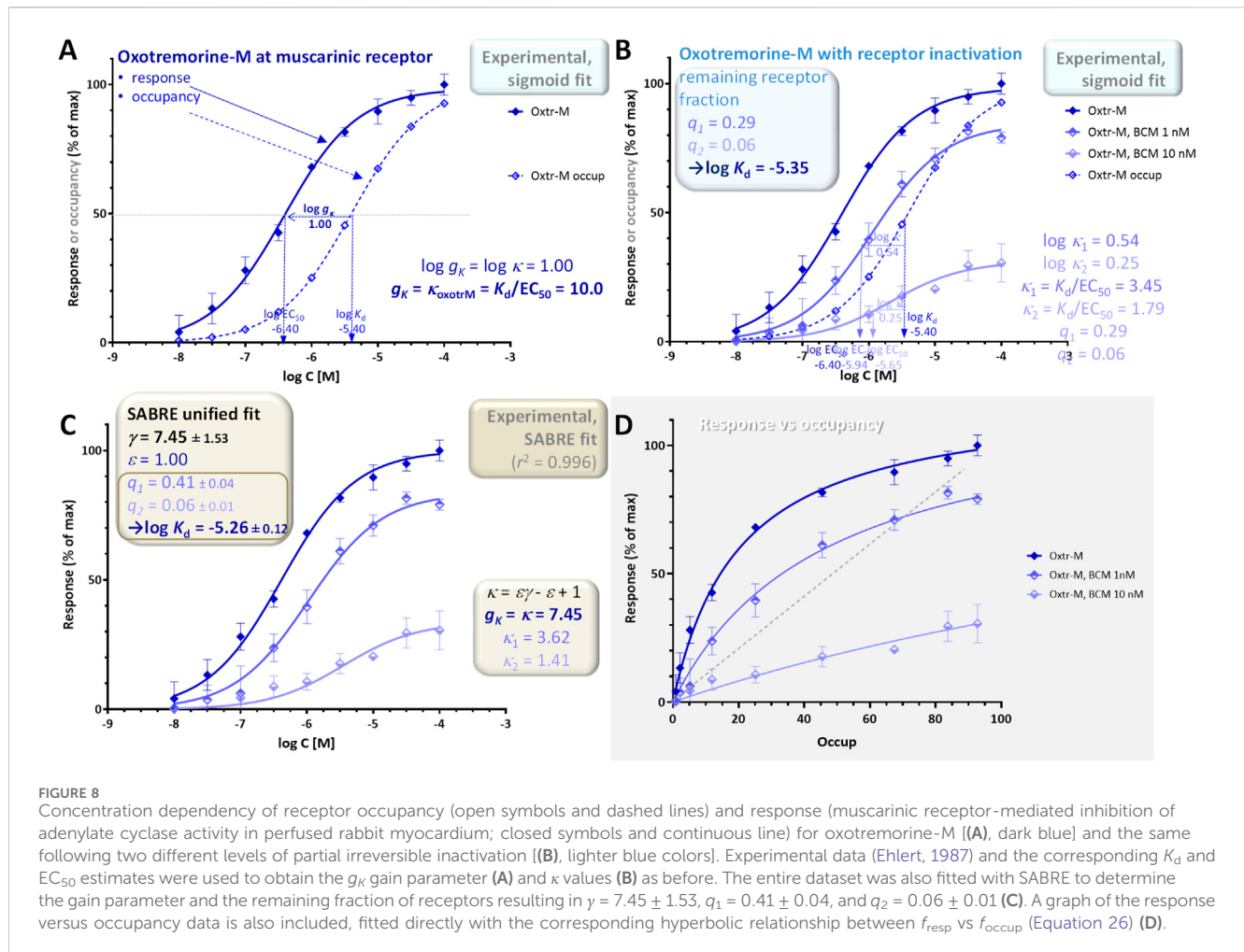


FIGURE 8

Concentration dependency of receptor occupancy (open symbols and dashed lines) and response (muscarinic receptor-mediated inhibition of adenylate cyclase activity in perfused rabbit myocardium; closed symbols and continuous line) for oxotremorine-M [(A), dark blue] and the same following two different levels of partial irreversible inactivation [(B), lighter blue colors]. Experimental data (Ehlert, 1987) and the corresponding K_d and EC_{50} estimates were used to obtain the g_K gain parameter (A) and κ values (B) as before. The entire dataset was also fitted with SABRE to determine the gain parameter and the remaining fraction of receptors resulting in $\gamma = 7.45 \pm 1.53$, $q_1 = 0.41 \pm 0.04$, and $q_2 = 0.06 \pm 0.01$ (C). A graph of the response versus occupancy data is also included, fitted directly with the corresponding hyperbolic relationship between f_{resp} vs f_{occup} (Equation 26) (D).

inhibition of adenylate cyclase activity as response (Figure 8). They were obtained in perfused rabbit myocardium homogenates following different levels of partial inactivation with an irreversible muscarinic antagonist (benzilylcholine mustard, BCM) (Ehlert, 1987). Responses obtained with the full agonist (oxotremorine-M) and no inactivation give a shift between the response and occupancy curves of $\log \kappa = 1.00$ corresponding to a gain of $g_K = \kappa_{\text{full agon}} = K_d/EC_{50} = 10.0$ ($\log K_d = -5.40$, $\log EC_{50} = -6.40$; Figure 8A). Following partial inactivations, the shifts become smaller: 0.54 and 0.25 for the two different levels used here (BCM at 1 and 10 nM for 15 min (Ehlert, 1987); Figure 8B). The fit of these curves with individual sigmoid curves suggest a $\log K_d$ of -5.35 for oxotremorine-M (in excellent agreement with the value measured by a competition assay, -5.40) as well as remaining fractions of receptors of $q_1 = 0.29$ and $q_2 = 0.06$, respectively (Figure 8B; see also Supplementary Table S4A in (Buchwald, 2022)). The response versus occupancy graph (Figure 8D) nicely shows the effect of these inactivations and corresponding irreversible reductions in receptor levels on the fractional responses achievable at various occupancy levels.

