



Astrocyte as Spatiotemporal Integrating Detector of Neuronal Activity

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The functional role of astrocyte calcium signaling in brain information processing was intensely debated in recent decades. This interest was motivated by high resolution imaging techniques showing highly developed structure of distal astrocyte processes. Another point was the evidence of bi-directional astrocytic regulation of neuronal activity. To analyze the effects of interplay of calcium signals in processes and in soma mediating correlations between local signals and the cell-level response of the astrocyte we proposed spatially extended model of the astrocyte calcium dynamics. Specifically, we investigated how spatiotemporal properties of Ca²⁺ dynamics in spatially extended astrocyte model can coordinate (e.g., synchronize) networks of neurons and synapses.

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INTRODUCTION

The functional role of astrocyte calcium signaling remains intensely debated. One of the principal reasons for such a debate is that the astrocytic Ca^{2+} dynamics possesses high complexity which was confirmed by new experimental approaches to study the signaling of astrocytes at qualitatively new spatial-temporal resolutions (Volterra et al., 2014; Bindocci et al., 2017; Wu et al., 2018). Another reason was the evidence of bi-directional astrocytic regulation of neuronal activity referred as gliotransmission [Ca²⁺-dependent release of neurotransmitters (glutamate, D-serine, ATP) by astrocytes] (Araque et al., 2014; Bazargani and Attwell, 2016; Fiacco and McCarthy, 2018; Savtchouk and Volterra, 2018).

Astrocytes respond to synaptic activity by intracellular Ca^{2+} elevations (Verkhratsky et al., 2012). Synaptically-released neurotransmitters (e.g., glutamate) can activate G-coupled receptors [e.g., the metabotropic glutamate receptors (mGluRs)] (Porter and McCarthy, 1996; Pasti et al., 1997; Perea and Araque, 2005), which, upon activation, promote inositol 1,4,5-triphosphate (IP₃) production by phosphoinositide-specific phospholipase C β (PLC β) (Zur Nieden and Deitmer, 2006). In turn, the elevation of cytosolic concentration of the second messenger IP₃ promotes the Ca²⁺-induced Ca²⁺ release (CICR) from the astrocyte's endoplasmic reticulum (ER) stores. Clustering of astrocytic receptors, targeted by synaptically released neurotransmitters at points of contact of synapses with astrocytic processes (Di Castro et al., 2011; Panatier et al., 2011; Arizono et al., 2012) provides spatially confined sites of IP₃ production, whose differential activation could result in rich spatiotemporal IP₃ and Ca²⁺ dynamics (Volterra et al., 2014).

There are two main types of IP₃-induced CICR observed in astrocytes (Volterra et al., 2014; Rusakov, 2015; Bindocci et al., 2017): small, fast Ca^{2+} events that are confined to their (primary) processes and caused by minimal synaptic activity; and Ca^{2+} elevations propagating

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along astrocytic processes that can reach the soma and trigger whole-cell global Ca^{2+} signal. The latter slow calcium events were induced by intense neuronal activity. This circumstance can be interpreted as the ability of astrocytes to perceive the information contained in the repetition rate of action potentials, however, this occurs on time scales larger than the characteristic times inherent in the synaptic activity.

The elevation of intracellular calcium concentration in astrocyte can trigger the release of various active chemicals, gliotransmitters, such as glutamate, GABA, ATP, and D-serine (Bezzi and Volterra, 2001). The concept of "tripartite synapse" (Araque et al., 1999) is based on the ability of gliotransmitters to regulate synaptic transmission and plasticity on time scales from seconds to minutes (see Araque et al., 2014 for a recent review).

Since effect of single gliotransmitter depends on the type of circuit and targeted neurons (Araque et al., 2014), we focused in our study on the excitatory transmission in hippocampus. It was shown that hippocampal astrocyte can release ATP (Zhang et al., 2003), D-serine-co-agonist of the NMDA receptor (NMDAR) (Henneberger et al., 2010; Zhuang et al., 2010) and glutamate. After conversion to adenosine, ATP can depress, or facilitate excitatory synaptic transmission acting on either A1 or A2A receptors, respectively (Serrano et al., 2006; Pascual et al., 2012). At CA3-CA1 synapses astrocytic glutamate acts on presynaptic NMDARs (Jourdain et al., 2007) or mGluRs (Navarrete and Araque, 2010; Navarrete et al., 2012) to potentiate or decrease release probability, respectively. In the CA1 region a long-term potentiation (LTP) which required presynaptic mGluR activation (Perea and Araque, 2007) can be induced by the postsynaptic activity accompanying by glutamate release from astrocyte due to Ca^{2+} elevation. Also, it was shown (Henneberger et al., 2010) that D-serine, released from astrocyte and being a coagonist of postsynaptic NMDARs, can trigger NMDAR-mediated LTP at synapses nearby of the astrocyte.

