



# Path-dependent Vortex Switching in Ferroelectric Nanoplate Junctions Toward a Memory Device Concept

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Ferroelectric vortex has attracted much attention as a promising candidate for memories with high density and high stability. It is a crucial problem to precisely manipulate the vortex chirality in order to utilize it to store information. Nevertheless, so far, a practical and direct strategy for vortex switching is still lacking. Moreover, the strong coupling of chirality between neighboring vortices in continuous systems like superlattices limits the application of ferroelectric-vortex-based memories. Here, we design a ferroelectric nanoplate junction to break the strong coupling between neighboring vortices. Phase-field simulation results demonstrate that the vortex chirality of the nanoplates could be efficiently tuned by sweeping local electric and thermal fields in the nanoplate junction. More importantly, the weak coupling between two neighboring nanoplates through the intermediate junction brings a deterministic vortex switching behavior. Based on this, we propose a concept of vortex memory devices. Our study provides an effective way to control the vortex chirality and suggests an opportunity for designing new memory devices based on ferroelectric vortex.

**Keywords:** ferroelectric, vortex, memory, switching, phase field

## INTRODUCTION

Ferroelectric vortex, the toroidal arrangement of electrical dipoles in ferroelectrics, has attracted much attention over the past decades in both theoretical and experimental studies due to their wonderful properties different from the conventional polar domain structures [1–5]. Generally, two degenerate chiral states of vortex, *i.e.*, clockwise (CW) and counterclockwise (CCW), could form stably in the low-dimensional ferroelectric systems. It is a natural idea to utilize the two distinguished states to carry information, *e.g.*, CW vortex denotes the information “0” and CCW vortex denotes the information “1.” Importantly, the vortex is a topological structure that possesses a strong stability property and small size (typically a few nanometers in diameter), holding promise in developing a new type of ferroelectric memory device with high stability and density (~10 Tb/inch<sup>2</sup>).

Since ferroelectric vortex was predicted in ferroelectric nanodisks and nanorods *via* a first-principles-derived effective Hamiltonian [1], a large number of theoretical and experimental studies were carried out to gain further understanding of the structure [2–8]. Toward the applications of vortex-based memories, one of the concerning issues is the deterministic manipulation of vortex chirality. Since the toroidal moment of a ferroelectric vortex is conjugated to a curled electric field, the chirality of a ferroelectric vortex could be switched by a curled electric field, which has been demonstrated based on the phase field method and effective Hamiltonian method [6–8].

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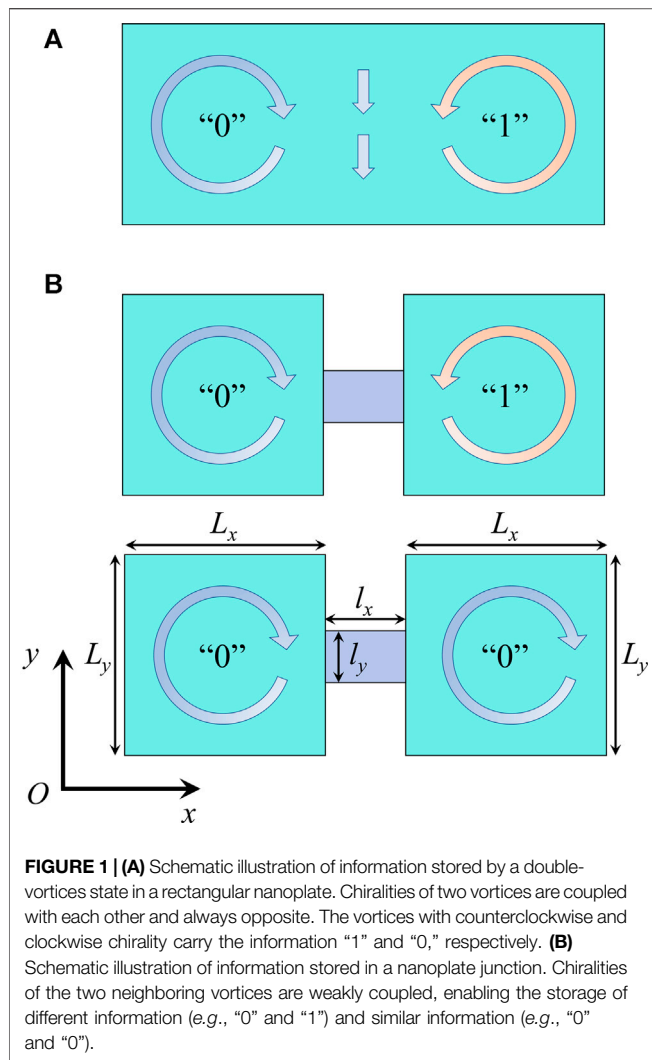
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Nevertheless, it is still a challenge in practice to realize a large enough and highly localized curled electric field to switch the vortex [9–18]. To avoid the use of curled electric fields, various vortex switching strategies have been also proposed, e.g., via geometry design [9–12], defect engineering [13, 14], asymmetric mechanical loads [14–16], nonuniform electric fields [17], sweeping tip fields [18], etc. The key idea of these strategies is to bring some kind of asymmetry to the vortex system, such that nucleation of vortex with a deterministic chirality is favored. For instance, Chen *et al.* [14] introduced an asymmetric mechanical field, e.g., caused by local clamping force or dislocations, to break the spatial symmetry of the ferroelectric vortex in nanodots. Consequently, the vortex is easily switched by a homogeneous electric field. Ma *et al.* [18] exploited a sweeping biased tip to break the time symmetry of annihilation and nucleation dynamics of the ferroelectric vortex. As a result, the vortex could be efficiently switched by such a sweeping tip-induced local electric field in a “dynamic switching” mode.

