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Frequency shift properties of a calcium beam optical clock

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The optical frequency transitions with long-lifetime spin triplet states produced by the two valence electrons in the outermost layer of alkaline earth atoms make calcium atom a promising quantum frequency reference. Electronshelving detection improves the signal-to-noise ratio of the clock transition spectrum, enabling a calcium atomic beam optical frequency standard. This scheme employs the ${}^{1}S_{0}$ - ${}^{1}P_{1}$ transition at 423 nm to detect the ${}^{1}S_{0}$ - ${}^{3}P_{1}$ transition at 657 nm, emphasizing the importance of 423 nm laser stability. While the performance of these clocks is well-studied, research on the atomic beam itself is limited. This study investigates frequency shifts in neutral calcium atoms' ${}^{1}S_{0}$ - ${}^{1}P_{1}$ transition at 423 nm and their ${}^{1}S_{0}$ - ${}^{3}P_{1}$ transition at 657 nm. We measure the frequency shift caused by temperature, laser power, and laser alignment, providing insights to optimize the design of the calcium beam's physical apparatus.

KEYWORDS

optical clock, frequency standard, frequency shift properties, electron-shelving detection, fielded optical timekeeping

1 Introduction

Optical frequency standards are essential in various fields, including fundamental scientific research and technical innovations [1-3]. At present, significant research efforts have been dedicated to the development of optical clocks, encompassing both ion-based optical clocks and lattice optical clocks [4-9]. The majority of existing optical frequency standards rely on cold atoms or ions, which necessitate large volumes and fragile and complex systems with limited up-time [10-12]. These configurations are suitable for frequency primary standards. Atomic beam optical clocks offer the benefits of a high signalto-noise ratio and miniaturization, making them advantageous for both laboratory-based and field-deployed timekeeping. Their applicability extends across positioning, navigation, and timing applications in civilian, commercial, and defense sectors [13-15]. Numerous research groups have developed several optical clocks based on atomic beams, utilizing strontium beams [16, 17], ytterbium beams [18], and calcium beams [19]. The relatively narrow natural linewidth of 375 Hz in calcium and commercial lasers make calcium an optimal atomic choice for achieving miniaturized thermal atomic beam frequency standard. In 1999, the Physikalisch-Technische Bundesanstalt (PTB) pioneered the first calcium atomic beam optical clock [20]. Peking University has done seminal work for the calcium beam frequency standard, which first proposed the electron-shelving detection scheme [21] and the velocity grating method [22]. In 2019, researchers at National Institute of Standards and Technology (NIST) demonstrated a stability of less than 6×10^{-16} at 1 s, which decreased



to less than 2×10^{-16} at 1,000 s by utilizing the Ramsey spectrum on calcium beams [23]. Their stability results exceed the performance of other thermal atomic or molecular systems by 1–2 orders of magnitude. The United States Naval Observatory (USNO) advanced this achievement by employing the spectroscopy laser modulation in a laser-cooled calcium beam, which increased the Ramsey fringe amplitude by a factor of 14 and improved the Allan deviation to 3.4 $\times 10^{-15}$ at 1 s [24].

While the majority of research groups focus on the performance of clocks, relatively little attention has been given to the study of atomic beams themselves. A research team at USNO has analyzed variations in clock frequency to assess the limits on the long-term frequency stability of a calcium atomic beam optical clock [25]. Meanwhile, another group has evaluated various perturbative effects in a strontium clock, including first- and second-order Doppler and Zeeman effects, AC Stark shift, collisional shifts, and the mechanical effects of light [26]. However, no studies to date have reported results on the frequency shifts of both the clock laser and the probe laser. The study investigates the frequency shift properties of the ${}^{1}S_{0}$ - ${}^{3}P_{1}$ 657 nm clock transition and the ${}^{1}S_{0}$ - ${}^{1}P_{1}$ 423 nm transition, which facilitates the detection mechanism of the narrow clock transition [21]. It quantifies the frequency variations induced by temperature fluctuations, laser power, and laser alignment. These findings guide the development of high-performance physical apparatuses for atomic beam optical clocks using the electronshelving detection scheme and offer a framework for parameter optimization.