Intense modeling efforts have been devoted in recent years to understand the functional role of astrocytic modulation of the neuronal communication (see Oschmann et al., 2018 for a recent review, Kanakov et al., 2019). There are several biophysical studies of astrocytic influence on post- and presynaptic neuronal activity (De Pittà et al., 2011; Gordleeva et al., 2012; Tewari and Majumdar, 2012a,b; Tewari and Parpura, 2013; De Pittà and Brunel, 2016; Flanagan et al., 2018). However, these works did not account for the impact of spatiotemporal patterns of calcium dynamics in astrocyte, i.e., the spatial distribution of the calcium activity was neglected. Meanwhile, under the action of highfrequency action potentials in one synapse or coherent activity of several synapses, the calcium signal originating in astrocyte can spread along the processes and throughout the astrocyte and cause the release of the gliotransmitter in remote locations, affecting other synapses.

There are also a few recent computational works which investigated mechanisms underlying IP₃-triggered CICR-mediated spatiotemporal dynamics in single astrocyte (Wu et al., 2014; Gordleeva et al., 2018; Savtchenko et al., 2018).

To analyze the principles of generation of calcium signals in processes and soma of the astrocyte and to seek mechanisms of correlations between local signals and the global signalization response of the astrocyte including its spatially distributed structure, we propose a spatially extended model of astrocyte calcium dynamics. In this paper we investigate how spatiotemporal Ca²⁺ dynamics in spatially extended astrocyte model can coordinate and synchronize network signaling.

METHODS

For our purpose we designed a neuron-astrocyte network composed of 100 synaptically coupled Hodgkin-Huxley excitatory neurons (Hodgkin and Huxley, 1952) and two astrocytes connected via gap junction. Each astrocyte has spatially distributed structure that repeated the morphology of real astrocyte (Bindocci et al., 2017). For illustration, we assumed that each process of the astrocyte, interacting with presynaptic and postsynaptic neurons, forms one tripartite synapse providing the connectivity between neuronal and astrocytic parts of the network. The schematic architecture of the model is shown in Figure 1. Our model of the tripartite synapse describes the effects of the astrocytic modulation of synaptic transmission in the CA1-CA3 area of hippocampus. We consider glutamate as the neurotransmitter, and glutamate and D-serine as the gliotransmitters. We describe three effects resulting from the influence of the gliotransmitters on the synapse: (i) potentiation of presynaptic release probability due to glutamate acting on presynaptic NMDARs; (ii) depression of presynaptic release probability due to glutamate acting on presynaptic mGluRs; and (iii) increase of the postsynaptic currents due to D-serine modulation of the postsynaptic NMDA receptors.

Neural Network

Neural network consists of 100 excitatory synaptically coupled Hodgkin-Huxley neurons (Hodgkin and Huxley, 1952; Esir et al., 2018). We use random coupling topology with connection probability for each pair of neurons equal to 20% (Braitenberg and Schüz, 1998). The dynamics of the neuronal membrane potential is described by the following ionic current balance equation:

$$C\frac{dV^{(n)}}{dt} = I_{channel}^{(n)} + I_{app}^{(n)} + \sum_{m} I_{syn}^{(mn)} + I_{p}^{(n)},$$
(1)

where capacitance, *C*, is 1 μ F/cm², the superscript (n = 1,..., M) corresponds to a neuronal index and (*m*) corresponds to an index of input connection. The Na⁺, K⁺, and leak currents are expressed as follows:

$$I_{channel} = -g_{Na}m^{3}h\left(V - E_{Na}\right) - g_{K}n^{4}\left(V - E_{K}\right)$$
$$- g_{leak}\left(V - E_{leak}\right), \qquad (2)$$

where g_{Na} and g_K are the potassium and sodium conductances (mS/cm²), E_{Na} , and E_K are the potassium and sodium reversal potentials (mV), g_{leak} and E_{leak} are the leak conductances and leak reversal potential, respectively.