Despite several advanced strategies have been proposed to realize the switching of vortex, a practical and direct method, which aims to get rid of requirements on the sample and harsh technologies, is still lacking. On the other aspect, neighboring vortices in continuous systems like superlattices are strongly coupled and always have opposite chirality to minimize the domain wall and electrostatic energies of the system (as shown schematically in **Figure 1A**). This means that the information of the vortex array cannot be individually stored and manipulated. This property limits the design and application of vortex-based memories. Therefore, it is necessary to break the coupling between two neighboring vortices.

In this work, we design a nanoplate junction system that consist of two nanoplates and one junction region (**Figure 1B**). The two nanoplates have the same geometry (i.e.,  $L_x$  and  $L_y$  along  $x$  and  $y$  directions, respectively), and the junction region has the lateral sizes of  $l_x$  and  $l_y$ , with  $l_{x(y)} < L_{x(y)}$ . It is expected that, in such a nanoplate junction, the chiralities of two neighboring vortices become weakly coupled with each other. The neighboring vortices in the nanoplate junction not only can carry different information (i.e., “1” and “0” or “0” and “1”), but also can carry similar information (i.e., “0” and “0” or “1” and “1”), hence enabling a two-bit memory element. More importantly, due to presence of an intermediate junction region, this two nanoplates are weakly coupled such that the vortex chirality could be switched more easily than that in the individual nanoplate. To demonstrate the above scenario, phase field simulations are performed to reveal the vortex formation and switching dynamics in nanoplate junctions of different geometries. Moreover, we construct nanoplate junction arrays in conjunction with a s region and show that the information carried by the vortices can be readily controlled by sweeping local electric and thermal fields. Our results thus demonstrate an efficient strategy to manipulate the chirality of ferroelectric vortex and suggest an alternative possibility of developing ferroelectric-vortex-based memory devices.

## METHODS

### Phase Field Model

In this work, a phase field model is established to capture the vortex formation and switching dynamics in ferroelectric nanoplate junctions. In this model, the spontaneous polarization field  $\mathbf{P}=(P_1, P_2, P_3)$  is chosen as order parameter field, whose temporal evolution can be described by the time-dependent Ginzburg-Landau (TDGL) equation,

$$\frac{\partial P_i}{\partial t} = -M \frac{\delta F}{\delta P_i} \quad (1)$$

Where  $F$  is the total free energy of the system,  $M$  is kinetic parameter related to the polarization switching dynamics and  $t$  is time.

For ferroelectric nanosystems, the total free energy is described by the sum of bulk free energies and a surface free energy,

$$F = \iiint [f_{\text{Land}}(P_i) + f_{\text{elas}}(P_i, \varepsilon_{ij}) + f_{\text{grad}}(P_{i,j}) + f_{\text{elec}}(P_i, E_i)] dV + \iint f_{\text{surf}}(P_i) dS \quad (2)$$

Where  $f_{\text{Land}}$ ,  $f_{\text{elas}}$ ,  $f_{\text{grad}}$ ,  $f_{\text{elec}}$  and  $f_{\text{surf}}$  are the energy densities of the Landau free energy, elastic energy, gradient energy, electrostatic energy and surface energy, respectively.  $P_{i,j}$ ,  $\varepsilon_{ij}$ , and  $E_i$  are the gradients of polarization, the components of the strain and electric field, respectively.

For perovskite ferroelectrics like  $\text{PbTiO}_3$  (PTO), the Landau free energy density  $f_{\text{Land}}$  is given by the form of a six-order polynomial [19, 20],

$$f_{\text{Land}}(P_i) = \alpha_1 \sum_i P_i^2 + \alpha_{11} \sum_i P_i^4 + \alpha_{12} \sum_{i>j} P_i^2 P_j^2 + \alpha_{111} \sum_i P_i^6 + \alpha_{112} \sum_{i \neq j} P_i^4 P_j^2 + \alpha_{123} \prod_i P_i^2 \quad (3)$$

With  $\alpha_i$ ,  $\alpha_{ij}$ ,  $\alpha_{ijk}$  and  $\alpha_{ijkl}$  being the thermodynamic coefficients of the Landau free energy. Here,  $\alpha_1$  is temperature-dependent and is expressed as  $\alpha_1 = (T - T_0)/(2\varepsilon_0 C_0)$  with  $T_0$  and  $C_0$  are the Curie-Weiss temperature and Curie-Weiss constant, respectively,  $\varepsilon_0$  is the vacuum permittivity, and  $T$  is the temperature.

The eigenstrain  $\varepsilon_{ij}^0$  induced by the electrostriction effect is given by  $\varepsilon_{ij}^0 = Q_{ijkl} P_k P_l$ , where  $Q_{ijkl}$  are the electrostrictive tensor. The elastic energy density  $f_{\text{elas}}$  is written as,

$$f_{\text{elas}}(P_i, \varepsilon_{ij}) = \frac{1}{2} c_{ijkl} \varepsilon_{ij} \varepsilon_{kl} = \frac{1}{2} c_{ijkl} (\varepsilon_{ij} - \varepsilon_{ij}^0) (\varepsilon_{kl} - \varepsilon_{kl}^0) \quad (4)$$

With  $c_{ijkl}$  being the elastic stiffness tensor and  $\varepsilon_{ij} = \varepsilon_{ij} - \varepsilon_{ij}^0$  being the components of elastic strain. The strain field is determined by the mechanical equilibrium equation  $\sigma_{i,j,j} = 0$ , where  $\sigma_{ij} = c_{ijkl} \varepsilon_{kl}$  are the stress field components. The mechanical boundary condition of the nanoplate junctions is set to be stress free.

