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## EDITED BY

Olivier Serot,  
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## REVIEWED BY

Marina Barbui,  
Texas A and M University, United States  
Christelle Schmitt,  
UMR7178 Institut Pluridisciplinaire Hubert  
Curien (IPHC), France

## \*CORRESPONDENCE

Walter Loveland,  
✉ lovelanw@oregonstate.edu

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# Total kinetic energy release in the fast neutron induced fission of actinide nuclei

Walter Loveland\*

Chemistry Department, Oregon State University, Corvallis, OR, United States

The total kinetic energy release and fission mass distributions for the fast neutron ( $E_n = 3\text{--}100$  MeV) induced fission of  $^{232}\text{Th}$ ,  $^{233}\text{U}$ ,  $^{235}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{239}\text{Pu}$ ,  $^{240}\text{Pu}$ , and  $^{242}\text{Pu}$  have been measured using the LANSCE facility. The neutron energies were deduced from time-of-flight measurements. The fission fragments were detected using Si PIN diode detectors, giving us the fragment energies. The actinide targets were made by vapor deposition leading to high-quality targets, that were thin and uniform with reduced impurities. Corrections were made to the data for pulse height defect and the fragment energy loss in the target and its backing. The TKE distributions were Gaussian in shape and their mean value as a function of incoming neutron energy could be fitted with second order polynomials. In the case of  $^{233}\text{U}$  and  $^{235}\text{U}$ , our measurements agree with prior work. Our measurements for  $^{232}\text{Th}$  are unique. Our data agree with Viola scaling. The constant position of the heavy mass peak is interpreted as being due to the influence of the  $N = 88$  and  $Z = 50$  shells. The GEF model predictions agree with the data in general as do the CGMF model predictions.

## KEYWORDS

fission, kinetic energy, mass distributions, actinide targets, Viola scaling

## 1 Introduction

Most of the energy released in the fission of actinide nuclei appears in the form of the total kinetic energy (TKE) of the fragments. Because of this fact, it is important to understand the TKE release for its practical importance and the information gained about large scale nuclear collective motions. There are many books that describe the fission process. Some general books are P. Talou and R. Vogt [1],

W. Younes and W. Loveland [2], R. Vandenbosch and J.R. Huizenga “Nuclear Fission” Academic Press (1974) [3], C. Wagemans, “The Nuclear Fission Process”, CRC Press (1991) [4], and H.J. Krappe and K. Pomorski, “Theory of Nuclear Fission” Springer, (2011) [5].

From time to time there are important review articles on fission that influence the development of the field. Among the list of such articles that influenced the author are [6–8], and [9].

Viola et al. [10] have suggested a simple parameterization of the TKE release in the low energy and spontaneous fission of actinide nuclei in the form:

$$\text{TKE} = (0.1189 \pm 0.0011) Z^2 / A^{1/3} + 7.3 \pm 1.5 \text{ MeV} \quad (1)$$

The first term in this equation represents the Coulomb energy of the deformed nascent fragments at scission while the second term represents an average estimate for the energy contributed to the TKE release from the conversion of the collective motion of the fissioning

TABLE 1 Summary of measurements of TKE in Fission of actinide nuclei.

Target	Projectile	Projectile energy (MeV)	References
<sup>232</sup> Th	n	thermal	[13]
<sup>232</sup> Th	n	1–6	[14]
<sup>232</sup> Th	n	3–91	[15]
<sup>232</sup> Th	photon	6.7,7.3	[16]
<sup>233</sup> U	n	thermal	[13]
<sup>233</sup> U	n	thermal	[17]
<sup>233</sup> U	p	7–13	[18]
<sup>233</sup> U	p	9.5–22	[19]
<sup>233</sup> U	n	0–40	[14]
<sup>234</sup> U	n	4,5	[20]
<sup>234</sup> U	n	2–5	[21]
<sup>234</sup> U	n	0.2–5.0	[22]
<sup>235</sup> U	p	8–13	[18]
<sup>235</sup> U	n	thermal	[13]
<sup>235</sup> U	n	thermal	[17]
<sup>235</sup> U	n	thermal	[23]
<sup>235</sup> U	n	0.06–130 eV	[24]
<sup>235</sup> U	n	0.5, 5.55	[25]
<sup>235</sup> U	n	0–6	[25]
<sup>235</sup> U	n	0.2–30	[26]
<sup>235</sup> U	n	3.2–50	[16]
<sup>237</sup> Np	n	0.80, 5.55	[27]
<sup>237</sup> Np	n	2.6–100	[28]
<sup>238</sup> U	p	8–13	[18]
<sup>238</sup> U	p	9.5–22	[19]
<sup>238</sup> U	n	1–30	[19]
<sup>239</sup> Pu	n	thermal	[20]
<sup>239</sup> Pu	n	thermal	[21]
<sup>239</sup> Pu	n	thermal	[29]
<sup>239</sup> Pu	n	0–5.5	[30]
<sup>239</sup> Pu	n	0.5–50	[22]
<sup>239</sup> Pu	n	2–100	[31]
<sup>240</sup> Pu	n	2–100	[32]
<sup>242</sup> Pu	n	2–100	[32]
<sup>245</sup> Cm	n	thermal	[13]
<sup>249</sup> Cf	n	thermal	[13]
<sup>254</sup> Es	n	thermal	[13]

system into kinetic energy of the fragment during the saddle to scission descent. This simple notion of Viola scaling Eq. 1 can be used to parameterize the important and complex subject of fission total kinetic energy release.

In Table 1, we summarize the available data on the TKE release in the fission of actinide nuclei induced by neutrons and protons. Authoritative summaries of the data for the neutron induced fission of <sup>235</sup>U, <sup>238</sup>U and <sup>239</sup>Pu are found in the work of Madland [11] and Lestone and Strother [12]. I omit discussion of the TKE release in transfer reactions and heavy ion induced reactions.

## Materials and methods

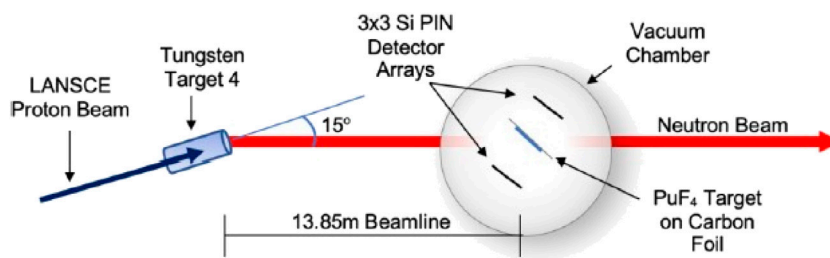
All the targets used in this work were made by vapor deposition. Vapor deposition avoids the presence of impurities in the target. Actinide oxides are converted to actinide fluorides in a dual glove box system. The actinide fluorides are vapor deposited onto thin carbon foils. Typical actinide thicknesses are 100 ug/cm<sup>2</sup>. The preparation of the targets and their characterization are described in [33].