The kinetics of the potassium channel is determined by:

$$\frac{dm}{dt} = \alpha_m (1-m) - \beta_m m,$$



$$\alpha_m = \frac{0.1(V+40)}{1-\exp(-(V+40)/10)},$$

$$\beta_m = 4\exp(-(V+65)/18),$$
(3)
$$\frac{dh}{dt} = \alpha_h(1-h) - \beta_h h,$$

$$\alpha_h = 0.07 \exp(-(V+65)/20),$$

$$\beta_h = \frac{1}{1+\exp(-(V+35)/10)}.$$
(4)

The kinetics of the sodium channel is determined by:

$$\begin{aligned} \frac{dn}{dt} &= \alpha_n (1-n) - \beta_n n, \\ \alpha_n &= \frac{0.01(V+55)}{1-\exp(-(V+55)/10)}, \\ \beta_n &= 0.125 \exp(-(V+65)/80). \end{aligned}$$
(5)

The applied currents $I_{app}^{(n)}$ are fixed at constant value controlling the depolarization level and dynamical mode of the neuron (Kazantsev and Asatryan, 2011). We use $I_{app}^{(n)} = 4.5 \ \mu \text{A/cm}^2$ which corresponds to the neuron's excitable mode. The synaptic current I_{syn} ($\mu \text{A/cm}^2$) simulating interactions between the neurons. Each neuron is stimulated by a Poisson pulse train mimicking external spiking inputs $I_p^{(n)}$ ($\mu \text{A/cm}^2$) with a certain average rate λ . Each Poisson pulse has rectangular shape with fixed width of 10 ms and variable height, which is sampled independently for each pulse from uniform random distribution on interval [0, 1.5]. Sequences of Poisson pulses applied to different neurons are independent.

Synaptic Dynamics

Each spike on presynaptic neuron results in the release of the glutamate quant. We describe presynaptic dynamics of the glutamate, G, using a mean field approach from Gordleeva et al. (2012):

$$\frac{dG}{dt} = -\alpha_G (G - k_{pre} \delta(t - t_k)), \tag{6}$$

where α_G denotes the clearance rate of the neurotransmitter, k_{pre} denotes the efficacy of the presynaptic release, δ denotes the Dirac delta function and t_k is spike time.

The release of the glutamate leads to excitatory postsynaptic current (EPSC). For description of the EPSCs dynamics we use the approach from our previous work (Gordleeva et al., 2012):

$$\frac{dI_{EPSC}}{dt} = -\alpha_I \left(I_{EPSC} - A\delta \left(t - t_k \right) \right), \tag{7}$$
$$P(A) = \frac{2A}{b^2} \exp(-\frac{A^2}{b^2}), \int_0^{+\infty} P(A) dA = \Gamma(1) = 1,$$

where α_I is rate constant. According to the experimental data (Fernández-Ruiz et al., 2012; Guzman et al., 2016) we supposed that amplitude of the EPSCs, *A*, is gamma-distributed with probability density function *P*(*A*), where *b* is the scaling parameter of gamma-distribution that denotes the impact of the synaptic input.

Integrated synaptic current of the neuron, *I*_{syn}, is described by the following equation (Gordleeva et al., 2012):

$$I_{syn} = \frac{I_{EPSC}}{1 + \exp(-(G - \theta_G)/k_G)},$$
(8)

where θ_G denotes the midpoint and k_G denotes the slope of the neuronal activation function.

Geometry of the Astrocytic Model and Astrocytic Ca²⁺ and IP₃ Dynamics

To design the architecture of the spatially distributed astrocyte model, we followed available experimental facts (Bindocci et al., 2017) (see **Figure 2A**). Specifically, we consider the astrocyte as network of inter-coupled small compartments, which have a cylindrical shape (Gordleeva et al., 2018). Each element is a unit-length cylinder with a finite radius *r* containing ER (**Figure 2B**). Compartments are coupled through the diffusion of calcium and IP₃ controlling the calcium exchange between the cytoplasm and intracellular stores of calcium (in particular, ER).