Figure 1 presents the atomic energy levels of calcium. The 423 nm transition from the ground state $4s4s^1S_0$ to the excited state $4s4p^1P_1$ serves as a spectroscopic detection tool, exhibiting a short energy level lifetime of approximately 4.6 ns as a cycling transition. Meanwhile, the 657 nm transition from the ground state $4s4s^1S_0$ to the excited state $4s4p^3P_1$ serves as the clock transition [27], featuring a 375 Hz linewidth and a 0.4 ms lifetime. Direct detection of the 657 nm clock transition yields a low signal-to-noise ratio. To enhance detection, we use electron-shelving detection, leveraging the rapid ${}^1S_0 {}^{-1}P_1$ 423 nm transition to observe the narrow ${}^1S_0 {}^{-3}P_1$ 657 nm clock transition [21]. The stabilization of 423 nm laser can also reflect the properties of atomic beams. Thus, we study the frequency shift of both the 423 nm transition and the 657 nm transition.

The remainder of the paper is structured as follows. Section 2 provides an overview of the experimental setup. Section 3 presents the results and the analysis of theoretical predictions. Finally, Section 4 concludes the study.

2 Experimental setup

2.1 Frequency shift of ${}^{1}S_{0}$ - ${}^{1}P_{1}$ transition at 423 nm

Two identical atomic beam vacuum systems are employed to minimize the impact of physical systems on the experiment. An ion pump with a 20 L/s pumping speed maintains long-term vacuum stability at 6E-8 Pa. As the atomic beam emitted from the oven exhibits divergence, a collimation aperture is positioned before the laser interaction zone to reduce its divergence angle, with a distance of d = 100 mm from the nozzle of the oven. The size of the crucible nozzle is r = 3 mm. A 10 mm-long capillary array with a 0.2 mm inner and 0.4 mm outer diameter further collimates the atomic beam. The divergence angle of the atomic beam is 30 mrad because of the angular selection given by the presence of the aperture. Quantum projection noise limits the signal-to-noise ratio of atomic transitions, requiring sufficient atomic beam intensity for laser interaction. Calcium, with a melting point of 1,113.15 K, is heated to 873.15 K in a vacuum, facilitating its rapid, directional ejection and spraying out of the crucible nozzle in the form of atomic vapor.

The 423 nm laser must be incident perpendicular to the atomic beam to target atoms with zero transverse velocity. A photomultiplier tube (PMT) detects the fluorescence signal produced by the interaction between the 423 nm laser and atoms. The 423 nm atomic absorption spectroscopy is recorded, and an error signal is generated using a lock-in amplifier. This study examines the frequency shift properties of the ${}^{1}S_{0}$ - ${}^{1}P_{1}$ transition in neutral calcium at 423 nm. The frequency shift is measured by heterodyning two independently locked 423 nm lasers, which are locked to the atomic resonance. An acousto-optic modulator (AOM) induces a 144 MHz frequency shift after one of the 423 nm lasers. We measure the frequency's dependence on temperature, laser power, and laser alignment. The experimental setup is depicted in Figure 2.

2.2 Frequency shift of ${}^{1}S_{0} - {}^{3}P_{1}$ transition at 657 nm

In this experiment, we employ a saturated absorption spectroscopy scheme to detect the clock signal. The calcium atomic beam frequency standard utilizes three locking loops, including stabilizing the 423 nm detection laser to atomic resonance, locking the 657 nm clock laser to a Fabry-Perot cavity, and locking of the 657 nm clock laser to atomic resonance by adjusting the AOM1 frequency. The 423 nm transition enables electron-shelving detection. After achieving stable locking of both lasers, the 423 nm laser serves as the shelved readout for population measurement and 657 nm clock signal detection. Figure 3 illustrates the schematic of the calcium atomic beam optical frequency standard.



Configuration of frequency shift measuring by heterodyning the two 423 nm lasers. HWP: half-wave plate.



FIGURE 3

Optical frequency standard based on a calcium atomic beam, including a clock laser (red) and a probe laser (blue). EOM: electro-optic modulator; PBS: polarizing beam splitter; CCD: charge-coupled device; PD: photodiode.