## Experimental details

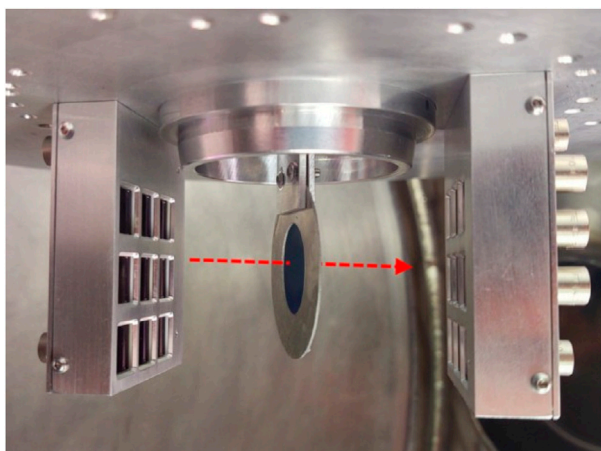
The experiments were carried out at the Weapons Neutron Research Facility (WNR) at the Los Alamos Neutron Science Center (LANSCE) at the Los Alamos National Laboratory (LANL) [34, 35]. “White spectrum” neutron beams were generated from an unmoderated tungsten spallation source using the 800 MeV proton beam from the LANSCE linear accelerator. The experiment was located on the 15R beam line (15° right with respect to the proton beam). The fast neutron beam intensities were ~10<sup>5</sup>–10<sup>6</sup>/s for E<sub>n</sub> = 2–100 MeV. The proton beam is pulsed allowing one to measure the time of flight (energy) of the neutrons arriving at the experimental area. The proton beam consists of a 625 us macro pulse containing about 340 micro pulses of width 250 ps that are spaced 1.8 us apart. The macro pulses had a repetition rate of 100 Hz. With neutron beam intensities of ~10<sup>5</sup>–10<sup>6</sup> n/s, one must use large solid angles for the detectors or long observation times or both to obtain statistically meaningful data.

The spallation neutrons from the LANSCE tungsten target traversed a 13.85 m flight path to the target position of our scattering chamber. The neutron beam was collimated to a 1 cm diameter at the entrance to the experimental area. At the entrance to the scattering chamber the beam diameter was measured to be 1.3 cm. A fission ionization chamber was used to continuously monitor the absolute neutron beam intensities. The targets and fission detectors were housed in an evacuated, thin-walled aluminum scattering chamber. The scattering chamber was located 55 cm from the collimator and ~14 m from the neutron beam dump.

Fission products were detected by eight to nine pairs of Si PIN diode detectors (Hamamatsu S3590-09) arranged on opposite sides of the beam at angles of ~60°–120° with respect to the incident beam.



**FIGURE 1**  
Schematic diagram of our experimental setup.



**FIGURE 2**  
Picture of detector arrays and target. The dashed arrow shows the expected beam trajectory.

the photofission peak in the fission time of flight spectrum and the observed time difference between the neutron timing signal and the accelerator RF signal. The uncertainties from each of the components of the calculation of the neutron energy were added in quadrature as uncorrelated uncertainties to determine the final uncertainty in the measured neutron energy. The neutron energies were thus determined with an average uncertainty of 4.7%. The neutron energies were generally binned logarithmically to give bins of equal associated uncertainty in neutron energy. The widths of these bins give the relative neutron energy resolution of our measurements. Our experimental setup is shown schematically in Figure 1.

The actual detailed arrangement of the detectors and target are shown in Figure 2.

We measure, on an event-by-event basis, the pulse heights of the coincident fission fragments. To transform these pulse heights into energies, we must correct for the pulse height defect in our Si PIN diode detectors and the energy losses of the fragments in the target and backing foil. To make these corrections, we need to estimate the masses of the fragment. To do this we use an iterative procedure. The fragment masses and total kinetic energies were deduced using the 2E method.

In the 2E method that we are using, we must assume conservation of momentum.

We need to (iteratively), correct for: (a) pre-equilibrium neutron emission (b) pre-fission neutron emission (c) the dependence of the post-neutron emission on fragment mass and (d) the mean atomic number associated with each post-neutron emission fragment.

### Predictions of the GEF and CGMF fission models for neutron multiplicity

The GEF (General Description of Fission Observables) model [36] is frequently used to estimate the pre-equilibrium, pre-fission, and post fission neutron emission.

GEF is a semiempirical code for predicting the outcomes of fast neutron induced fission reactions. It has ~50 free parameters in the code allowing it to do quite well in its predictions. GEF can be used to treat reactions with  $Z = 80$  to 112 and spontaneous and induced fission with excitation energies up to 100 MeV.

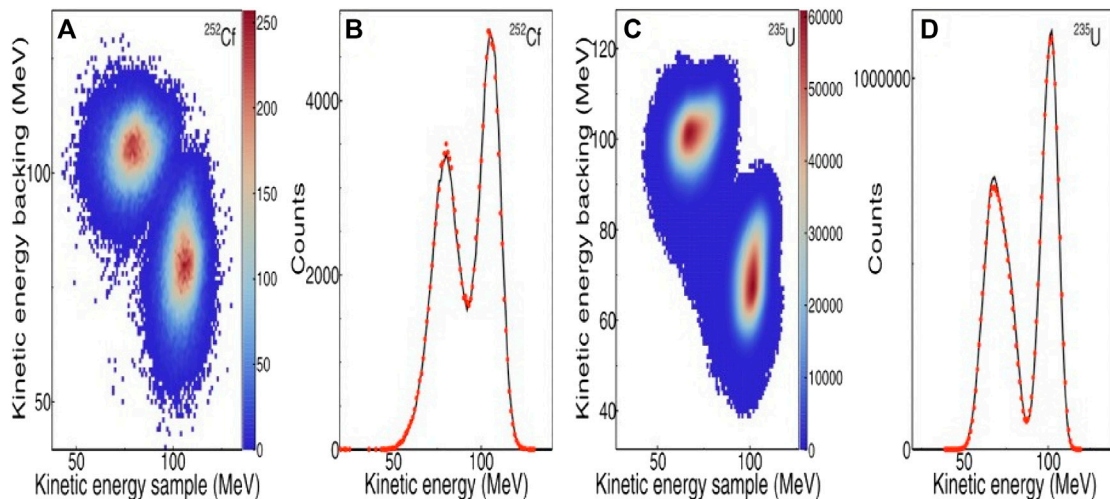
The CGMF (Cascade Gamma Multiplicities from Fission) model uses the ratio of the initial fragment temperatures to determine the

**TABLE 2** Mean total neutron multiplicity predicted by the GEF [36] and CGMF models for  $^{240,242}\text{Pu}$  (n,f).

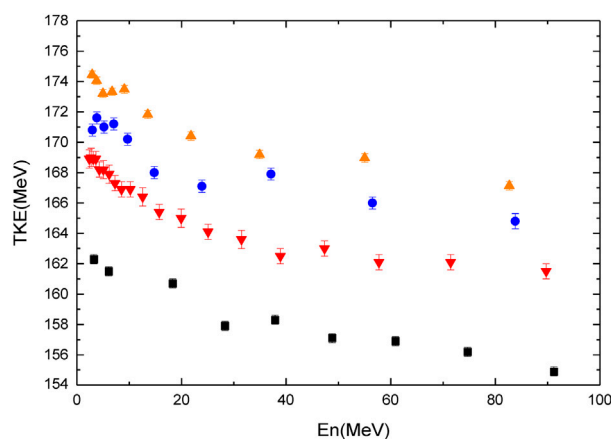
$E_n$ (MeV)	240-GEF	240 CGMF	242 GEF	242 CGMF
1	2.70	2.78	2.78	3.01
5	3.27	3.59	3.37	3.55
10	4.07	4.29	4.17	4.21
15	4.81	4.95	4.90	4.86
20	5.3	5.52	5.44	5.57

The area of the individual PIN diodes was  $1 \text{ cm}^2$ . The distance of the detectors from the center of the target was  $\sim 2.1 \text{ cm}$ .