The dynamics of each compartment is described by the following set equations (modified from Li and Rinzel, 1994; Gordleeva et al., 2018). The balance of calcium fluxes in cytosol for particular compartment is described by

$$\frac{d[Ca_c]_i}{dt} = \frac{S_{ERi}}{F \cdot V_i} (J_{IP3R} - J_{SERCA} + J_{ERleak}) + J_{Cadiff}.$$
 (9)



Changing free calcium concentration in the cytosol of the compartment *i* is defined by calcium exchange with the ER involving the calcium release from the ER to the cytosolic volume through IP₃ receptors, J_{IP3R} , the ATPase Ca²⁺- pump "SERCA" by J_{SERCA} , and by calcium leak from the ER, J_{ERleak} . $S_{ERi} = S_i \sqrt{r_{ERi}}$ denotes the surface of the ER. The volume and the surface of the intracellular space are defined as V_i and S_i , respectively. r_{ER} is the ratio of the volume of ER to the volume of cytoplasm in the considered compartment of the astrocyte. The distribution of values over compartments in the developed model was chosen according to experimental data (Patrushev et al., 2013; Oschmann et al., 2017) and can be found in **Supplementary Table 2**.

The current J_{IP3R} is expressed by the following equations (Li and Rinzel, 1994) approximating the kinetics of ER IP₃Rs:

$$J_{IP3R} = \frac{FV_i}{S_i} v_1 m_\infty^3 n_\infty^3 h^3 ([Ca_{ER}]_i - [Ca_c]_i),$$

$$\frac{dh_i}{dt} = \frac{h_\infty - h_i}{\tau_h},$$

$$h_\infty = d_2 \frac{([IP_3]_i + d_1)([IP_3]_i + d_3)}{(d_2([IP_3]_i + d_1) + [Ca_c]_i([IP_3]_i + d_3))},$$

$$n_\infty = \frac{[Ca_c]_i}{[Ca_c]_i + d_5}, \quad m_\infty = \frac{[IP_3]_i}{[IP_3]_i + d_1},$$

$$\tau_h = \frac{([IP_3]_i + d_3)}{a_2(d_2([IP_3]_i + d_1) + [Ca_c]_i([IP_3]_i + d_3))}.$$
 (10)

Here $[Ca_c]_i$ and $[Ca_{ER}]_i$ are calcium concentrations in the cytosol and in the ER of the compartment *i*, respectively. The dynamics

of the Ca^{2+} concentration in the ER is described by:

$$\frac{d[Ca_{ER}]_i}{dt} = \frac{S_{ERi}}{F \cdot V_{ERi}} (-J_{IP3R} + J_{SERCA} - J_{ERleak}) + J_{CaERdiff}$$
(11)

where S_{ERi} and V_{ERi} denote the area and the volume of the ER, respectively.

The variable *h* denotes the fraction of activated IP₃ receptors and the other gating variables for IP₃Rs are set to their equilibrium values m_{∞} and n_{∞} . Active ATP-dependent current *J*_{SERCA} pumping calcium back to the ER and the Ca²⁺ leak current from the ER, *J*_{ERleak}, are given by the following equations:

$$J_{SERCA} = \frac{FV_i}{S_i} v_3 \frac{[Ca_c]_i^2}{[Ca_c]_i^2 + k_3^2},$$

$$J_{ERleak} = \frac{FV_i}{S_i} v_2([Ca_{ER}]_i - [Ca_c]_i).$$
 (12)

The change of the IP₃ concentration is defined by production and degradation that are regulated by cytosolic Ca²⁺. These include Ca²⁺-dependent phospholipase C δ (PLC δ) mediated IP₃ synthesis and Ca²⁺-dependent IP₃ degradation by the IP₃ 3kinase (IP₃-3K) and the inositol polyphosphate 5-phosphatase (IP-5P) (De Pitta et al., 2009):

$$\frac{d[IP_3]_i}{dt} = J_{PLC\beta} + J_{PLC\delta} - J_{\deg 3K} - J_{\deg 5P} + J_{IP3diff}.$$
 (13)