The gradient energy density  $f_{\text{grad}}$  induced by the gradient of polarization is given by a form in a second-order approximation of Taylor expansion,

$$f_{\text{grad}}(P_{i,j}) = \frac{1}{2} g_{ijkl} P_{i,j} P_{k,l} \quad (5)$$

Where  $g_{ijkl}$  are the gradient energy coefficients.

Based on the concept of background dielectric constant, the electrostatic energy density  $f_{\text{elec}}$  is given by,

$$f_{\text{elec}}(P_i, E_i) = -P_i E_i - \frac{1}{2} \varepsilon_b E_i E_i \quad (6)$$

Where  $\varepsilon_b = \varepsilon_0 + \chi_b$  is the background dielectric constant with  $\varepsilon_0$  and  $\chi_b$  being the vacuum permittivity and background susceptibility, respectively [21, 22]. To stabilize ferroelectric vortices, in the simulation, the polarization evolves under the ideal open-circuit conditions. The depolarization field is calculated by the electrostatic equilibrium equation of  $D_{i,i} = 0$ , by assuming the free charges are negligible inside the ferroelectric. Here,  $\mathbf{D} = \varepsilon_b \mathbf{E} + \mathbf{P}$  is the electric displacement field.

The relaxation of local spontaneous polarization near the surface contributes to the surface energy. Based on the

**TABLE 1** | Values of parameters in simulations (SI units and  $T$  in K).

$\alpha_1$	$3.85(T-752) \times 10^5$	$c_{11}$	$1.746 \times 10^{11}$	$G_{110}$	$1.73 \times 10^{-10}$
$\alpha_{11}$	$-7.3 \times 10^7$	$c_{12}$	$0.7937 \times 10^{11}$	$G_{111}$	$3.46 \times 10^{-10}$
$\alpha_{12}$	$7.5 \times 10^8$	$c_{44}$	$1.1111 \times 10^{11}$	$G_{444}$	$1.73 \times 10^{-10}$
$\alpha_{111}$	$2.6 \times 10^8$	$Q_{11}$	0.089	$\delta_b^{\text{eff}}$	$5 \times 10^9$
$\alpha_{112}$	$6.1 \times 10^8$	$Q_{12}$	-0.026	$\varepsilon_b$	$4.425 \times 10^{-10}$
$\alpha_{123}$	$-3.7 \times 10^9$	$Q_{44}$	0.0675	$P_0$	0.757

concept of extrapolation length, the surface energy density  $f_{\text{surf}}$  can be modeled by the following simple form [23],

$$f_{\text{surf}}(P_i) = \frac{1}{2} \left( \frac{D_1^S}{\delta_1^{\text{eff}}} P_1^2 + \frac{D_2^S}{\delta_2^{\text{eff}}} P_2^2 + \frac{D_3^S}{\delta_3^{\text{eff}}} P_3^2 \right) \quad (7)$$

Where  $\delta_i^{\text{eff}}$  and  $D_i^S$  are extrapolation lengths and surface energy coefficients related to a specific surface  $S$ , respectively. It is worth noting that the predominant factor for the formation of vortex in ferroelectric low-dimensional systems would be the long-range electrostatic interaction rather than the short-range surface effects [1, 24]. Thus, the selection of parameters  $\delta_i^{\text{eff}}$  and  $D_i^S$  would not have significant influence on the formation of the vortex structure.

In this simulation, the nanoplate junctions are modeled to be made of PTO. Two-dimensional (2D) discrete grids are employed with grid spacings both being 1 nm along the lateral  $x$  and  $y$  directions. It is worthy to notice that the tetragonal vortex state prefers to form in the tetragonal PTO nanoplate. Therefore, the 2D model can capture the features and its evolution of the vortex state in ferroelectrics at suitable conditions. To have a good control of the vortex switching, nanofilm regions with a polar-domain state are also included in the system in the demo of vortex array memory devices. Periodic boundary conditions are applied along the  $y$  direction in the nanofilm region. The evolution of polarization is solved numerically by discretizing the TDGL equation in time. At each time step, the strain and electric fields are obtained by solving the mechanical and electrostatic equilibrium equations with the appropriate boundary conditions. Values of the material coefficients [20, 22, 25, 26] used in the simulation are listed in the **Table 1**.

## Finite Element Method

In the phase-field simulations, strain and electric fields are solved by the finite element method. According to variation relationship, the mechanical and electrostatic equilibrium equations (**Eqs 4, 6**) can be solved by looking for the extreme value of following functionals, i.e.,

$$I_{\text{elas}}(u_i) = \iiint_V \frac{1}{2} c_{ijkl} (\varepsilon_{ij} - \varepsilon_{ij}^0) (\varepsilon_{kl} - \varepsilon_{kl}^0) dV - \iint_S \tau_i u_i dS \quad (8a)$$

$$I_{\text{elec}}(\varphi) = \iiint_V (\varepsilon_b \varphi_{,i} \varphi_{,i} + 2\varphi P_{i,i}) dV - 2 \iint_S \varphi P_i n_i dS \quad (8b)$$