The 657 nm external cavity semiconductor laser serves as the clock transition laser. Its frequency is stabilized using the Pound-Drever-Hall (PDH) technique, locking it to an ultra-stable resonant cavity. After frequency stabilization by PDH locking, the linewidth of the 657 nm laser is heterodyned with another set of 657 nm laser using PDH technique. The fitted Lorentz linewidth is 32.16 Hz, and one set of the 657 nm laser linewidth is less than 32.16 Hz. To bridge the frequency difference between the ultra-cavity stabilized 657 nm laser and the calcium atomic resonance frequency, AOM1 and AOM2 apply four frequency shifts to align the laser frequency with the atomic transition. AOM1 operates at 101.894 MHz and AOM2 at 198.26 MHz, resulting in a total frequency shift of about 600 MHz via a double pass configuration. The 657 nm clock laser is then stabilized to the atomic resonance through feedback control of an AOM frequency, ensuring the output of the optical frequency standard.

After stabilizing the calcium atomic beam frequency standard, we analyze the frequency shifts induced by temperature, laser power, and laser alignment. The stabilized clock laser output after AOM1 is heterodyned with an optical frequency comb locked to a hydrogen maser, enabling measurement of the 657 nm laser's frequency shift. The frequency stability of the hydrogen maser is 6.0×10^{-14} at 1 s and 1.1×10^{-15} at 1,000 s. The schematic of frequency shift measuring experimental setup is shown in Figure 4.

3 Results

3.1 Frequency shift of ${}^{1}S_{0}$ - ${}^{1}P_{1}$ transition at 423 nm

3.1.1 Frequency shift of ${}^{1}S_{0}$ - ${}^{1}P_{1}$ transition at 423 nm caused by oven temperature

The temperature of one oven is set to 873.15 K, while the temperature of the second oven is adjusted within the range of 868.15 K–903.15 K. Figure 5 illustrates the frequency shift of the 423 nm transition in calcium as a function of oven temperature, with a



fitted coefficient of 26.78 kHz/K between the frequency shift and temperature. For 423 nm laser long-term stability at the E–13 level, the frequency shift must remain below 70.9 Hz, which requires that oven temperature fluctuations be limited to 2.65×10^{-3} K.

3.1.2 Frequency shift of ${}^{1}S_{0}$ - ${}^{1}P_{1}$ transition at 423 nm caused by laser power

We maintain the temperature of two ovens at 873.15 K and adjust the laser power using a HWP before a polarization beam splitter. One 423 nm laser's power varies from 25 to 50 mW, while the other 423 nm laser power is fixed at 17 mW. Figure 6 illustrates the frequency shift of the 423 nm transition as a function of laser intensity, with a fitted coefficient of 502.52 Hz/(mW/cm²) between frequency shift and laser intensity. For 423 nm laser long-term stability at the E–13 level, the laser power fluctuations should be limited to 4.43 μ W.





3.1.3 Frequency shift of ${}^{1}S_{0}$ - ${}^{1}P_{1}$ transition at 423 nm caused by laser alignment

We set the two ovens to 873.15 K and examined the frequency dependence on the two orthogonal adjustments of the mirror mount by varying the actuator on the last mirror. Figures 7, 8 illustrate the resulting frequency shift of the 423 nm transition as a function of vertical position and horizontal position, respectively. The fitted coefficient between frequency shift and laser alignment is 2.17×10^4 Hz/µrad. By aligning the laser vertically at the atomic beam's radial center—as can be seen by the inflection point in Figure 7—the frequency shift can be minimized due to the beam's symmetry. For 423 nm laser long-term stability at the E-13 level, the laser alignment fluctuations should be limited to 3.27 nrad.



3.2 Frequency shift of ${}^{1}S_{0} - {}^{3}P_{1}$ transition at 657 nm

3.2.1 Frequency shift of ${}^{1}S_{0}$ - ${}^{3}P_{1}$ transition at 657 nm caused by oven temperature

After stabilizing the calcium atomic beam frequency standard, we measure the stable output clock laser using an optical frequency comb referenced to a hydrogen maser. The stability of clock laser is 2.43×10^{-13} at 1 s and 5.31×10^{-14} at 200 s as shown in Figure 9A. We also demonstrate the fluctuations of beat frequency in Figure 9B. The frequency stability of the clock laser at 1 s is limited to the noise of an optical frequency comb locked to a hydrogen maser and the noise in the beat frequency link. The stabilized clock laser output after AOM1 is also heterodyned with an optical cavity stabilized laser and the stability of clock laser is $\sim 5 \times 10^{-14}$ at 1 s.