The first current, $J_{PLC\beta}$, describes agonist dependent IP₃ production by PLC β . The activation of PLC β by G-protein

is controlled by the glutamate concentration, *G*, (Equation 6) (De Pitta et al., 2009):

$$J_{PLC\beta} = \nu_{\beta} \frac{G^{0.7}}{G^{0.7} + (K_R + K_p \cdot \frac{[Ca_c]_i}{[Ca_c]_i + K_\pi})^{0.7}},$$
(14)

where v_{β} is the rate of IP₃ production by PLC β , K_R is the glutamate affinity of the receptor, K_p is Ca²⁺/PLC- dependent inhibition constant, and K_{π} is Ca²⁺ affinity of PLC.

The second term in Equation (13) describes cytosolic calcium dependent PLC[§] activation (De Pitta et al., 2009):

$$J_{PLC\delta} = \frac{\nu_{\delta}}{1 + \frac{[IP_3]_i}{k_{\delta}}} \frac{[Ca_c]_i^2}{[Ca_c]_i^2 + K_{PLC\delta}^2},$$
(15)

where v_{δ} described the maximal rate of IP₃ production by PLC δ , k_{δ} - the inhibition constant, and $K_{PLC\delta}$ - the Ca²⁺ affinity of PLC δ .

The IP₃ degradation by IP₃-3K and IP-5P described by the following equations (De Pitta et al., 2009):

$$J_{\deg 3K} = v_{3K} \frac{[Ca_c]_i^4}{[Ca_c]_i^4 + K_D^4} \cdot \frac{[IP_3]_i}{[IP_3]_i + K_3}, \ \ J_{\deg 5P} = r_{5P}[IP_3]_i.$$
(16)

The whole process dynamics is formed by the intracellular diffusion of calcium and IP₃ accounted by the following fluxes:

$$J_{IP3diff} = d_{IP3(i,i+1)}([IP_3]_{(i+1)} - [IP_3]_i) + d_{IP3(i,i-1)}([IP_3]_{(i-1)} - [IP_3]_i), J_{Cadiff} = d_{Ca(i,i+1)}([Ca_c]_{(i+1)} - [Ca_c]_i) + d_{Ca(i,i-1)}([Ca_c]_{(i-1)} - [Ca_c]_i).$$
(17)

The diffusion flux through compartments of ER described by the following:

$$J_{CaERdiff} = d_{CaER}([Ca_{ER}]_{(i+1)} + [Ca_{ER}]_{(i-1)} - 2[Ca_{ER}]_i).$$
(18)

Note, that the values of the diffusion rates from compartment j (j = i+1; j = i-1) to compartment i for IP₃, d_{IP3ij} , and for calcium, d_{Caij} , depend on the compartment geometry (e.g., compartment volume) and are different the inward and outward fluxes at the process branching sites:

$$d_{IP3ij} = \frac{D_{IP3}A_{ij}}{V_i \cdot x_{ij}}, \quad d_{Caij} = \frac{D_{Ca}A_{ij}}{V_i \cdot x_{ij}}, \tag{19}$$

where A_{ij} is the cross-section area between compartments, V_i is the volume of compartment *i*, x_{ij} is the distance between









the centers of the nearest-neighbor compartments, which is equal to the unite length of compartment. D_{IP3} and D_{Ca} is the diffusion constant for IP₃ and Ca²⁺, respectively. For simplicity, we assume that the size of the ER is the same in all compartments and therefore the diffusion coefficient of Ca²⁺ in the ER does not depend on the geometry of the compartment and is constant. Values of model parameters can be found in **Supplementary Table 1**. Note that the time unit in the neuronal model (1–5) is 1 ms. Due to a slower time scale, in the astrocytic model empirical constants are indicated using seconds as time units. When integrating the joint system of differential equations, the astrocytic model time is rescaled so that the units in both models match up.