The time of flight of each interacting neutron was measured using a timing pulse from a silicon PIN diode and the accelerator RF signal. As stated previously, the distance from the spallation target to the actinide target was measured to be  $1384.9 \pm 1.1 \text{ cm}$ . The position of the photofission peak in the time-of-flight spectrum was measured to have an uncertainty of 2.4%. The neutron energies were calculated using relativistic relationships, between the distance traveled by the neutrons, the mid-point of



**FIGURE 3**  
 The kinetic energy distributions for  $^{252}\text{Cf}$  in (A), (B), and  $^{235}\text{U}$  in (C) and (D). The energies from the sample side are plotted versus the energies from the backing side. The projections of the two-dimensional distributions are plotted in (B,D). The energies from the sample and backing sides are in good agreement. The data is from [43].



**FIGURE 4**  
 By the phrase “TKE distributions” we mean the mean value of the TKE distributions as a function of neutron energy. Average TKE measured by our group for the fast neutron induced fission of  $^{232}\text{Th}$ ,  $^{235}\text{U}$ ,  $^{237}\text{Np}$ , and  $^{239}\text{Pu}$ . See text for color code and further details.

partition of the excitation energy. The ratio of the fragment temperatures is correlated to the fragment deformation. The fragments near the  $Z = 50$  and  $N = 82$  closed shells are expected to be more spherical than the lighter fragments and as such to have lower excitation energies. Thus, their lighter partners will be more excited, resulting in higher associated neutron multiplicities. As shown in Table 2, the predicted total neutron multiplicities are similar in these models.

### Corrections for pulse height defect

The pulse height defect is defined as the difference between the true energy of a fission fragment and its nominal energy based upon an energy calibration of the detector with alpha

particles. This loss in energy is due to: (a) loss of energy of the fragment in the entrance window and dead layer of the detector (b) recombination of the electron-hole pairs created in the interaction of the fragment with the detector prior to charge collection and (c) loss of energy by nuclear stopping, an effect not that is not present in alpha particle interactions. For Si surface barrier detectors, the method of Schmitt et al. [37] is used to make the correction for pulse height defect which was 4.8–7.7 MeV. In measurements made with gas ionization detectors, a similar effect occurs but the magnitude of the energy loss is much less (pulse height defect = 2.5–4.5 MeV). All the measurements described in this work was made with silicon surface barrier detectors (SSB) or silicon pin diode detectors (PIN). The pulse height defect in Si PIN diode

**TABLE 3** The results of fitting the observed TKE release as a function of the energy of the neutron inducing fission for the systems we have studied.

Target nucleus	Constant term	Linear term	Quadratic term
$^{232}\text{Th}$	162.8 MeV	0.1884	1.866
$^{233}\text{U}$	165.5 MeV	2.0	
$^{235}\text{U}$	170.9 MeV	3.73	0.65
$^{237}\text{Np}$	$174.4 \pm 0.7$ MeV	$5.1 \pm 0.6$	
$^{239}\text{Pu}$	$177.1 \pm 1.0$ MeV	$4.9 \pm 0.8$	
$^{240}\text{Pu}$	$175.8 \pm 0.3$ MeV	$2.4 \pm 0.8$	$1.4 \pm 0.4$
$^{242}\text{Pu}$	$177.1 \pm 0.3$ MeV	$1.2 \pm 0.9$	$1.8 \pm 0.5$

detectors is believed to be the same as that observed in Si surface barrier detectors [38]. Additional data on corrections for pulse height defect can be found in the work of Pleasanton (F. Pleasanton [31]) where the thermal neutron induced fission of  $^{233}\text{U}$  is studied and the work of [32]) where a scheme like the Schmitt method is proposed.

## Corrections for the energy loss in the target and backing

Corrections for the energy loss of the fission products in the actinide deposits and the  $\sim 100$   $\mu\text{g}/\text{cm}^2$  C target backing foils were made using the Northcliffe -Schilling tables [39]. These tables are used instead of the relations in the widely used SRIM [40] code because it has been shown [41] that the  $dE/dx$  relations in SRIM misrepresent the correct  $dE/dx$  relations.

An important issue with respect to fragment energy losses in the target is the presence of “crud” in the target. “Crud” refers to the residues of solvent molecules that are frequently deposited when actinide targets are prepared by molecular plating. This “crud” material is of generally unknown composition. The best solution to this problem is to prepare the actinide deposits by vapor deposition. When that is not possible, one must use the well-known values of the TKE release for thermal neutron induced fission to make corrections for the presence of this “crud” material.

The effect of the target backing upon the measured TKE values is discussed in the work of A. Al-Adili et al., [42].

In Figure 3, I show the kinetic energy distributions for the fission fragments (after neutron emission) for the spontaneous fission of  $^{252}\text{Cf}$  and the thermal neutron induced fission of  $^{235}\text{U}$ . The point of this figure is to show that the fragment energies deduced in this work have proper corrections for energy losses in the target and backing materials.

Recent work on the preparation of targets for research on heavy and superheavy nuclei can be found in the review article of Lommel, Dullmann, Kindler and Renisch, [44].

## Benchmarking

To benchmark the experimental method, the TKE release in the thermal neutron induced fission of  $^{235}\text{U}$  was measured/

deduced. The measured/deduced value of the TKE release was  $170.0 \pm 0.15$  MeV compared to the known value of 170.1 MeV for the  $^{235}\text{U}$  (n,f) reaction (16). Thus, no normalizations of the data were needed and thus our measurements are absolute measurements.

## Results

### General observations

The TKE distributions for each system studied, i.e., the fast neutron ( $E_n = 3\text{--}100$  MeV) induced fission of  $^{232}\text{Th}$ ,  $^{233}\text{U}$ ,  $^{235}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{239}\text{Pu}$ ,  $^{240}\text{Pu}$ , and  $^{242}\text{Pu}$ , were Gaussian in shape. The words “TKE distributions” refer to the fragment energies after neutron emission, The words “TKE distributions” refer to the fragment energies after neutron emission.