Where the displacement  $u_i$  and the electric potential  $\varphi$  are employed as the freedoms of the functionals. Then, these two equations could be rewritten into the matrix form, i.e.,

$$\begin{aligned}
I_{\text{elas}}(u_i) &= \iiint_V \frac{1}{2} (\{\varepsilon\} - \{\varepsilon^0\})^T [C] (\{\varepsilon\} - \{\varepsilon^0\}) dV - \iint_S \{\tau\}^T \{u\} dS \\
&= \iiint_V \frac{1}{2} ([L_u]\{u\} - [Q]\{P^2\})^T [C] ([L_u]\{u\} - [Q]\{P^2\}) dV - \iint_S \{\tau\}^T \{u\} dS
\end{aligned} \quad (9a)$$

$$\begin{aligned}
I_{\text{elec}}(\varphi) &= \iiint_V (\varepsilon_b \{\nabla\varphi\}^T \{\nabla\varphi\} + 2\varphi P_{i,i}) dV - 2 \iint_S \varphi P_i n_i dS \\
&= \iiint_V [\varepsilon_b (\{L_\varphi\}\varphi)^T \{\{L_\varphi\}\varphi\} + 2\varphi P_{i,i}] dV - 2 \iint_S \varphi P_i n_i dS
\end{aligned}$$

For 2D model, vectors and matrices are defined as,

$$\begin{aligned}
\{u\} &= \begin{Bmatrix} u_1 \\ u_2 \end{Bmatrix}, \{\tau\} = \begin{Bmatrix} \tau_1 \\ \tau_2 \end{Bmatrix}, \{L_\varphi\} = \begin{Bmatrix} \frac{\partial}{\partial x} \\ \frac{\partial}{\partial y} \end{Bmatrix}, \{\nabla\varphi\} = \begin{Bmatrix} \frac{\partial\varphi}{\partial x} \\ \frac{\partial\varphi}{\partial y} \end{Bmatrix}, \{\sigma\} = \begin{Bmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{12} \end{Bmatrix}, \\
\{\varepsilon\} &= \begin{Bmatrix} \varepsilon_{11} \\ \varepsilon_{22} \\ 2\varepsilon_{12} \end{Bmatrix}, \{\varepsilon^0\} = \begin{Bmatrix} \varepsilon_{11}^0 \\ \varepsilon_{22}^0 \\ 2\varepsilon_{12}^0 \end{Bmatrix}, \{P^2\} = \begin{Bmatrix} P_1^2 \\ P_2^2 \\ P_1 P_2 \end{Bmatrix}, [L_u] = \begin{Bmatrix} \frac{\partial}{\partial x} & 0 \\ 0 & \frac{\partial}{\partial y} \\ \frac{\partial}{\partial y} & \frac{\partial}{\partial x} \end{Bmatrix}, \\
[C] &= \begin{bmatrix} c_{11} & c_{12} & 0 \\ c_{12} & c_{11} & 0 \\ 0 & 0 & c_{44} \end{bmatrix}, [Q] = \begin{bmatrix} Q_{11} & Q_{12} & 0 \\ Q_{12} & Q_{11} & 0 \\ 0 & 0 & Q_{44} \end{bmatrix}
\end{aligned} \quad (10)$$

In the simulations, the ferroelectric is meshed into four-node cubic elements. After denoting the displacement vector and the electric potential at the  $i$ th nodes of an element as  $\{\delta_i\} = \{u^i, \varphi_i\}$  ( $i = 1, 2, 3, 4$ ), the displacement vector and the electric potential of the eight nodes in each element could be written as,

$$\{\delta^e\} = \{\{\delta_1\}\{\delta_2\}\{\delta_3\}\{\delta_4\}\}^T \text{ and } \{\varphi^e\} = \{\varphi_1, \varphi_2, \varphi_3, \varphi_4\}^T \quad (11)$$

Then, the displacement and the electric potential in the element are given by,

$$\{u\} = [N_u]\{\delta^e\} \text{ and } \varphi = [N_\varphi]\{\varphi^e\} \quad (12)$$

With

$$\begin{aligned}
[N_u] &= \begin{bmatrix} N_{u1} & 0 & \dots & N_{u4} & 0 \\ 0 & N_{u1} & \dots & 0 & N_{u4} \end{bmatrix} \text{ and } [N_\varphi] \\
&= [N_{\varphi 1} N_{\varphi 2} N_{\varphi 3} N_{\varphi 4}]
\end{aligned} \quad (13)$$

Where  $N_{ui}$  and  $N_{\varphi i}$  are the interpolation functions.

In the next step, the **Eq. 12** is substituted into **Eq. 9**. In order to find out the extreme value of these two functionals, and the variation of two functionals with respect to the  $\{\delta^e\}$  and  $\{\varphi^e\}$  should be zero and expressed as,

$$\begin{aligned}
\delta I_{\text{elas}} &= \sum_e \iiint_{V_e} ([B_u]\{\delta^e\} - [Q]\{P^2\})^T [C] [B_u]\{\delta^e\} dV \\
&\quad - \sum_{e'} \iint_{S_e} \{\tau\}^T [N_u]\{\delta^e\} dS = 0
\end{aligned} \quad (14a)$$

$$\begin{aligned}
\delta I_{\text{elec}} &= \sum_e 2 \iiint_{V_e} [\varepsilon_b \{\varphi^e\}^T [B_\varphi]^T [B_\varphi] + P_{i,i} [N_\varphi]] \delta\{\varphi^e\} dV \\
&\quad - \sum_{e'} 2 \iint_{S_e} P_i n_i [N_\varphi] \delta\{\varphi^e\} dS = 0
\end{aligned} \quad (14b)$$