The oven temperature is varied from 893.15 K to 923.15 K, and the resulting frequency shift of the 657 nm transition as a function of oven temperature is depicted in Figure 10. The frequency shift-temperature fitted coefficient is 374.21 Hz/K. We calculate the temperature changes of the oven temperature by measuring the voltage fluctuations of the thermocouple. The fluctuation of oven temperature per second does not exceed 0.04 K, therefore the frequency shift is within 3.74 Hz. This drift would correspond to a fractional frequency change of 3.28×10^{-14} , which was below the calcium system performance at the time. For clock long-term stability at the E-17 level, the frequency shift must remain below 5 mHz, requiring oven temperature fluctuations to be limited to 1.34×10^{-5} K.

The second-order Doppler frequency shift, primarily driven by atom velocity, is the dominant source of temperature-induced frequency shift [28]. Because atom velocity is determined by oven temperature, higher temperatures increase the atomic beam speed, altering the relative velocity felt during the interaction between atoms and laser [29], which in turn shifts atomic resonance frequencies. Meanwhile, an increase in temperature can cause the opto-mechanics to expand slightly, inducing a residual first-order Doppler shift.







3.2.2 Frequency shift of ${}^{1}S_{0}$ - ${}^{3}P_{1}$ transition at 657 nm caused by laser power

We set the oven temperature at 923.15 K. Laser power is adjusted via a HWP positioned before a polarization beam splitter, varying the 657 nm laser power between 5.2 and 6.0 mW. Figure 11 illustrates the frequency shift of the 657 nm transition as a function of laser intensity, with a fitted coefficient between frequency shift and laser intensity of 91.35 Hz/(mW/cm²). We record the fluctuations of laser power which do not exceed 5.15×10^{-5} mW per second, corresponding to the frequency shift within 0.05 Hz. This drift would correspond to a fractional frequency change of 1.1×10^{-16} , which was well below the calcium system performance at the time. To maintain the clock long-term stability at the E–17 level, the laser power fluctuations should be limited to 1.72 nW. The frequency shift variation with laser power results from the ac Stark shift, where a near-resonant pump laser alters atomic energy levels based on its frequency and intensity.

3.2.3 Frequency shift of ${}^{1}S_{0}-{}^{3}P_{1}$ transition at 657 nm caused by laser alignment

We set the temperature of the two ovens at 923.15 K and investigated the influence of laser alignment on clock frequency by adjusting the actuator on the final mirror of the saturated absorption spectroscopy. Frequency dependence is assessed along the two orthogonal axes of the mirror mount. Figure 12 illustrates the frequency shift of the 657 nm transition as a function of laser alignment. The fitted correlation coefficient between frequency shift and laser alignment is 279 Hz/µrad. Maintaining clock longterm stability at the E-17 level requires limiting the frequency shift to below 5 mHz, necessitating laser alignment fluctuations within 1.03 nrad.

The key Doppler-related effect in our thermal atomic beam ensemble is the first- and second-order Doppler shift. The firstorder Doppler shift can be mitigated using saturated absorption spectroscopy. In our experiment, the clock frequency variations with laser alignment indicate instabilities due to residual first-order





Doppler shifts [30]. We find that laser alignment stability is critically required in the horizontal direction, aligned with atomic motion, while the frequency shift remains relatively small at the vertical inflection point. The first-order Doppler frequency shift can be expressed as Equation 1.

$$\Delta v = \frac{\vec{v} \cdot \hat{k}}{c} v_0 \tag{1}$$

where Δv is the first-order Doppler shift, \vec{v} is the velocity vector of the calcium atoms, \hat{k} is the unit vector in the direction of light propagation, *c* is the speed of light in vacuum, and v_0 is the transition frequency of the atom. Assuming that the angular deviation from the atomic beam to the laser is θ , as shown in Figure 13, then we can obtain Equation 2

$$\vec{v} \cdot \hat{k} = v \cdot \cos \theta \tag{2}$$

where $v = |\vec{v}|$ is the magnitude of the atomic velocity. From this, we can obtain the residual first-order Doppler shift through Equation 3.