### TKE distributions

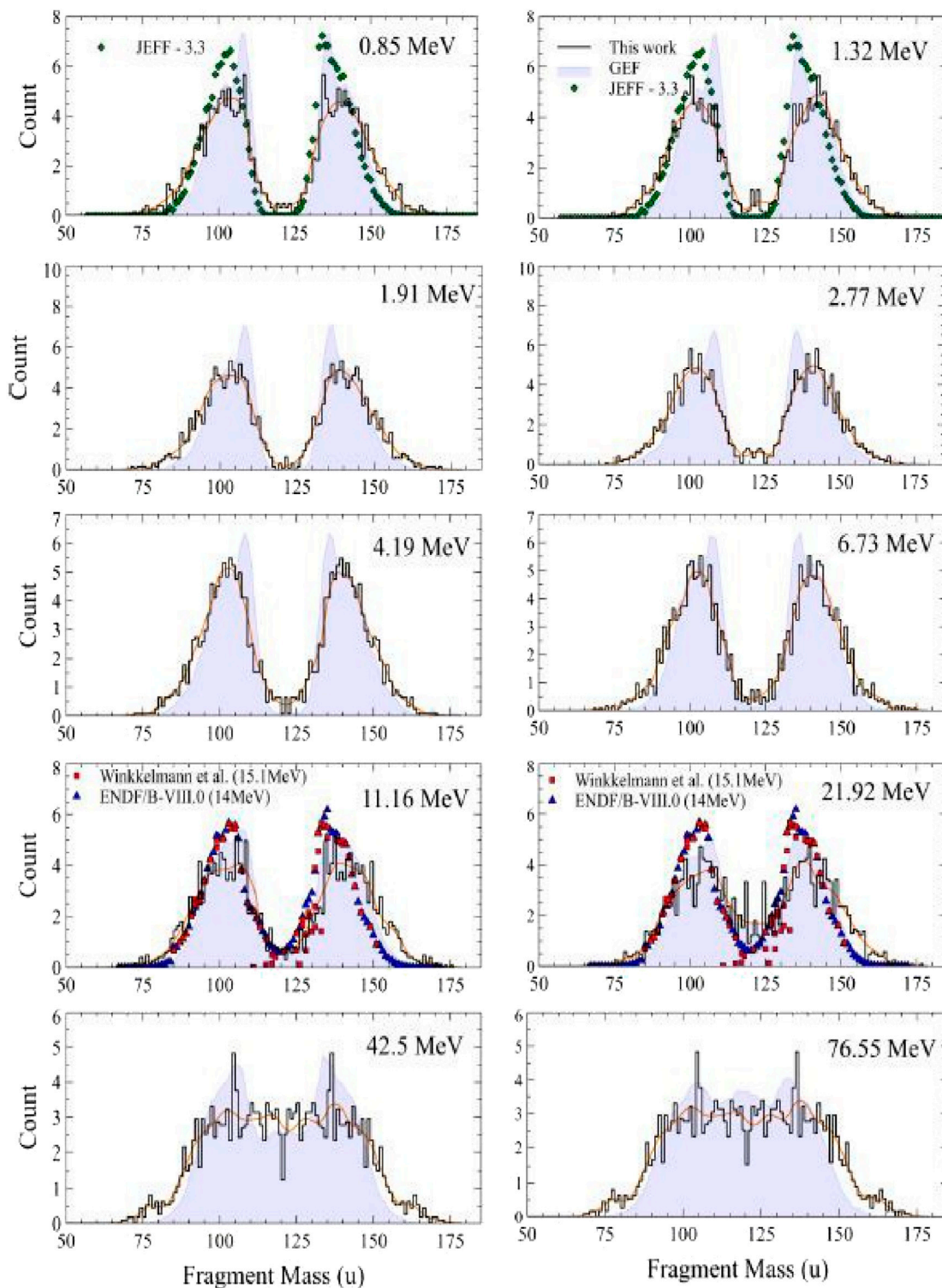
The measured TKE distributions in the fast neutron induced fission of  $^{232}\text{Th}$  (black squares)  $^{235}\text{U}$  (red triangles)  $^{237}\text{Np}$  (blue circles) and  $^{239}\text{Pu}$  (orange triangles) are shown in.

In general, the dependence of the mean TKE on neutron energy is similar for each of the reactions studied with the obvious point that the absolute values of the TKE increase with the Z of the fissioning system.

Earlier, I mentioned the role of Viola scaling in describing the general shape of the TKE distributions. The Viola systematics would predict TKE values of 170.1 and 163.8 MeV for the thermal neutron induced fission of  $^{235}\text{U}$  and  $^{232}\text{Th}$ , respectively. The Viola predictions are in remarkable agreement with the observed values (Figure 4). Thus, we can conclude that Viola scaling describes the essential physics of the scission point. (We can extend these calculations to include  $^{237}\text{Np}$  (which is not thermally fissionable) and  $^{239}\text{Pu}$  which is thermally fissionable and the predictive power of Viola scaling holds).

Let’s pick “representative” values of the neutron energy like 10 and 20 MeV. Extrapolating in Figure 4, we deduce measured values of the TKE of 161, 166.5, 170, and 173.5 MeV for the case of  $E_n = 10$  MeV for the fast neutron induced fission of  $^{232}\text{Th}$ ,  $^{235}\text{U}$ ,  $^{237}\text{Np}$ , and  $^{239}\text{Pu}$  and 160.5, 165, 167.5, and

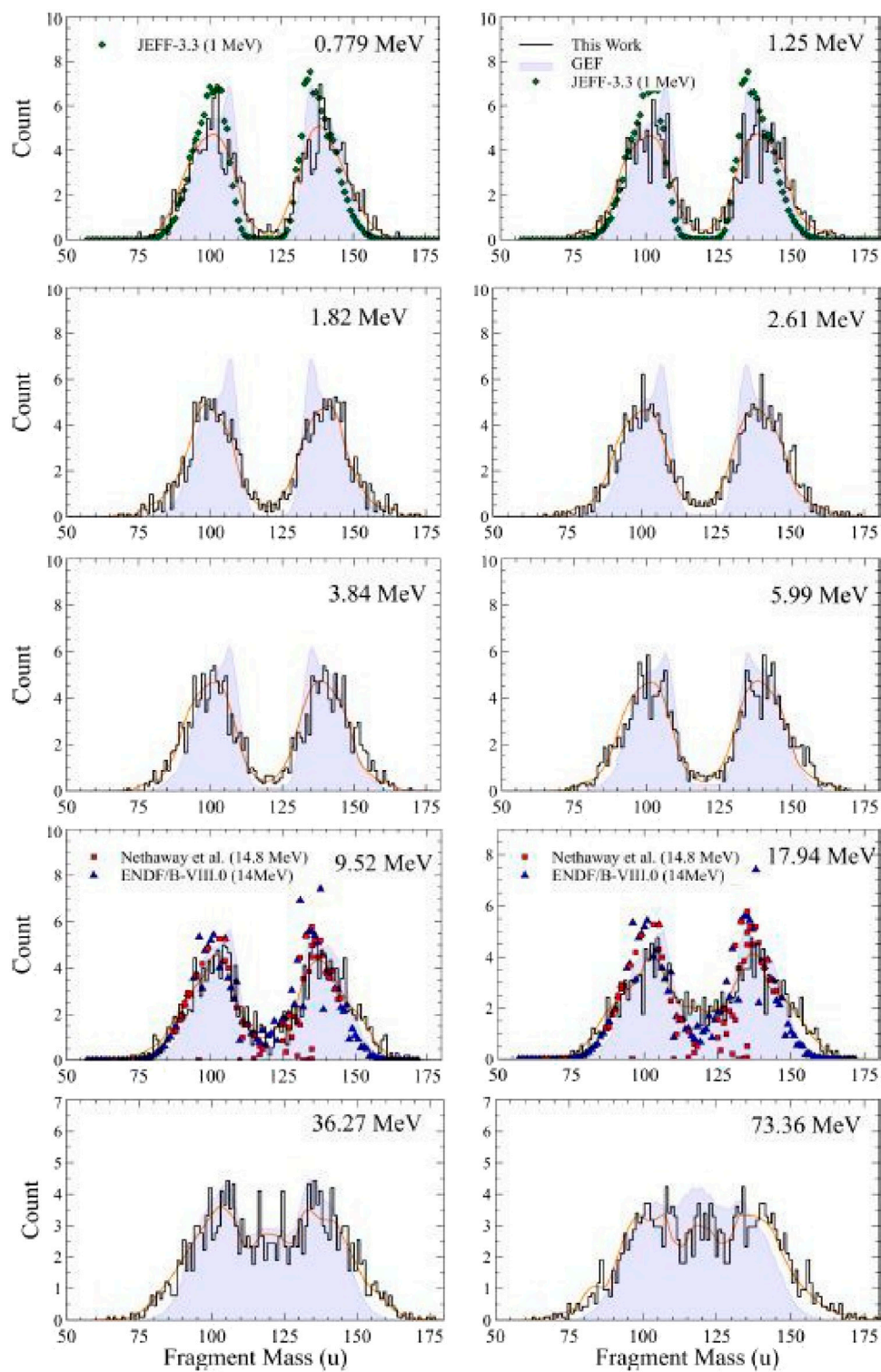




**FIGURE 5**  
 Comparison of the measured values of the mass distributions for the  $^{240}\text{Pu}$  ( $n,f$ ) reaction with previous measurements (Winkelmann et al. [41]), the ENDF model (ENDF) [42] and the semiempirical JEFF 3.3 [45] and GEF [26] models.