Here,  $e$  and  $e'$  label the elements in the volume and at the surface, respectively,  $[B_u] \equiv [L_u][N_u]$  and  $[B_\varphi] \equiv [L_\varphi][N_\varphi]$ . Based on the variation principle, we can obtain the element equations, *i.e.*,

$$[K_u^e]\{\delta^e\} = \{F_u^e\} \text{ and } [K_\varphi^e]\{\delta^e\} = \{F_\varphi^e\} \quad (15)$$

With

$$\begin{aligned}
[K_u^e] &= \iiint_{V_e} [B_u]^T [C] [B_u] dV, [K_\varphi^e] = \iiint_{V_e} \varepsilon_b [B_\varphi]^T [B_\varphi] dV \\
\{F_u^e\} &= \iiint_{V_e} [B_u]^T [C] [Q]\{P^2\} dV + \iint_{S_e} [N_u]\{\tau\} dS, \\
\{F_\varphi^e\} &= \iiint_{V_e} P_{i,i} [N_\varphi]^T dV + \iint_{S_e} P_i n_i [N_\varphi] dS
\end{aligned} \quad (16)$$

Here,  $[K_u^e]$  and  $[K_\varphi^e]$  are the stiffness matrices of element,  $\{F_u^e\}$  and  $\{F_\varphi^e\}$  are the node force vectors of element. Furthermore, the global stiffness matrices (*i.e.*,  $[K_u]$  and  $[K_\varphi]$ ) and global force vectors (*i.e.*,  $\{F_u\}$  and  $\{F_\varphi\}$ ) can be written in following form,

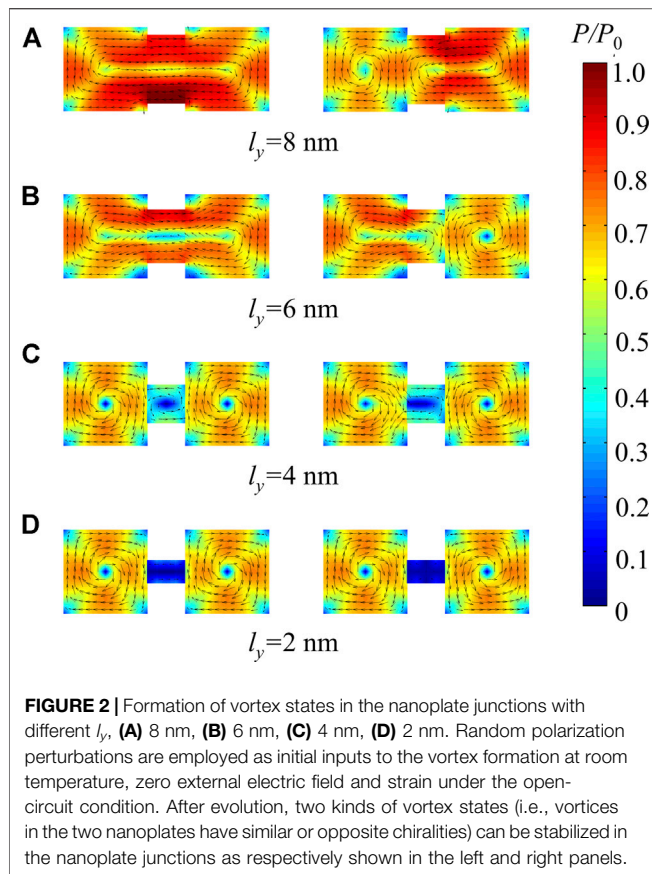
$$[K_u]\{U\} = \{F_u\} \text{ and } [K_\varphi]\{\Phi\} = \{F_\varphi\} \quad (17)$$

Where  $\{U\}$  and  $\{\Phi\}$  are the vectors containing all the node displacement and electric potential, respectively. Then, the node displacement and electric potential could be obtained by solving the **Eq. 17** *via* the Gauss-Seidel iteration method.