As in the previous examples, the entire data can also be fitted with SABRE using a single set of parameters to obtain unified model-based estimates. For this data, SABRE gives excellent overall fit ($r^2 = 0.996$; Figure 8C), and the unified fitting of all

three curves result in a gain parameter of $\gamma = 7.45 \pm 1.53$ for this response and $\log K_d = -5.26 \pm 0.12$ for oxotremorine-M—in good agreement with the previous sigmoid fit based estimates as well as the measured value of $\log K_d$. With SABRE, the inactivation-caused fold decreases in receptor level show up as apparent fold reduction in efficacy ($\epsilon' = q\epsilon$; see (Buchwald, 2022) for details); the corresponding values obtained here are $q_1 = 0.41 \pm 0.04$ and $q_2 = 0.06 \pm 0.01$, which are again consistent with the sigmoid-based estimates.

Example 4: single receptor (AT1R angiotensin), two different pathways and readouts (G $_q$ -mediated inositol monophosphate increase and β -arrestin2 endocytosis) with balanced and biased agonists

The fourth illustration involves two different pathways originating from the same receptor, the angiotensin II receptor 1 (AT1R), but mediated by a G-protein and β -arrestin, respectively. Signal amplification can be different along such divergent pathways, so that even if the activation signal is the same, responses can be different—this is sometimes designated as “system bias”. It is also possible that, even if these pathways originate from the same