171.5 MeV for  $E_n = 20$  MeV for the fast neutron induced fission of  $^{232}\text{Th}$ ,  $^{235}\text{U}$ ,  $^{237}\text{Np}$ , and  $^{239}\text{Pu}$ . One can compare these measurements with the predictions of the Viola formula for

spontaneous and thermal neutron induced fission to understand the effect of increasing the energy of the neutron inducing fission.



**FIGURE 6**  
 Measured fission mass distributions for  $^{242}\text{Pu}(n,f)$  reaction and comparisons with previous work (Nethaway [44]), ENDF [42] estimates and calculations of the GEF [26] and JEFF [45] codes.

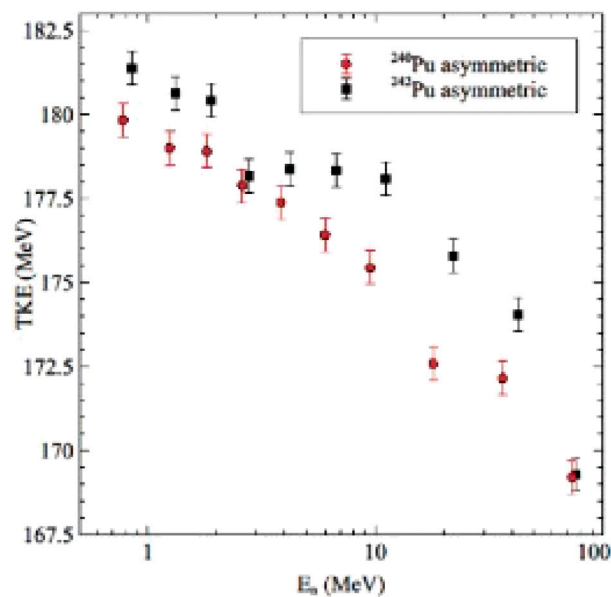


FIGURE 7  
The TKE release in the asymmetric fission of  $^{240,242}\text{Pu}$ .

## Other detailed models of TKE distributions (arranged chronologically) or “Works on TKE distributions over time.”

Among the earliest papers on the TKE release in the fast neutron induced fission of actinide nuclei was the paper of Bishop et al. [19]. In a study of the proton induced fission of  $^{233}\text{U}$  and  $^{238}\text{U}$ , [19] measured the energies and yields of the neutrons emitted from the fission fragments of known mass. They found a washing out of the sawtooth dependence of the emitted neutrons on fragment mass with increasing excitation energy with the effect being most pronounced for the heavy fragment. Bishop et al. presented data on the total fragment kinetic energy as a function of the proton energy.

A useful early compilation of the TKE release in the fission of  $^{239}\text{Pu}$  (n,f) in steps of 100 keV for neutron energies from 0 to 5.5 MeV is found in the work of N.I. Akimov et al. [45].

Bjornholm [46] related the fine structure of the mass yields and total kinetic energy of the even nuclides to the possibility of superfluid vs. a viscous descent from saddle to scission.

One of the most interesting and comprehensive early treatments of low energy fission of the actinides was the work of Wilkins, Steinberg and Chasman [47]. These authors proposed a static model that assumed statistical equilibrium among the collective degrees of freedom at the scission point. The general trends of the mass, charge, and kinetic energy distributions for a large range of nuclei from Po to Fm were correctly described. The role of deformed shell corrections for neutrons was emphasized.

Scheuter, Gregoire, Hofmann and Nix [48], calculated the fission total kinetic energy distributions for the fission of  $^{213}\text{At}$ , using a two-dimensional Fokker-Planck equation.

These authors showed how the effects of spreading in the stretching degree of freedom and fluctuations in the fission

degree of freedom affected the TKE distributions. The Fokker-Planck equation is also the basis of papers describing the mass-energy distributions of fission fragments and the dependences of the mean kinetic energy for a wide variety of heavy nuclei ranging from Hg to Pu [49]. A two-dimensional diffusion model is also used to describe the TKE release [50].

H.R. Faust [51] showed that a statistical model can reproduce the mean values of the fragment kinetic energy for compound systems ranging from  $^{219}\text{Ac}$  to  $^{258}\text{Fm}$  very accurately. The variances of the TKE distributions were also well reproduced. These calculations also gave the total excitation energy in the systems studied.

Wada, Abe and Carjan [52] studied the fission dynamics of hot nuclei using two dimensional Langevin equations. The pre-scission multiplicities of neutrons, protons and alpha particles were calculated. The average total kinetic energy of the fission fragments was correctly calculated when one body dissipation was assumed. They assumed a strong dissipation mechanism and a compact scission configuration.

[53] have made several important contributions to understand the total kinetic release in fission. Starting with the Los Alamos model of the TKE release, they were able to use semi-empirical models to correctly describe the TKE release in the fission of  $^{232-226}\text{Th}$ ,  $^{233-224}\text{Pa}$ ,  $^{238-229}\text{U}$ ,  $^{237-231}\text{Np}$ ,  $^{242-235}\text{Pu}$  and  $^{245-240}\text{Am}$ . Manea and Tudora proposed a simple approach for the calculation of the fission fragment total kinetic energy, TKE(A), based on the electrostatic repulsion between the fragments connected by a neck in the pre-scission configuration is described. The calculated TKE(A) is obtained in good agreement with the experimental data for many fissioning systems in the EXFOR library, such as  $^{233,235}\text{U}$  (nth, f),  $^{239}\text{Pu}$  (nth, f),  $^{237}\text{Np}$  (n, f), and  $^{242}\text{Pu}$  (SF), with minor adjustment of only **one** parameter, the neck length. This lack of a dependence



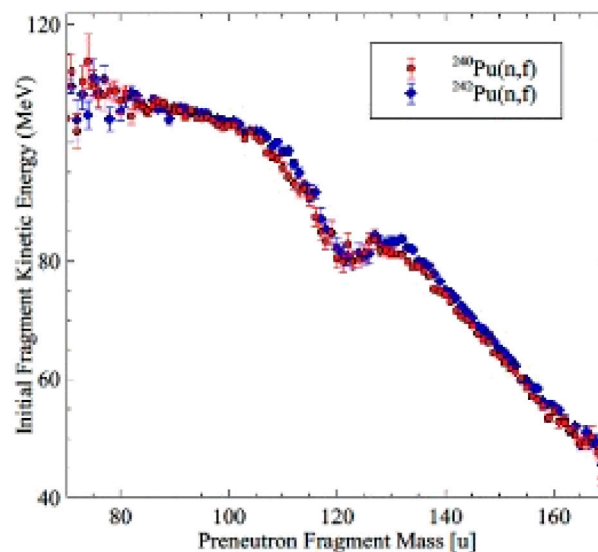


FIGURE 8  
Fragment KE as a function of pre-neutron fragment mass for  $E_n < 5$  MeV.

of the TKE upon the excitation energy of the fissioning system is interesting.

V.M. Maslov has written several review articles that attempt to summarize the data on fast neutron induced fission of Th, Pa, U, Np, Pu and Am. Special attention is given to the role of symmetric and asymmetric fission in these systems [54].