## RESULTS AND DISCUSSIONS

### Domain Formation in Nanoplate Junction

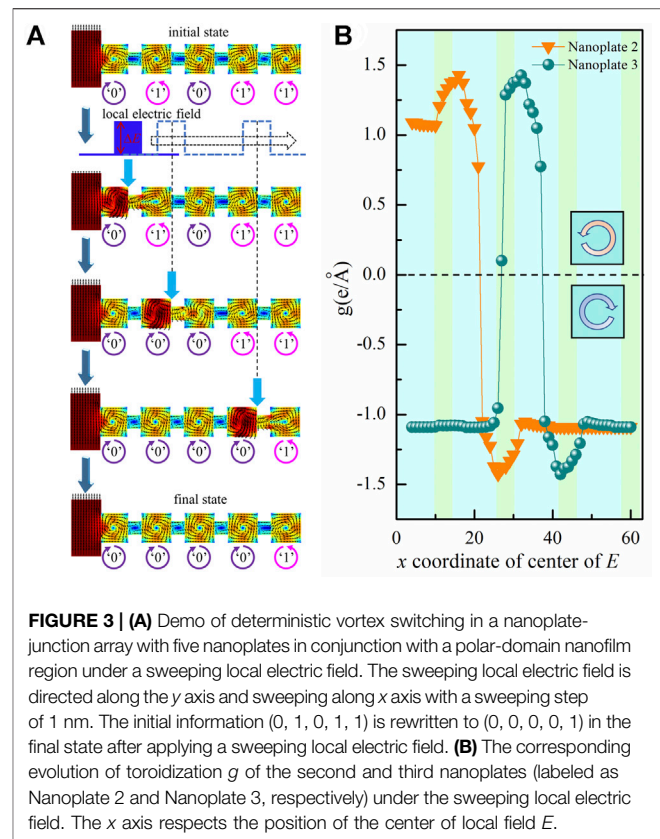
First of all, we have an insight into the effect of geometry of the junction region on the formation of vortices in the nanoplate junction. In the nanoplate junction, the  $L_x$  and  $L_y$  of the nanoplates are both set to be 10 nm,  $l_x$  of the junction region is set to be 4 nm, and  $l_y$  varies in the range of 8–2 nm. For the nanoplate junctions with different  $l_y$ , various random polarization perturbations are employed as initial inputs to the vortex formation at room temperature, zero external electric field and strain under the open-circuit condition. After evolution according to the TDGL equations, two kinds of vortex states (*i.e.*, vortices in the two nanoplates have similar or opposite chiralities) can be stabilized in the nanoplate junctions. In **Figure 2**, the left panels show the vortex states with similar dipole rotation in the two nanoplates of nanoplate junctions under different  $l_y$ . When  $l_y$  is equal to 8 and 6 nm, as respectively shown in **Figures 2A,B**, only one vortex forms in the nanoplate junction. These results are similar to the vortex state with one vortex in the PTO nanoplate in previous works [14, 15]. When



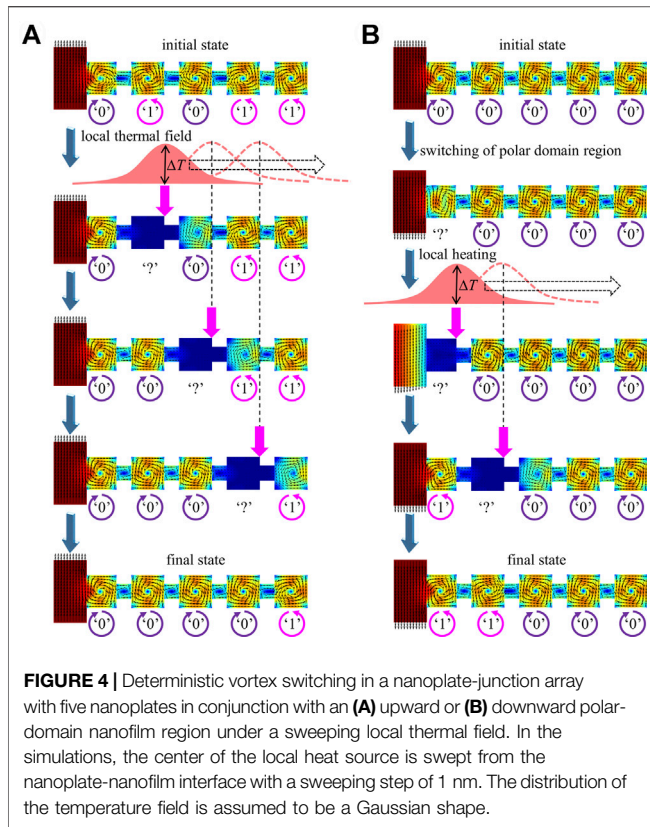
$l_y$  decreases to 4 nm (**Figure 2C**), two complete vortices could be stably formed in the two nanoplates. In this case, a vortex also forms in the junction region and the polarization magnitude is about half of the magnitude in the two nanoplates. More importantly, the vortices of two nanoplates are coupled with the junction region and could be affected by the vortex state of the junction region. If  $l_y$  decreases to 2 nm (**Figure 2D**), the junction region is almost paraelectric. The coupling between the two vortices in the nanoplates becomes even weaker. Moreover, vortices with opposite toroidal arrangements of the dipoles in two nanoplates are also found, as shown in the right panels in **Figure 2**. For cases  $l_y$  equal to 8 and 6 nm, the polarization in the junction region is strongly coupled with one of the nanoplates and the nanoplate and the junction region together form a vortex. When  $l_y$  decreases to 4 and 2 nm, two complete vortices with opposite chiralities could be stably formed in the two nanoplates. Consistent with the previous results, the polarization magnitude is about half of the magnitude in the nanoplates when  $l_y = 4$  nm while the polarization in the junction region is almost zero when  $l_y = 2$  nm.

### Controllability of Vortex Chirality Under a Sweeping Local Electric Field

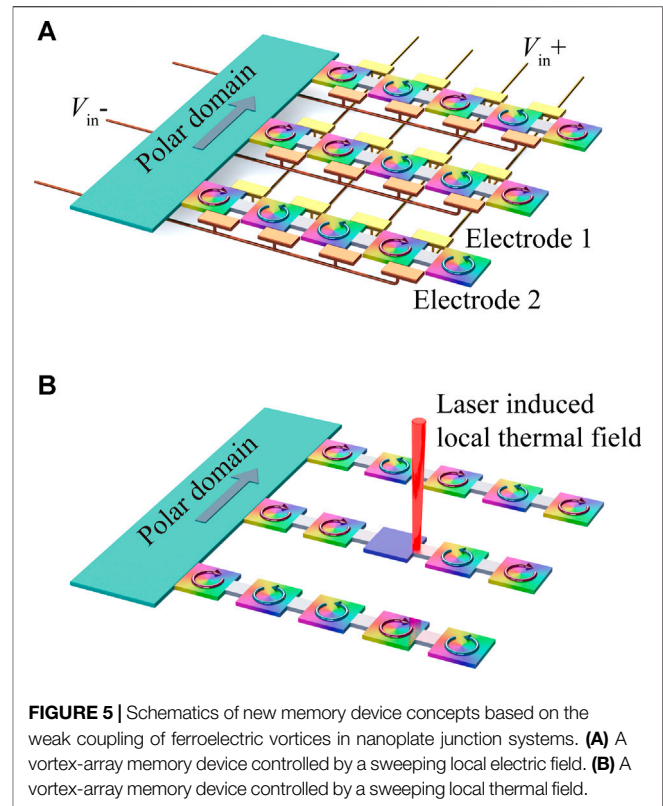
Based on the vortex states in the nanoplate junctions,  $l_y$  is chosen as 4 nm to ensure the independence of two vortices in the two