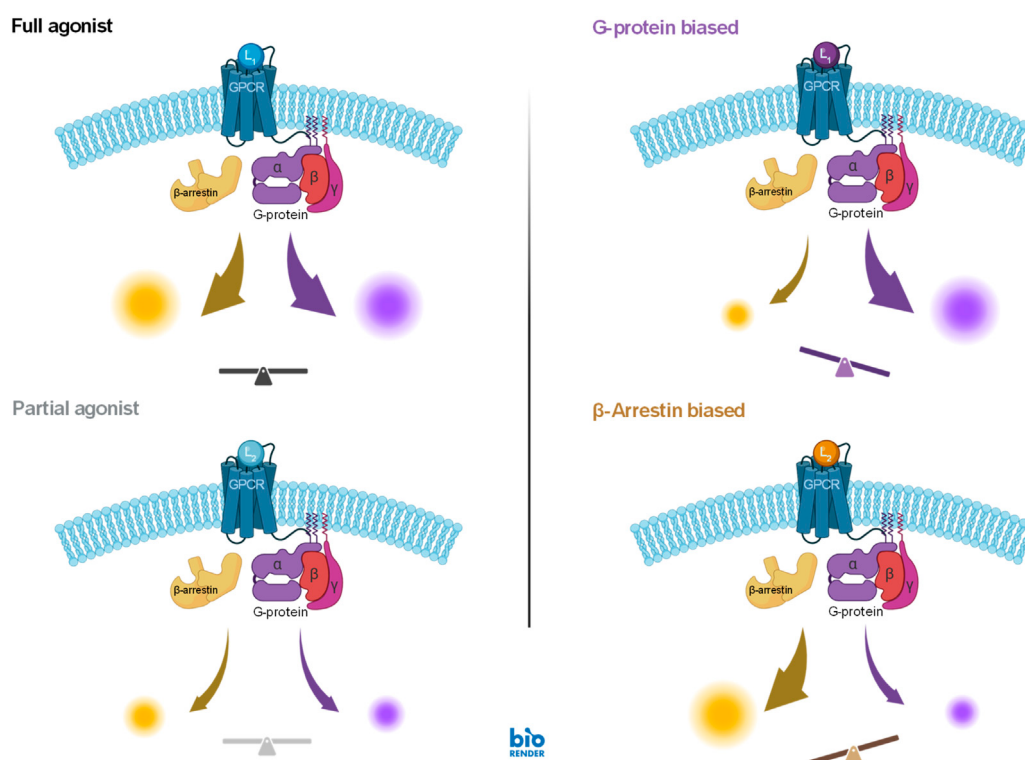


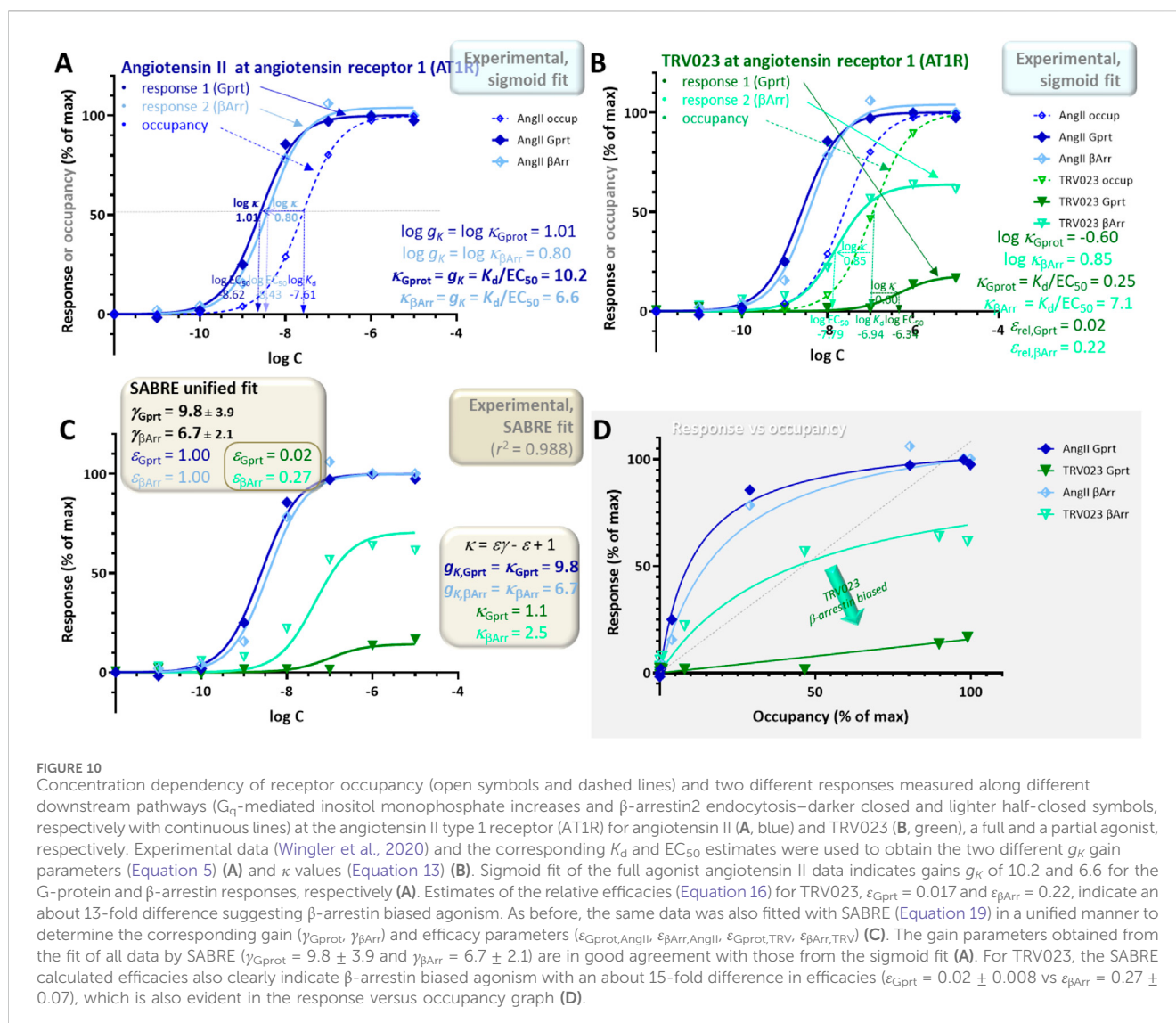
FIGURE 9
Illustration of the concept of biased agonism, which can achieve different activations along different pathways even if they originate from the same receptor (right column), compared to that of classic full and partial agonism, which activate all downstream pathway to the same full or partial degree (left column). A case of a G-protein coupled receptor (GPCR) is shown here with downstream signaling along a G-protein and a β -arrestin modulated pathway (figure created in BioRender). For the heterotrimeric G proteins, the $G\alpha$ and $G\beta\gamma$ subunits can each mediate distinct intracellular signaling, they are not shown separately here.

receptor, ligands can activate them differently—a phenomenon termed as biased agonism (functional selectivity) (Figure 9) (Kenakin and Christopoulos, 2013; Smith et al., 2018; Wooten et al., 2018; Ehlert, 2018; Kenakin, 2019; Kolb et al., 2022). For biased agonism to exist, there must be different active states of the receptor that can preferentially initiate either one or the other downstream signal, and there must be agonists that can differentially stabilize these active states. Biased agonism is of considerable interest as it might allow improved therapeutic action by separating the desired activity from the unwanted side effects that are mediated by separate pathways, which is not possible with classical full or partial agonists (Figure 9). Biased agonism is, however, difficult to quantify (Onaran et al., 2017; Michel and Charlton, 2018; Kenakin, 2018). For example, it is possible that even oliceridine, which was developed as a μ -opioid receptor (MOPr) biased agonist (Wadman, 2017) and is being often touted to illustrate the clinical promise of biased agonists since its approval by the FDA (Olinvyk, 2020), is not a biased agonist but a regular weak agonist acting on one amplified and one unamplified or possibly attenuated pathway (Buchwald, 2023; Gillis et al., 2020).

Experimental data used for this example are for two responses, G_q -mediated inositol monophosphate increase and β -arrestin2 endocytosis, generated by angiotensin II and TRV023 as agonists of AT1R (Figure 10) (Wingler et al., 2020). Responses were measured using the IP-One G_q kit from Cisbio and the PathHunter assay from DiscoverX, respectively, while binding

affinities (K_d values) were determined in equilibrium competition radioligand binding assays with [3 H]-olmesartan (Wingler et al., 2020). Fit of the sigmoid responses for the full agonist angiotensin II indicate gains $g_K = K_{full\ agonist}$ of 10.2 and 6.6 for the G-protein and β -arrestin responses, respectively (Figure 10A). The same $\kappa = K_d/EC_{50}$ ratios for the partial agonist TRV023 are 0.25 and 7.1, respectively indicating a notably weaker G-protein response (Figure 10B). Accordingly, biased agonism for TRV023 is clearly evident in the response versus occupancy graph, where the G-protein response significantly deviates from the β -arrestin one for TRV023, whereas it does not for angiotensin II (Figure 10D). In agreement with this, the relative efficacies for TRV023 (Equation 16) for the two pathways, $\epsilon_{Gprt} = 0.0017$ and $\epsilon_{\beta Arr} = 0.22$ indicate an approximately 13-fold difference.