Simenel and Umar [55] have studied the symmetric fission of  $^{258}_{264}\text{Fm}$  using a time dependent Hartree-Fock method. They showed that non-adiabatic evolution affects the kinetic and excitation energies of the fragments. Low-lying collective vibrations are more easily excited than giant resonances.

Sierk [43] used a Langevin model to calculate various features of fission at low to medium excitation energies. After benchmarking his calculational results to  $^{235}\text{U}(n,f)$ , Sierk was able to reproduce the properties of the TKE release in a number of nuclei.

Chebbouhi et al. [56] made a theoretical investigation of the fission fragment kinetic energy distributions in the symmetric mass region for the  $^{233}\text{U}(n,f)$  reaction. The Monte Carlo code FIFRELIN was used along with the Brosa model to get the kinetic energy distributions. The effect of energy losses in the measurements was considered.

The fission of the even-even isotopes of Hs to Og is studied in the work of Carjan, Ivanyuk and Oganessian [57]. For the isotopes of Hs, Ds, and Cn, a transition from symmetric to asymmetric fission is predicted for increasing neutron number.

Supersymmetric fission occurs at  $N \sim 160$ . The mean values of the TKE are predicted for  $Z = 108\text{--}118$  along with the variances of the TKE distributions.

Randrup and Vogt [58] have made several important contributions to our understanding of the physics involved in the fast neutron induced fission of actinide nuclei using their code FREYA. In their FREYA calculations, they specified the A, Z,  $E^*$  of the fissioning system and FREYA calculated the A and Z of both

fission fragments and the total kinetic energies. Angular momentum was specifically accounted for in the calculations.

Specifically, FREYA does the calculation for the spontaneous fission of  $^{238}\text{U}$ ,  $^{238}\text{Pu}$ ,  $^{240}\text{Pu}$ ,  $^{242}\text{Pu}$ ,  $^{244}\text{Cm}$  and  $^{252}\text{Cf}$  along with the neutron induced fission of  $^{233}\text{U}$ ,  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{239}\text{Pu}$ , and  $^{241}\text{Pu}$  at neutron energies up to 20 MeV. The rotational and statistical excitations of the fragments are considered. Angular momentum conservation is considered at pre-scission, scission, and post-scission stages. The nuclei are allowed to rotate and evaporate neutrons and then photons.

Three and four dimensional Langevin calculations of the TKE release in fission were made by Usang and co-workers [59]. Similar Langevin calculations were done by a Chinese group [60]. The paper by Ishizuka et al. focused on the low energy fission of  $^{236}\text{U}$ , while the work of Usang et al. treated a larger number of systems. The three-dimensional calculations do not describe the data as well as the four-dimensional calculations and the four-dimensional calculations do a better job of describing the Brosa modes.

Jaffke, Moller, Talou and Sierk [61] combined information from calculated macroscopic-microscopic calculations of the mass yields with a de-excitation model based on Hauser-Feshbach statistical decay theory. The authors restricted their attention to the thermal neutron induced fission of  $^{235}\text{U}$  and  $^{239}\text{Pu}$  where the experimental data is relatively well known. The uncertainties in the TKE release were estimated to be 0.3%–0.8% for  $^{235}\text{U}$  and 0.1%–0.2% for  $^{239}\text{Pu}$ .

Li-Le Liu et al. [62], used a Langevin approach to study the fission of  $^{233,236,239}\text{U}$  and  $^{239}\text{Pu}$  at low excitation energies. Their calculations describe the details of the fast neutron reactions studied.

A fully microscopic scission-point model is used to predict the fission fragment observables in the thermal neutron induced fission of  $^{235}\text{U}$ ,  $^{239}\text{Pu}$  and the spontaneous fission of  $^{252}\text{Cf}$  by Lemaitre, Goriely, Hilaire and Sida [63]. The model, called the SPY2 model, is said to be fully microscopic and involves the properties of

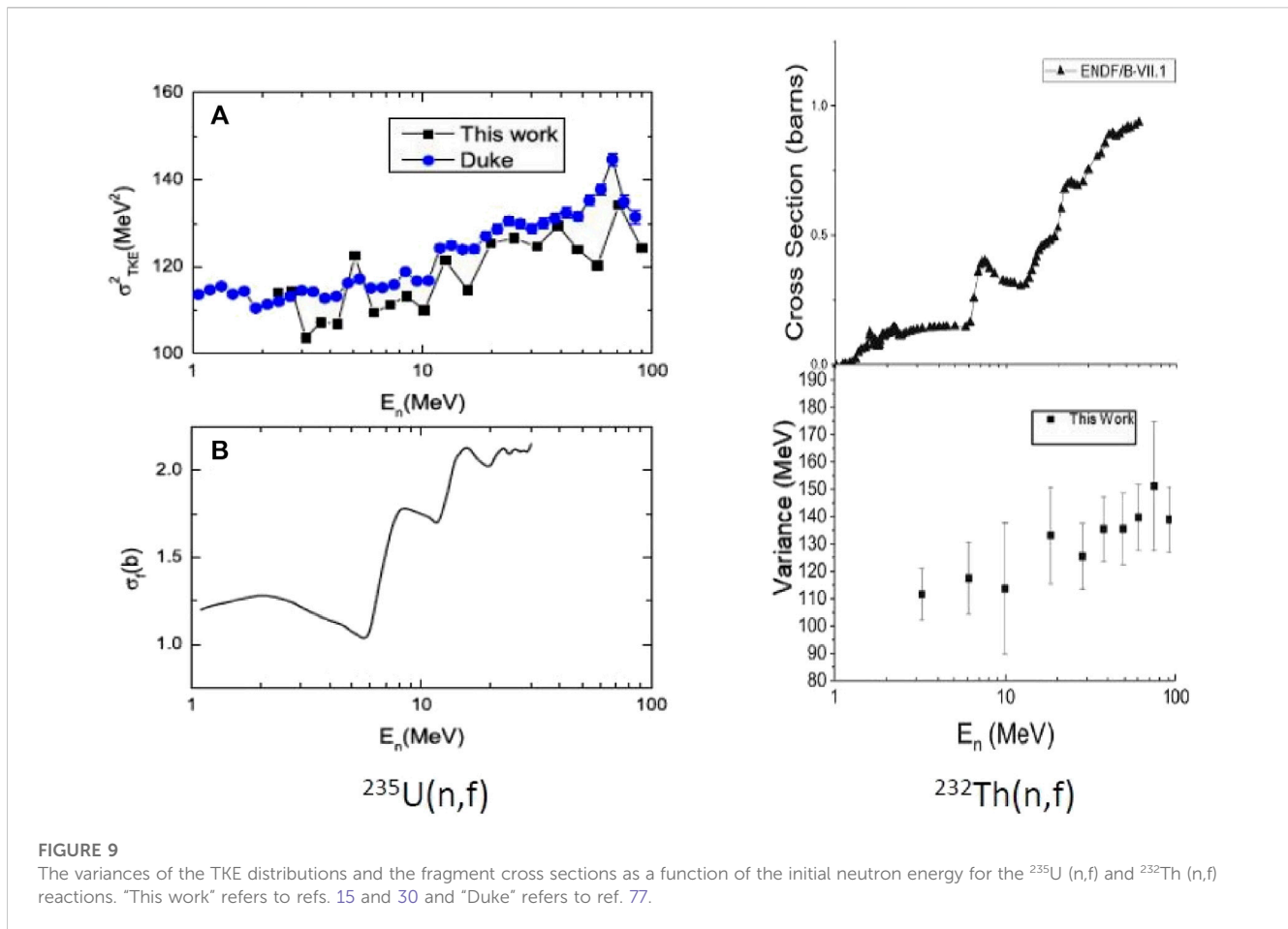


FIGURE 9

The variances of the TKE distributions and the fragment cross sections as a function of the initial neutron energy for the  $^{235}\text{U}(n,f)$  and  $^{232}\text{Th}(n,f)$  reactions. "This work" refers to refs. 15 and 30 and "Duke" refers to ref. 77.