nanoplates. Meanwhile, the chiralities of these two vortices could interact with each other through the polarization in the junction region. In the following, a nanoplate-junction array with five nanoplates in conjunction with a polar-domain nanofilm region is constructed to demo the deterministic switching of vortex chirality and the possibility of developing a new kind of vortex-based memory device. We first consider the vortex switching induced by a sweeping local electric field. The initial information carried by the vortex array is set to be (0, 1, 0, 1, 1), as shown in **Figure 3**. The local electric field is applied to the system with a profile  $E(x) = E_0\delta(x)$ , where  $E_0$  is the strength of applied electric field and is set to be  $-5 \times 10^8$  V/m,  $\delta(x)$  is a subsection function and is expressed as  $\delta(x) = \begin{cases} 1, & |x - x_0| \leq \Delta x \\ 0, & |x - x_0| > \Delta x \end{cases}$  with  $x_0$  being the  $x$ -coordinate of the center of local electric field, and  $2\Delta x$  being the width of the local electric field along  $x$ -axis (i.e., 8 nm in the simulations). The sweeping local electric field is applied to the system from the nanoplate-nanofilm interface with a sweeping step of 1 nm. When the local electric field is swept to the edge of the first nanoplate, the polarization amplitude of the first nanoplate has a large increase. And the vortex chirality in the nanoplate is not reversed because of the coupling between vortex chirality and polarization direction in nanofilm region. At the next step, the center of the local electric field is swept to the edge of the second nanoplate. Accompanied by the application of the local electric field, the chirality of the vortex is altered and the information “1” in the nanoplate is written to “0.”



Then, the center of the local electric field is swept to the edge of the fourth nanoplate, the initial CCW vortex state is switched into the CW vortex state. The final state after applying the sweeping local electric field is also exhibited in **Figure 3A**. To clearly characterize the switching behaviors of the vortices, we calculate the toroidization, *i.e.*,  $g = \frac{1}{V} \int_V \mathbf{r} \times (\mathbf{P} - \bar{\mathbf{P}}) dV$ , where  $\mathbf{r}$  respects the position vector,  $\mathbf{P}$  is the polarization field,  $\bar{\mathbf{P}}$  is the average polarization and  $V$  is the volume of the nanoplate. Note that the positive  $g$  indicates that the vortex is CCW in the nanoplate and the negative  $g$  means the vortex is CW. As an example, we have plotted the evolution of  $g$  of the second and third nanoplates (labeled as Nanoplate 2 and Nanoplate 3, respectively), which have contrary vortex chiralities under the sweeping of the center of electric field in **Figure 3B**. Here, the nanoplates and junction regions are colored in the **Figure 3B** by shading light blue and light green, respectively. For Nanoplate 2, its toroidization  $g$  begins to increase from 1.07  $e/\text{\AA}$  to 1.43  $e/\text{\AA}$  when the center of electric field moves across the junction region between the first nanoplate and Nanoplate 2. Subsequently,  $g$  of nanoplate 2 decreases with the further sweeping of the local electric field and the sign of  $g$  changes from positive to negative. This reflects that the vortex of Nanoplate 2 has been switched by the sweeping local electric field. Then,  $g$  increases and becomes stable when the electric field moves further away from Nanoplate 2. Evolution of  $g$  of Nanoplate 3 differs from that of Nanoplate 2. Initially,  $g$  of Nanoplate 3 is negative because



of the CCW vortex. When the center of local electric field reaches the right surface of Nanoplate 2,  $g$  of Nanoplate 3 increases and suddenly changes to be positive, indicating that the vortex of Nanoplate 3 has been switched. However, with the further sweeping of local electric field,  $g$  of Nanoplate 3 evolves into a negative value once again. Finally, Nanoplate 3 maintains a negative value of toroidization and the stable vortex with CCW chirality. According to the above results, we can find that the vortices of the nanoplate junction system could be effectively switched under the stimulus of a sweeping local electric field. According to the above results, we can find that the vortex could be effectively switched under the stimulus of a sweeping local electric field in the nanoplate junction.