Dynamics of Gliotransmitters

When the $[Ca_c]$ in astrocytic processes exceeds a threshold $[Ca_c]_{th}$ concentration, gliotransmitter is released by the astrocyte into the extra-synaptic space. For illustration, we consider that the gliotransmitter is released only from the distal compartment on each astrocytic process forming the tripartite synapse. We describe the concentration of gliotransmitter by the following equations (Gordleeva et al., 2012):

$$\frac{dY_k}{dt} = -\alpha_k (Y_k - H_k([Ca_c])),$$

$$H_k([Ca_c]) = \frac{1}{1 + \exp(-\frac{[Ca_c] - [Ca_c]_{th}}{k_k})},$$
 (20)

where index k denotes the type of gliotransmitter released from astrocyte: k = 1 for glutamate and k = 2 for D-serine. α_k denotes the gliotransmitter clearance rate. The amount of the gliotransmitter released from astrocyte if the Ca²⁺ concentration exceeds a threshold accounted by the function $H_k([Ca_c])$.

Glutamate released from astrocyte can modulate presynaptic release. Equation for presynaptic dynamics (6) considering the astrocytic modulation should be modified to:

$$\frac{dG}{dt} = -\alpha_G \left(G - k_0 (1 + \gamma_1 Y_1) \delta(t - t_k) \right), \qquad (21)$$

where the influence of glutamate released from astrocyte on the amount of neurotransmitter describes by parameter γ_1 . $\gamma_1 > 0$ for the potentiation and $\gamma_1 < 0$ for the depression of neurotransmitter release, respectively.

Astrocytic D-serine modulates the response of the NMDARs on the postsynaptic terminal. This modulation leads to increase the amplitudes of postsynaptic currents. In the model it means the increase of the scaling parameter, b, of the probability density function P(A) (7):

$$b = b_0 (1 + \gamma_2 Y_2), \tag{22}$$

where γ_2 is the parameter which describe impact of the astrocytic D-serine on the amplitudes of the EPSCs.

RESULTS

First, let us consider the dynamics of single tripartite synapse without influence of the gliotransmitters on the synaptic

strength. The dynamics of synaptic transmission obtained in model (1-20) is shown in Figure 3. We consider quite low frequency of presynaptic firing (Figure 3A). The model has been tuned to follow recent experimental data on the calcium activity of astrocyte taken in vivo on a subcellular scale (Bindocci et al., 2017). They showed that astrocyte could response even on the low frequency of neuronal activity. According to experimental data the parameters values were chosen so that even individual action potential on the presynaptic neuron could induce small calcium event in the most distant astrocytic compartment. In response to the glutamate release from presynaptic terminal, the calcium concentration in the distal compartment increases. This increase, however, is not sufficient to trigger the gliotransmission (e.g., Y(t) is close to zero), because the intracellular diffusion calcium concentration consequently increases in all elements of this process. However, the amplitude of these pulses is smaller than the amplitude of the basic response. With increase of presynaptic firing rate the amplitudes of the calcium signals in the distal compartment substantially increase and exceed the threshold of gliotransmission (Figure 3B).

Next, we consider the interaction of whole astrocyte and neural network. All neurons of the network are stimulated by Poisson process with fixed frequency. The model architecture of the astrocyte model includes 14 processes, and, hence, the astrocyte interacts with 14 synapses from neural network of 36 neurons. **Figure 4A** illustrates the space-time diagram of calcium signals in the compartmental model. Note that the frequency of calcium signals in soma is much lower than in all compartments of the astrocyte. Calcium signals generated in the distal elements of different processes of the astrocyte propagate to the soma due to diffusion. An increase in the calcium concentration in the soma of the cell induces the propagation of the Ca^{2+} signal back through all processes of the model. If one compares the astrocytic calcium activity firing rate (the number of calcium



FIGURE 5 | Average frequencies of generation of calcium signals in soma (red dots), in all distal processes (black dots), and in all proximal processes the nearest to soma (green dots) vs. the frequency of the presynaptic neurons.

signals in all compartments in the 100-ms time window) (Figure 4C) and corresponding time trace of the intracellular calcium concentration in soma (Figure 4D), then it happens that the calcium response in the soma occurs as the result of a space-time integration of calcium fluctuations in the processes of the astrocyte. To estimate the level of functional connectivity between activity of neurons and calcium activity in astrocyte, we calculated the cross correlation (CC) between neuronal firing rate (Figure 4B) and astrocytic firing rate (Figure 4C). The peak of the CC (Figure 4E) indicates the presence of cross correlation (e.g., a synchrony) and estimates the communication delay time