7,000 nuclei. The use of this input of real data improves the predictive abilities of the model.

Kaldiani made a study [64] of the kinetic energy distribution the photofission of the light actinides. The deformation parameters of the fission fragments have a large change near the symmetric region. Kaldiani studied the TKE distributions for neutron-induced fission, spontaneous fission and photofission to predict the actinide TKE distributions. The TKE distributions are similar for all nuclei but the TKE distribution for spontaneous fission are different.

In a series of papers, Lovell and co-workers [Phys. Rev. C **100**, 054610 (2019), Phys. Rev. C **102**, 024621 (2020), Phys. Rev. C **103**, 014615 (2021)], used the fission event generator CGMF to study various aspects of the correlations between fission observables in fast neutron induced reactions. Among the reactions studied were  $^{233,234,235,238}\text{U}$ ,  $^{239, 241}\text{Pu}$ , and  $^{237}\text{Np}(n,f)$ .

Albertson and coworkers [Eur. Phys. J. A **56**, 46 (2020); Phys. Rev. C **103**, 014609, (2021)] made a series of encyclopedic studies of fast neutron induced fission that involved the calculation of fission-fragment mass yields and average total kinetic energies for 896 e-nuclei ( $74 < Z < 126$ ,  $92 < N < 230$ ) as well as the total kinetic energy and its uncertainty for  $^{235}\text{U}(n,f)$  for thermal and 5.5 MeV neutrons. In the latter studies, the correlation between the fragment properties and the TKE distributions are discussed in detail.

Bulgac [Phys. Rev. C **102**, 044609 (2020)] points out that fission fragments share excitation energy long after they stop exchanging

nucleons, leading to a lower total kinetic energy of the fission fragments.

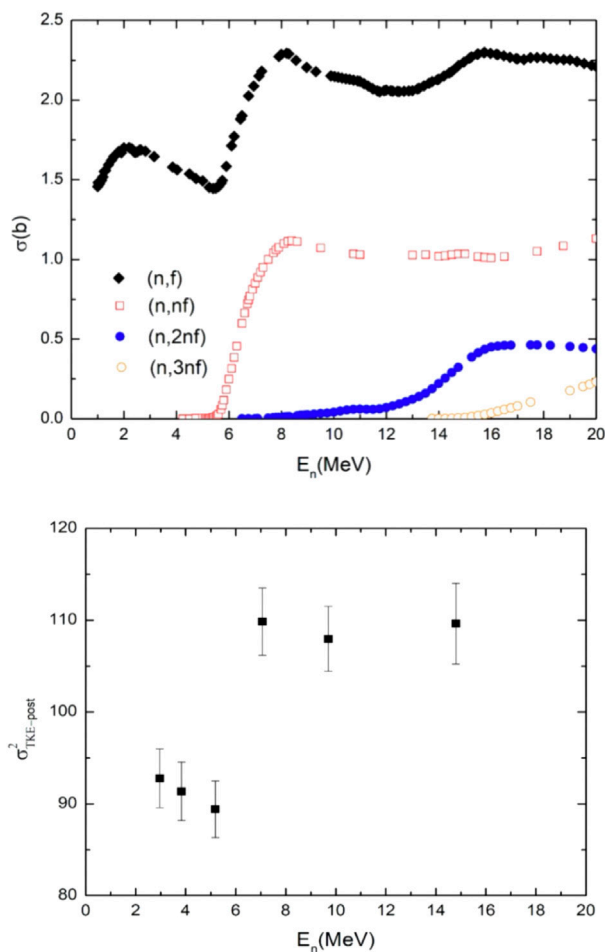
An "improved" scission-point model is used by H. Pasca, A.V. Andreev, G.G. Adamian and N.V. Antonenko [Phys. Rev. C **104**, 014604 (2021)] to provide a simultaneous description of the charge, mass, total kinetic energy and neutron multiplicities for the  $^{222}\text{Th}$ ,  $^{226}\text{Th}$ ,  $^{230}\text{Th}$ ,  $^{230}\text{U}$  and  $^{234}\text{U}$  at 11 MeV. Detailed comparisons of theory and experiment are provided. For induced fission of  $^{250}\text{Cf}$ , the TKE distributions are calculated and found to agree with measurements.

L. Tong and S. Yan [Phys. Rev. C **106**, 044611 (2022)] make time-dependent Hartree-Fock-Bogoliubov calculations of symmetric and asymmetric fission of  $^{240}\text{Pu}$ . The calculations agree with the measured data for  $^{240}\text{Pu}$ .

V. Yu Denisov and I. Yu. Sedykh describe the data on the average total kinetic energy of the fission fragments in the fission of  $^{234,236, 239}\text{U}$  and  $^{240}\text{Pu}$  using a simple expression. [Phys. Lett B **824**, 136814 (2022)].

In a review article in this journal, D. Neudecker et al., Frontiers Phys. **10**:1056324 (2023) reported the TKE values for the fast neutron induced fission of  $^{239}\text{Pu}$  and compared the measurements and the CGMF model for  $E_n = 0\text{--}20$  MeV. The need for further experiments is clearly indicated.

Li et al. present time-dependent density functional theory calculations for the fast neutron induced fission of  $^{240}\text{Pu}$ ,  $^{234}\text{U}$ ,  $^{244}\text{Cm}$  and  $^{250}\text{Cf}$ . The partition of the initial energy of the system



**FIGURE 10** (A) The cross section for the  $^{237}\text{Np}(n,f)$  reaction from the evaluated nuclear data file (ENDF)/B=VIII and ENDF/B-VI. (B) Measured TKE variance vs.  $E_n$  for this reaction.

into the various components at scission is traced out. (Phys. Rev. C **107**, 014303 (2023).)

### GEF, CGMF and FREYA

There are certain omnibus approaches to predicting the outcome of fast neutron induced fission of heavy nuclei. Three such codes are GEF, FREYA and CGMF. As remarked earlier, GEF is a semiempirical code for predicting the outcomes of fast neutron induced fission reactions. It has ~50 free parameters in the code allowing it to do quite well in its predictions. GEF can be used to treat reactions with  $Z = 80$  to 112 and spontaneous and induced fission with excitation energies up to 100 MeV. A benchmark paper [C. Schmitt, K.-H. Schmidt and B Jurado, Phys. Rev. **98**, 044605 (2018)] provides a summary description of the code and its use.