### Controllability of Vortex Chirality Under a Sweeping Local Thermal Field

Furthermore, we carried out another stimulus, *i.e.*, a sweeping local thermal field, to explore the controllability of vortex chirality in a nanoplate-junction array with five nanoplates in conjunction with a polar-domain nanofilm region. Such a local thermal field could be practically realized by a laser spot. At the beginning, the nanoplate array is set to carry the information of (0, 1, 0, 1, 1). In the simulations, the center of the local heat source is swept from the nanoplate-nanofilm interface with a sweeping step of 1 nm. The distribution of the temperature field is assumed to be a Gaussian shape, *i.e.*,  $T(x) = T_0 + \Delta T \exp\left[\frac{x-x_0}{2(\Delta x)^2}\right]$ . Here,  $T(x)$  is the temperature at

the position  $x$ ,  $T_0$  is the base temperature of the system and is set to be 300 K in the simulations,  $\Delta T$  is the temperature difference against to the  $T_0$  at the center of local heat source and is set to be 500 K in the simulations (*i.e.*, the peak temperature reaches 800 K, which is much higher than the ferroelectric-paraelectric phase transition temperature of PTO [12]),  $x_0$  is the  $x$  coordinate of the center of local heat source, and  $\Delta x$  is set to be 8 nm in the simulations. As shown in **Figure 4A**, after the local heat source is swept to the edge of the second nanoplate, the second nanoplate is heated beyond the phase transition temperature and occurs a ferroelectric-paraelectric phase transition. The polarization in the second nanoplate is near zero. Then, the center of the local heat source is swept to the edge of the third nanoplate and the temperature of the second nanoplate returns to the base temperature (*i.e.*, 300 K). After removing the local heat source, the polarization in the second nanoplate is rearranged. Interestingly, we can observe that the vortex in the second nanoplate is switched from CCW (information “1”) to CW (information “0”). At the next step, the third nanoplate with CW vortex is heated and transforms into the paraelectric phase. After removing the heat source, the chirality of the vortex is not changed, and the CW vortex is reformed in the third nanoplate. Furthermore, the local heat source is swept to the edge of the fourth nanoplate, which has a CCW vortex and carries the information “1.” After the application of the sweeping local thermal field, the vortex in the fourth nanoplate is switched, and the information is changed from “1” to “0.” Finally, the stored information has been rewritten from (0, 1, 0, 1, 1) to (0, 0, 0, 0, 1), as shown in the final state in **Figure 4A**. According to the results, we can clearly see that the chirality of the vortex can be manipulated by the sweeping local thermal field in a deterministic way.

From the above simulations, it is clear to see that the vortex chirality of a nanoplate bit can be switched to be the same as the neighboring nanoplate (either the left or the right nanoplate depending on the sweeping direction). This is to say, if a local electric or thermal field sweeps above a nanoplate-junction array from left to right (or reversely), all the bits swept across by the field would be finally in the same state with the leftmost (right most) bit. How can we switch the vortices if all vortices have the same chirality? It is noteworthy that as demonstrated in previous work [12], the chirality of the vortex can be alternated by switching the polarization of the nanofilm right below in a PTO nanofilm-nanodot system. Based on this finding, one can make use of a nanofilm region with a polar domain to control the vortex chirality of the first nanoplate of the nanoplate array. We take the case of vortex switching under a sweeping local thermal field as an example, as shown in **Figure 4B**. After reversing the polarization direction of nanofilm region, a local heat source is swept from the nanoplate-nanofilm interface to the edge of the first nanoplate. When the local thermal field is removed, we find that the vortex chirality is switched from CW to CCW. The initial information “0” is rewritten to the information “1.” Furthermore, the local heat source is swept to the edge of the second nanoplate and a vortex switching from

CW (“0”) to CCW (“1”) is observed. Therefore, the bidirectional switching of the vortex state has been demonstrated in ferroelectric nanoplate junction system.

## Discussion

The above path-dependent vortex switching behaviors under the sweeping local electric and thermal fields therefore indicate new memory device concepts based on the weak coupling of ferroelectric vortices in nanoplate junction systems, as schematically shown in **Figure 5**. **Figure 5A** depicts a vortex-array memory device controlled by a sweeping local electric field. The nanoplates with vortices of different chiralities are employed to carry the information. Local electric field is applied through two sets of electrodes, *i.e.*, electrode 1 and electrode 2. By selectively applying the bias voltages (*i.e.*,  $V_{in+}$  and  $V_{in-}$ ) to electrodes, a local electric field is applied to a specific nanoplate to manipulate the vortex chirality of the nanoplate. Meanwhile, a nanofilm region with polar domain is also included in the device to reset the information. Similarly, we can also design a vortex-array memory device controlled by a sweeping local thermal field, as shown in **Figure 5B**. For this device, the laser could be used to provide a local heat source. With the sweeping of laser-induced local thermal field, the vortex chirality of nanoplates could be controlled in a feasible way.

## CONCLUSIONS

In conclusion, we propose a ferroelectric nanoplate junction structure to break the strong coupling between neighboring vortices such that vortex-based memory devices which enable independent information storage and feasible vortex switching scheme can be realized. *Via* phase field simulations, we first study the vortex formation in the nanoplate junction with various geometries of the junction region. It shows that when the junction region is small enough, the vortex chiralities of two neighboring nanoplates in the nanoplate junction become almost independent. Meanwhile, the vortices of two nanoplates weakly interact with each other through the polarization field in the junction region. Due to the presence of the intermediate junction region, the chirality of the vortex in a nanoplate can be deterministically switched *via* a sweeping local electric or thermal field. This work proposes an efficient and practical strategy to manipulate the chirality of ferroelectric vortex and suggests an opportunity for designing the memory devices based on ferroelectric vortex.

## DATA AVAILABILITY STATEMENT

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

## AUTHOR CONTRIBUTIONS

WC and YZ conceived the research. WX, WC, and YZ designed, performed and analyzed the modeling, WX and WC wrote the

manuscript. All authors discussed the results, commented on the manuscript and approved it for publication.

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