Such multi-pathway responses can also be fitted within the unified framework of SABRE using a single gain parameter γ_{Pi} for each pathway (P_i) and a single experimental K_d but different pathway-dependent efficacies $\epsilon_{Pi,Lj}$ for each ligand (L_j) (Buchwald, 2022; Buchwald, 2019). Such unified fit of the present data with this six-parameter model ($\gamma_{Gprt}, \gamma_{\beta Arr}, \epsilon_{Gprt,Ang}, \epsilon_{\beta Arr,Ang}, \epsilon_{Gprt,TRV}, \epsilon_{\beta Arr,TRV}$) gives good fit ($r^2 = 0.988$; Figure 10C), and the gain parameters obtained from the fit of all data with SABRE ($\gamma_{Gprt} = 9.8 \pm 3.9$ and $\gamma_{\beta Arr} = 6.7 \pm 2.1$) are in general agreement with the g_K pathway amplifications obtained from the K_d/EC_{50} ratios of the full agonist angiotensin II (Figure 10). For TRV023, the SABRE calculated efficacies indicate clear β -arrestin biased agonism with



an about 15-fold different in efficacies: $\epsilon_{Gpr, TRV} = 0.02 \pm 0.008$ vs $\epsilon_{\beta Arr, TRV} = 0.27 \pm 0.07$.

Example 5: single receptor (μ -opioid), two different pathways and readouts (G_{ai2} activation and β -arrestin2 recruitment) with both left- and right-shifted responses

A fifth example included here also involves G-protein and β -arrestin mediated diverging pathways, but this time with responses initiated at the μ -opioid receptor (MOPr) by DAMGO (D-Ala², N-MePhe⁴, Gly-ol⁵-enkephalin) and morphine as full and partial agonists, respectively (Figure 11). It is included to illustrate the unusual case where response curves are right- and not left-shifted compared to occupancy (meaning $\kappa = K_d/EC_{50} < 1$). In the present context, this indicates not signal amplification, but apparent signal attenuation/dampening or loss ($g_K < 1$) (Buchwald, 2023). Experimental data were obtained in HEK293A cells using BRET assays to measure G_{ai2} activation as well as β -arrestin2 recruitment

(Pedersen et al., 2019). Binding measurements were done with [³H] naloxone, and equilibrium dissociation constants, K_d , were calculated using the Cheng-Prusoff equation (Cheng and Prusoff, 1973) to account for radioligand concentration (Pedersen et al., 2019). Notably, while both responses follow classic hyperbolic shapes, and the G-protein mediated responses are left-shifted as typical for signal amplification cases as discussed here, the β -arrestin responses are clearly right-shifted compared to occupancy despite originating from the very same receptor (Figure 11). This is evident in the classic concentration-response curves (Figure 11A, B) as well as in the response versus occupancy graph, where they clearly have a different curvature (Figure 11D). The β -arrestin response is clearly lagging the occupancy even for the full agonist (DAMGO) while the G-protein response is ahead (dark vs light blue curves). For example, at 25% receptor occupancy, the G-protein response is already plateauing as it is approaching its maximum, whereas the β -arrestin response is minimal and still barely separated from baseline ($f_{occup} = 25\% \rightarrow f_{resp, Gpr} > 80\%$, $f_{resp, \beta Arr} < 5\%$ for DAMGO in Figure 11D). Thus, for these MOPr responses, $EC_{50, Gpr} < K_d < EC_{50, \beta Arr}$, so that the G-protein responses are