 τ equal about to 2 s. It is important to note that the peak of the CC exists only for firing rate of presynaptic neurons not all neurons in network (red line on the **Figure 4E**). Thus, the model verified that activation of the astrocyte is stimulated by synchronous in time and in space neuronal activity. This correspond to the experimental data presented in Bindocci et al. (2017). They found very large events *in vivo*, which they called global Ca²⁺ events, that spread spatially to most of the astrocytic structures. Most of global calcium events were registered during movement of the mouse associated intense neuronal discharges. The dependences of the average frequencies of generation of



FIGURE 6 The dynamics of the tripartite synapse with astrocytic influence on synaptic transmission. (A) Time traces of membrane potentials of pre- ($V_{pre}(t)$) and post-synaptic ($V_{post}(t)$) neurons and calcium concentration ($Ca^{2+}(t)$) in distal compartment of the astrocytic process without impact of astrocyte ($\gamma_1 = \gamma_2 = 0$). (B) Astrocyte-mediated potentiation of presynaptic release. Red line corresponds to the post-synaptic activity with astrocytic influence ($\gamma_1 = 0.1$). Black-without. Y(t) is the time trace of gliotransmitter concentration. (C) Astrocyte-mediated inhibition of presynaptic release. Red line corresponds to the postsynaptic activity with astrocytic activity with astrocytic influence ($\gamma_1 = -0.4$). (D) Astrocyte-mediated increasing of PSCs amplitudes. Red line corresponds to the postsynaptic activity with astrocytic influence ($\gamma_2 = 1$). $\lambda = 9$ Hz.

calcium signals in the soma and processes of the astrocyte on the firing frequency of the presynaptic neurons are shown on the **Figure 5**. Note that the frequency at the distal compartments reaches the highest values being monotonically dependent on the firing rate of presynaptic neurons and accordingly on the release rate of the neurotransmitter. Calcium signals on the astrocyte soma occur less often when exceeding a certain threshold of the spiking frequency of the presynaptic neurons. Let us now consider the impact of gliotransmitter on the synaptic transmission. **Figure 6** shows dynamics of single tripartiate synapse. We stimulate the presynaptic neuron by Poisson process and register the activities of postsynaptic neuron, gliotransmitter, and Ca²⁺ concentration in perisynaptic process. We analyze the following astrocyte-mediated modulations of synaptic transmission: (i) astrocytic glutamate potentiates of neurotransmitter release by acting on presynaptic NMDARs, γ_1





> 0 in (21) (Jourdain et al., 2007) (**Figure 6B**), (ii) astrocytic glutamate can target presynaptic mGluRs which decrease release probability, $\gamma_1 < 0$ in (21) (Semyanov and Kullmann, 2000; Perea and Araque, 2007; Navarrete et al., 2012) (**Figure 6C**); (iii) the gliotransmitter D-serine triggers increase of the amplitudes of post synaptic currents by acting as the coagonist of postsynaptic NMDARs, $\gamma_2 > 0$ in (22) (Henneberger et al., 2010) (**Figure 6D**).

Gliotransmission can co-ordinate several synapses and networks of neurons (Serrano et al., 2006; Pascual et al., 2012). **Figure 7** illustrates the heterosynaptic astrocyte-induced modulation of neurotransmission in our model. Ca²⁺ signals evoked locally by high-frequency discharge of synapse 1 (**Figure 7A**) can propagate intracellularly from their initial source toward different process and trigger gliotransmitter release at nearby synapse (synapse 2) facilitating (**Figure 7B**) or depressing (**Figure 7C**) synaptic transmission.

Next, we study a bidirectional regulation of the signal transmission in neural ensemble by astrocytes. According to the



FIGURE 8 | A raster plots of the neuronal and calcium activities in astrocyte. $\lambda = 7$ Hz. We consider astrocyte-mediated potentiation of presynaptic release ($\gamma_1 = 0.1$). Neuron-astrocyte network under study consists of (**A**) one astrocyte and 36 neurons. Neurons 0–14 are postsynaptic; (**B**) two connected via gap-junction astrocytes (color of dots correspond to different cells) and 100 neurons. Neurons 0–28 are postsynaptic.