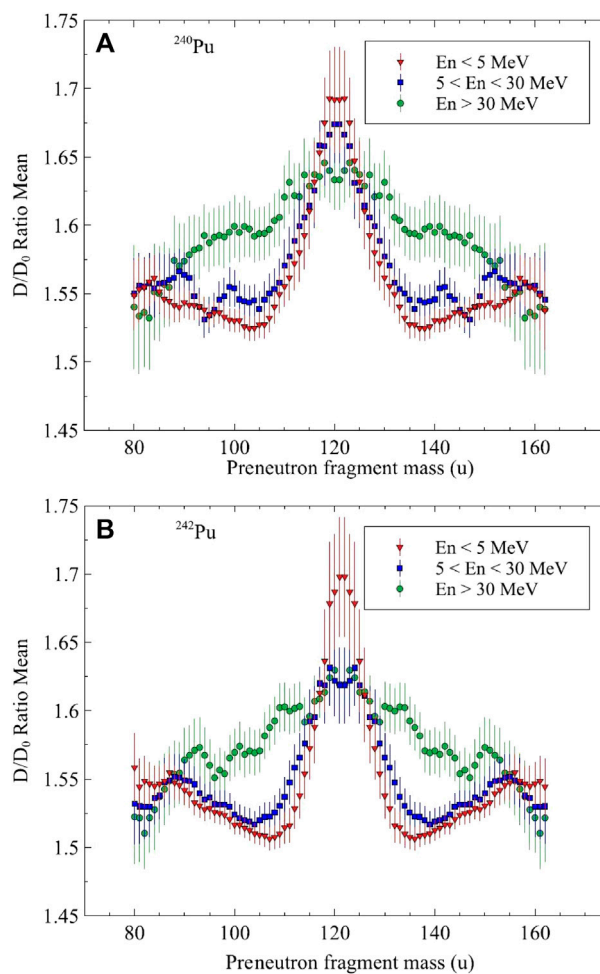
The CGMF code is a Monte Carlo implementation of the statistical Hauser-Feshbach nuclear reaction theory applied to the de-excitation of primary fission fragments. CGMF requires an input of fission fragment mass, charge, and kinetic energies. From these

inputs, the code calculates the final cross sections. There is no statistical difference between the TKE values calculated by the CGMF and GEF codes.

FREYA is a more complete model that provides the full kinematic information on the two product nuclei and the emitted photons and neutrons. The input for FREYA is the fission mass distributions and the average total kinetic energy. FREYA treats spontaneous fission and neutron induced fission (up to 20 MeV). FREYA is described in J.M. Verbeke, J. Randrup and R. Vogt, LLNL-SM-705798, and M. Verbeke, J. Randrup and R. Vogt, Comp. Phys. Communication, **222**, 263 (2018)

### Contributions of the Oregon State group

I would be remiss if I did not specifically mention the contributions of the Oregon State group to the study of the fast fission of the actinide nuclei. The TKE release in the fast neutron induced fission of  $^{232}\text{Th}$  was studied by King et al. while similar studies of the TKE release in the fast fission of  $^{235}\text{U}$  were made by



**FIGURE 11**

A rolling average ratio of the distance between the charge centers of the fragments at scission and that of spherical touching nuclei ( $D/D_0$ ) for  $^{240}\text{Pu}$  ( $n,f$ ) (A) and  $^{242}\text{Pu}(n,f)$  (B).

Yanez et al. The TKE release in the fast fission of  $^{237}\text{Np}$  was studied by Pica et al. The TKE release in the fast fission of  $^{239}\text{Pu}$  was studied by Chemey, Pica, Yao, Loveland, Lee and Kuvín. The TKE release in the fast fission of  $^{240}\text{Pu}$  and  $^{242}\text{Pu}$  were made by Pica, Chemey, and Loveland. Yao and co-workers studied the fast fission of  $^{241}\text{Am}$ . (See References for details).

## Polynomial fits to the observed TKE distributions

The mean post neutron emission TKE release decreases nonlinearly with increasing neutron energy. In Table 3, we give the results of fitting, using a quadratic equation, the observed TKE distributions as a function of energy of the neutron inducing fission for the systems we have studied.

While one can see the expected general increase in the TKE values with increasing  $Z$  and  $A$  of the fissioning system, there are some strange “bumps (errors??)” in the data such as the data for  $^{240}\text{Pu}$ . When an entry in Table 3 is blank, that means the term is not statistically significant in the fitting procedure. Also, the reader

should not take the data described in Table 3 as an attempt to create an “energy dependent” Viola model.

## Measurement of the $^{240,242}\text{Pu}(n,f)$ mass and kinetic energy distributions

Our most recent work has involved measuring the total kinetic energy release in the fast neutron induced fission of  $^{240,242}\text{Pu}$ . Our measurements of the fission fragment mass distributions for the  $^{240,242}\text{Pu}(n,f)$  reactions can be compared to previous work and some semiempirical models (Figures 5, 6). The agreement of the measured data and the semi-empirical models is excellent, suggesting we can correctly measure the fragment mass distributions in the fast neutron induced fission of  $^{240,242}\text{Pu}$  and can understand the data in terms of accepted models for these reactions.

The fission mass distributions show the expected evolution from asymmetric fission at low neutron energies to symmetric fission at higher neutron energies. If we focus our attention on the events involving asymmetric fission, we get the results shown in



Figure 7, where we show the TKE release in the asymmetric fission events.

The data clearly show the expected decrease in the TKE release with increasing neutron energy but there are some “bumps and wiggles” in the data. The observed TKE decrease with increasing  $E_n$  is a consequence of two factors: shell effects fade out at high excitation energies and the TKE associated with asymmetric fission decreases due to changes in the fragment shapes. (See Ref. [65]).

The data for low neutron energies is shown in Figure 8.

The data clearly show the importance of shell closures near  $A = 134$  reflecting the extra stability of  $Z = 56$ , due to octupole deformation. The data are in general agreement with the predictions of the GEF model but with smaller jumps in the TKE release at  $n$ th chance fission energies. Similar agreement with the predictions of the CGMF model are observed. (See the work of Pica et al., Phys. Rev. C 106, 044603 (2022) for examples).

## Variations of TKE distributions

One of the findings in our TKE data was the values of the variances of the TKE distributions. The features of the variances were: (a) the variances decrease as  $(Z, A)$  of the fissioning system increases (b) the variances are larger than expected from conventional models of scission (c) the variances show “bumps” at the onset of second chance, third chance, etc. fission.

Note the similarities between the measurements of Duke et al. and our data for the  $^{235}\text{U}$  (n,f) reaction (Figure 9). Also please note the relative insensitivity of the variances to the large changes in the fission cross sections with increasing neutron energy. The variances, while important measures of the physics, are difficult to measure.

In Figure 10, we observe a significant increase in the measured variance at the onset of second chance fission ( $\sim 7$  MeV). For a detailed discussion of these trends in the variances, the reader is referred to the work of Pica et al. [28, 66].

## Fragment shapes at scission

We can transform the TKE distributions into representations of the shapes of the fragment at scission (Figure 11). The details of this analysis can be found in [66]. References 67–69, 70, 71, 72, 73, 74, 75–78 contain additional information about the fast neutron induced fission of actinide nuclei.

## Summary of paper

What have we learned from this review of the fast neutron induced fission of actinide nuclei? We begin with a summary of prior work (Materials and Methods). We discuss Experimental Details with separate discussions of Corrections for Pulse Height Defect and Corrections for Energy Loss in the Target and Backing. We interpose a discussion of the GEF and CGMF models. We then discuss

Benchmarking of our data and our results (Experimental Observations, TKE distributions and Other detailed models of TKE distributions.) We then return to a more in-depth discussion of the GEF, CGMF and FREYA models. At this point, it seemed important to specifically call out the Contributions of the Oregon State Group. The most recent data is discussed in sections on the measurements of  $^{240,242}\text{Pu}$ , the variances of the TKE distributions and the fragment shapes at scission.

## Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

## Author contributions

The author confirms being the sole contributor of this work and has approved it for publication.

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## Conflict of interest

The author declares that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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