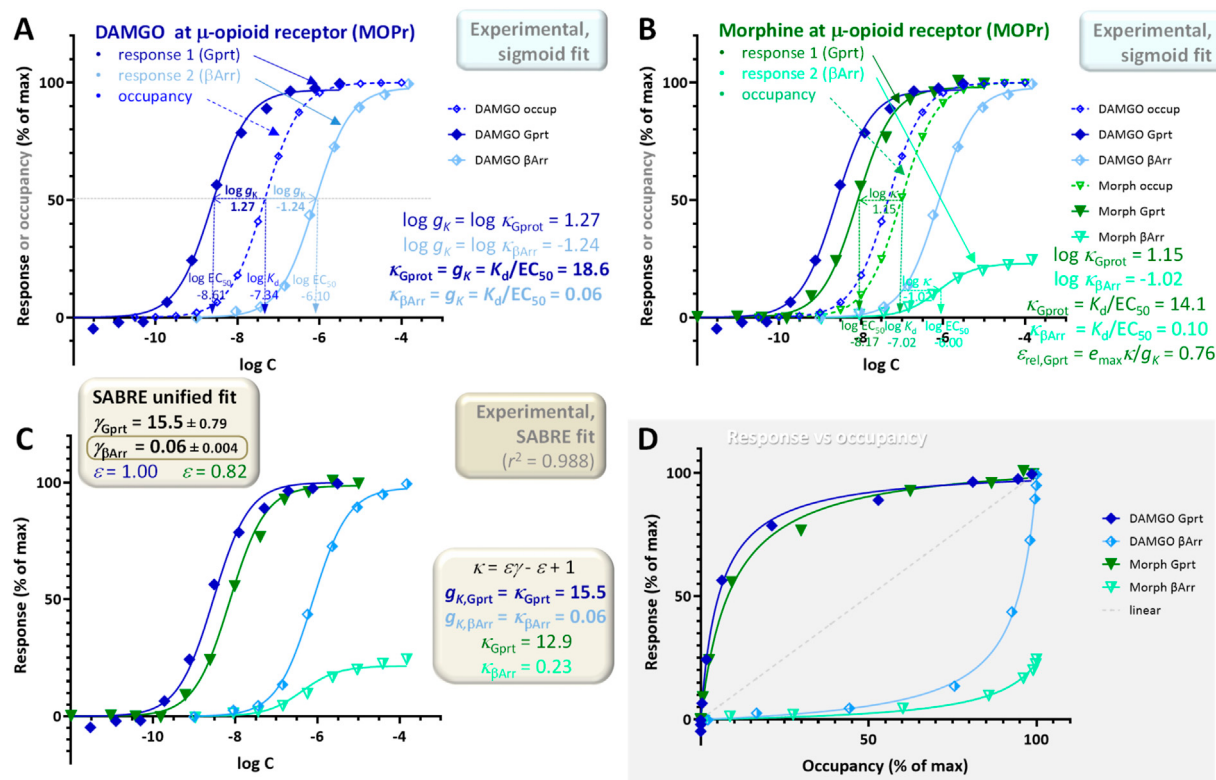


FIGURE 11
 Concentration dependency of receptor occupancy (open symbols and dashed lines) and two different responses measured along different downstream pathways (G_{ai2} activation as well as β -arrestin2 recruitment—darker closed and lighter half-closed symbols, respectively with continuous lines) at the μ -opioid receptor (MOPr) for DAMGO [(A), blue] and morphine [(B), green]. Experimental data (Pedersen et al., 2019) and the corresponding K_d and EC_{50} estimates were used to obtain the two different g_K gain parameters (Equation 5) (A) and κ values (Equation 13) (B). Note that one response is left- and one is right-shifted compared to the occupancy ($EC_{50, Gpr} < K_d < EC_{50, \beta Arr}$); accordingly, sigmoid fit of the full agonist DAMGO data indicated gains g_K of 18.6 and 0.06 for the G-protein and β -arrestin responses, respectively (A). As before in Figure 10, the same data was also fitted with SABRE (Equation 19) to determine the corresponding gain (γ_{Gpr} , $\gamma_{\beta Arr}$) and efficacy parameters; however, here the same efficacy was assumed for both pathways (i.e., $\epsilon = \epsilon_{Gpr} = \epsilon_{\beta Arr}$; no bias) (C). The gain parameters obtained from the unified fit of all data by SABRE (15.5 ± 0.8 and 0.06 ± 0.004 ; (C) also indicate $\gamma_{\beta Arr} < 1$, i.e., signal attenuation (dampening) and not amplification in this pathway. Because of this, the relatively weak response in the β -arrestin pathway for morphine can be fitted by SABRE without having to assume biased response ($\epsilon = \epsilon_{Gpr} = \epsilon_{\beta Arr} = 0.82 \pm 0.02$); lack of a clearly biased response is also noticeable in the response versus occupancy (f_{resp} vs f_{occup}) graph (D).

left-shifted compared to occupancy indicating signal amplification ($g_{K, Gpr} = \kappa_{full\ agon} = K_d/EC_{50, Gpr} > 1$), but the β -arrestin responses are right-shifted (less concentration sensitive), indicating the opposite ($g_{K, \beta Arr} = \kappa_{full\ agon} = K_d/EC_{50, \beta Arr} < 1$). Indeed, sigmoid fit of the DAMGO data gave $g_{K, Gpr} = 18.6$ and $g_{K, \beta Arr} = 0.06$ (Figure 11A). Notably, this unusual behavior of one left- and one right-shifted response is not just the case for the data shown here (Pedersen et al., 2019) as very similar results have been obtained in two other independent works with both DAMGO and morphine (McPherson et al., 2010; Hothersall et al., 2017) (see (Buchwald, 2023) for more detailed comparisons and discussions).

As for all other cases, these data can also be fitted within the unified framework of SABRE; however, this requires extending the range of the gain parameter γ by allowing it to have values less than one, $\gamma < 1$, i.e., modeling the response in the corresponding pathway as apparent signal attenuation (dampening) (Figure 11C). With this extension, good fit can be obtained ($r^2 = 0.988$; Figure 11C) even with a four-parameter version model (γ_{Gpr} , $\gamma_{\beta Arr}$, ϵ_{DAMGO} , $\epsilon_{morphine}$), i.e., without having to assume different efficacies for the different pathways ($\epsilon = \epsilon_{Gpr} = \epsilon_{\beta Arr}$; no biased agonism). The