experimental data astrocytes occupy non-overlapping territories (Halassa et al., 2007). Thus, only one astrocyte can impact on transmission in a determined set of thousands synapses. We consider neuron-astrocyte network consists of two astrocytes connected via gap junction and 100 synaptically coupled neurons (Figure 8). Figure 8A shows communication of one astrocyte and small neuronal network of 36 neurons the same as on Figure 4 but with taking into consideration astrocytic modulation of synaptic transmission. High frequency of neuronal firing rate increases the probability of synchronous activity in neighboring to astrocyte synapses. Such coherent synaptic activity induces Ca²⁺ elevations in different astrocytic processes, which due to spatial-temporal integration results in global, long lasting Ca²⁺ events. This large calcium signal reaching the cell soma and triggering whole-cell Ca²⁺ signaling can stimulate the release of gliotransmitter to multiple synapses coordinating activity of the neuronal circuit (Figure 8A) defined by the morphological territory of individual astrocyte. Thus, astrocytemediated potentiation of presynaptic release results in longterm increasing of neuronal activity from domain defined by the astrocytic morphology (Figure 8A). This kind of response can even propagate to neighboring astrocytes, through gap junction channels. Figure 8B shows the simulation of the calcium signal propagation through the processes of one astrocyte to another triggering modulation of communication in large neuronal ensembles.

DISCUSSION

The majority of known data is extracted from Ca^{2+} signals monitoring in astrocyte soma. Slow Ca^{2+} events in astrocyte used to be associated with the high level of neuronal activity (Pasti et al., 1997; Sul et al., 2004). Recent studies, indeed, revealed that even a minimal synaptic activity is capable of small, rapid, and localized Ca^{2+} response excitation in astrocyte (Volterra et al., 2014; Bindocci et al., 2017). These data gave a ground to assume that astrocytes generate large calcium signal by integrating the activity of several individual synapses. Thus, the astrocyte Ca^{2+} signaling represents self-coordinated spatio-temporal patterns including local fast responses as well as, respectively, slow global responses resulting from the integration of the signals. The integration can encapsulate the mechanism of the global responses control via local changes in neuronal activity.

Our model accounting for spatial morphology of the tripartite synapses revealed interesting functional features of calcium activity in astrocyte-mediated modulation of signal transmission. It was shown that astrocyte can act as temporal and spatial integrator, hence, detecting the level of spatio-temporal coherence in the activity of accompanying neuronal network.

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Araque, A., Carmignoto, G., Haydon, P. G., Oliet, S. H., Robitaille, R., and Volterra, A. (2014). Gliotransmitters travel in time and space. *Neuron* 81, 728–739. doi: 10.1016/j.neuron.2014.02.007 Specifically, such time and space integration based on rapid and local events of activation of small compartments along the astrocytic processes results in the long-term astrocyte-mediated changes of the synaptic functionality of the neuronal network. Revealed by a correlation analysis of obtained numerical simulations, a presence of the synchrony between neuronal and astrocytic activity has verified that activation of the astrocyte is stimulated by neuronal activity, which is synchronous in time and in space.

In this study we show that different level of the neuronal activity can trigger Ca²⁺ dynamics in astrocyte with various spatio-temporal characteristics which can lead to different astrocytic-induced regulatory effects on synaptic transmission. The minimal synaptic activity causes the fast and local Ca²⁺ elevation in astrocytic process. This small Ca²⁺ signal triggers the gliotransmission in the active synapse induces localized regulatory astrocytic feedback of the synapse (Figure 6). Increasing frequency of synaptic activity can produce Ca²⁺ signal which can spread to another astrocytic process (Figure 7) and to the whole cell (Figure 8). Therefore, it can result in modulation of activity in neighboring synapses (Figure 7) and domain of synapses restricted by the territory of astrocytic morphology (Figure 8). In other words astrocyte can induce spatial synchronization in neuronal circuits defined by the morphological territory of the astrocyte. It is known that spatial synchronization in the brain is responsible for various cognitive functions (attention, recognition, navigation, making decisions, etc.) and for various pathologies (epileptic discharges, etc.).

AUTHOR CONTRIBUTIONS

SG, AE, and VK: conceptualization. SG and AE: data curation. SG, AE, and IK: formal analysis, investigation, and software. SG and VK: supervision and writing original draft.

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fphys. 2019.00294/full#supplementary-material

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Conflict of Interest Statement: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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