$$\Delta v = \frac{v \cdot \cos \theta}{c} v_0 \tag{3}$$

For the residual first-order Doppler shift, we assume that the mean velocity of the atomic beam is $\overline{\nu}$. Since there is a certain distribution of atomic velocity, we take the mean velocity to simplify the analysis. Then the residual first-order Doppler shift is given by Equation 4

$$\Delta v = \frac{\overline{v} \cdot \cos \theta}{c} v_0 \tag{4}$$

For the calcium atom transition at 657 nm, $v_0 = \frac{c}{\lambda} \approx 4.566 \times 10^{14}$ Hz. Thus, the residual first-order Doppler shift is given by Equation 5.

$$1.522 \times 10^6 \overline{\nu} \cos \theta \tag{5}$$

The longitudinal speed of the calcium atomic beam is given by [31] as Equation 6

$$\overline{\nu} = \sqrt{\frac{3k_BT}{M}} \tag{6}$$

where k_B is Boltzmann constant, *T* is the oven temperature, and *M* is calcium atom mass. When the oven temperature is 923.15 K, $\bar{\nu} \approx$ 772 m/s. Therefore, the residual first-order Doppler shift is $1.175 \times 10^9 \cos\theta$ Hz. Because the frequency shift of 657 nm transition as a function of laser alignment is a linear variation, we use the maximum θ to predict the frequency shift to be given by Equation 7.

$$\Delta v = 1.175 \times 10^9 \times 5.25 \times 10^{-6} = 6.17 \times 10^3 \,\mathrm{Hz} \tag{7}$$

Considering the fitting coefficient we measured is 279 Hz/ μ Rad, the maximum actual frequency shift is 1.46 \times 10³ Hz. Thus, theoretical analysis can predict our measured values appropriately.

3.2.4 Frequency shift of 657 nm clock laser relative to 423 nm probe laser

We also measure the power and frequency shifts of the 423 nm probe laser on the clock transition frequency. We first record the frequency shift of 657 nm laser relative to 423 nm laser power. We set the oven temperature at 903.15 K. Laser power is adjusted via a HWP positioned before a polarization beam splitter, varying the 423 nm laser power between 1.2 and 12 mW. Figure 14 illustrates the frequency shift of the 657 nm clock laser as a function of 423 nm laser intensity. The saturation intensity of laser can be expressed as Equation 8

$$I_s = \frac{\pi h c}{3\lambda^3 \tau} \tag{8}$$

where *h* is the Planck constant, λ is the wavelength of 423 nm

transition of calcium atoms, and τ is the lifetime of 423 nm transition. Then we obtain the 423 nm saturation intensity of calcium atoms to be 55.01 mW/cm². Figure 14 demonstrates that the slope of frequency shift decreases when the laser intensity exceeds 55 mW/cm². The laser intensity tends to be saturated.

Then we study the frequency shift of 657 nm laser relative to 423 nm laser frequency. We set the oven temperature at 903.15 K. Figure 15 illustrates the frequency shift of the



The frequency shift of 657 nm clock laser relative to 423 nm laser intensity.



657 nm clock laser as a function of the frequency of 423 nm probe laser, with a fitted coefficient of 0.00106. As the 423 nm laser drifts 2 Hz per second, the clock laser drifts 2.12 mHz per second. These drifts would correspond to a fractional frequency change of 4.65 $\times 10^{-18}$, which was well below the calcium system performance at the time.

4 Conclusion

Our study systematically analyzes the frequency shift properties induced by temperature, laser power, and laser alignment, focusing on both the ${}^{1}S_{0}$ - ${}^{3}P_{1}$ 657 nm clock transition and the ${}^{1}S_{0}$ - ${}^{1}P_{1}$ 423 nm transition used for electron-shelving detection. We determine the fitted coefficients correlating frequency shift with oven temperature, laser power, and laser alignment. These frequency shifts enable precise control of key parameters to achieve the desired frequency stability. This work serves as a reference for optimizing our high-performance physical system for a calcium atomic beam optical clock, with the calcium beam optical clock offering significant advancements in the fielded optical atomic timekeeping.

Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding authors.

Author contributions

YC: Conceptualization, Writing – review and editing, Formal Analysis, Software, Investigation, Methodology, Data curation, Writing – original draft. YS: Writing – review and editing, Supervision, Conceptualization. JM: Methodology, Writing – review and editing. JP: Writing – review and editing. MM: Writing – review and editing. XX: Writing – review and editing. SZ: Writing – review and editing.

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