gain parameters obtained from SABRE ($\gamma_{Gpr} = 15.5 \pm 0.8$ and $\gamma_{\beta Arr} = 0.06 \pm 0.004$; Figure 11C) are in good agreement with those from the sigmoid fit of the full agonist data (18.6 and 0.06; Figure 11A). Thus, there is consistent evidence for $g_{K, \beta Arr}$ indicating signal attenuation and not amplification in this pathway. Because of the combination of the less than unity gain in the β -arrestin pathway ($\gamma_{\beta Arr} = 0.06 \pm 0.004$) and ligand efficacy of morphine ($\epsilon_{morphine} = 0.82 \pm 0.02$), the relatively weak β -arrestin response of morphine can be fitted without having to assume biased agonism (i.e., $\epsilon_{Gpr} = \epsilon_{\beta Arr}$). The lack of a biased response is also noticeable in the response versus occupancy graph (Figure 11D), where the responses for morphine and DAMGO follow the same pattern contrary to the case of TRV023 and angiotensin II in the previous example (Figure 10D). This is even more evident in a bias plot, which shows the response produced in one pathway directly as a function of the response produced in the other (i.e., f_{resp2} vs f_{resp1}) (Figure 12B) especially as compared to the clearly biased response shown in Figure 12A. Thus, these data suggest that morphine produces a relatively weak β -arrestin response due to a combination of its partial agonism at MOPr and the apparent

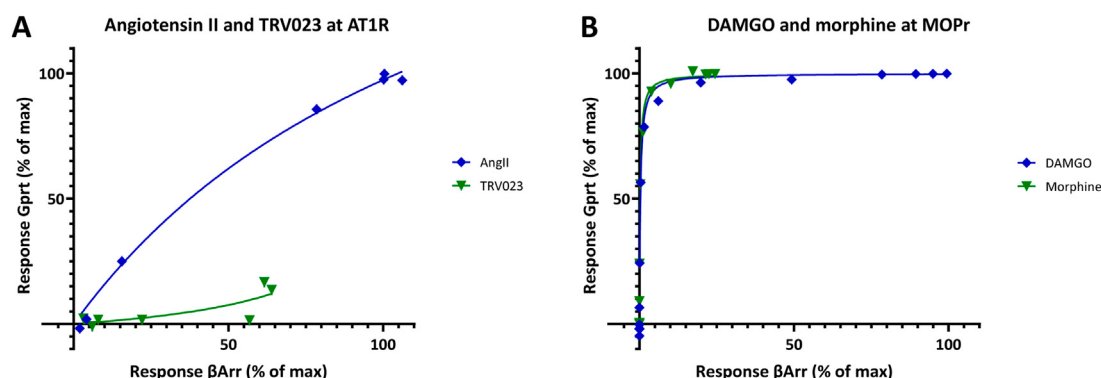


FIGURE 12
Bias (relative response) plots showing one fractional response as a function of the other (f_{resp1} vs f_{resp2}) for the angiotensin II receptor 1 (AT1R) data from Figure 10A and the μ -opioid receptor (MOPr) data from Figure 11B. While a β -arrestin-biased response for TRV023 is evident when compared to the balanced (nonbiased) agonist AngII (A), there is no clear indication of bias for morphine as compared to DAMGO (B). However, indications of bias could be somewhat masked in (B) as the plots are strongly curved due to the large difference between the amplifications in these pathways (>250-fold). AT1R data could be used directly as it was (A) as both responses were measured at the same agonist concentrations; for the MOPr data (B), interpolated values had to be used for the β -arrestin response as they were not measured at the same concentrations as the G-protein response.

signal attenuation in this pathway and not due to biased agonism (similar to the case of olliceridine mentioned earlier (Buchwald, 2023; Gillis et al., 2020)).

Spare receptors—a misnomer

As discussed here, in many systems, maximal or close to maximal response can be achieved when only a relatively small fraction of the receptors is occupied. In current pharmacological terminology, such systems are said to possess “*spare receptors*” or “*receptor reserve*”. According to IUPHAR *spare receptors* are assumed to exist if “a full agonist can cause a maximum response when occupying only a fraction of the total receptor population” (i.e., $f_{\text{resp}} \approx 1$ with $f_{\text{occup}} < 1$) (Neubig et al., 2003). Similarly, in widely used textbooks, *spare receptors* are said to be present if “it is possible to elicit a maximal biologic response at a concentration of agonist that does not result in occupancy of all of the available receptors” (Katzung’s Basic and Clinical Pharmacology (Katzung, 2018)) or “*spare receptors* are said to exist if the maximal drug response (E_{max}) is obtained at less than 100% occupation of the receptors (B_{max})” (Katzung and Trevor’s Pharmacology Examination and Board Review (Katzung et al., 2019)). They are judged to be “present if $K_d > EC_{50}$ ”, and “in practice, the determination is usually made by comparing the concentration for 50% of maximal effect (EC_{50}) with the concentration for 50% of maximal binding (K_d). If the EC_{50} is less than the K_d , *spare receptors* are said to exist” (Katzung et al., 2019) (Figure 13A). These criteria are, however, very much in line with the presence of signal amplification and the definition of the gain factor g_k as introduced here (Equation 5) since $EC_{50} < K_d$ implies $g_k = K_d/EC_{50} > 1$, i.e., amplification. *Spare receptor* implies a “receptor that does not bind drug when the drug concentration is sufficient to produce maximal effect” (Katzung et al., 2019). Considering the standard definition of spare, i.e., “additional to what is required for ordinary use”, this suggests that they are only used in special circumstances the way, e.g., spare tires or spare rooms are, but this is not the case. In these systems, there is indeed an excess

or surplus of receptors, as receptors do not need to be all occupied to achieve maximal response; however, there is no special population of “*spare*” receptors in addition to that of “*regular*” receptors that start to fill up only after the “*regular*” ones are all occupied, as their name might imply. As more correctly described in another textbook (Rang and Dale’s Pharmacology (Ritter et al., 2020)): “The existence of spare receptors does not imply any functional subdivision of the receptor pool, but merely that the pool is larger than the number needed to evoke a full response”. Accordingly, *spare receptor*, which is a misnomer, should be avoided. If needed, *receptor reserve*, which is less frequently used, is a better, less confusing terminology (Neubig et al., 2003). In some cases, it is feasible that there is a *receptor reserve* in the sense they are in excess and do not contribute to the maximum response because of limited downstream transducer availability, so that even if occupied, they cannot generate a response (e.g., only half of GPCRs have access to a G-protein). However, these receptors are again not part of any special *spare* population, and they are subject to being occupied by a ligand just as all others even if they might not be able to initiate signal transduction resulting in a response.

Furthermore, not only is the *spare receptor* term a misnomer, but there is no clear-cut way to quantify them (Figure 13). The percent of excess receptors (i.e., percent response over percent occupancy as judged from the vertical axis, $f_{\text{resp}} - f_{\text{occup}}$ with the present notation) depends on the point of assessment as it has been discussed (Kenakin, 1997) and even illustrated (Gesztelyi et al., 2013) before. If the response is sufficiently left-shifted compared to occupancy, essentially maximal response (e.g., 95% or 99%) can be achieved at (very) different occupancies as illustrated in Figures 13A, B. For the response shown there, 95% of maximum is achieved at 15% occupancy (80% excess) while 99% of maximum at 50% occupancy (49% excess), and these are both essentially maximum responses, typically well within the margin of experimental error. The amount of *spare receptors* is impossible to quantify unequivocally in cases where multiple responses are assessed downstream from the same receptors, such as it was, for example, the case of very differently shifted responses shown in

“*spare receptors*” are present if $K_d > EC_{50}$, but are difficult to quantify (e.g., as excess percent)

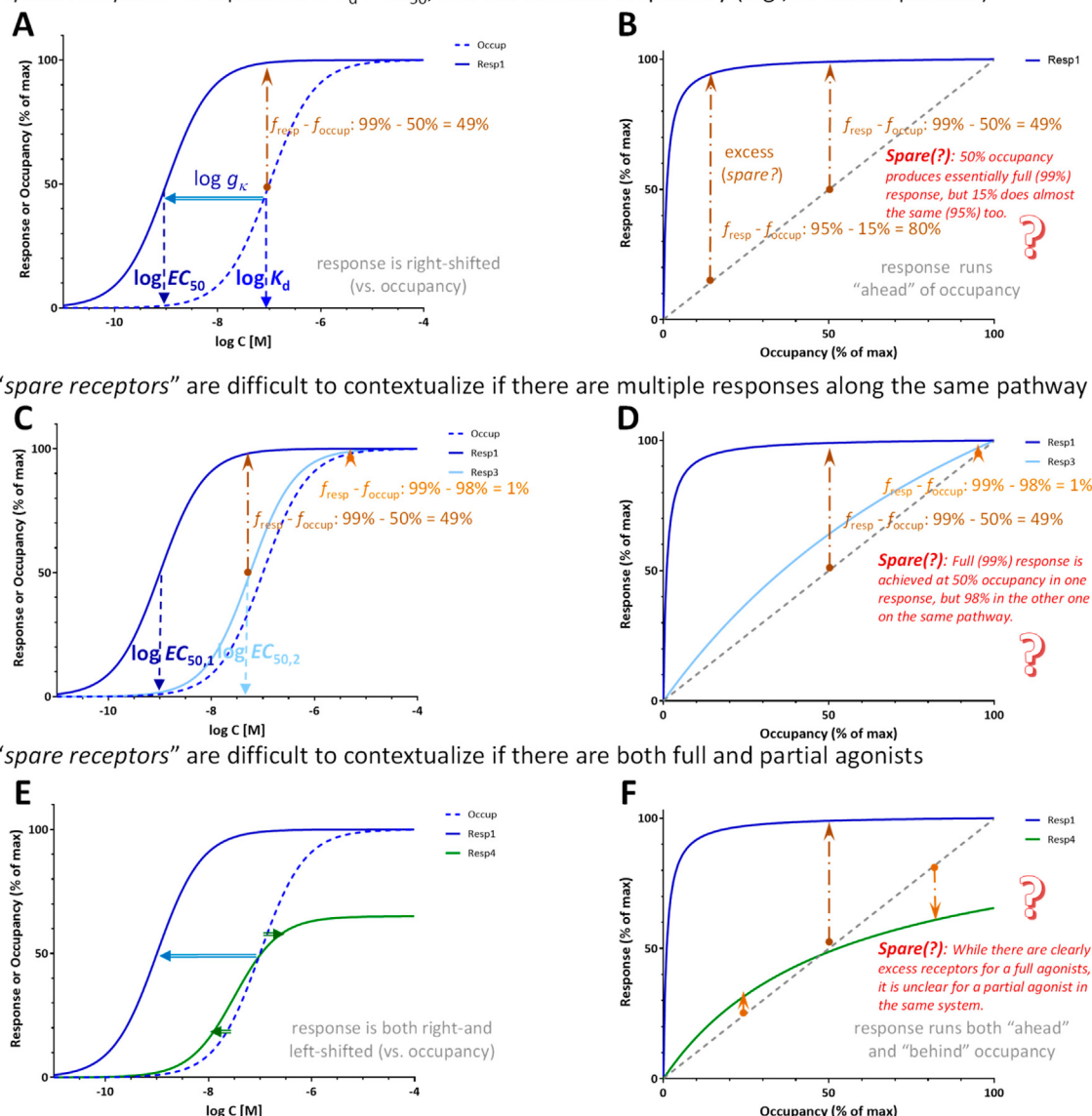


FIGURE 13

Difficulties related to the quantification of *spare receptors*. They are assumed to exist if (essentially) maximal response is obtained at less than full occupation of receptors and are judged to be present if $K_d > EC_{50}$ (Katzung, 2018; Katzung et al., 2019). The excess fraction of receptors as assessed on the vertical axis when comparing response vs. occupancy depends on the point of assessment (A, B); for example, as shown here, the excess is 80% at 95% response but only 49% at 99% response, both of which could be considered essentially maximal responses. They are also difficult to contextualize if two different responses are assessed downstream from the same receptor (C, D). Here, for example, 99% response is already achieved at 50% occupancy for one response, but only at 98% occupancy for the other even if they can be assessed on the same pathway just assessed at different vantage points. *Spare receptors* are also difficult to contextualize if both full and partial agonists are present, as for partial agonists, the response can run both ahead and behind the receptor occupancy (E, F).

Figure 6. For a corresponding illustration shown in Figures 13C, D, maximal (99%) response is achieved at 50% occupancy in one response, but only 98% occupancy in the other one despite both being on the same pathway downstream from the same receptor just subject to different amplifications. *Spare receptors* are also difficult to contextualize if both full and partial agonists are present because for partial agonists, the response can run both ahead and behind the receptor occupancy. In such cases, it might appear that there are spare receptors when assessed at a low occupancy, but they “disappear” at higher occupancies (Figure 13E, F). Thus, the amount of spare receptors depends,

among others, on where it is assessed (i.e., at what occupancy or effect level), what is considered essentially maximal response, what response is assessed, and what ligand is used.

Another more complex approach used to demonstrate the existence of *spare receptors* is “by using irreversible antagonists to prevent binding of agonist to a proportion of available receptors and showing that high concentrations of agonist can still produce an undiminished maximal response” (Katzung, 2018). Further, “higher concentrations of antagonist ... reduce the number of available receptors to the point that maximal response is diminished”. This is, of course, the classic Furchgott method of

irreversible receptor inactivation (Furchgott, 1966; Furchgott and Bursztyn, 1967) discussed earlier (Equation 3; Figure 7). As shown there, the same change in response curves can be produced with the assumption of signal amplification.

Thus, *spare receptor* is a misnomer and a terminology that should be avoided—there is no special pool of “spare” receptors (additional to what is required for ordinary use), just there are excess receptors and not all need to be occupied to elicit full response. In fact, this can be considered a hallmark of a well-engineered system designed to provide some redundancy. Signal amplification with gain as defined here ($g_K = K_d/EC_{50}$; Equation 5) is a convenient alternative, and the criteria for its presence, $g_K = K_d/EC_{50} > 1.0$, fully agrees with the textbook definition of the evidence for the presence of *spare receptors*: “ EC_{50} is less than the K_d ” (Katzung et al., 2019). Furthermore, while the vertical shift for “excess” varies, the horizontal shift that on semi-log graph corresponds to the log gain, $\log g_K = \log K_d - \log EC_{50}$, remains constant (for full agonists) regardless of the point of assessment; thus it is also intuitive and easy to visualize (Figures 4, 13A). As discussed, there are many cases where such signal amplification is needed to achieve sufficient sensitivity, and there are many cases where they have physiological or therapeutic relevance (Kleene, 1997; Tinsley et al., 2016; Grubelnik et al., 2009; McNeil and Evavold, 2002; Fenouillet et al., 2019).

Conclusion

In conclusion, a signal amplification-based approach can account for complex receptor-occupancy curves where responses run both ahead and behind fractional occupancy (Figure 5), for differences caused in the response by altering receptor levels (e.g., by partial irreversible inactivation such as in the Furchgott method; Figure 8), as well as for different responses at different readout points either downstream on the same signaling pathway (Figure 6) or along diverging pathways caused by balanced and biased agonists (Figures 10, 11). Signal amplification downstream from receptors can be conveniently quantified using the gain parameter $g_K = K_d/EC_{50}$ measured for full agonists. This gain parameter is analogous to those used elsewhere (e.g., in electronics, $g_V = V_{out}/V_{in}$), and it also corresponds to the γ gain parameter of SABRE. Further, it is also an intuitive parameter as on customarily used semi-log representations, it equals the horizontal shift between the response and occupancy curves, $\log g_K = \log K_d - \log EC_{50}$. The presence of such shift (i.e., $K_d > EC_{50}$) was generally considered as evidence for the existence of *receptor reserve* or *spare receptors*, a misnomer that should be avoided. For partial agonists, the $\kappa = K_d/EC_{50}$ shift is smaller than for full agonists as not all occupied receptors are active, and relative efficacies can be estimated by comparing $e_{max} \cdot \kappa$ products.

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Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

Author contributions

PB: Conceptualization, Data curation, Formal Analysis, Investigation, Methodology, Software, Writing – original draft, Writing – review and editing.

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Supplementary material

The Supplementary Material for this article can be found online at: <https://www.frontiersin.org/articles/10.3389/fphar.2025.1541872/full#supplementary-material>

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